

Assignment 4

2.1

Criteria for equivalence of a lazy list or generator :

The first item in both of the lists will be equal and the functions in the second item in the lists will be generator functions that are equivalent functions from the definition of functional equivalent

2.2

```
Const evensquares1=filterGen(mapGen(naturalNumber(), x=>x*x), x=>(x%2==0));
```

```
Const evensquares2= mapGen(filterGen(naturalNumber(), x=>x*x),  
x=>(x%2==0));
```

Criteria for equivalence of a lazy list or generator :

The first item in both of the lists will be equal and the functions in the second item in the lists will be generator functions that are equivalent functions from the definition of functional equivalent .

We will prove that evenSquire1 equivalent to evenSquare2 by induction on recursive calls.

Base: $n=1$: for evenSquire1 we will compute the map on the function $x*x$ and we will get 0 , the filter function return true and evenSquire1 return 0.

For evenSquire2 we will compute the filter function on 0 and return true than the map on the function $x*x$ and we will get 0 and evenSquire2 return 0.

Induction step : assume for n and prove for $n+1$ steps:

For the first n steps ,from the induction assumption $evensquire1=evensquire2$.

For the $n+1$ step ,

For the function `evenSquare1` we will compute the square of the number and then we will filter the odd numbers, a square of a number keeps its parity the same and the filter will drop the odd numbers.

the computation of `evenSquare2` is on the even number (if it takes an odd number the function of the filter will drop it) and after filter the odd numbers it will compute square on the even number.

We can see that we get the same value in the first n items and we get the same computation on the $n+1$ item.

So the functions are equivalent.

2.3

We will prove that `fib1` equals to `fib2` by induction on the recursive steps.

Base: $n=0$:

For `fib1`: we will call to `fibGen` with the values 0 and 1 and will build a lazy list that the first element is 0 and the second element is procedure of the sum of 1 and 0;

For `fib2`: we will build a lazy list that its first element is 0 and the second is a procedure.

Base $n=1$:

For `fib1`: we will apply the procedure on the list from the previous step and get a lazy list that the first item is the sum of 0 and 1 and that the second item in Fibonacci series, and the second item in the list is a procedure that calls `fibGen` with the current item and the sum of the current item and the previous item.

For `fib2`: we will apply the procedure on the list from the previous step and get a lazy list that has the value 1 and the second item is procedure that calls `lz-lst-add` that gets 2 lazy lists that one of them is `fib2` and the other one is the tail of `fib2` and compute the sum of the two heads of the lists and return a lazy list that its first part of it is the sum of the heads and the other one is function that calls recursively to `lz-lst-add` with the tail of both lists.

Induction assumption: assume the correctness on n steps and prove on $n+1$ steps.

For `fib1`: for the $n+1$ item in Fibonacci series, for the n steps from the induction assumption we will get the n number in Fibonacci series and for the $n+1$ item we will sum the value on the n place in the list and the $n-1$ and get the $n+1$ number in Fibonacci series that process is the same to base case 1.

For `fib2`: for the $n+1$ item in Fibonacci series, for the n steps from the induction assumption we will get the n number in Fibonacci series and for the $n+1$ item we will pay attention that in order to calculate the n number and the $n-1$ number in Fibonacci series from the induction assumption we will get two lazy lists with that the first item is n and $n-1$ items in Fibonacci series and when we send those lists to the function `lz-lst-add` we will get a lazy list that the

first item is the sum of n and n-1 and we will get the n+1 item is Fibonacci series and the second item is a procedure that get the tail that call lz-lst-add with the tail of the two list .

For conclusion both function return the same values.

3.2

נוכיח כי. $(\text{append\$ lst1 lst2 cont}) = (\text{cont} (\text{append lst1 lst2}))$
 נוכיח באינדוקציה על אורך הרשימה - lst1. נסמן אורך זה כ: $|lst1|$

בסיס:

$|lst1|=0$ כלומר מדובר ברשימה ריקה לכן:

$AE[(\text{append\$ lst1 lst2 cont})] ==>$

$AE[(\text{if} (\text{null? lst1'}) (\text{cont lst2'})$

$(\text{append\$} (\text{cdr lst1'}) lst2'$

$(\text{lambda} (res) (\text{cont} (\text{cons} (\text{car lst1'}) res))))] ==>$

If is special form – $AE[(\text{null? lst1'})] = \#t$

Therefore :

$AE[(\text{append\$ lst1 lst2 cont})] = AE[(\text{cont lst2'})]$

$AE[(\text{cont} (\text{append lst1 lst2}))] ==>$

$AE[(\text{append lst1 lst2})] = AE[(\text{if} (\text{null? lst1'})$
 $lst2'$
 $(\text{cons} (\text{car lst1'})$
 $(\text{append} (\text{cdr lst1'}) lst2')))]$

= if is special form – $AE[(\text{null? lst1})] = \#t$

Therefore : $AE[(\text{append lst1 lst2})] = AE[lst2'] = lst2'$

$AE[(\text{cont} (\text{append lst1 lst2}))] = AE[(\text{cont lst2'})]$

Therefore: $AE[(\text{cont} (\text{append lst1 lst2}))] = AE[(\text{cont lst2'})] = AE[(\text{append\$ lst1 lst2 cont})]$

הוכחנו את מקרה הבסיס. נניח נכונות ל $|lst1| = n > 0$ ונוכיח ל $|lst1| = n+1$

$AE[(\text{append\$ lst1 lst2 cont})] ==>$

$AE[(\text{if} (\text{null? lst1'}) (\text{cont lst2'})$

(append\$ (cdr lst1') lst2'

(lambda (res) (cont (cons (car lst1') res))))]) ==>

If is special form – AE[(null? lst1')] = #f

Therefore :

AE[(append\$ lst1 lst2 cont)] = AE[(append\$ (cdr lst1') lst2'

(lambda (res) (cont (cons (car lst1') res))))]

ומהנחת האינדוקציה מתקיימת-

AE[(append\$ (cdr lst1') lst2'

(lambda (res) (cont (cons (car lst1') res))))] =

AE[((lambda (res) (cont (cons (car lst1') res))) (append (cdr lst1') lst2'))] =

AE[(cont (cons (car lst1') (append (cdr lst1') lst2')))] =

AE[(cont (append lst1' lst2'))]

(append\$ lst1 lst2 cont)=(cont (append lst1 lst2)). אזי מתקיים:

4b

1)

. unify[p(v(v(d(1), M, ntuf3), X)), p(v(d(B), v(B, ntuf3),

KtM))] Sub={} p=p so we unify inner AtomicFormula

v=v so we unify the inner AtomicFormula

the length of parameters of AtomicFormulas isn't equal so unify fail.

2)

b. unify[p(v(v(d(1), M, ntuf3), X)), p(v(d(B), v(B, ntuf3), ntuf3))]

Sub={} p=p so we unify inner AtomicFormula

v=v so we unify the inner AtomicFormula

the length of parameters of AtomicFormulas isn't equal so unify fail.

3)

c. $\text{unify}[p(v(v(d(M), M, \text{ntuf3}), X)), p(v(d(B), v(B, \text{ntuf3}), \text{KtM}))]$

$\text{Sub}=\{\}$ $p=p$ so we unify inner AtomicFormula

$v=v$ so we unify the inner AtomicFormula

the length of parameters of AtomicFormulas isn't equal so unify fail.

4)

$\text{unify}[p(v(v(d(1M, p), X)), p(v(d(B), v(B, \text{ntuf3}), \text{KtM}))]$

$\text{Sub}=\{\}$ $p=p$ so we unify inner AtomicFormula

$v=v$ so we unify the inner AtomicFormula

the length of parameters of AtomicFormulas isn't equal so unify fail.

