



Numpy及其应用

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NumPy

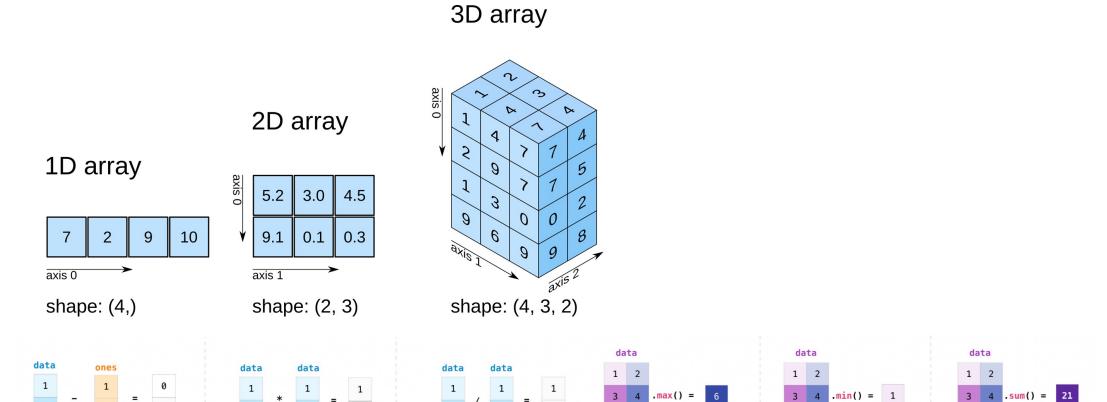


- NumPy is the fundamental package for scientific computing in Python.
 - a multidimensional array object
 - various derived objects (such as masked arrays and matrices)
 - an assortment of routines for fast operations on arrays, including mathematical, logical, shape manipulation, sorting, selecting, I/O, discrete Fourier transforms, basic linear algebra, basic statistical operations, random simulation and much more.



multi-dimensional array





https://numpy.org/doc/stable/user/absolute_beginners.html

NumPy ndarray v.s. Python List

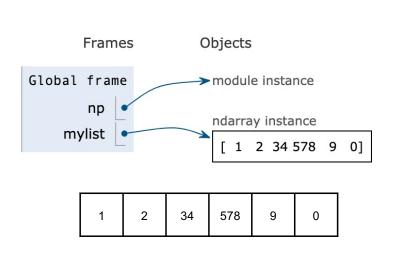


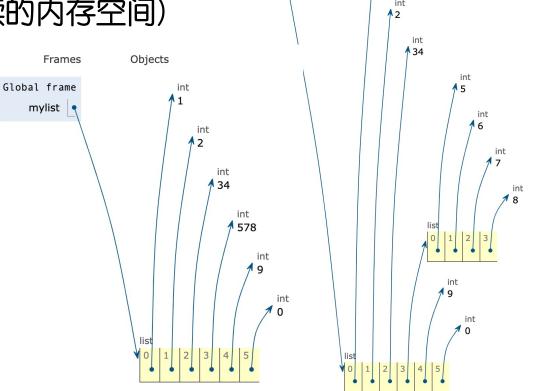
- 目标: 更高的计算效率
- 更高效的数据组织
 - 同类型元素 + 固定长度
- ・更高效的计算方式
 - 向量化编程 v.s. 循环
- ・实现和底层支持
 - 基于C的实现
 - 利用Basic Linear Algebra Subprograms, BLAS
 - Intel MTK、Open BLAS、CUDA等

NumPy Array v.s. Python List



- 数据组织上的差异
 - 更贴近C的数组实现(连续的内存空间)
 - 同质结构(元素类型相同)





Frames

Global frame mylist

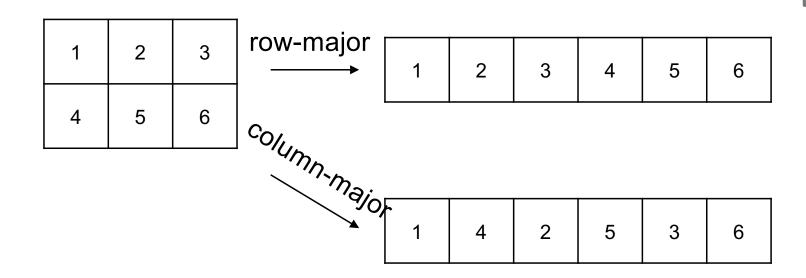
Objects

mylist = np.array([1, 2, 34, 578, 9,0])



· 行主序 v.s. 列主序

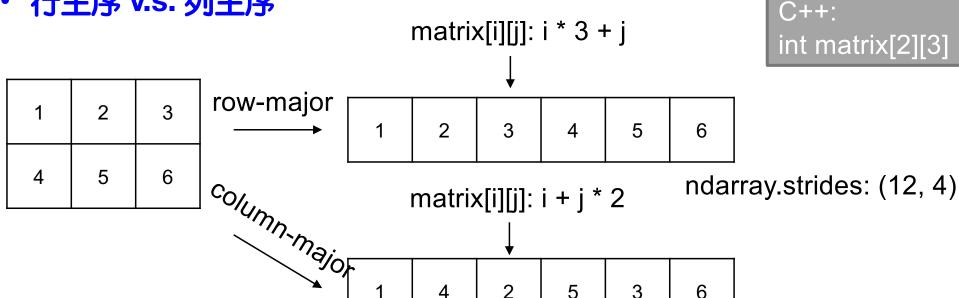
C++: int matrix[2][3]



行主序是C等语言的格式,列主序是Fortran等语言的格式



・ 行主序 v.s. 列主序



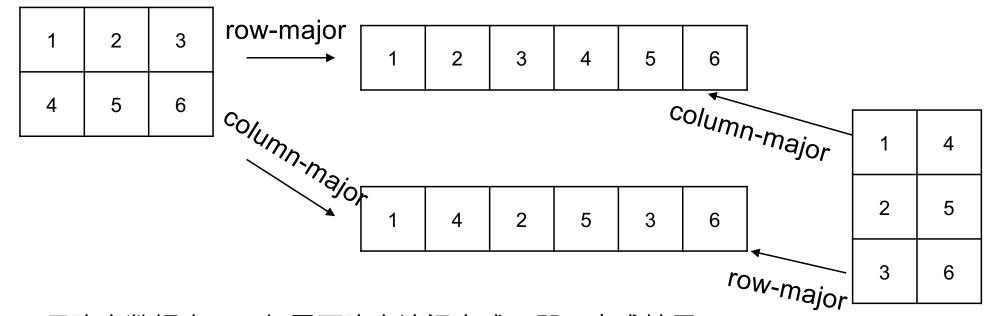
ndarray.strides: (4, 8)

strides: 表示高维数组每一维对应的下标每次偏移时,在一维数组的存储中发生的偏移量(此处假设元素为int32,4个字节)。



· 行主序 v.s. 列主序





不用改变数据表示,仅需要改变访问方式,即可完成转置!

numpy中的转置



import numpy as np #默认引用和别名,后续大多省略

```
def print_array(arr):
    print(arr.dtype)
    print(arr)
    print(arr.strides)
    print()

myarray = np.array([[1,2,3],[4,5,6]])
print_array(myarray)
```

```
myarrayT = myarray.T
print_array(myarrayT)
```

```
myarray2 = np.array([[1,4],[2,5],[3,6]])
print_array(myarray2)
```

同样的数组,不一样的内部表示!



C++: int matrix[2][3]

1	2	3
4	5	6

row-major

1 2 3 4 5 6

row-major

同样的内部表示,不一样的外部形式!

numpy中改变数组的形状



```
data = np.arange(1, 7)
print_array(data)

data1 = np.arange(1, 7).reshape((3,2))
print_array(data1)

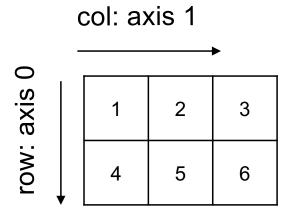
data2 = np.arange(1, 7).reshape((2,3))
print_array(data2)
```

同样的数组,不一样的内部表示!同样的内部表示,不一样的外部形式!

抽象和封装: 数据内部表示 v.s. 数据的外部使用

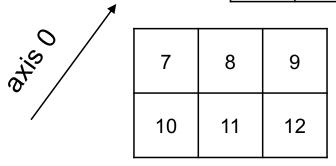
高维数组



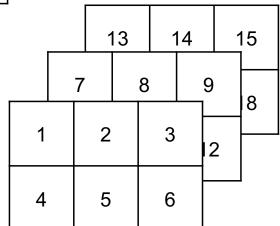


strides: (12, 4)





_	1	2	3
axis	4	5	6
	axi	s 2	→



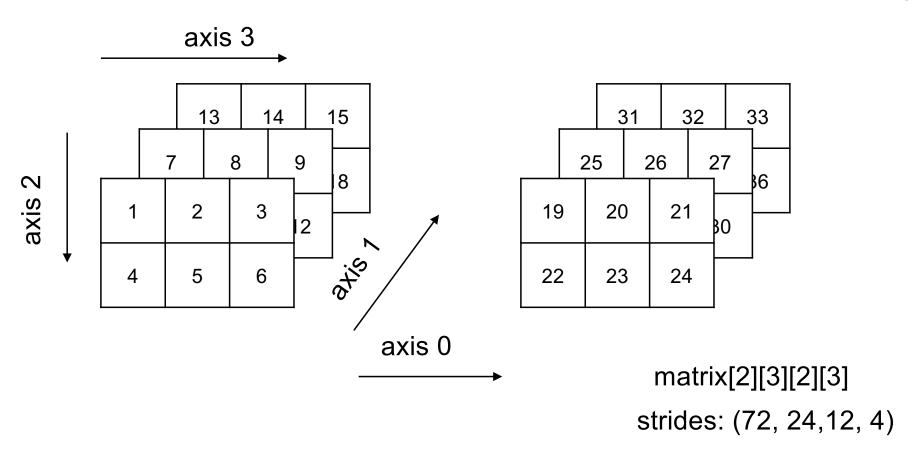
matrix[3][2][3]

strides: (24,12, 4)

高维数组



Tensor





```
data = np.arange(1, 19)
print_array(data)

data1 = np.arange(1, 19).reshape((3,2,3))
print_array(data1)

data2 = np.arange(1, 19).reshape((2,3,3))
print_array(data2)
```

试着自己实现一个n维矩阵类,创建任意维度的矩阵,提供元素访问操作、转置操作、reshape操作等功能。

ndarray的基本属性



・ dtype: 元素类型

· ndim: 维数

· shape: 数组形状

- 整数构成的元组, 如: (2, 3), (1, 4)等

- 向量的形状是元素仅有1个的元组, 须加逗号区分, 如:(3,)

・ size: 所有元素个数

· itemsize: 单个元素大小 (bytes)

• strides: 访问规则

•

```
Attributes
                                                           help(np.ndarray)
T : ndarray
                                                           np.ndarray?
    Transpose of the array.
data: buffer
    The array's elements, in memory.
dtype : dtype object
    Describes the format of the elements in the array.
size : int
    Number of elements in the array.
itemsize : int
    The memory use of each array element in bytes.
ndim : int
    The array's number of dimensions.
shape : tuple of ints
    Shape of the array.
strides : tuple of ints
    The step-size required to move from one element to the next in
    memory. For example, a contiguous ``(3, 4)`` array of type
    ``int16`` in C-order has strides ``(8, 2)``. This implies that
    to move from element to element in memory requires jumps of 2 bytes.
    To move from row-to-row, one needs to jump 8 bytes at a time
    (``2 * 4``).
```



NDARRAY的创建

ndarray的创建



- ・从已有列表创建
 - 使用np.array函数

```
查阅 np.array?
```

```
array(object, dtype=None, copy=True, order='K', subok=False, ndmin=0)
```

```
In [62]: np.array([1, 2, 3, 4])
Out[62]: array([1, 2, 3, 4])
In [63]: a1 = np.array([1, 2, 3, 4])
Out[63]: a2 = np.array(a1, order = 'F', ndmin = 2)
```

ndarray的创建



- ・从已有列表创建
- ・数值自动填充
 - zeros, ones, empty, full ...
 - zeros_like, ones_like, empty_like, full_like ...
 - identity, eye
 - diag, arrange
 - linspace, logspace, meshgrid
 - fromfunction, fromfile
 - np.random.rand

```
In [58]: np.zeros(2)
Out[58]: array([0., 0.])
In [59]: np.ones(3)
Out[59]: array([1., 1., 1.])
In [60]: np.diag(range(1,5))
Out[60]:
array([[1, 0, 0, 0],
       [0, 2, 0, 0],
       [0, 0, 3, 0],
       [0, 0, 0, 4]]
In [69]: np.arange(1,6,2)
Out[69]: array([1, 3, 5])
                                     more examples on test numpy.ipynb
In [71]: np.linspace(0, 10, num=5)
Out[71]: array([ 0. , 2.5, 5. , 7.5, 10. ])
                                                               20
```

NumPy支持的数据类型



- 各种字长的5种基础数据类型
 - booleans, integers, unsigned integers, floating point, complex
 - 例如: bool_, int8, int16, int32, float32, uint64, complex64 等
- 更精确指定数据类型,以获取存储和计算上的性能提升
- · NumPy也可以用于支持自定义类型 (Structured arrays)
 - https://numpy.org/doc/stable/user/basics.rec.html#structuredarrays



索引、切片、视图

NDARRAY的访问



索引和切片

- ・定位单个元素
 - 下标(正值、负值)
- ・选择多个元素
 - 切片((start, end, step) 序列开始、序列结尾)
- · 对于高维数组,须从0-ndim指明每个需要切片的维度
- 每个维度的索引和切片操作相互独立
 - myarray[-3:,-3:]

・语法说明



- 结束位置元素不在结果列表中
- 步长用于跳过部分元素
- start、end 可以省略,分别表示从列表开始、直到列表结束
- step可以省略,表示默认步长为1

```
In [7]: myarray = np.arange(100).reshape(10, 10)
In [8]: myarray
Out[8]:
array([[0, 1, 2, 3, 4, 5, 6, 7, 8, 9],
      [10, 11, 12, 13, 14, 15, 16, 17, 18, 19],
      [20, 21, 22, 23, 24, 25, 26, 27, 28, 29],
In [9]: myarray[: ,1]
In [10]: myarray[-3:,-3:]
In [11]: myarray[:,-3:]
In [12]: myarray[-3:]
```



切片和视图



- · 切片操作得到的数据子集是原数组的一种展示方式(称为视图)
 - 视图仍然具有正常数组的行为、效率得到提升
 - 视图中的改动将影响原数组数据

```
In [20]: newarray2 =
In [19]: newarray =
                                  np.array([[ 7, 8, 9], [57, 58,
myarray[::5,-3:]
                                  59]], dtype="int32")
    ...: print array(newarray)
                                  print_array(newarray2)
Element Type: int64
Shape: (2, 3)
                                  Element Type: int32
Strides: (400, 8)
                                  Shape: (2, 3)
[[ 7 8 9]
                                  Strides: (12, 4)
 [57 58 59]]
                                  [[ 7 8 9]
```

抽象和封装: 数据内部表示 v.s. 数据的外部使用[57 58 59]]



```
In [21]: newarray3 = newarray[:,-2:] 创建切片的切片
```

In [22]: newarray3.fill(0)

将切片数组置零

```
In [23]: print(newarray3)
    ...: print(newarray)
    ...: print(myarray)
```

原数组也被置零,除非显式指明copy: newarray3 = newarray[:,-2:].copy()

试着自己实现一个三维矩阵类,让它能进行多次slicing操作,操作结果是原矩阵的一个视图。

```
[[0 0]
[0 0]]
[[7 0 0]
 [57 0 0]]
[[0 1 2 3 4 5 6 7 0 0]
 [10 11 12 13 14 15 16 17 18 19]
 [20 21 22 23 24 25 26 27 28 29]
 [30 31 32 33 34 35 36 37 38 39]
 [40 41 42 43 44 45 46 47 48 49]
 [50 51 52 53 54 55 56 57 0 0]
 [60 61 62 63 64 65 66 67 68 69]
 [70 71 72 73 74 75 76 77 78 79]
 [80 81 82 83 84 85 86 87 88 89]
 [90 91 92 93 94 95 96 97 98 99]]
```

fancy indexing & boolean indexing



• 花式索引

- 使用一个索引序列从ndarray中选择元素,并创建新数组

```
In [24]: myarray = np.arange(0, 100, 10)
    ...: indices = [1, 5, -1]
    ...: newarray = myarray[indices]
```

・布尔索引

- 使用一个bool序列进行元素选择,并创建新数组

```
In [25]: myarray = np.arange(8)
    ...: b = [False, True, False, False, False, False, True, False]
    ...: myarray[b]
Out[25]: array([1, 6])
```



调整数组形状和值

改变数组维度



- 基于底层表示支持上层的高效实现(一般返回视图)
 - np.reshape/np.ndarray.reshape
 - np.ravel/np.ndarry.ravel(折叠为一维数组)
 - np.squeeze(删除长度为1的维度)
 - np.expand_dims和np.newaxis (增加新的维度)
 - np.transpose/np.ndarray.transpose/np.ndarray.T

改变数组大小、形状、内容



- 一般将会按照要求创建新的数组
 - np.resize
 - np.ndarray.flatten
 - np.hstack, np.vstack, np.dstack, np.concatenate
 - np.append, np.insert, np.delete



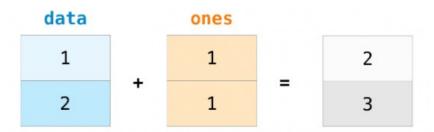
矩阵的运算

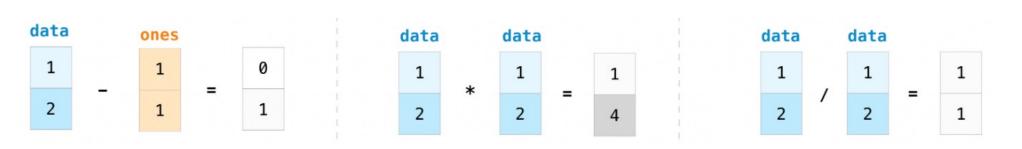
基本算术运算



• 算术运算定义为对应元素进行运算

- 对于大小相同的矩阵, 运算结果与原矩阵形状相同





循环 v.s. 向量化运算(vectorized operation)



- · 通过python的循环依次访问每个元素并运算效率较低
 - 创建访问迭代器
 - 类型匹配和操作符运算函数调用

```
c = np.empty(a.size)
for i in range(a.size):
    c[i] += a[i] + b[i]
```

- 将对矩阵中每个元素的运算 封装为 对矩阵整体的运算
 - 通过基于c的实现和底层优化提升计算效率
- · 提供一系列封装好的计算函数 (Universal functions, ufunc) , 避免显式使用元素遍历循环

```
In [28]: size = 10000
                                             ...: a = np.random.rand(size)
In [27]: size = 10000
                                             ...: b = np.random.rand(size)
    ...: a = np.random.rand(size)
    ...: b = np.random.rand(size)
                                             . . . .
                                             ...: %timeit c = np.dot(a, b)
    . . . .
    ...: %timeit c = np.add(a, b)
                                             . . . :
                                             ...: def mydot(a , b):
    . . . .
    ...: def myadd(a , b):
                                             ...: c = 0
    ...: c = np.empty(a.size)
                                             ...: for i in
    ...: for i in range(a.size):
                                        range(a.size):
                                             ...: c += a[i] * b[i]
                 c[i] += a[i] + b[i]
    ...: return c
                                             ...: return c
    . . . .
                                             ...: %timeit mydot(a, b)
    ...: %timeit myadd(a, b)
5.39 \mus \pm 39.7 ns per loop (mean \pm
                                        2.41 \mus \pm 140 ns per loop (mean \pm
std. dev. of 7 runs, 100000 loops each) std. dev. of 7 runs, 100000 loops
5.43 ms \pm 22.5 \mus per loop (mean \pm
                                        each)
std. dev. of 7 runs, 100 loops each)
                                        4.13 ms \pm 23.7 \mus per loop (mean \pm
                                         std. dev. of 7 runs, 100 loops eac⊮)
```

Universal functions (ufuncs)



- Math operations 数学运算
 - add, substract, multiply, matmul, divide, power, remainder, ...
- Trigonometric functions 三角函数
 - sin, cos, tan, sinh, cosh, tanh, arcsin, arccos, ...
- Bit-twiddling functions 位运算
 - bitwise_add, bitwise_or, bitwise_xor, invert, left_shift, ...
- Comparison functions 比较运算
 - greater, greater_equal, less, equal, logical_and, logical_or, ...
- Floating functions
 - isfinite, isinf, isnan, fabs, fmod, floor, ceil, ...

https://numpy.org/doc/stable/reference/ufuncs.html

Calling ufuncs:

from np.ufunc?



op(*x[, out], where=True, **kwargs)

Apply $\circ p$ to the arguments *x elementwise, broadcasting the arguments.

Parameters

*x : array_like
Input array

Input arrays.

out : ndarray, None, or tuple of ndarray and None, optional

Alternate array object(s) in which to put the result; if provided, it

must have a shape that the inputs broadcast to. A tuple of arrays (possible only as a keyword argument) must have length equal to the number of outputs; use `None` for uninitialized outputs to be

allocated by the ufunc.

where : array_like, optional

This condition is broadcast over the input. At locations where the condition is True, the `out` array will be set to the ufunc result. Elsewhere, the `out` array will retain its original value. Note that if an uninitialized `out` array is created via the default `out=None``, locations within it where the condition is False will remain uninitialized.

**kwargs

For other keyword-only arguments, see the :ref:`ufunc docs <ufuncs.kwargs>`. ³⁶

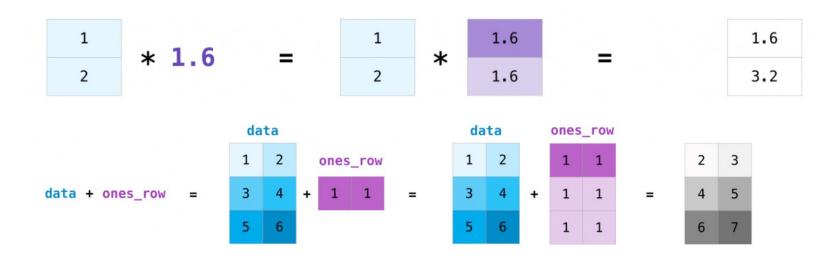
指定作用元素

指定输出位置

操作数匹配和广播 (Broadcasting)



- 当运算的两个操作数矩阵形状不同时,运算需要重新定义
 - NumPy通过广播机制自动扩展小矩阵,以匹配大矩阵
 - 将不同大小的矩阵转换为同样大小,便于进行统一运算

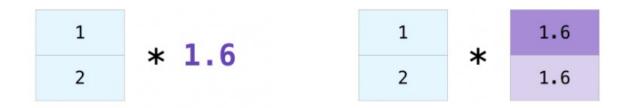


https://numpy.org/doc/stable/user/basics.broadcasting.html

广播和向量化运算



·广播后的计算可以采用通用的ufunc进行,以保证运算效率



```
In [26]: x = np.arange(10000)
    ...: %timeit x * 1.6
    ...: %timeit [i * 1.6 for i in x]

9.38 μs ± 68 ns per loop (mean ± std. dev. of 7 runs, 100000 loops each)
19.8 ms ± 109 μs per loop (mean ± std. dev. of 7 runs, 100 loops each)
```



- 从右到左依次匹配两个矩阵各维度的长度:
 - 当 两个维度长度相等 或者 其中一个为1 时,两者compatible
 - 当 其中一个矩阵维度不足 时,用长度为1的新维度进行补充
- 广播:
 - 将长度为1的维度内容复制匹配另一矩阵对应长度
 - strides = 0

https://numpy.org/doc/stable/user/basics.broadcasting.html



• 常见的广播是用于扩展标量、向量和低维矩阵

```
A (2d array): 5 x 4
B (1d array): 1
Result (2d array): 5 x 4

A (2d array): 5 x 4

B (1d array): 5 x 4

B (1d array): 4

Result (2d array): 5 x 4

A (3d array): 5 x 4

A (3d array): 5 x 4
```



- 常见的广播是用于扩展标量、向量和低维矩阵
 - 可能扩展的是中间的维度
 - 或扩展多个不连续维度

```
A (3d array): 15 x 3 x 5
B (2d array): 15 x 1 x 5
Result (3d array): 15 x 3 x 5
```

```
A (3d array): 15 x 3 x 5
B (2d array): 3 x 1
Result (3d array): 15 x 3 x 5
```



- 常见的广播是用于扩展标量、向量和低维矩阵
 - 可能扩展的是中间的维度
 - 或扩展多个不连续维度
 - 广播也可能同时扩展两个矩阵

A (4d array): 8 x 1 x 6 x 1 B (3d array): 7 x 1 x 5 Result (4d array): 8 x 7 x 6 x 5



- 一些广播失败的例子
 - ValueError: operands could not be broadcast together

```
A (1d array): 3
B (1d array): 4 # trailing dimensions do not match

A (2d array): 2 x 1
B (3d array): 8 x 4 x 3 # second from last dimensions mismatched
```

```
In [3]: x = np.arange(4)
                             In [4]: x + y
   \dots: xx = x.reshape(4,1)
                              ValueError: operands could not be
   \dots: y = np.ones(5)
                              broadcast together with shapes (4,)
   ...: Z =
                              (5,)
np.ones((3,4))
                              In [5]: xx + y
                              Out[5]:
                              array([[1., 1., 1., 1., 1.],
                                     [2., 2., 2., 2., 2.]
                                     [3., 3., 3., 3., 3.]
                                     [4., 4., 4., 4., 4.]
                              In [6]: x + z
                              Out[6]:
                              array([[1., 2., 3., 4.],
                                     [1., 2., 3., 4.],
                                                                44
                                     [1., 2., 3., 4.]
```

ufuncs



· ufunc中的out参数用于指定结果存储位置

```
In [32]: x = np.arange(1000000)
                                    In [33]: y = np.random.rand(100,100)
    ...: %time y = x * 2
    ...: %time x = x * 2
                                        ...: %time np.round(y, decimals = 4)
    ...: %time x *= 2
                                        ...: %time np.round(y, decimals = 4,
CPU times: user 2.33 ms, sys:
                                   out = v)
3.06 ms, total: 5.39 ms
                                   CPU times: user 775 μs, sys: 970 μs, total:
Wall time: 4.74 ms
                                   1.74 ms
CPU times: user 2.17 ms, sys:
                                   Wall time: 3.73 ms
3.43 ms, total: 5.6 ms
                                   CPU times: user 58 μs, sys: 6 μs, total:
Wall time: 5.64 ms
                                    64 µs
CPU times: user 858 μs, sys: 0
                                   Wall time: 60.1 μs
ns, total: 858 µs
Wall time: 862 µs
```

ufuncs



· ufunc中的where参数用于指定参与运算的元素

```
In [1]: x = np.arange(5)
...: y = [True, True, False, True, False]
...:
...: #z = np.add(x, 5, where = y)
...: z = np.add(x, 5, where = (x%3==0))
...: print(x)
...: print(z)
```

其他ufunc的相关功能



aggregates

- np.add.reduce(x)
- np.add.accumulate(x)
- reduceat等

outer products

np.multiply.outer(x , x)

```
In [41]: x = np.arange(1, 5)
    ...: xacc = np.multiply.accumulate(x)
    ...: xred = np.multiply.reduce(x)
    ...:
    print(xacc, xred)
[ 1 2 6 24] 24
```

```
In [40]: x = np.arange(1,10)
    ...: print(np.multiply.outer(x, x))
[[ 1  2  3  4  5  6  7  8  9]
  [ 2  4  6  8  10  12  14  16  18]
  [ 3  6  9  12  15  18  21  24  27]
  [ 4  8  12  16  20  24  28  32  36]
  [ 5  10  15  20  25  30  35  40  45]
  [ 6  12  18  24  30  36  42  48  54]
  [ 7  14  21  28  35  42  49  56  63]
  [ 8  16  24  32  40  48  56  64  72]
  [ 9  18  27  36  45  54  63  72  81]]
```

其他ufunc的相关功能



・ 创建一个ufunc

np.vectorize(myfunc)

聚合函数



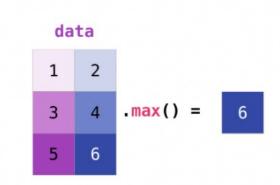
• 用于对数组进行聚合计算

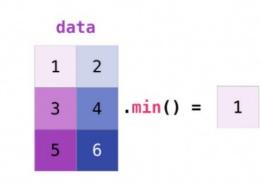
- np.mean, std, var, sum, prod, cumsum, cumprod,
- min, max, argmin, argmax
- all(所有元素不为零,返回True)
- any(任一元素不为零,返回True)

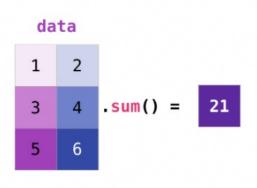
· 默认对整个输入数组进行聚合,也可以用axis关键字参数指定 聚合的轴

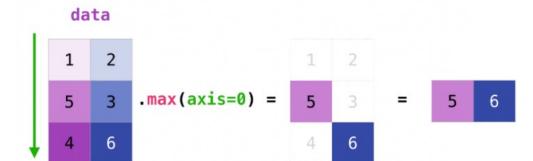
- data.max(axis=0)
- data.max(axis=(0, 2))

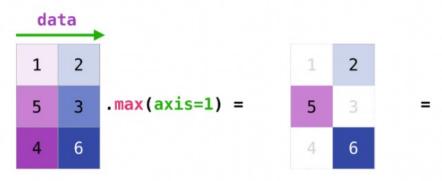














条件计算函数



- np.where
 - 从两个数组中选取值
- np.choose
 - 根据给定的索引数组从数组列表中选取值
- np.select
 - 根据条件列表从数组列表中选取值
- np.nonzero
 - 返回非零元素的索引



其他效率相关问题



```
In [30]: a = np.random.rand(5000,
5000)
    ...: %timeit a[0, :].sum()
    ...: %timeit a[:, 0].sum()
    ...: b = a.T
    ...: %timeit b[0, :].sum()
    ...: %timeit b[:, 0].sum()
    \ldots: c = np.array(a, copy = True,
order = 'F')
    ...: %timeit c[0, :].sum()
    ...: %timeit c[:, 0].sum()
    ...: d = np.array(a, copy = True,
order = 'C')
    ...: %timeit d[0, :].sum()
    ...: %timeit d[:, 0].sum()
```

对行与列求和的差别:

```
3.77 \mus \pm 42.3 ns per loop (mean \pm std.
dev. of 7 runs, 100000 loops each)
35.7 \mus \pm 149 ns per loop (mean \pm std.
dev. of 7 runs, 10000 loops each)
35.4 \mus \pm 180 ns per loop (mean \pm std.
dev. of 7 runs, 10000 loops each)
3.76 \mus \pm 24.8 ns per loop (mean \pm std.
dev. of 7 runs, 100000 loops each)
35.3 \mus \pm 162 ns per loop (mean \pm std.
dev. of 7 runs, 10000 loops each)
3.75 \mus \pm 15.2 ns per loop (mean \pm std.
dev. of 7 runs, 100000 loops each)
3.76 \mus \pm 20.3 ns per loop (mean \pm std.
dev. of 7 runs, 100000 loops each)
35.3 \mus \pm 177 ns per loop (mean \pm std.
dev. of 7 runs, 10000 loops each)
```



```
np.nditer是numpy中用于
In [31]: a = np.arange(6).reshape(2,3)
                                          高效遍历矩阵元素的对象,
                                          遍历顺序可以由数据存储
    ...: def print_nditer(b):
                                          方式决定。
            #print_array(b)
            #print(b.ravel())
                                                  Iters:
    ...: print("Iters: ")
                                                 0 1 2 3 4 5
    ...: for x in np.nditer(b):
                                                 Iters:
                print(x, end = ' ')
                                                 0 1 2 3 4 5
            print("\n")
                                                  Iters:
                                                 0 3 1 4 2 5
   ...: print_nditer(a)
   ...: print_nditer(a.T)
    ...: print nditer(a.T.copy(order = 'C'))
```

https://numpy.org/doc/stable/reference/generated/numpy.nditer.html

numpy应用示例(一)



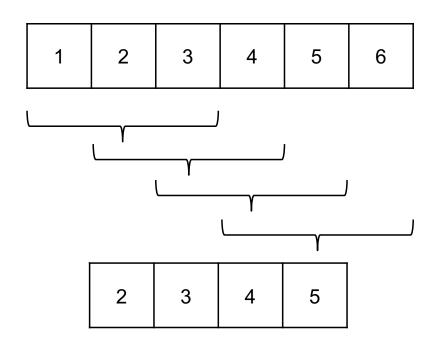
• 计算两个给定序列的均方误差。

$$MeanSquareError = \frac{1}{n} \sum_{i=1}^{n} (Y_prediction_i - Y_i)^2$$

numpy应用示例 (二)



• 计算数组中连续三个值的平均值



如何计算给定窗口大小w中的元素的平均值?

numpy应用示例 (三)



· 计算给定矩阵的平方根矩阵。其中,负数的平方根为其绝对值的平方根的相反数。

```
x = np.random.randint(-100, 101, (5,5))
np.sqrt(x)
```

- 组合现有ufunc, 自定义ufunc?

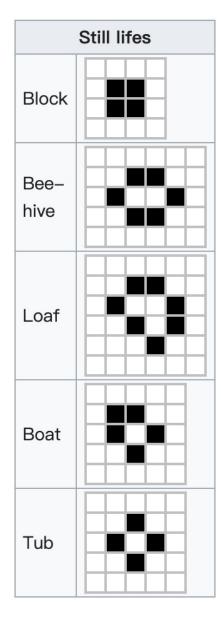


```
In [46]: def method1(x):
    x = np.array(x, dtype = "float32")
    ...: np.sqrt(x, where = x > 0, out = x)
    ...: np.sqrt(-x, where = x < 0, out = x)
         return x
    . . . .
    ...: def method2(x):
            mysqrt = np.vectorize(lambda x: np.sqrt(x) if x > 0 else np.sqrt(-x))
    ...: return mysqrt(x)
   In [47]: %timeit method1(x)
       ...: %timeit method2(x)
   7.88 \mus \pm 120 ns per loop (mean \pm std. dev. of 7 runs, 100000 loops each)
   44.6 \mus \pm 174 ns per loop (mean \pm std. dev. of 7 runs, 10000 loops each)
```

numpy应用示例 (四)



- The Game of Life
- These rules, which compare the behavior of the automaton to real life, can be condensed into the following:
 - Any live cell with two or three live neighbours survives.
 - Any dead cell with three live neighbours becomes a live cell.
 - All other live cells die in the next generation. Similarly, all other dead cells stay dead.
- 由随机初始的矩阵开始,输出每一代的生物存活情况





回顾



NumPy

- 对高维数组的一种抽象: 高效存储和计算
- 数据创建,索引、切片和视图
- 向量化运算、广播、聚合函数



・其他教程阅读

- https://numpy.org/doc/stable/user/absolute_beginners.html
- https://www.numpy.org.cn/article/basics/understanding_numpy.html

100 numpy exercises

https://github.com/rougier/numpy-100