```
In [ ]: import numpy as np
        import torch as torch
        import torch.nn as nn
        import torch.nn.functional as F
        import torch.optim as optim
        import seaborn as sns
        import pandas as pd
        import matplotlib.pyplot as plt
        from datetime import datetime
        import random
        from scipy.stats import norm
        import os
        import pathlib
        from Model import *
        from utils import *
        torch.autograd.set detect anomaly(True)
        start time=datetime.now().strftime('%B %d - %H:%M:%S')
In [ ]: #Global parameters
        GlobalParams1=Params(param_type='k1',target_type='indicator',trick='clamp',loss_type='BCELoss',delta=0.01,w=1,lr=0.0001)
        dB1 = SampleBMIncr(GlobalParams=GlobalParams1)
        init x1 = Sample Init(GlobalParams=GlobalParams1)
        init c1= torch.zeros like(init x1)
        GlobalParams2=Params(param type='k2',target type='indicator',trick='clamp',loss type='BCELoss',delta=0.01,w=1,lr=0.0001)
        dB2 = SampleBMIncr(GlobalParams=GlobalParams2) ## TODO: same dB?????
        init_x2 = Sample_Init(GlobalParams=GlobalParams2)
        init c2= torch.zeros like(init x2)
        NT1=GlobalParams1.NT1
        NT2=GlobalParams1.NT2
        dt=GlobalParams1.dt
        device=GlobalParams1.device
        learning rate = GlobalParams1.lr
        #Forward Loss
        forward_losses = []
        #How many batches
        MaxBatch= 750
        #How many optimization steps per batch
        OptimSteps= 25
        #Train on a single batch?
        single batch = True
```

```
#Set up main models for y0 and z (z will be list of models)
v0 model main1 = Network(scaler type='sigmoid')
u0 model main1 = Network(scaler type='sigmoid')
y0 model main1 = Network(scaler type='sigmoid')
zv models main1 = [Network() for i in range(NT1)]
zu models main1 = [Network() for i in range(NT1)]
zy models main1 = [Network() for i in range(NT2)]
main models1=Main Models(GlobalParams=GlobalParams1)
main models1.create(v0 model=v0 model main1,
                    u0 model=u0 model main1,
                    y0 model=y0 model main1,
                    zv models=zv models main1,
                    zu models=zu models main1,
                    zv models=zv models main1.
                    forward loss=forward losses,
                    dB=dB1,
                    init_x=init_x1,
                    init c=init c1)
v0 model main2 = Network(scaler type='sigmoid')
u0 model main2 = Network(scaler type='sigmoid')
y0 model main2 = Network(scaler type='sigmoid')
zv models main2 = [Network() for i in range(NT1)]
zu models main2 = [Network() for i in range(NT1)]
zy models main2 = [Network() for i in range(NT2)]
main models2=Main Models(GlobalParams=GlobalParams2)
main models2.create(v0 model=v0 model main2,
                    u0 model=u0 model main2,
                    y0_model=y0_model_main2,
                    zv models=zv models main2,
                    zu models=zu models main2,
                    zv models=zv models main2,
                    forward loss=forward losses,
                    dB=dB2.
                    init_x=init_x2,
                    init c=init c2)
pop1_dict={'dB':dB1,
            'init_x':init_x1 ,
            'init c':init c1 ,
           'GlobalParams':GlobalParams1,
            'main models':main models1}
pop2 dict={'dB':dB2,
            'init_x':init_x2 ,
           'init c':init c2 ,
            'GlobalParams':GlobalParams2,
            'main models':main models2}
```

```
In [ ]: #Define optimization parameters
        params=[]
        params = list(main models1.v0 model.parameters())+\
                 list(main models1.u0 model.parameters())+\
                 list(main models1.y0 model.parameters())+\
                 list(main models2.v0 model.parameters())+\
                 list(main models2.u0 model.parameters())+\
                 list(main models2.y0 model.parameters())
        for i in range(NT1):
            params += list(main models1.zv models[i].parameters())
            params += list(main models1.zu models[i].parameters())
            params += list(main models2.zv models[i].parameters())
            params += list(main models2.zu models[i].parameters())
        for i in range(NT2):
            params += list(main models1.zv models[i].parameters())
            params += list(main models2.zv models[i].parameters())
        #Set up optimizer and scheduler
        optimizer = optim.Adamax(params, lr=learning rate)
        scheduler = torch.optim.lr scheduler.StepLR(optimizer, step size=100, gamma=0.95)
        for k in range(0,MaxBatch):
            print("Batch Number: ", k+1)
            sloss=0
            #optimize main network wrt the foward loss
            for l in range(0,0ptimSteps):
                optimizer.zero grad()
                loss = get foward loss(pop1 dict=pop1 dict, pop2 dict=pop2 dict)
                loss.backward()
                # torch.nn.utils.clip grad norm (parameters=params, max norm=0.7)
                optimizer.step()
                scheduler.step()
                nloss = loss.detach().numpy()
                sloss += nloss
                # print('OptimStep: '+ str(l+1))
                # print('forward_loss: ' + str(nloss))
            avgloss = sloss/OptimSteps
            print("Average Error Est: ", avgloss)
            forward losses.append(avgloss)
            #Generate a new batch if using multiple batches
            if(not single batch):
                dB1 = SampleBMIncr(GlobalParams=GlobalParams1)
                init x1 = Sample Init(GlobalParams=GlobalParams1)
                init_c1= torch.zeros_like(init_x1)
                pop1_dict={'dB':dB1,
                         'init x':init x1 ,
                        'init_c':init_c1 ,
```

```
'GlobalParams':GlobalParams1,
    'main_models':main_models1}

dB2 = SampleBMIncr(GlobalParams=GlobalParams2) ## TODO: same dB?????
init_x2 = Sample_Init(GlobalParams=GlobalParams2)
init_c2= torch.zeros_like(init_x2)
pop2_dict={'dB':dB2,
    'init_x':init_x2,
    'init_c':init_c2,
    'GlobalParams':GlobalParams2,
    'main_models':main_models2}
```

Batch Number:	511	
Average Error	Est:	1.6824539709091186
Batch Number:	512	
Average Error	Est:	1.6865029382705687
Batch Number:	513	
Average Error	Est:	1.684301724433899
Batch Number:	514	
Average Error	Est:	1.6838127660751343
Batch Number:	515	
Average Error	Est:	1.6852887630462647
Batch Number:	516	
Average Error	Est:	1.6869824409484864
Batch Number:	517	
Average Error	Est:	1.685720772743225
Batch Number:	518	
Average Error		1.683901653289795
Batch Number:	519	1 (02(001101(1000
Average Error	Est:	1.6836091184616089
Batch Number:	520 Eat.	1.6861657094955445
Average Error Batch Number:	Est: 521	1.000103/094933443
Average Error	Est:	1.6839993810653686
Batch Number:	522	1.0059995010055000
Average Error	Est:	1.6859577989578247
Batch Number:	523	110033377303370217
Average Error	Est:	1.6876707649230958
Batch Number:	524	
Average Error	Est:	1.68301260471344
Batch Number:	525	
Average Error	Est:	1.6881186294555663
Batch Number:	526	
Average Error	Est:	1.6858909606933594
Batch Number:	527	
Average Error	Est:	1.6855929899215698
Batch Number:	528	4 6024070760245450
Average Error	Est:	1.6834970760345458
Batch Number:	529	1 6062510200602610
Average Error Batch Number:	Est:	1.6862510299682618
	530 Ect:	1.6863108444213868
Average Error Batch Number:	531	1.0003100444213000
Average Error		1.6869402360916137
Batch Number:		110005402500510157
Average Error		1.6851856184005738
Batch Number:		110031030101003730
Average Error		1.6861200046539306
Batch Number:		
Average Error		1.6854363012313842
Batch Number:	535	
Average Error	Est:	1.6847105503082276
Batch Number:	536	

Average Error Batch Number:	Est: 537	1.688040804862976
Average Error Batch Number:		1.6848394203186035
Average Error Batch Number:	Est: 539	1.6905893564224244
Average Error Batch Number:	Est: 540	1.6880903100967408
Average Error Batch Number:	Est: 541	1.687672996520996
Average Error Batch Number:	Est: 542	1.6845133590698242
Average Error Batch Number:	Est: 543	1.6838258123397827
Average Error Batch Number:	544	1.6850829601287842
Average Error Batch Number:	545	1.6830358219146728
Average Error Batch Number: Average Error	Est: 546 Est:	1.6877766895294188 1.6819846439361572
Batch Number: Average Error	547	1.6824767303466797
Batch Number: Average Error	548	1.6843154907226563
Batch Number: Average Error	549	1.686055154800415
Batch Number: Average Error	550 Est:	1.6807348537445068
Batch Number: Average Error	551 Est:	1.6849817371368407
Batch Number: Average Error	552 Est:	1.6858178520202636
Batch Number: Average Error		1.6840467929840088
Batch Number: Average Error Batch Number:	Est:	1.6850014543533325
Average Error Batch Number:		1.6862866020202636
Average Error Batch Number:	Est:	1.6829587316513062
Average Error Batch Number:	Est:	1.685247507095337
Average Error Batch Number:	Est:	1.685205111503601
Average Error Batch Number:	Est: 560	1.6863167142868043
Average Error Batch Number:	561	1.6792222452163696
Average Error	Est:	1.6849729442596435

Batch Number:	562	
Average Error	Est:	1.6844683408737182
Batch Number:	563	
Average Error	Est:	1.6848991107940674
Batch Number:	564	
Average Error	Est:	1.6826937770843506
Batch Number:	565	
Average Error	Est:	1.6852263975143433
Batch Number:	566	
Average Error	Est:	1.6875631046295165
Batch Number:	567	
Average Error	Est:	1.6825312852859498
Batch Number:	568	
Average Error	Est:	1.6866102266311644
Batch Number:	569	
Average Error		1.6836942911148072
Batch Number:	570	
Average Error		1.6856303882598878
Batch Number:	571	
Average Error		1.6851705598831177
Batch Number:	572	1 (025 47007002424
Average Error	Est:	1.683547887802124
Batch Number:	573	1 6021574407606156
Average Error	Est:	1.6831574487686156
Batch Number:	574	1.6853477668762207
Average Error Batch Number:	Est: 575	1.00004//000/0220/
Average Error	Est:	1.6859348106384278
Batch Number:	576	1:0039340100304270
Average Error	Est:	1.6865145921707154
Batch Number:	577	110003113321707131
Average Error	Est:	1.687988429069519
Batch Number:	578	
Average Error	Est:	1.6861838483810425
Batch Number:	579	
Average Error	Est:	1.6853610801696777
Batch Number:	580	
Average Error	Est:	1.6885153579711913
Batch Number:	581	
Average Error	Est:	1.686638717651367
Batch Number:	582	
Average Error		1.6861371278762818
Batch Number:		
Average Error		1.6896436023712158
Batch Number:		
Average Error		1.6871112537384034
Batch Number:		
Average Error		1.6829937982559204
Batch Number:		4 (04000070750010
Average Error		1.6810900783538818
Batch Number:	587	

Average Error Batch Number:	Est: 588	1.6829934453964233
Average Error Batch Number:		1.6852147817611693
Average Error Batch Number:		1.6844466543197631
Average Error Batch Number:	Est: 591	1.683593430519104
Average Error Batch Number:	Est: 592	1.6839492893218995
Average Error Batch Number:	Est: 593	1.6814739608764648
Average Error Batch Number:	Est: 594	1.6864438915252686
Average Error Batch Number:		1.6801946020126344
Average Error Batch Number:		1.6818813848495484
Average Error Batch Number:	Est: 597	1.6812762880325318
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Average Error Batch Number:		1.6851806926727295
Average Error Batch Number:	Est: 600	1.682796883583069
Average Error Batch Number:	Est: 601	1.6848869514465332
Average Error Batch Number:	Est: 602	1.685491828918457
Average Error Batch Number:	Est: 603	1.6862303256988525
Average Error Batch Number:	Est: 604	1.6767702913284301
Average Error Batch Number:	Est:	1.6828896951675416
Average Error Batch Number:		1.6865469121932983
Average Error Batch Number:	Est:	1.6831800842285156
Average Error Batch Number:	Est:	1.6846273422241211
Average Error Batch Number:	Est:	1.685716052055359
Average Error Batch Number:	Est:	1.6838742208480835
Average Error Batch Number:	Est:	1.6888931846618653
Average Error Batch Number:	Est:	1.6852046060562134
Average Error		1.688194055557251

Batch Number:	613	
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Batch Number:	614	
Average Error	Est:	1.686228675842285
Batch Number:	615	
Average Error	Est:	1.6872141456604004
Batch Number:	616	
Average Error	Est:	1.6870223522186278
Batch Number:	617	
Average Error	Est:	1.6827640438079834
Batch Number:	618	
Average Error	Est:	1.6850918436050415
Batch Number:	619	
Average Error		1.6828772306442261
Batch Number:	620	
Average Error		1.688934144973755
Batch Number:	621	
Average Error		1.6815928649902343
Batch Number:	622	1 602442002202745
Average Error		1.682413902282715
Batch Number:	623	1.6860722732543945
Average Error Batch Number:	Est: 624	1.0000722732343943
Average Error	Est:	1.6873084163665772
Batch Number:	625	1:00/5004105005//2
Average Error		1.684215989112854
Batch Number:	626	11001213303112031
Average Error	Est:	1.6833538866043092
Batch Number:	627	
Average Error	Est:	1.6812486410140992
Batch Number:	628	
Average Error	Est:	1.6839825057983397
Batch Number:	629	
Average Error	Est:	1.681229591369629
Batch Number:	630	
Average Error		1.6797702169418336
Batch Number:	631	
Average Error		1.6853371858596802
Batch Number:	632	1 670506000601016
Average Error		1.679506883621216
Batch Number:	633	1 6704207026220566
Average Error		1.6794397926330566
Batch Number: Average Error		1.6761370277404786
Batch Number:		1.0/013/02//404/00
Average Error		1.674396014213562
Batch Number:		T:0/7550017Z15502
Average Error		1.6776970100402833
Batch Number:		
Average Error		1.676101622581482
Batch Number:	638	

Average Error Batch Number:	Est: 639	1.681574397087097
Average Error Batch Number:		1.6819225454330444
Average Error Batch Number:		1.6818053436279297
Average Error Batch Number:	Est: 642	1.6825605821609497
Average Error Batch Number:	Est: 643	1.6782325506210327
Average Error Batch Number:	Est: 644	1.6864886951446534
Average Error Batch Number:	Est: 645	1.6818683195114135
Average Error Batch Number:	646	1.6851281547546386
Average Error Batch Number:	647	1.6851215553283692
Average Error Batch Number:	648	1.687384376525879
Average Error Batch Number:	Est: 649	1.6805355310440064
Average Error	Est: 650 Est:	1.6880376958847045 1.6786086940765381
Average Error Batch Number: Average Error	651 Est:	1.6902610778808593
Batch Number: Average Error	652 Est:	1.6886256551742553
Batch Number: Average Error	653 Est:	1.6848976039886474
Batch Number: Average Error	654 Est:	1.6857871532440185
Batch Number: Average Error	655	1.6815054273605348
Batch Number: Average Error	656	1.6894613885879517
Batch Number: Average Error	657 Est:	1.6843632030487061
Batch Number: Average Error	Est:	1.6845126485824584
Batch Number: Average Error	Est:	1.685157494544983
Batch Number: Average Error	Est:	1.6840274810791016
Batch Number: Average Error	Est:	1.6913042497634887
Batch Number: Average Error Batch Number:	Est:	1.684259819984436
Average Error		1.6896032285690308

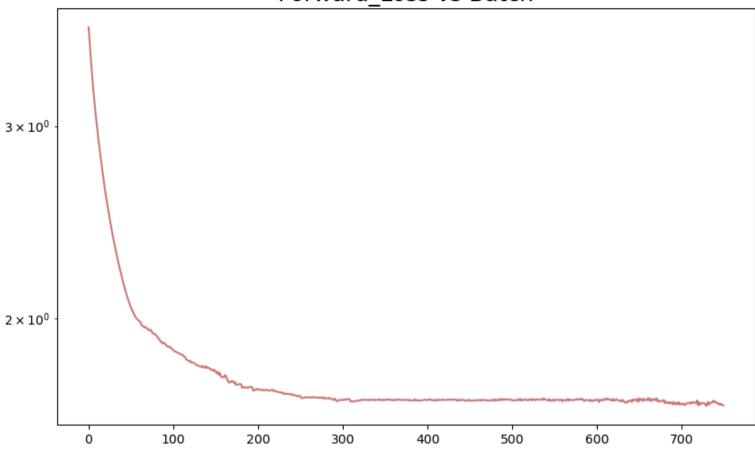
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Average Error	Est:	1.6816156911849975
Batch Number:	665	
Average Error	Est:	1.6872336673736572
Batch Number:	666	
Average Error	Est:	1.682069149017334
Batch Number:	667	
Average Error	Est:	1.6856876087188721
Batch Number:	668	
Average Error	Est:	1.6882993698120117
Batch Number:	669	
Average Error	Est:	1.6858474493026734
Batch Number:	670	
Average Error	Est:	1.6833963775634766
Batch Number:	671	
Average Error	Est:	1.6908513498306275
Batch Number:	672	
Average Error	Est:	1.6809662008285522
Batch Number:	673	
Average Error	Est:	1.6843592166900634
Batch Number:	674	4 6700564447442554
Average Error	Est:	1.6780561447143554
Batch Number:	675	1 6010701052011646
Average Error	Est: 676	1.6812781953811646
Batch Number:		1.681375036239624
Average Error Batch Number:	Est: 677	1.0013/3030239024
Average Error	Est:	1.6808476114273072
Batch Number:	678	1.00004/01142/30/2
Average Error	Est:	1.6797665166854858
Batch Number:	679	110737003100034030
Average Error	Est:	1.6836106491088867
Batch Number:	680	
Average Error	Est:	1.6845550298690797
Batch Number:	681	
Average Error	Est:	1.6731566429138183
Batch Number:	682	
Average Error	Est:	1.679128737449646
Batch Number:	683	
Average Error	Est:	1.675900831222534
Batch Number:	684	
Average Error	Est:	1.6745230770111084
Batch Number:	685	
Average Error	Est:	1.6719684648513793
Batch Number:	686	
Average Error		1.6771343660354614
Batch Number:	687	
Average Error		1.6738365507125854
Batch Number:		4 0000400
Average Error		1.6759105110168457
Batch Number:	689	

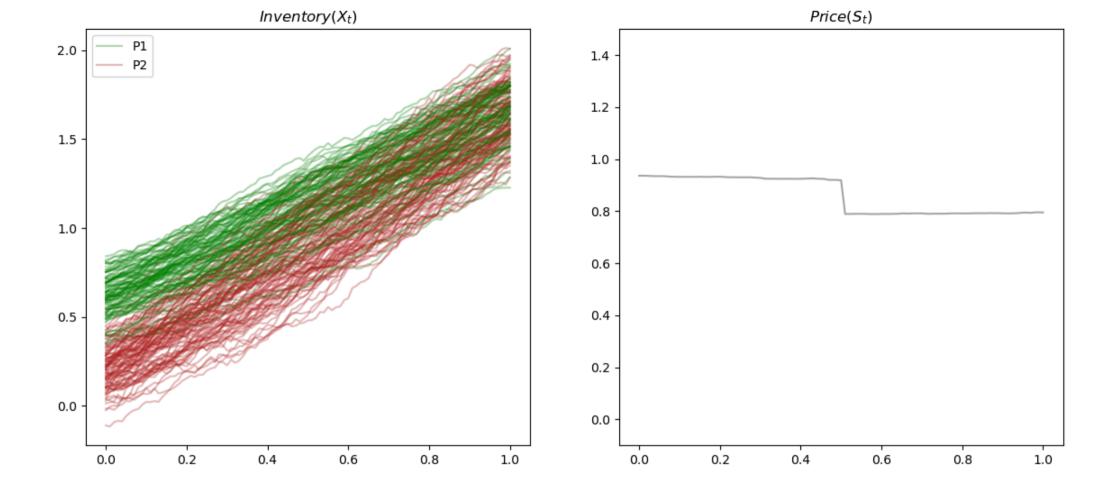
Average Error Batch Number:	Est: 690	1.6743533945083617
Average Error	Est:	1.6694537258148194
Batch Number: Average Error	691 Est:	1.6782470369338989
Batch Number: Average Error	692 Est:	1.6697843503952026
Batch Number:	693	
Average Error Batch Number:	Est: 694	1.6711703205108643
Average Error Batch Number:	Est: 695	1.6745183372497559
Average Error Batch Number:	Est: 696	1.6691656684875489
Average Error Batch Number:	Est: 697	1.6727126741409302
Average Error	Est:	1.6771802616119384
Batch Number: Average Error	698 Est:	1.6680183982849122
Batch Number: Average Error	699 Est:	1.672044849395752
Batch Number: Average Error	700 Est:	1.6694517087936402
Batch Number: Average Error	701 Est:	1.6715086364746095
Batch Number:	702	
Average Error Batch Number:	Est: 703	1.6681405019760132
Average Error Batch Number:	Est: 704	1.673098177909851
Average Error Batch Number:	Est: 705	1.6696885585784913
Average Error Batch Number:	Est: 706	1.6662631511688233
Average Error Batch Number:	Est:	1.6711353397369384
Average Error		1.6733931827545165
Batch Number: Average Error		1.673092474937439
Batch Number: Average Error		1.6752186584472657
Batch Number: Average Error		1.6720041513442994
Batch Number: Average Error	711	1.6752968072891234
Batch Number:	712	
Average Error Batch Number:	713	1.672436056137085
Average Error Batch Number:		1.6775158643722534
Average Error		1.6743745613098144

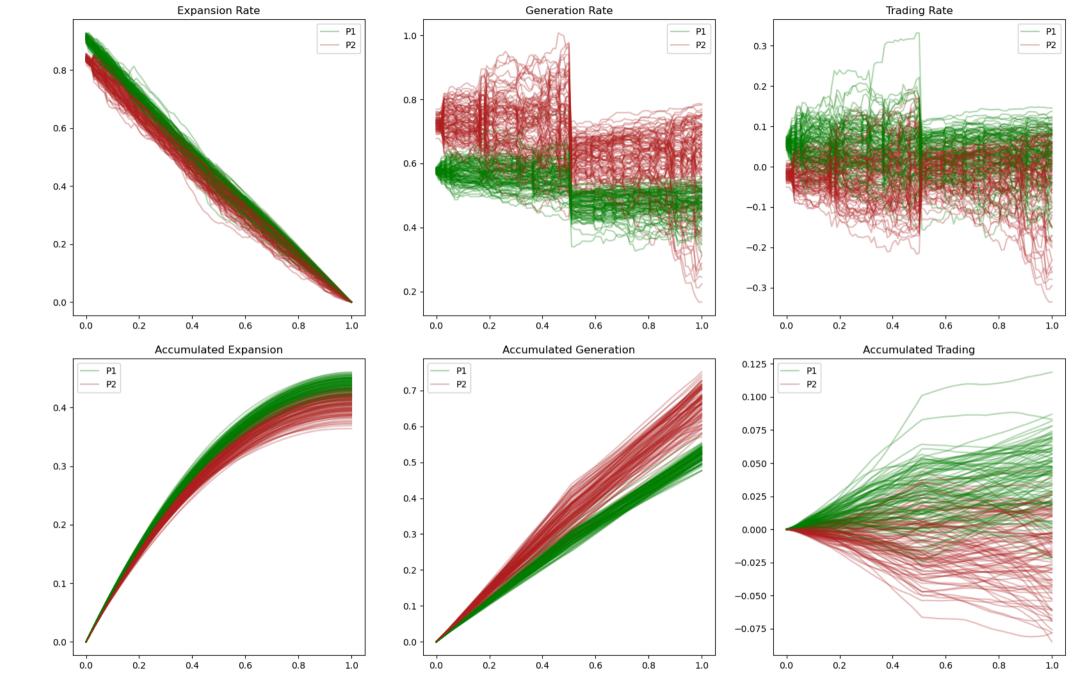
Batch Number:	715	
Average Error	Est:	1.6760258150100709
Batch Number:	716	
Average Error	Est:	1.6756342649459839
Batch Number:	717	
Average Error	Est:	1.672943639755249
Batch Number:	718	
Average Error	Est:	1.676301393508911
Batch Number:	719	
Average Error	Est:	1.683203854560852
Batch Number:	720	
Average Error	Est:	1.6661761045455932
Batch Number:	721	
Average Error	Est:	1.6763416051864624
Batch Number:	722	
Average Error	Est:	1.6670189094543457
Batch Number:	723	
Average Error	Est:	1.6738581132888795
Batch Number:	724	4 6722224426
Average Error	Est:	1.6723020458221436
Batch Number:	725	1 6725550520721426
Average Error Batch Number:	Est: 726	1.6725559520721436
Average Error	Est:	1.6734485340118408
Batch Number:	727	1.0/34403340110400
Average Error	Est:	1.673474612236023
Batch Number:	728	110/54/4012250025
Average Error	Est:	1.670504002571106
Batch Number:	729	11070301002371100
Average Error	Est:	1.670697979927063
Batch Number:	730	
Average Error	Est:	1.6634385442733766
Batch Number:	731	
Average Error	Est:	1.6711410522460937
Batch Number:	732	
Average Error	Est:	1.6782033967971801
Batch Number:	733	
Average Error	Est:	1.6678334045410157
Batch Number:	734	
Average Error		1.6719546031951904
Batch Number:	735	
Average Error		1.6749273538589478
Batch Number:	736	4 6755000007647006
Average Error		1.6755289697647096
Batch Number:	737	1 6755241100602740
Average Error		1.6755341100692749
Batch Number: Average Error	738 Est:	1.6819331073760986
Batch Number:	739	T.0013331013100300
Average Error		1.6775695896148681
Batch Number:	740	1.07,3033030170001
Daten Nambel :	, 10	

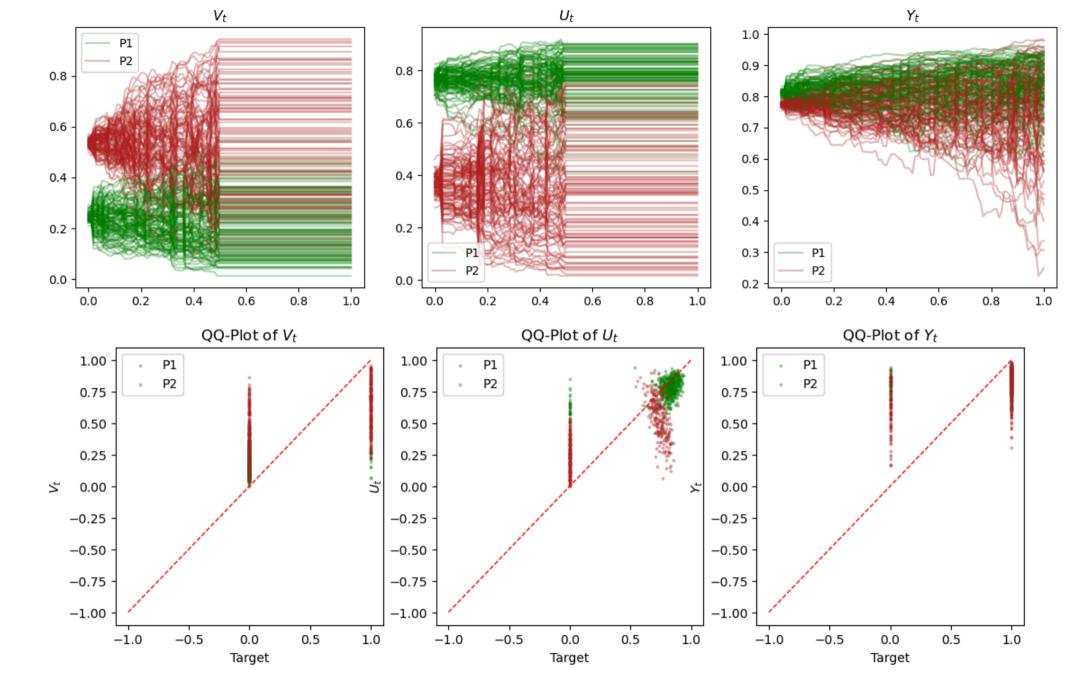
```
Average Error Est: 1.6803805255889892
       Batch Number: 741
       Average Error Est: 1.6775617504119873
       Batch Number: 742
       Average Error Est: 1.673789668083191
       Batch Number: 743
       Average Error Est: 1.6724073266983033
       Batch Number: 744
       Average Error Est: 1.6738758420944213
       Batch Number: 745
       Average Error Est: 1.6689344453811645
       Batch Number: 746
       Average Error Est: 1.667996597290039
       Batch Number: 747
       Average Error Est: 1.671448721885681
       Batch Number: 748
       Average Error Est: 1.6672642755508422
       Batch Number: 749
       Average Error Est: 1.667117977142334
       Batch Number: 750
       Average Error Est: 1.665627236366272
In []: plot=plot_results(pop1_dict=pop1_dict, pop2_dict=pop2_dict, loss=forward_losses)
        plot.FwdLoss(log=True)
        plot.Inventory_And_Price()
        plot.Decomposition Inventory()
        plot.Key Processes()
        plot.Terminal_Convergence()
```



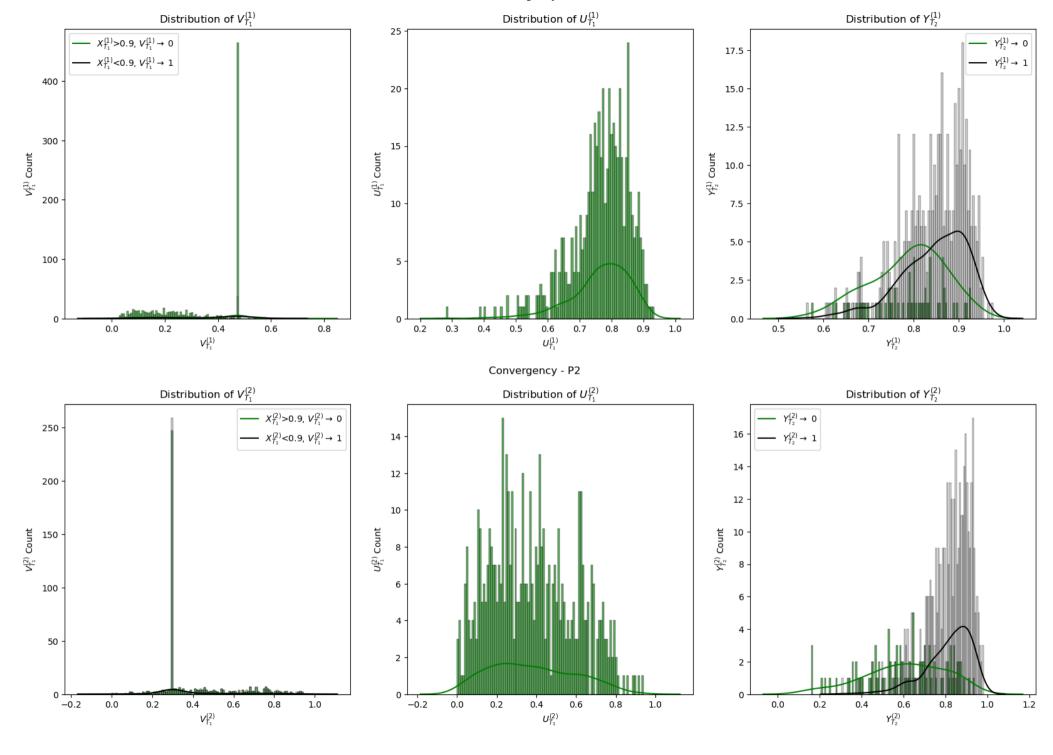








Convergency - P1



## Save The Models

## **Load The Models**

```
In []: # # GlobalParams1=Params(param_type='k1',target_type='indicator',trick='clamp',loss_type='MSELoss',delta=0.03,K=0.9,lr=0.01)
        ## GlobalParams2=Params(param type='k2',target type='indicator',trick='clamp',loss type='MSELoss',delta=0.03,K=0.9,lr=0.01)
        # models1=Main Models(GlobalParams=GlobalParams1)
        # models2=Main Models(GlobalParams=GlobalParams2)
        # path dir=pathlib.Path(os.getcwd(),
                                 "Results",
                                 "Best Models Saved",
                                 'minmax logit 0.01lr 300steps BCELogits 1 dt')
        # path1=pathlib.Path(path dir,'pop1.pt')
        # path2=pathlib.Path(path dir,'pop2.pt')
        # model dict1=models1.load entire models(path=path1,overwrite=True)
        # model dict2=models2.load entire models(path=path2,overwrite=True)
        # dB1=model_dict1['dB']
        # init x1=model dict1['init x']
        # init_c1=model_dict1['init_c']
        # pop1_dict= {'dB':dB1,
                       'init x':init x1,
                      'init c':init c1,
                      'GlobalParams':GlobalParams1,
                      'main models':models1}
        # dB2=model dict2['dB']
        # init_x2=model_dict2['init_x']
        # init c2=model dict2['init c']
        # pop2_dict= {'dB':dB2,
                      'init x':init x2 ,
                      'init c':init c2 ,
```

```
# 'GlobalParams':GlobalParams2,
    'main_models':models2}
# dt=GlobalParams1.dt
# NT1=GlobalParams1.NT1
# NT2=GlobalParams1.NT2
# NumTrain=GlobalParams1.NumTrain
# K=GlobalParams1.K
# loss=models1.loss
# plot=plot_results(pop1_dict=pop1_dict,pop2_dict=pop2_dict,loss=loss)
# plot.FwdLoss(log=True)
# plot.Inventory_And_Price()
# plot.Key_Processes()
# # plot.Terminal_Convergence()
```