

Master thesis

**Work Distribution of a Heterogeneous Library Staff - A
Personnel Task Scheduling Problem**

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Abstract

Here is where you can write your abstract. It may be very long, or it may be very short, the reason you have an abstract is for people not to be forced to read lots of crap.

But still, they will have to read your abstract. After all, the abstract is what everyone reads...

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Nomenclature

Most of the reoccurring definitions, symbols and abbreviations are described here.

Definitions

| | |
|-------------------|------|
| Plocklista | Text |
| Library on wheels | Text |
| Rostering | Text |
| Matheuristic | Text |

Symbols

Abbreviations

| | |
|--------|------|
| Exp | Text |
| Info | Text |
| PL | Text |
| PTSP | Text |
| SMPTSP | Text |

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Chapter 1

Introduction

1.1 Background

At a library, staff absence can cause problems and can result in either a general shortage of staff or of staff with a special competence. If a worker is unavailable a certain day because of a meeting or illness it would require a stand-in to fill the vacancy. Therefore, it is of great interest to create schedules with as many skilled stand-ins as possible to overcome such disturbances when they occur. Furthermore, the library personnel have certain demands and preferences as to how a satisfactory working schedule should be. For instance, it is neither preferable to work more than one evening per week nor work more weekends than required.

The problem addressed in this thesis work concerns the library staff at the Central Library of Norrköping. The library has more than 40 employees and the culturally important building from the 1950's is known to all inhabitants of Norrköping. The library is open weekdays between 08:00 and 20:00 and during weekend days between 11:00 and 16:00. The generous opening times also creates a challenge for the library as it requires a large pool of well coordinated personnel. In addition to keeping the library running the library also provides its services to one other smaller library. This creates a challenge for the library schedulers.

1.2 Problem description

In this section, the most important features of the librarian scheduling problem studied in this thesis work will be explained.

1.2.1 Description of the daily tasks at the library

The most important activity at a library is the activity directed towards the public. This includes book loan services as well as providing customers with helpful information about the resources at the disposal of the library. These activities are referred to as "outer tasks". In addition, the book collection must be maintained, the returned books must be sorted and put back to the shelves, the web page must be updated and so on. Such work is often referred to as "inner

work” and this non-public work is an equally important part of the everyday activities of the library staff.

At the library of Norrköping, three main outer task types can be identified; working in the service counter (sv. expeditionsdiken), working in the information counter (sv. informationsdiken) and assembling books which are to be sent to other libraries according to the ”fetch list” (sv. plocklista). The fetch list is a task types which for which the worker is shceduled during a whole day, while the other task types have two or three hour shifts. The outer tasks can be performed by either librarians or assistants or both, as descirbed in Table 1.1.

Table 1.1: Outer tasks can be performed exclusively by librarians or by both librarians and assistants.

| Task | Description | Qualification |
|----------------------------|---|------------------------|
| Service Counter (Exp) | Administring loans, library cards and the loaning machine | Librarian or Assistant |
| Information Counter (Info) | Handling questions about the library’s resources. | Librarian |
| Fetch List (PL) | Fetching books that are to be sent to other libraries. | Librarian or Assistant |

Since the number of visitors at the library varies throughout the day and also during different days of the week, so does the demand for personnel for the three tasks. The demand of personnel for the different task types is illustrated in table 1.2, according to figures given by the library.

Table 1.2: Demand of staff for the three daily tasks.

| Day | Time | Exp demand | Info demand | PL demand |
|---------|-------------|------------|-------------|-----------|
| Mon-Fri | 08:00-10:00 | 2 | 2 | 1 |
| Mon-Fri | 10:00-13:00 | 3 | 3 | 1 |
| Mon-Fri | 13:00-16:00 | 3 | 3 | 1 |
| Mon-Fri | 16:00-20:00 | 3 | 3 | - |
| Sat | 11:00-16:00 | 3 | 3 | - |
| Sun | 11:00-16:00 | 3 | 3 | - |

As is the case with most libraries, the Central Library of Norrköping also has responsibilities that fall outside of it’s normal daily activities. One such responsibility is the running of a smaller library filial in Hageby, situated in a suburban area of Norrköping, during weekends. For this tasks only librarians are qualified as the placement implies all types of library tasks.

Similarly, only librarians are qualified for the task known as the ”Library on Wheels” (sv. Bokbussen), which is a type of library bus, providing citizens in remoter areas of the city with books and other library services. A qualified librarian is needed for this task type. The Library on Wheels only operates a few times a week and the schedule differs between even and odd weeks.

1.2.2 Personnel attributes

At a library, the main group of workers are librarians and assistants. The librarians make sure the library’s resource collection is up to date, that the

Table 1.3: Demand of staff at Hageby

| Day | Time | HB |
|-----|-------------|----|
| Sat | 11:00-16:00 | 1 |
| Sun | 11:00-16:00 | 1 |

Table 1.4: Demand of staff Library on Wheels

| Day | Time | BokB - odd week | BokB - even week |
|-----|-------------|-----------------|------------------|
| Mon | 08:00-10:00 | 1 | 1 |
| Mon | 16:00-20:00 | 1 | - |
| Tue | 08:00-10:00 | - | - |
| Tue | 16:00-20:00 | - | - |
| Wed | 08:00-10:00 | 1 | 1 |
| Wed | 16:00-20:00 | 1 | 1 |
| Thu | 08:00-10:00 | 1 | 1 |
| Thu | 16:00-20:00 | 1 | 1 |
| Fri | 08:00-10:00 | 1 | - |
| Fri | 16:00-20:00 | - | - |

visitors find what they're looking for and perform a larger number of inner tasks. Assistans can perform most of theses tasks, while others require librarian competence.

The Central Library of Norrköping currently has 39 workers, 23 of which are librarians and 16 of which are assistants. All staff have different availability for performing tasks, depending on their working hours and the amount of inner work they are in charge of. In the standard case, each worker is assigned one evening per week and once per five weeks, he/she is assigned to work during the weekend. The following week is compensated by two free days, placed according to the wishes of the worker.

Let's consider a sample worker who is qualified for librarian tasks. The worker works full time and is also assigned to work on Wednesday evenings. The worker also works weekend on the fourth week and has chosen to take out his days off on Thursdays and Fridays on week five. His availability is thus illustrated in table 1.5. The schedule repeats itself after five weeks and illustrates only the availability for tasks but says nothing about whether he has been assigned any tasks or not.

All workers have a five week schedule in the same manner as the sample worker. However, in order to meet the weekend demands as illustrated by Tables 1.2, 1.4 and 1.3, it is evident that not all workers can be assigned for weekend work at week 4. Instead, a worker's schedule should be seen as a *relative schedule*, which can be shifted by whole weeks. We refer to this as the *week rotation*.

The relative schedule is relative to the *overall schedule* for the library. If the sample worker for example has week rotation 1, this means the weekend week in his relative schedule would be shifted to week 1 in the overall schedule. In Table 1.5, the weekend rotation is 4.

Considering again the sample worker's schedule, it may look as if the worker can be scheduled for tasks at any yellow shift. However, there are regulations

Table 1.5: Availability schedule for a sample worker. Yellow signifies that the worker is available. In parenthesis, the weekend shift. The week rotation is 4.

| Week 1 | Mon | Tue | Wed | Thu | Fri | Sat | Sun |
|---------------------------|------------|------------|------------|------------|------------|------------|------------|
| 08:00-10:00 (11:00-16:00) | | | | | | | |
| 10:00-13:00 | | | | | | | |
| 13:00-16:00 | | | | | | | |
| 16:00-20:00 | | | | | | | |
| Week 2 | Mon | Tue | Wed | Thu | Fri | Sat | Sun |
| 08:00-10:00 (11:00-16:00) | | | | | | | |
| 10:00-13:00 | | | | | | | |
| 13:00-16:00 | | | | | | | |
| 16:00-20:00 | | | | | | | |
| Week 3 | Mon | Tue | Wed | Thu | Fri | Sat | Sun |
| 08:00-10:00 (11:00-16:00) | | | | | | | |
| 10:00-13:00 | | | | | | | |
| 13:00-16:00 | | | | | | | |
| 16:00-20:00 | | | | | | | |
| Week 4 | Mon | Tue | Wed | Thu | Fri | Sat | Sun |
| 08:00-10:00 (11:00-16:00) | | | | | | | |
| 10:00-13:00 | | | | | | | |
| 13:00-16:00 | | | | | | | |
| 16:00-20:00 | | | | | | | |
| Week 5 | Mon | Tue | Wed | Thu | Fri | Sat | Sun |
| 08:00-10:00 (11:00-16:00) | | | | | | | |
| 10:00-13:00 | | | | | | | |
| 13:00-16:00 | | | | | | | |
| 16:00-20:00 | | | | | | | |

set up by the library controlling how the outer tasks are to be distributed among the workers. The regulation are put in place to guarantee that worker schedules are not too unbalanced and uncomfortable.

For one thing, workers are only allowed to take at a maximum one task per day. Secondly, workers only work one weekend per five weeks. During this weekend it is customary that you work Friday evening shift, Saturday and Sunday shift consecutively. This is not true for Hageby, which is far away and is thus compensated by not entailing Friday evening work. Thirdly, weekend work is compensated by days off. There are a few possible variations of the weekend compensation, but usually the worker takes one and a half or two days off the week following upon weekend work. Lastly, a worker is only allowed to work one evening per week, excluding the Friday which belongs to the weekend week.

An example of a feasible schedule for the sample worker is provided in Table 1.6. It should be noted that this schedule is created for a general worker and does not necessarily apply to all workers. Among workers, special availability restrictions due to odd-and even weeks exist and only a subset of the librarians are available for the Library on Wheels and Hageby. Also, some workers never work evening or weekend shifts.

Table 1.6: Example of a feasible first week for the sample worker.

| Week 1 | Mon | Tue | Wed | Thu | Fri | Sat | Sun |
|---------------------------|-----|-----|------|-----|------|-----|-----|
| 08:00-10:00 (11:00-16:00) | | Exp | | PL | | | |
| 10:00-13:00 | Exp | | | PL | | | |
| 13:00-16:00 | | | | PL | Info | | |
| 16:00-20:00 | | | Info | | | | |

1.2.3 Scheduling objectives: stand-in maximization and schedule variation

What is investigated in this thesis is not primarily how to distribute the tasks according to the rules given above, but rather how to do this in a way so that the number of stand-in personnel is maximized. The emergency back-up system of stand-ins is crucial for the library in order to be able to keep the library desks open and fully staffed. Thus is the highest priority of the library to maximize the number of stand-in personnel.

A stand-in is defined as a worker who is available for outer tasks during shifts one to three, but who is not scheduled at any shift scheduled in that day. Inner work sometimes prevents personnel from being scheduled as a stand-in for the outer tasks, and therefore also information about such work must be known to the scheduler. Both librarians and assistants can be scheduled as a stand-in, but only librarians are qualified to take emergency shifts at the Info desk. Since the regular library activity is the most crucial activity, there is no need for stand-ins during evening and weekends. Similarly, there are no assigned stand-ins for the Library on Wheels or for Hageby.

Apart from maximizing the number of stand-ins for each day at the library, another important measurement of a good schedule is the level of variation. It is desirable for the sake of the personnel to create schedules in which the weeks resemble each other or are repeated according to some pattern. On the other hand, since some shifts are more attractive than others and in order to avoid too much repetitiveness it is desirable that the days during a work week are not too similar. The example schedule in Table 1.6 is an example of a sufficiently varied weekly schedule.

1.3 Method

1.4 Topics Covered

Chapter 2

Literature review

The scheduling problem is a mathematical optimization problem which has been studied since the 1950's and concerns creating a feasible and satisfactory schedule for workers or machines performing tasks. One of the most extensive overviews in the area is provided by Ernst et al. (2004). They state that, although the complexity of the scheduling problem has not increased in recent years, the mathematical models used to solve the scheduling problems have become more realistic and refined. Modern scheduling problems often concern the distribution of tasks and the creation of worker shifts, taking also into account softer values such as worker satisfaction and worker fatigue. Due to this modeling refinement as well as the development of more powerful computational methods, it is possible today to solve scheduling problems in a more satisfactory way than before.

In this section, the scheduling problem is classified into different subcategories which are areas related to the work of this paper. A few relevant areas for our work include Personnel Task Scheduling Problems (PTSP), Shift Minimization Task Scheduling Problems (SMTSP), Tour Scheduling Problems (TSP) and a few variations of these. Models and solutions methods of these problems will be discussed during each topic and a summary of the discussion will be provided.

2.1 Personnel Task Scheduling Problem

In many practical instances production managers will face the Personnel Task Scheduling Problem (PTSP) while scheduling service operations. Krishnamoorthy and Ernst (2001) writes in their article that the PTSP occurs when the rosterer or shift supervisor need to allocate tasks with specified start and end times to available personnel who have the required qualifications. Furthermore, it also occurs in situations where tasks of fixed times shall be assigned to machines. Decisions will then have to be made regarding the amount of maintenance workers needed and which machine the workers are assigned to look after.

There are numerous variants to the PTSP. Studies on these have been made by Krishnamoorthy and Ernst (2001) who gives a list of attributes that commonly appear in a PTSP, which are listed in Table 2.1. Furthermore, there are

traits that always appear in a PTSP; tasks with fixed start and end time are to be distributed to staff members that possess certain skills, allowing them to perform only a subset of the available tasks. Start and end time of their shifts are also predetermined for each day.

One variant, which also is the most simple, is mentioned in Krishnamoorthy and Ernst (2001) and is called the *Feasibility Problem* where the aim is to just find a feasible solution. This requires that each task is allocated to a qualified and available worker. It is also required that a worker cannot be assigned more than one task simultaneously as well as tasks cannot be pre-empted, meaning that each task has to be completed by one and the same worker.

In Table 2.1 attributes of PTSP variants are shown. The nomenclature of the attributes T, S, Q and O refer to the *Task type*, *Shift type*, *Qualifications* and *Objective function* respectively.

Table 2.1: PTSP variants

| Attribute | Type | Explanation |
|-----------|------|---|
| T | F | Fixed contiguous tasks |
| | V | Variable task durations |
| | S | Split (non-contiguous) tasks |
| | C | Changeover times between consecutive tasks |
| S | F | Fixed, given shift lengths |
| | I | Identical shifts which are effectively of infinite duration |
| | D | Maximum duration without given start or end times |
| | U | Unlimited number of shifts of each type available |
| Q | I | Identical qualification for all staff (homogeneous workforce) |
| | H | Heterogeneous workforce |
| O | F | No objective, just find a feasible schedule |
| | A | Minimise assignment cost |
| | T | Worktime costs including overtime |
| | W | Minimise number of workers |
| | U | Minimise unallocated tasks |

Many of the most basic and a few more complex problems can be described with this definition of PTSP attributes. It is, however, not possible to describe all of the numerous types of PTSP using these nomenclatures according to Krishnamoorthy and Ernst (2001).

By combining attributes it is possible to obtain more complex variants of the PTSP. An example would be the PTSP[F;F;H;A-T-W] mentioned in Krishnamoorthy and Ernst (2001), where multiple objectives are used. This problem has fixed contiguous tasks, fixed shift lengths, heterogeneous workforce and three objective functions (A-T-W), which represent assignment costs, work time with overtime included and requirements to minimize the number of workers respectively. The objective function for this problem is then a linear combination with parameters used to weigh (prioritize) them against each other.

Given the nomenclature above, our problem would be most related to the PTSP[F;F;H;F]. The difference is that the objective function is not empty. We are looking to maximize the number of qualified stand-ins each day as well as maximize employee satisfaction by meeting their recommendations. We have a fix number of workers, no costs and no unallocated tasks when a feasible solution

is found. Therefore, none of the objective function types given in Table 2.1 are relevant in our case.

Some variants of the PTSP are given names in the literature, which is stated by Krishnamoorthy and Ernst (2001). An example is when the shifts and qualifications are identical ($S=I$, $Q=I$) and the objective function is to minimize the number of workers that are used ($O=W$). This variant, $PTSP[F;I;I;W]$, has been published as the Fixed Job Schedule Problem and is described in Section 2.4.

2.1.1 Applications

An example where the PTSP can be found is when developing a rostering solution for ground personnel at an airport. This is mentioned in the article by Krishnamoorthy and Ernst (2001). The problem can be dealt with by first assigning the workers to days in order to satisfy all the labour constraints, followed by assigning the tasks to the scheduled workers.

In the article mentioned above, three further problems of type PTSP, related to airplanes are mentioned. They occur when scheduling for either airport maintenance staff, planes to gates or staff that do not stay in one location, such as airline stewards. Scheduling for airport maintenance staff can lead to either $PTSP[F;I;H;U-A]$ or $PTSP[F;I-U;H;W]$, which are similar problems but given two different names: Operational Fixed Interval Scheduling Problem and Tactical Fixed Interval Scheduling Problem respectively. These are described further in Section 2.4.

Another application, which has been frequently studied, is classroom assignments and is discussed in Krishnamoorthy and Ernst (2001). Based on specifications such as the amount of students in a class or the duration of a class, different classrooms have to be considered. Requirements of equipment, e.g. for a laboratory, may also greatly limit the available classrooms to choose from. A majority of the complications of this problem is due to the fact that lessons can span over multiple periods.

Worth noting for classroom assignment problems is that there are no start or end times for the shifts, as they represent the rooms. The aim in the present problem would be to simply find a feasible assignment of classrooms. Therefore, the nomenclature of the problem would be $PTSP[S;I;H;F]$, according to Krishnamoorthy and Ernst (2001), with the possibility of adding preferences to the objective function. An example of a preference would be to assign the lessons as close to each other as possible on a day, preventing travel distances for teachers and students.

2.2 Shift Minimisation Personnel Task Scheduling Problem

A close relative to the PTSP is the Shift Minimisation Personnel Task Scheduling Problem (SMPTSP) and is a special case in which the aim is to minimize the cost occurring due to the number of personnel that are used. The same common traits are mentioned in the article Krishnamoorthy et al. (2012) for this problem as in the PTSP; workers with fixed work hours are to be assigned tasks, with specified start and end times, that they are qualified for.

In the same article as above they "... concentrate mainly on a variant of the PTSP in which the number of personnel (shifts) required is to be minimised.". In doing so, it is possible to determine the lowest number and mix of skilled staff a company should have to be able to complete the tasks and still be operational. They also presumed that the pool of workers are unlimited for either skill group, which is not the case in the present problem due to the limitations on the amount of librarians and assistants available.

Furthermore, it is said in Krishnamoorthy et al. (2012) that SMPTSP can be applied when there are a large number of workers available with different qualifications and it is needed to ensure that the tasks for that day are performed. The PTSP and SMPTSP are therefore useful day-to-day management tools and commonly occur in many practical instances where tasks are allocated on a daily basis.

It is shown in Kroon et al. (1995) that SMPTSP is a complex problem even if the preemption constraint were to be removed. However, it is stated in Krishnamoorthy et al. (2012) that if the qualifications of the workers were identical it would be an easily solvable problem.

SMPTSP is almost identical to another problem introduced by Kroon et al. called the Tactical Fixed Interval Scheduling Problem, which is described further in Section 2.4.2.

During the last decade, a couple heuristics have been implemented to deal with the SMPTSP. One method introduced by Krishnamoorthy et al. (2012) is a Lagrangean relaxation approach that combines two problem specific heuristics: Volume Algorithm (VA) and Wedelin's Algorithm (WA). These heuristics exploit the special structure of the SMPTSP by relaxing some of the harder constraints into the objective function, thus being problem specific heuristics. All that remain after the relaxation is a problem decomposed into several independent problems that can be solved independently. A solution to these decomposed problems is discussed further in Krishnamoorthy et al. (2012).

Another method to solve the SMPTSP is to use a very large-scale neighbourhood search algorithm, which was presented by Smet and Vanden Berghe (2012). The main purpose of their implemented hybrid local search is to repeatedly fix and optimize to find neighbouring solutions. Using this method on 137 benchmark instances introduced by Krishnamoorthy et al. (2012), Smet and Vanden Berghe managed to find 81 optimal solutions compared to Krishnamoorthy et al. who only managed to find 67. Furthermore, both methods found feasible solutions for 135 out of the 137 problem instances. This comparison is presented in Smet et al. (2014).

Smet et al. (2014) introduced a third and most effective method to solve the benchmark instances related to the SMPTSP. By using a versatile two-phase matheuristic approach, solutions to all 137 benchmark instances could be found for the first time. The procedure used in their implementation is to first generate an initial solution by using a constructive heuristic, followed by improving the solution using an improvement heuristic. Which constructive and improvement heuristic they considered can be seen in their article.

2.3 Tour Scheduling Problem

The Tour Scheduling Problem (TSP) is described by Loucks and Jacobs (1991) as a combination of shift scheduling and days-off scheduling. Using the notation used described in the section 2.1, this would be classified as a variant of the PTSP[F;D;I;W] or PTSP[F;D;H;W]. Shift scheduling refers to creating sets of contiguous hours during which a worker is assigned for work. The need for days off scheduling typically occurs when the time horizon for scheduling is weekly or more and when weekend staff is needed.

According to Loucks and Jacobs (1991), the vast majority of all tour scheduling problems up to 1991 involved a homogeneous workforce, that is, any worker can perform any assigned task. One such early study of the tour scheduling problem often mentioned in literature is provided by Roberts and Escudero (1983a). The problem studied in this PhD thesis concern only homogeneous work forces and the task assignment part is lacking.

In the article by Loucks and Jacobs, the authors study a tour scheduling problem with a heterogeneous work force. The problem both involves tour scheduling and task assignment, where the latter part is most interesting to us. The problem is studied in the context of fast food restaurants, where certain personnel is qualified only for certain stations in the restaurant. In such industries, the demand of staff differs between different weekdays and different times of the day. Two worker attributes are considered, their availability for work and their qualification for performing different tasks. The problem concerns finding shifts for all workers which are to have a length between a minimum and maximum number of hours per day.

The representative problem studied in the article involves creating a one-week schedule for 40 workers in a fast food restaurant, available for eight different tasks with a seven-day, 128-hour workweek. Several synthetic problems are studied in the article, all, however with minimum shift length three hours, maximum shift length eight hours and five maximum number of work days.

A similar problem to the one described by Loucks and Jacobs is studied by Choi et al. (2009). They focus on a particular fast food restaurant in Seoul, which is made a representative of fast food chains in general. In this study, only two types of workers are available, fulltime and part time workers, with no other reference to difference in skill. The different shifts are already given by the restaurant managers and the task is to combine them into a tour. The task assignment aspect is lacking in this article.

In both articles the main objective is to minimize both overstaffing and understaffing, which will both have economical consequences for the fast food chain. This is done by reducing or increasing the work force. For a problem with a fixed work force, such as ours, this objective is not relevant. In the example studied by Loucks and Jacobs there is also a goal to meet staff demand on total working hours. This is modeled as a secondary goal and is similar to our goal and somehow models a "soft" value, which is of interest to us.

A more recent tour scheduling problems concern monthly tour scheduling, as opposed to most literature which concerns only weekly scheduling. Such a study was done by Rong (2010). The main advantage of monthly scheduling over shorter time periods, as stated in the article, is the possibility to plan a schedule with respect to fairness and balance over a longer period of time. The problem concerns workers with different skills, where each worker also can

possess multiple skills. This is referred to as a mixed skill problem. Thus the problem is similar to our problem, where mixed skill is also present. In the study, workers have individual weekend-off requirements. The problem does not involve task assignment, which makes it less relevant for us.

The solution methods used to solve the tour scheduling problem differs greatly between the articles studied. In the older articles, such as Roberts and Escudero (1983a) and Loucks and Jacobs (1991), custom made algorithms very similar to the methods used in manual scheduling are proposed to solve the problem. These solution methods involve classifying staff and distributing them according to some rule (for example, the staff with the most scarce skill is assigned first). General commercial solvers are not proposed, due to lack of efficiency during these times. In Hojati and Patil (2011), the same model and data is used as in Loucks and Jacobs (1991). Also this article states that commercial solvers are insufficient for solving the problem. Instead two methods are proposed, one which decomposes the problem into two problems solvable by commercial solvers and one customized heuristic method based on the Lagrangian relaxation method. In Choi et al. (2009), a pure integer programming method is used.

2.4 Other similar problems

In this section a couple of problems, similar to our own, will be described. The focus will not be on the variety of methods used to solve these problem. Instead, the focus will be to give clarity to how closely related many of these problem types are.

2.4.1 Fixed Job Schedule Problem

Variations of the task assignment problem relevant for our problem include for example the Fixed Job Schedule Problem (FJSP). The FJSP has been studied since the 1970s in the context of task assignment in processors. The problem concerns the distribution of tasks with fixed starting and ending times over a workforce with identical skills, such as processing units Krishnamoorthy et al. (2012). Such problems have been solved by Gertsbakh and Stern (1978) and Fischetti et al. (1992).

In the article by Gertsbakh and Stern (1978) a situation is studied where n jobs need to be scheduled over an unlimited number of procesors. The objective function of such a problem becomes to minimize the number of machines needed to perform all tasks. Fischetti solves a similar problem, but adds time constraints, saying that no processor is allowed to work for more than a fixed time T during a day as well as a spread time constraint forcing tasks to spread out with time gap S over a processor.

2.4.2 Tactical Fixed Interval Scheduling Problem

The Tactical Fixed Interval Scheduling Problem (TFISP) is a problem very closely related to the SMPTSP with the sole difference that the TFISP concerns workers which always are available, such as industrial machines or processors.

The problem is studied in Kroon et al. (1995). A typical TFISP can be expressed using the nomenclature in Table 2.1 and written as PTSP[F;I-U;H;W] **Krishnamoorthy and Ernst (2001)**.

Opposed to the FJSP, the TFISP deals with a heterogeneous workforce. Two different contexts are studied by Kroon et al. (1995). One of them concerns the handling of arriving aircraft passengers at an airport. Two modes of transport from the airplane to the airport are investigated, directly by gate or by bus. The two transportation modes thus correspond to two processing units, which can only handle a number of jobs at the same time.

2.4.3 Operational Fixed Interval Scheduling Problem

The Operational Fixed Interval Scheduling Problem (OFISP) is a close relative to TFISP, where both types are restricted by the following: Each machine (worker) cannot handle more than one job at a time, can only handle a subset of the jobs and preemption of jobs is not allowed. The difference between them occurs in the objective function, as described in Kroon et al. (1995). TFISP tries to minimize the number of workers, while OFISP tries to minimize the operational costs and the number of unallocated tasks using priority indices. In the present nomenclature this would give rise to the problem PTSP[F;I;H;U-A].

Given the problem definition above, working shifts are to be created for the workers and tasks have to be allocated on a day-to-day basis. OFISP, studied by Kroon et al. (1995), can therefore be seen both as a job scheduling problem and an assignment problem.

2.4.4 Stochastic job problems

What differs mostly between the problem types described above and the problem studied in this thesis work, is the difference in objective function. The main objective function is often to minimize staff for a number of fixed jobs, not taking into consideration the need for stand-ins to perform critical tasks. An area where the need for stand-in personnel appears is in the maintenance industry, where some jobs can be foreseen and other (emergency) jobs are of a stochastic nature, that is, there is a probability that such jobs will occur a certain hour. The problem combining both unplanned and planned maintenance worker scheduling was studied by Duffuaa and Al-Sultan (1999), as a continuation of Roberts and Escudero (1983b).

In the article, a fixed, heterogeneous work force consisting of electricians, plumbers and mechanics is studied. The shifts of the personnel are predetermined by their given work times and thus the problem becomes a pure task assignment problem. An objective function is used where the goal is to maximize the number of planned and unplanned jobs performed by the workers, by taking into account the probability of unplanned work to occur. Thus, certain workers will be left at the station as stand-ins in the case an unplanned job arrives.

2.5 Problems with soft constraints

For most scheduling problems, the main objective is to minimize worker-related costs by reducing the number of workers needed to perform a task, or by reducing the working time for part-time employees. Equivalently, the goal in production industries is to reduce the number of machines needed. Recently, however, many studies have started to focus more on softer values such as worker satisfaction as an objective. Such values are usually considered when scheduling is done manually, but have been forgotten or set aside in mathematical modeling.

In an article by Akbari et al. (2013) a scheduling problem for part-time workers with different preferences, seniority level and productivity is investigated. In this article, these aspects are reflected in the objective function and weighted against each other. A similar problem was also studied by Mohan (2008), but for a work force of only part-time workers.

Other factors which may affect worker satisfaction, and in the long run efficiency and presence at work are fatigue, fairness and boredom. These are discussed by Eiselt and Marianov (2008). Repetitiveness of a job as well as the level of challenge can cause boredom in workers. Increasing variance is done by Eiselt and Marianov (2008) through providing an upper bound of how many tasks can be performed in a given time span. The article suggests some sort of measurement of the distance between the task requirements and the worker abilities is used. This will then be minimized in the objective function.

Another modeling method which is relevant specifically for scheduling problems featuring soft constraints is fuzzy goal programming. The method is discussed by Shahnazari-Shahrezaei et al. (2013), who model soft constraints as "fuzzy goals". These goals can become contradictory, for example could a preference of high seniority level workers come in conflict with a preference in working hours by an employee. The article uses fuzzy set theory, and uses a solution approach involving Li's two-phase method, Lee (1989). Soft constraints are modeled as trapezoid functions and an optimal solution which finds the best average of all of them is found.

The solution methods proposed by Akbari et al. (2013) to solve a scheduling problem with soft constraints are two metaheuristics: Simulated Annealing (SA) and Variable Neighbourhood Search (VNS). According to Akbari et al. (2013), SA has been studied as a solution method for the scheduling problem since the 1990's and many studies have shown that it is capable of providing near-optimal solutions in a short time compared to optimal integer-programming models for a variety of problems. The method is a random meta heuristic, which finds new random solutions and chooses it to be the current solution if sufficiently good. With time, the threshold for what is considered good is increasing.

VNS is the other proposed method by Akbari et al. (2013). A big difference between this and other methods is that VNS requires very little parameter tuning while often providing good solutions. The method involves a random and a systematic phase. In the random phase, new shifts are generated randomly and better solutions are saved. In the systematic phase, two shifts are swapped and again better solutions are saved.

In the article by Eiselt and Marianov (2008), a commercial solver was used. This was also the case in Mohan (2008), although the article compares these results with the results obtained from a branch-and-cut algorithm. Also Shahnazari-Shahrezaei et al. (2013) uses a commercial solver.

2.6 Summary

Stycke ett: Modeller
Stycke två: Metoder
historiskt kronologiskt

2.7 Relevance to our problem

Kan börjas med syftesformulering. Referera tillbaka i texten, samt lägg till nya reflektioner.

2.8 Solution Methods

Integrate into previous parts!

In many real life situations, the scheduling method used to create worker schedules is a simple matching algorithm between two can do what and when. The process is most often left in the hands of experienced and knowledgeable schedulers, who know the capacity of the work force and how to maximize productivity by meeting task demands as well as employee demands and individual personality traits. This is referred to as the "art" of scheduling Roberts and Escudero (1983b). However, when personnel forces grow large and there are regulations, task skill requirements or several personnel preferences to take into account, the problem becomes too large to solve manually in a satisfactory manner.

The first computational methods used for solving scheduling problems were in many cases simple heuristics resembling the scheduling process as performed in a manual way. One example of this is the heuristic presented by Loucks and Jacobs which assigns workers to tasks, following certain rules, until all tasks are assigned Loucks and Jacobs (1991). An overview of solution methods is given by Ernst et al, where almost 30 different methods are presented and it is not uncommon that special purpose algorithms are used to suite a specific problem Ernst et al. (2004). Some of the more interesting solution methods with respect to the problem studied in this thesis are discussed in this section. These include solving with commercial solvers, matheuristic methods such as simulated annealing and variable neighbourhood search, pure heuristic methods, goal programming and fuzzy goal programming.

2.8.1 Commercial software

Commercially available scheduling programs.

2.8.2 Mathematical Programming

Formulating a mathematical model. Objective function and constraints. Solving using commercial solver such as CPLEX or Guroby.

Stochastic and non-stochastic

2.8.3 Simulated Annealing

Simulated Annealing (SA) has been studied as a solution method to the scheduling problem by researchers such as Brusco and Jacobs in the early 1990's. The method is a metaheuristic method which has the advantage over local search methods that it does not easily get stuck in local optima. The method is a random optimization method designed to find a global optimum solution. The method allows bad moves according to a function According to Akbari, Simulated Annealing

2.8.4 Variable Neighbourhood Search

Also avoids local optima.

"A variable neighborhood search based matheuristic for nurse rostering problems" Della Croce et Salassa. "VNS outperforms exact commercial general purpose solvers" Matheuristic approach!

Early work by: Hansen and Mladenovic, 2001, Mladenovic and Hansen, 1997

2.8.5 Tabu Search

Commonly used meta-heuristic.

2.8.6 Goal programming and Fuzzy Goal Programming

GP: Used for multiple goals.

FGP: Used for contradictory goals.

Bellman and Zadeh's max-min operator!

Fuzzy goal programming. "Fuzzy goals" = soft constraints. Fuzzy set theory. The basic idea of FGP is to present some of the model parameters as imprecise numbers. Goal programming: good when combining soft and hard constraints.

Using an average value approach with goals that are contradictory makes it possible to maximize the amount of "goodness" in the solution, by prioritizing one constraint over another, which in total generates the most good.

Chapter 3

The mathematical model

In this chapter the mathematical model implemented to solve this problem will be presented. Prior to the objective function and constraints, the most significant variables and sets will be stated to give the reader an idea of how the work has proceeded. In Section 3.3 the constraints will be presented only in pseudocode. Complete model with the full set of constraints can be found in Attachment ??.

3.1 Set and variable definitions

To solve the problem many sets and variables had to be declared as there are many unique and personal requirements that have to be met. An example is that some personnel want a day free from outer tasks so that they can focus on other assignments or attend meetings. Another one is that some have two different schedules whether it is an odd or even week. These specific cases have to be modeled and result in a variety of set and variable definitions. Hence, only the most important ones are listed below. A complete list of the definitions can be found in Appendix A.

| | |
|-----------|---|
| I | Set of workers |
| I_{lib} | Set of librarians ($I_{lib} \subseteq I$) |
| I_{ass} | Set of assistants ($I_{ass} \subseteq I$) |
| W | Set of weeks |
| D | Set of days in a week |
| S_d | Set of shifts day d |
| J_d | Set of task types day d |

In order to further define the problem we introduce the following variables.

Let,

$$x_{iwdsj} = \begin{cases} 1, & \text{if worker } i \text{ is assigned in week } w, \text{ day } d, \text{ shift } s \text{ to a task } j \\ 0, & \text{otherwise} \end{cases} \quad (3.1)$$

$$H_{iwh} = \begin{cases} 1, & \text{if worker } i \text{ works weekend } h, \text{ week } w \\ 0, & \text{otherwise} \end{cases} \quad (3.2)$$

$$r_{iw} = \begin{cases} 1, & \text{if worker } i \text{ has its scheduled rotated } w-1 \text{ steps} \\ 0, & \text{otherwise} \end{cases} \quad (3.3)$$

$$l_{iwd} = \begin{cases} 1, & \text{if librarian } i \text{ is a stand-in week } w, \text{ day } d \\ 0, & \text{otherwise} \end{cases} \quad (3.4)$$

$$a_{iwd} = \begin{cases} 1, & \text{if assistant } i \text{ is a stand-in week } w, \text{ day } d \\ 0, & \text{otherwise} \end{cases} \quad (3.5)$$

$$y_{iwd} = \begin{cases} 1, & \text{if worker } i \text{ works week } w, \text{ day } d, \text{ shift } s \text{ regardless of task type} \\ 0, & \text{otherwise} \end{cases} \quad (3.6)$$

$$h_{iw} = \begin{cases} 1, & \text{if worker } i \text{ works at HB week } w \\ 0, & \text{otherwise} \end{cases} \quad (3.7)$$

$$f_{iw} = \begin{cases} 1, & \text{if worker } i \text{ is assigned to work friday evening week } w \\ 0, & \text{otherwise} \end{cases} \quad (3.8)$$

$$l_{min} = \text{lowest number of stand-in librarians found (integer)} \quad (3.9)$$

$$a_{min} = \text{lowest number of stand-in assistants found (integer)} \quad (3.10)$$

$$s_{iwd} = \text{number of shifts } s \text{ that differ for a worker } i \text{ between week } w \text{ and } w+5, \text{ day } d \text{ (integer)} \quad (3.11)$$

Based on the variables defined above it has been possible to solve our scheduling problem. l_{min} and a_{min} are the variables of most significance as they represent the number of stand-ins found after a run.

3.2 Objective function

Due to multiple objective functions it has been necessary to weigh them against each other using parameters. These are shown in Equation 3.12 below as $N1l$, $N1a$ and $N2$.

$$\begin{aligned} & max N1l * l_{min} \\ & + N1a * a_{min} \\ & - N2 * \sum_{i \in I} \sum_{w=1}^5 \sum_{d=1}^5 \sum_{s=1}^3 s_{iwd} \end{aligned} \quad (3.12)$$

If $N1l < N1a$ then the function were to prioritize assistants as stand-ins

rather than librarians. Librarians are, however, more desired as stand-ins, due to their ability to perform all task types. Therefore, it is desired to set $N1l \geq N1a$.

3.3 Constraints

To model this problem it has been of relevance to divide many of the constraints into weekend- and weekday constraints. Several help constraints have also been added to avoid quadratic variables. These would otherwise occur when two decision variables are multiplied with each other.

The most crucial constraint is to ensure that the demand of workers is met each day. This can be modeled as,

$$\sum_{i \in I} x_{iwsj} = task_demand_{wsj}, \forall w \in W, d \in D, s \in S, j \in J_d \quad (3.13)$$

where $task_demand_{wsj}$ is the number of workers required week w , day d , shift s for a task j .

To ensure that no worker is assigned more than one task the following constraint is implemented,

$$\sum_{s \in S} \sum_{j \in J_d} x_{iwsj} \leq 1, \forall i \in I, w \in W, d \in D \quad (3.14)$$

However, if we allow a person to have two shifts at the library on wheels in a day Equation 3.14 has to be slightly modified.

A preference is to only allow one PL per week. This is easily modeled with the following constraint,

$$\sum_{s \in S_d} \sum_{d \in D} x_{iwsj=PL} \leq 1, \forall i \in I, w \in W \quad (3.15)$$

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Appendix A

Problem definitions

A.1 Sets

| | |
|----------------------|---|
| I | Set of workers |
| I_{lib} | Set of librarians ($I_{lib} \subseteq I$) |
| I_{ass} | Set of assistants ($I_{ass} \subseteq I$) |
| W | Set of weeks |
| D | Set of days in a week |
| S_d | Set of shifts day d |
| J_d | Set of task types day d |
| I_{LOW} | Set of librarians available to work in library on wheels |
| I_{free_day} | Set of workers that shall be assigned a free weekday per week |
| I_{odd_even} | Set of all workers with odd or even weeks |
| $I_{weekend_avail}$ | Set of workers available for weekend work |

A.2 Variables

$$x_{i w d s j} = \begin{cases} 1, & \text{if worker } i \text{ is assigned in week } w, \text{ day } d, \text{ shift } s \text{ to a task } j \\ 0, & \text{otherwise} \end{cases} \quad (\text{A.1})$$

$$H_{i w h} = \begin{cases} 1, & \text{if worker } i \text{ works weekend } h \text{ in week } w \\ 0, & \text{otherwise} \end{cases} \quad (\text{A.2})$$

$$r_{i w} = \begin{cases} 1, & \text{if worker } i \text{ has its scheduled rotated } w-1 \text{ steps} \\ 0, & \text{otherwise} \end{cases} \quad (\text{A.3})$$

$$lib_{i w d} = \begin{cases} 1, & \text{if librarian } i \text{ is a stand-in week } w \text{ day } d \\ 0, & \text{otherwise} \end{cases} \quad (\text{A.4})$$

$$ass_{i w d} = \begin{cases} 1, & \text{if assistant } i \text{ is a stand-in week } w \text{ day } d \\ 0, & \text{otherwise} \end{cases} \quad (\text{A.5})$$

$$y_{i w d s} = \begin{cases} 1, & \text{if worker } i \text{ is working } w \text{ day } d \text{ regardless of task type} \\ 0, & \text{otherwise} \end{cases} \quad (\text{A.6})$$

$$hb_{i w} = \begin{cases} 1, & \text{if assistant } i \text{ is a stand-in week } w \text{ day } d \\ 0, & \text{otherwise} \end{cases} \quad (\text{A.7})$$

$$friday_evening_{i w} = \begin{cases} 1, & \text{if assistant } i \text{ is a stand-in week } w \text{ day } d \\ 0, & \text{otherwise} \end{cases} \quad (\text{A.8})$$

$$lib_min = \text{lowest number of stand-in librarians found (integer)} \quad (\text{A.9})$$

$$ass_min = \text{lowest number of stand-in assistants found (integer)} \quad (\text{A.10})$$

A.3 Parameters

$$N1l = \text{a value to prioritize the amount of stand-in librarians} \quad (\text{A.11})$$

$$N1a = \text{a value to prioritize the amount of stand-in assistants} \quad (\text{A.12})$$

$$N2 = \text{a value to prioritize similar weeks} \quad (\text{A.13})$$

$$avail_day_{iwd} = \begin{cases} 1, & \text{if worker } i \text{ is available for work week } w, \text{ day } d \\ 0, & \text{otherwise} \end{cases} \quad (\text{A.14})$$

$$task_demand_{dsj} = \text{number of workers required day } d, \text{ shift } s \text{ for task type } j \quad (\text{A.15})$$

$$qualavail_{iwsj} = \begin{cases} 1, & \text{if worker } i \text{ is qualified and available week } w, \text{ day } d, \text{ shift } s \text{ for task type } j \\ 0, & \text{otherwise} \end{cases} \quad (\text{A.16})$$

$$LOW_demand_{wds} = \text{number of workers required day } d, \text{ shift } s \text{ at the library on wheels} \quad (\text{A.17})$$

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