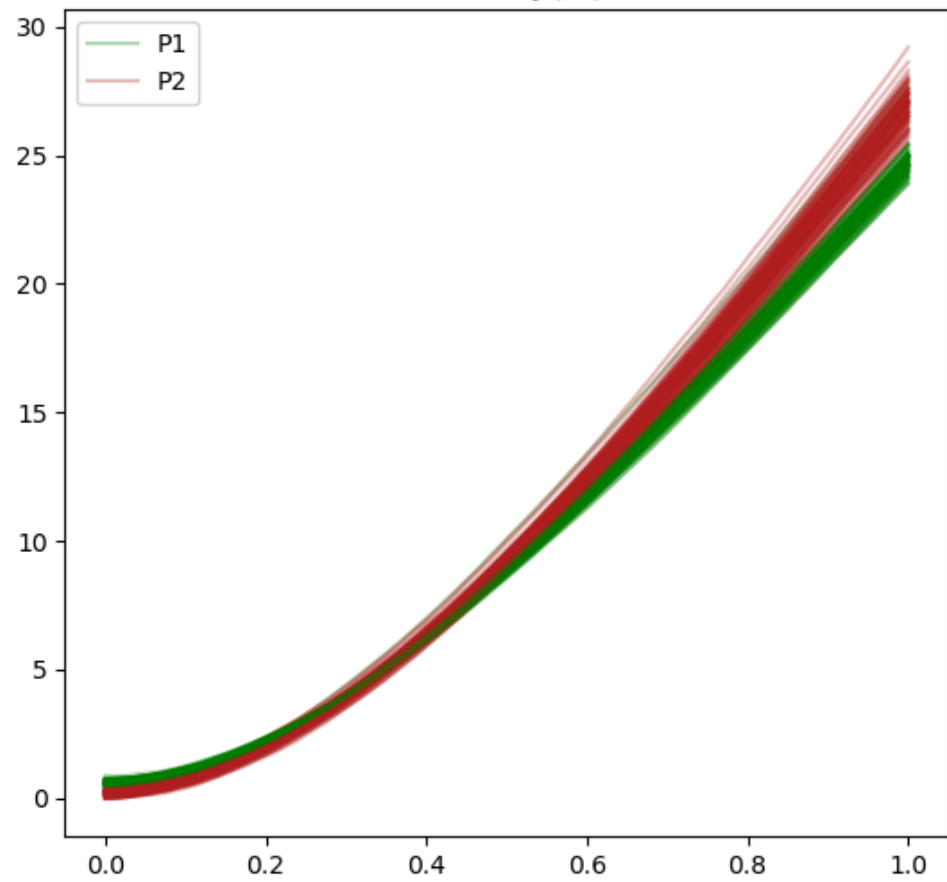


minmax: all
 target: ind
 loss: BCELogits: 1*loss
 trick: $v_{\tilde{t}}, u_{\tilde{t}}, y_{\tilde{t}} = \text{logit}(v, u, y)$

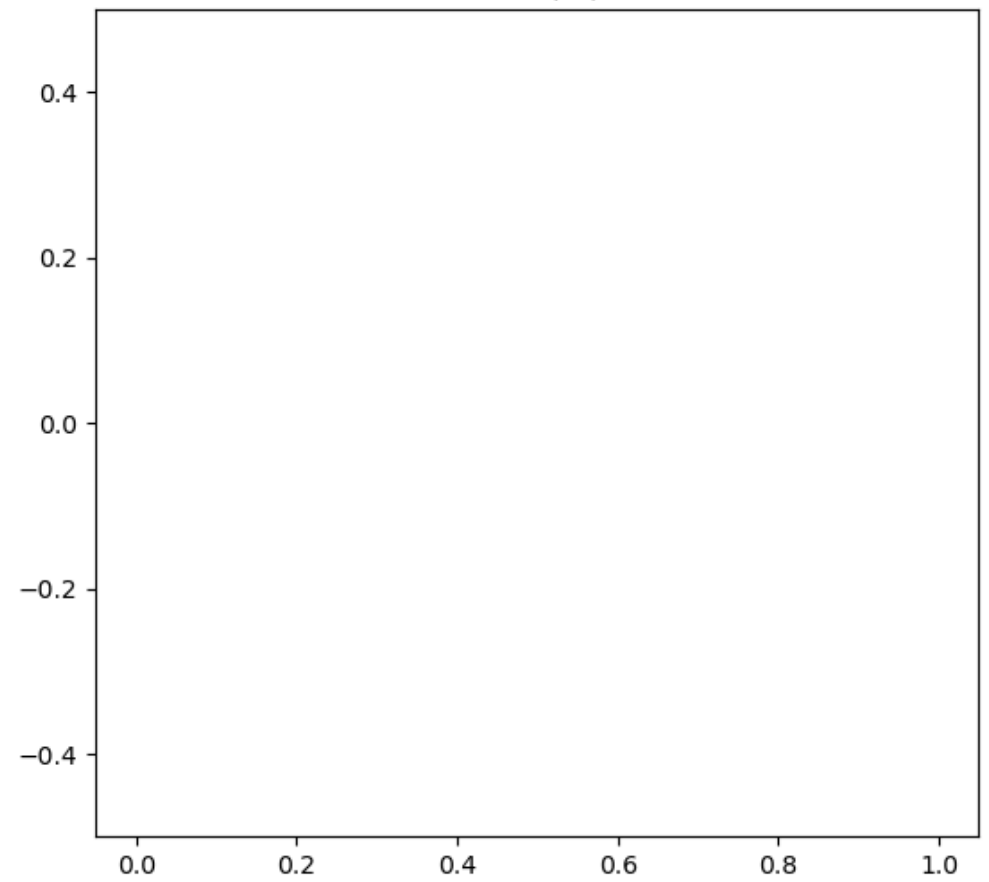
300 steps

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Inventory(X_t)



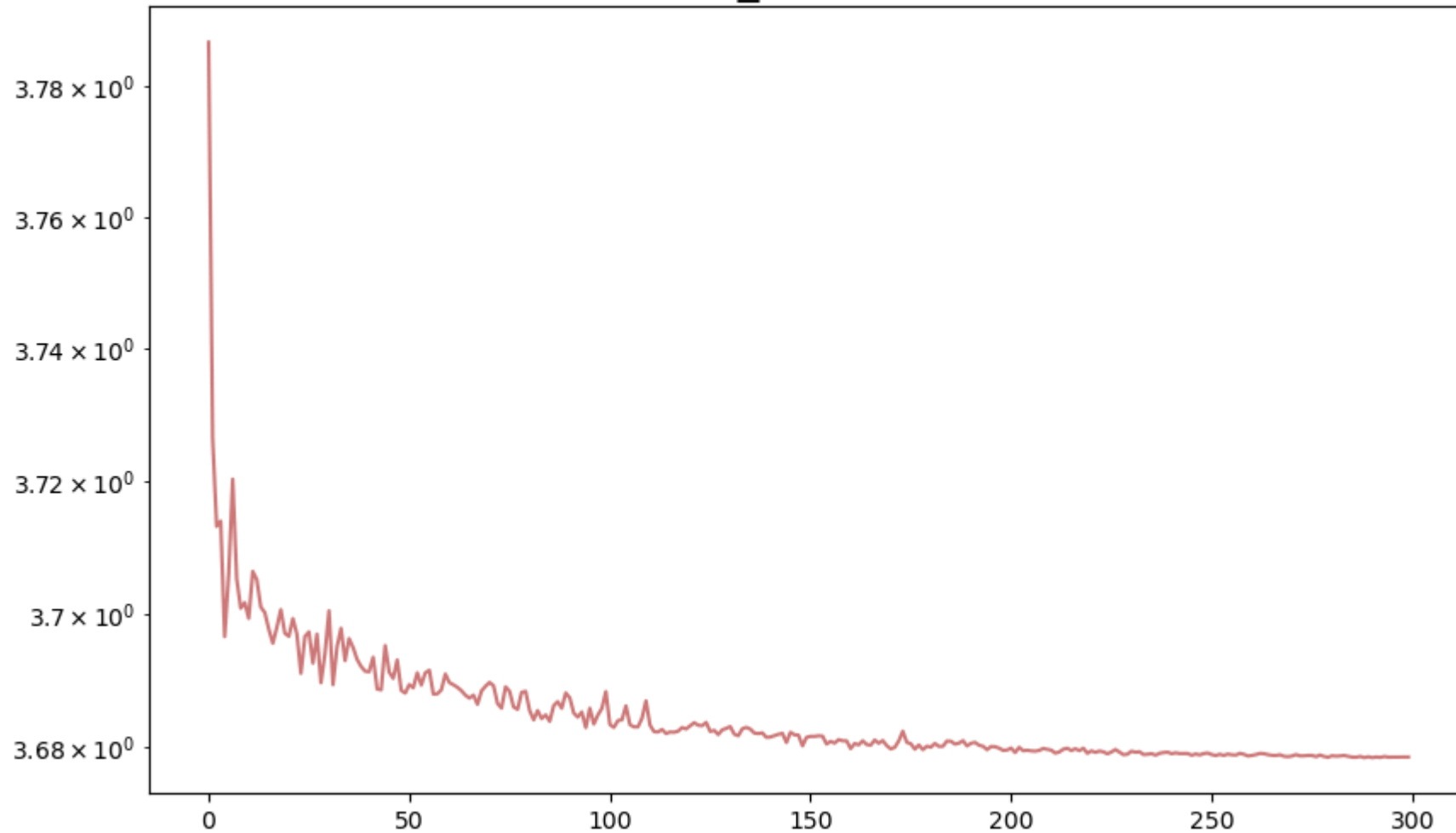
Price(S_t)



Batch Number: 300
Average Error Est: 3.6786077880859374

```
In [ ]: plot=plot_results(pop1_dict=pop1_dict, pop2_dict=pop2_dict, loss=forward_losses)
plot.FwdLoss(log=True)
plot.Inventory_And_Price()
plot.Decomposition_Inventory()
plot.Terminal_Convergence()
```

Forward_Loss vs Batch

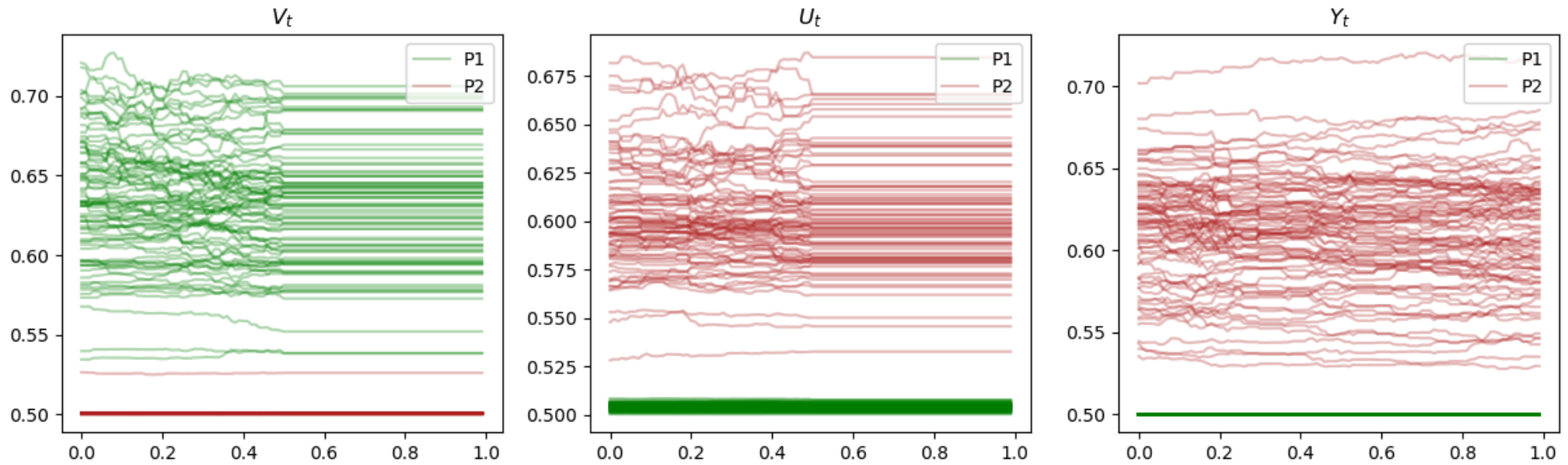


```

t=np.array([i for i in range(NT2)]) * dt
for i in range(80):
    ax5=plt.plot(t, pop1_path_dict['y'][i,:NT2], color="green", alpha=0.3)
    ax6=plt.plot( t, pop2_path_dict['y'][i,:NT2], color="firebrick", alpha=0.3)
plt.legend({'P1':ax5, 'P2':ax6})

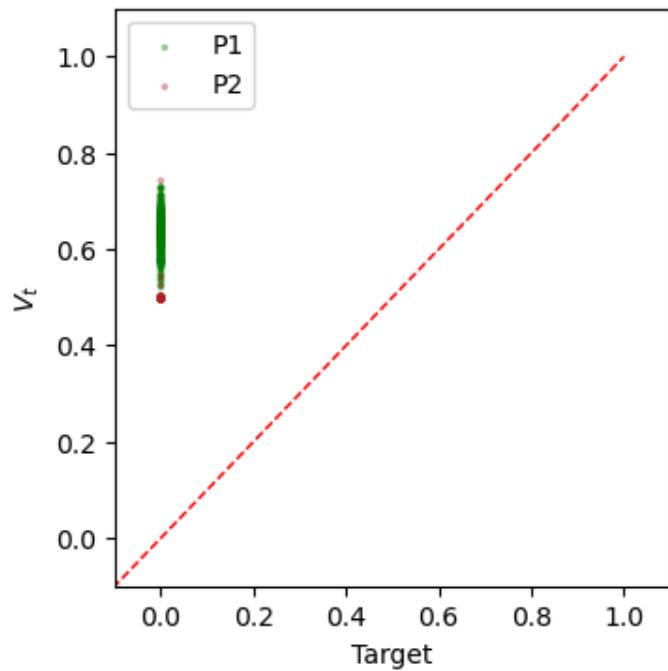
```

Out[]: <matplotlib.legend.Legend at 0x11b1a5fd0>

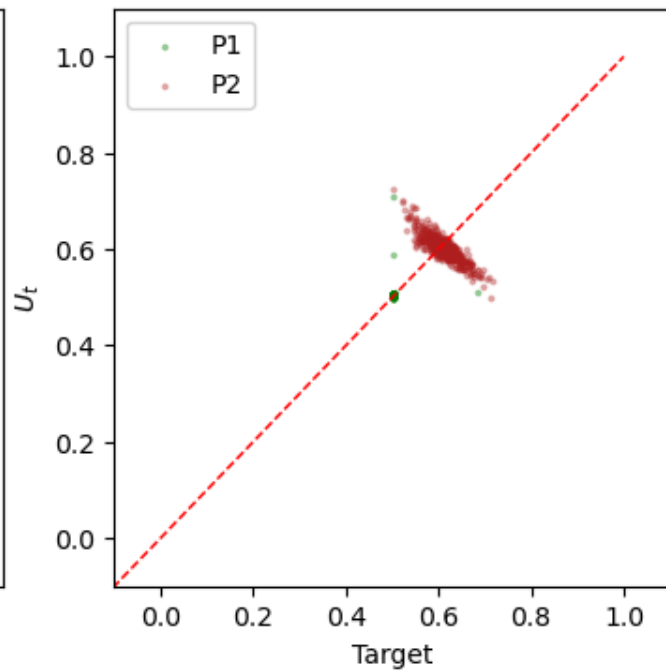


In []:

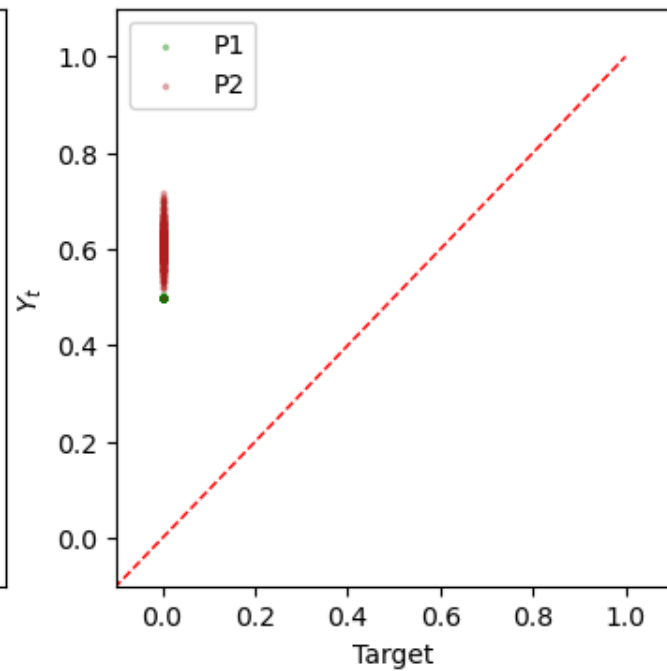
QQ-Plot of V_t



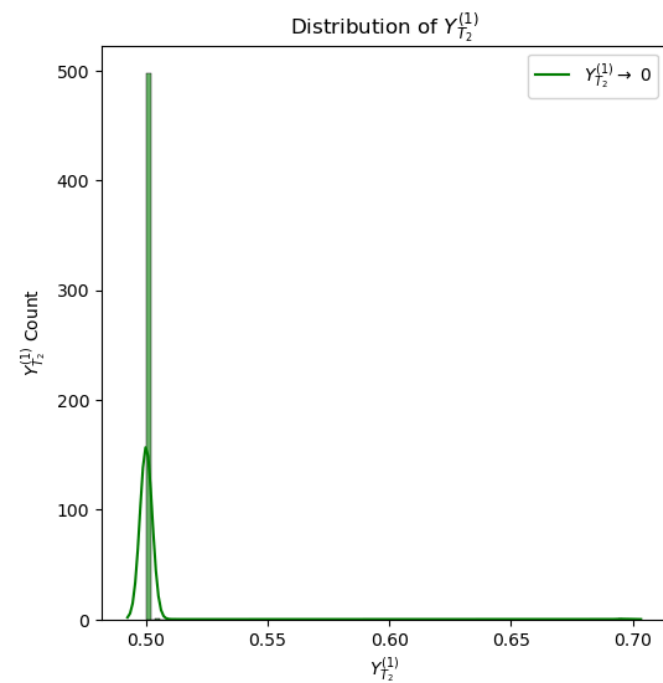
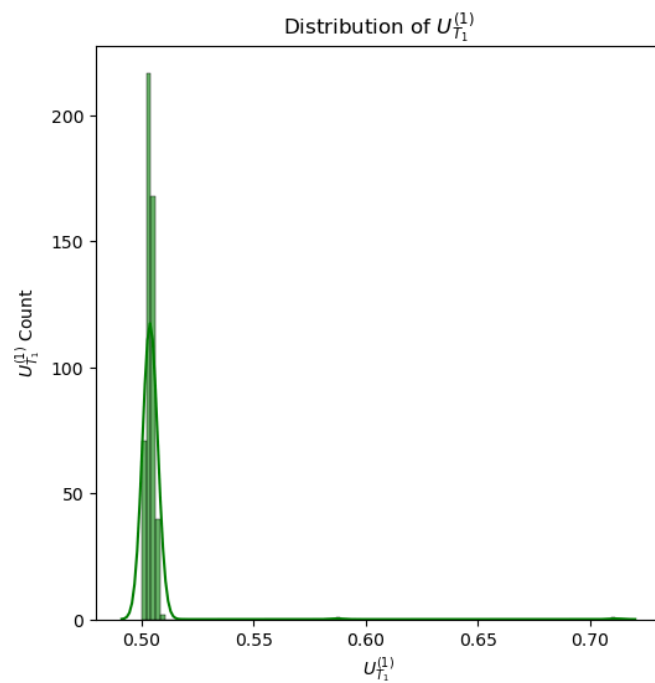
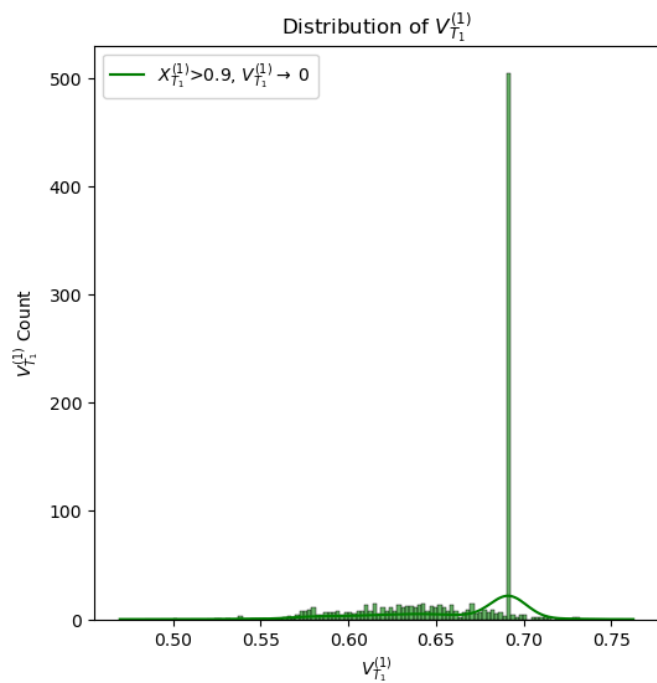
QQ-Plot of U_t

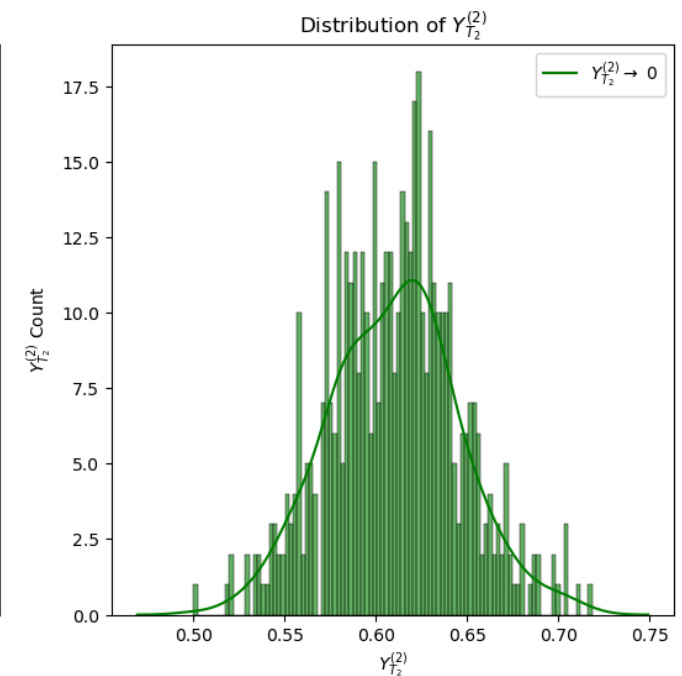
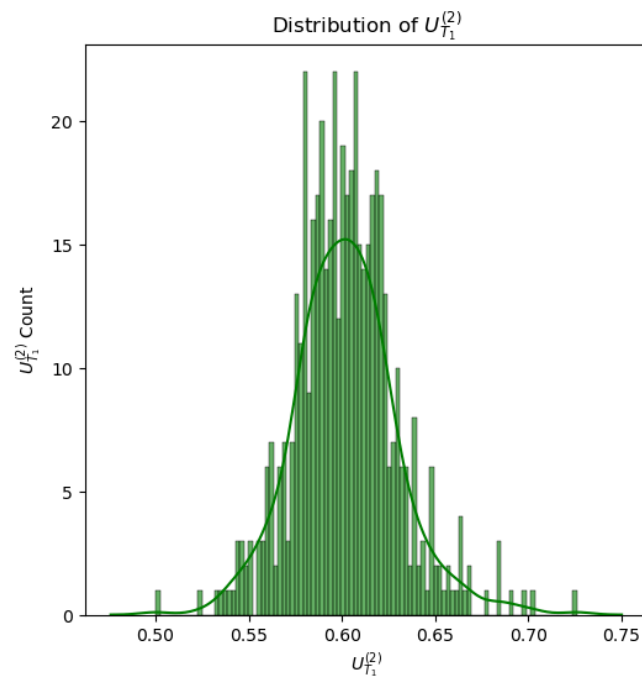
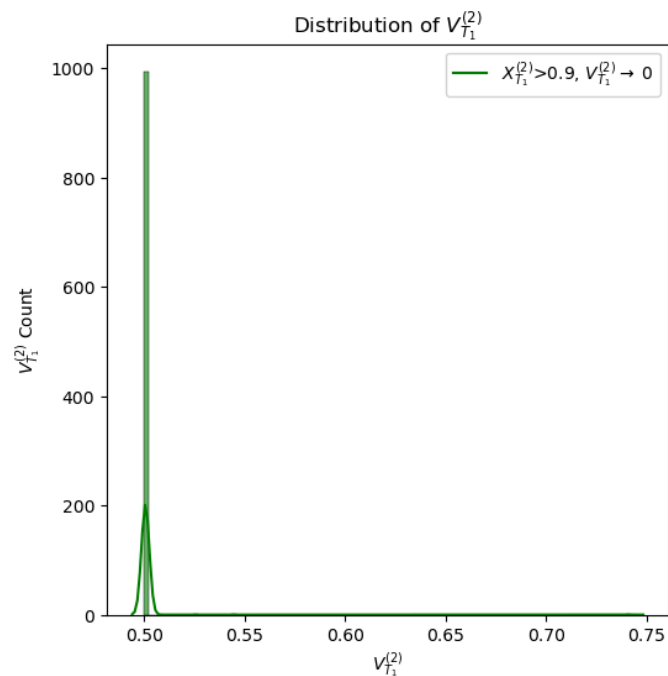


QQ-Plot of Y_t



Convergency - P1





Save The Models

```
In [ ]: print(f"{len(main_models1.loss)} steps\nStarted @ {start_time}\nSaved @ {datetime.now().strftime('%B %d - %H:%M:%S')}") ## to
dir_path=pathlib.Path(os.getcwd(),
                        'Results',
                        'Best Models Saved',
                        'Adamax_minmax_logit_0.01lr_300steps_BCELogits_1')

dir_path.mkdir()
path1=pathlib.Path(dir_path,'pop1.pt')
path2=pathlib.Path(dir_path,'pop2.pt')
main_models1.save_entire_models(path=path1)
main_models2.save_entire_models(path=path2)
```

300 steps

Saved @ August 01 - 02:27:46

Load The Models

```
In [ ]: # dir_path=pathlib.Path(os.getcwd(),'Results','Best Models Saved','Adamax_logit_0.05delta_0.01lr_500steps_BCE')
# path1=pathlib.Path(dir_path,'pop1.pt')
# path2=pathlib.Path(dir_path,'pop2.pt')
```

```

In [ ]: import numpy as np
import torch as torch
import torch.nn as nn
import torch.nn.functional as F
import torch.optim as optim
import seaborn as sns
import pandas as pd
import matplotlib.pyplot as plt
from datetime import datetime
import random
from scipy.stats import norm

import os
import pathlib

from Model import *
from utils import *

torch.autograd.set_detect_anomaly(True)
start_time=datetime.now().strftime('%B %d - %H:%M:%S')

```

```

Out[ ]: <torch.autograd.anomaly_mode.set_detect_anomaly at 0x317be1210>

```

```

In [ ]: #Global parameters
GlobalParams1=Params(param_type='k1',target_type='indicator',trick='logit',loss_type='BCEWithLogitsLoss',delta=0.03,K=0.9,lr=0.
dB1 = SampleBMIncr(GlobalParams=GlobalParams1)
init_x1 = Sample_Init(GlobalParams=GlobalParams1)
init_c1= torch.zeros_like(init_x1)

GlobalParams2=Params(param_type='k2',target_type='indicator',trick='logit',loss_type='BCEWithLogitsLoss',delta=0.03,K=0.9,lr=0.
dB2 = SampleBMIncr(GlobalParams=GlobalParams2)  ## TODO: same dB?????
init_x2 = Sample_Init(GlobalParams=GlobalParams2)
init_c2= torch.zeros_like(init_x2)

NT1=GlobalParams1.NT1
NT2=GlobalParams1.NT2
dt=GlobalParams1.dt
device=GlobalParams1.device
learning_rate = GlobalParams1.lr

#Forward Loss
forward_losses = []

#How many batches

```

MaxBatch= 300

#How many optimization steps per batch

OptimSteps= 25

#Train on a single batch?

single_batch = True

#Set up main models for y0 and z (z will be list of models)

v0_model_main1 = Network()

u0_model_main1 = Network()

y0_model_main1 = Network()

zv_models_main1 = [Network() for i in range(NT1)]

zu_models_main1 = [Network() for i in range(NT1)]

zy_models_main1 = [Network() for i in range(NT2)]

main_models1=Main_Models(GlobalParams=GlobalParams1)

main_models1.create(v0_model=v0_model_main1,
 u0_model=u0_model_main1,
 y0_model=y0_model_main1,
 zv_models=zv_models_main1,
 zu_models=zu_models_main1,
 zy_models=zy_models_main1,
 forward_loss=forward_losses,
 dB=dB1,
 init_x=init_x1,
 init_c=init_c1)

v0_model_main2 = Network()

u0_model_main2 = Network()

y0_model_main2 = Network()

zv_models_main2 = [Network() for i in range(NT1)]

zu_models_main2 = [Network() for i in range(NT1)]

zy_models_main2 = [Network() for i in range(NT2)]

main_models2=Main_Models(GlobalParams=GlobalParams2)

main_models2.create(v0_model=v0_model_main2,
 u0_model=u0_model_main2,
 y0_model=y0_model_main2,
 zv_models=zv_models_main2,
 zu_models=zu_models_main2,
 zy_models=zy_models_main2,
 forward_loss=forward_losses,
 dB=dB2,
 init_x=init_x2,
 init_c=init_c2)


```

pop1_dict={'dB':dB1,
          'init_x':init_x1 ,
          'init_c':init_c1 ,
          'GlobalParams':GlobalParams1,
          'main_models':main_models1}

pop2_dict={'dB':dB2,
          'init_x':init_x2 ,
          'init_c':init_c2 ,
          'GlobalParams':GlobalParams2,
          'main_models':main_models2}

```

```

In [ ]: #Define optimization parameters
params=[]
params = list(main_models1.v0_model.parameters())+\
          list(main_models1.u0_model.parameters())+\
          list(main_models1.y0_model.parameters())+\
          list(main_models2.v0_model.parameters())+\
          list(main_models2.u0_model.parameters())+\
          list(main_models2.y0_model.parameters())
for i in range(NT1):
    params += list(main_models1.zv_models[i].parameters())
    params += list(main_models1.zu_models[i].parameters())
    params += list(main_models2.zv_models[i].parameters())
    params += list(main_models2.zu_models[i].parameters())

for i in range(NT2):
    params += list(main_models1.zy_models[i].parameters())
    params += list(main_models2.zy_models[i].parameters())

#Set up optimizer and scheduler
optimizer = optim.Adamax(params, lr=learning_rate)
scheduler = torch.optim.lr_scheduler.StepLR(optimizer, step_size=100, gamma=0.95)

for k in range(0,MaxBatch):

    print("Batch Number: ", k+1)
    sloss=0
    #optimize main network wrt the foward loss
    for l in range(0,OptimSteps):
        optimizer.zero_grad()
        loss = get_foward_loss(pop1_dict=pop1_dict, pop2_dict=pop2_dict)
        loss.backward()
        # torch.nn.utils.clip_grad_norm_(parameters=params,max_norm=0.7)
        optimizer.step()

```

```

    scheduler.step()
    nloss = loss.detach().numpy()
    sloss += nloss
    # print('OptimStep: ' + str(l+1))
    # print('forward_loss: ' + str(nloss))
avgloss = sloss/OptimSteps
print("Average Error Est: ", avgloss)
forward_losses.append(avgloss)

#Generate a new batch if using multiple batches
if(not single_batch):

    dB1 = SampleBMIncr(GlobalParams=GlobalParams1)
    init_x1 = Sample_Init(GlobalParams=GlobalParams1)
    init_c1= torch.zeros_like(init_x1)
    pop1_dict={'dB':dB1,
               'init_x':init_x1 ,
               'init_c':init_c1 ,
               'GlobalParams':GlobalParams1,
               'main_models':main_models1}

    dB2 = SampleBMIncr(GlobalParams=GlobalParams2)  ## TODO: same dB?????
    init_x2 = Sample_Init(GlobalParams=GlobalParams2)
    init_c2= torch.zeros_like(init_x2)
    pop2_dict={'dB':dB2,
               'init_x':init_x2 ,
               'init_c':init_c2 ,
               'GlobalParams':GlobalParams2,
               'main_models':main_models2}

```

```

# model_dict1=main_models1.load_entire_models(path=path1,overwrite=True)
# model_dict2=main_models2.load_entire_models(path=path2,overwrite=True)

# pop1_dict={'dB':main_models1.dB,
#           'init_x':main_models1.init_x ,
#           'init_c':main_models1.init_c ,
#           'GlobalParams':main_models1.GlobalParams,
#           'main_models':main_models1}

# pop2_dict={'dB':main_models2.dB,
#           'init_x':main_models2.init_x ,
#           'init_c':main_models2.init_c ,
#           'GlobalParams':main_models2.GlobalParams,
#           'main_models':main_models2}

```

```

In [ ]: # plot=plot_results(pop1_dict=pop1_dict,pop2_dict=pop2_dict,loss=main_models1.loss)
# plot.FwdLoss(log=True)
# plot.Integrate_Inventory()
# plot.Decomposition_Inventory(base_rate=True,market_price=True)
# plot.Terminal_Convergence()
# print(datetime.now().strftime("%B %d - %H:%M:%S"))

```

Loss Scale

```

In [ ]: pop1_path_dict,pop2_path_dict=get_target_path(pop1_dict=pop1_dict,pop2_dict=pop2_dict)
plt.figure(figsize=(15,4))
plt.subplot(131)
plt.title("$V_t$")
t=np.array([i for i in range(NT2)]) * dt
for i in range(80):
    ax1=plt.plot(t, pop1_path_dict['v'][i,:NT2], color="green", alpha=0.3)
    ax2=plt.plot( t, pop2_path_dict['v'][i,:NT2], color="firebrick", alpha=0.3)
plt.legend({'P1':ax1,'P2':ax2})

plt.subplot(132)
plt.title("$U_t$")
t=np.array([i for i in range(NT2)]) * dt
for i in range(80):
    ax3=plt.plot(t, pop1_path_dict['u'][i,:NT2], color="green", alpha=0.3)
    ax4=plt.plot( t, pop2_path_dict['u'][i,:NT2], color="firebrick", alpha=0.3)
plt.legend({'P1':ax3,'P2':ax4})

plt.subplot(133)
plt.title("$Y_t$")

```