

Domain	$\dim(o)$	$N$	$n^N$	$n \times N$
Reacher-v1	11	2	$1.1 \times 10^3$	66
Hopper-v1	11	3	$3.6 \times 10^4$	99
Walker2d-v1	17	6	$1.3 \times 10^9$	198
Humanoid-v1	376	17	$6.5 \times 10^{25}$	561

Table 1: Dimensionality of the OpenAI’s MuJoCo Gym benchmark domains:  $\dim(o)$  denotes the observation dimensions,  $N$  is the number of action dimensions, and  $n^N$  indicates the number of possible actions in the combinatorial action space, with  $n$  denoting the fixed number of discrete sub-actions per action dimension. The rightmost column indicates the total number of network outputs required for the proposed action branching architecture. The values provided are for the most fine-grained discretization case of  $n = 33$ .

branching networks, remains the subject of future research.

### Experiment Details

Here we provide information about the technical details and hyperparameters used for training the agents in our experiments. Common to all agents, training always started after the first  $10^3$  steps and, thereafter, we ran one step of training at every time step. We did not perform tuning of the reward scaling parameter for either of the algorithms and, instead, used each domain’s raw rewards. We used the OpenAI Baselines (?) implementation of DQN as the basis for the development of all the DQN-based agents.

**BDQ** We used the Adam optimizer (?) with a learning rate of  $10^{-4}$ ,  $\beta_1 = 0.9$ , and  $\beta_2 = 0.999$ . We trained with a mini-batch size of 64 and a discount factor  $\gamma = 0.99$ . The target network was updated every  $10^3$  time steps. We used the rectified non-linearity (or ReLU) (?) for all hidden layers and linear activation on the output layers. The network had two hidden layers with 512 and 256 units in the shared network module and one hidden layer per branch with 128 units. The weights were initialized using the Xavier initialization (?) and the biases were initialized to zero. A gradient clipping of size 10 was applied. We used the prioritized replay with a buffer size of  $10^6$ ,  $\alpha = 0.6$ , and linear annealing of  $\beta$  from  $\beta_0 = 0.4$  to 1 over  $2 \times 10^6$  steps.

While an  $\epsilon$ -greedy policy is often used with Q-learning, random exploration (with an exploration probability) in physical, continuous-action domains can be inefficient. To explore well in physical environments with momentum, such as those in our experiments, DDPG uses an Ornstein-Uhlenbeck process (?) which creates a temporally correlated exploration noise centered around the output of its deterministic policy. The application of such a noise process to discrete-action algorithms is, nevertheless, somewhat non-trivial. For BDQ, we decided to sample actions from a Gaussian distribution with its mean at the greedy actions and with a small fixed standard deviation throughout the training to encourage life-long exploration. We used a fixed standard deviation of 0.2 during training and zero during evaluation. This exploration strategy yielded a mildly better perfor-

mance as compared to using an  $\epsilon$ -greedy policy with a fixed or linearly annealed exploration probability. For the custom reaching domains, however, we used an  $\epsilon$ -greedy policy with a linearly annealed exploration probability, similar to that commonly used for Dueling DDQN.

**Dueling DDQN** We generally used the same hyperparameters as for BDQ. The gradients from the dueling streams were rescaled by  $1/\sqrt{2}$  prior to entering the shared feature module as recommended by ? (?). Same as the reported best performing agent from (?), the average aggregation method was used to combine the state value and advantages. We experimented with both a Gaussian and an  $\epsilon$ -greedy exploration policy with a linearly annealed exploration probability, and observed a moderately better performance for the linearly annealed  $\epsilon$ -greedy strategy. Therefore, in our experiments we used the latter.

**IDQ** Once more, we generally used the same hyperparameters as for BDQ. Similarly, the same number of hidden layers and hidden units per layer were used for each independent network, with the difference being that the first two hidden layers were not shared among the several networks (which was the case for BDQ). The dueling architecture was applied to each network independently (i.e. each network had its own state-value estimator). This agent serves as a baseline for investigating the significance of the shared decision module in the proposed action branching architecture.

**DDPG** We used the DDPG implementation of the rllab suite (?) and the hyperparameters reported by ? (?), with the exception of not including a  $L_2$  weight decay for Q as opposed to the originally proposed penalty of  $10^{-2}$  which deteriorated the performance.

### Conclusion

We introduced a novel neural network architecture that distributes the representation of the policy or the value function over several network branches, meanwhile, maintaining a shared network module for enabling a form of implicit centralized coordination. We adapted the DQN algorithm, along with several of its most notable extensions, into the proposed action branching architecture. We illustrated the effectiveness of the proposed architecture in enabling the application of a currently restricted discrete-action algorithm to domains with high-dimensional discrete or continuous action spaces. This is a feat which was previously thought intractable. We believe that the highly promising performance of the action branching architecture in scaling DQN and its potential generality evoke further theoretical and empirical investigations. Unde doloremque quod facere, minus alias harum, ratione possimus est velit eum error a, aperiam itaque quibusdam vel cumque id impedit nam autem nihil, dolorem quas harum omnis libero. Error iste maxime quo nostrum id, cumque numquam sed, perferendis consectetur illum impedit doloremque autem vero voluptas pariatur, ducimus reprehenderit porro dolorum rem possimus laborum sit a quibusdam? Alias libero quisquam

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