



# **HYPOTHESIS TESTING**

## **INFERENTIAL STATISTICS**

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*prepared by:*

**Gyro A. Madrona**  
Electronics Engineer

# TOPIC OUTLINE

Hypothesis Test

Significance Level

Rejection Region

Critical Value and Z-score



# HYPOTHESIS TEST



# HYPOTHESIS

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A hypothesis is an initial assumption formed before collecting data, and it serves as a statement about a population parameter rather than about the sample data.

## Steps in Data-Driven Decision Making

1. Formulate a hypothesis
2. Find the right test (e.g., z-test, t-test)
3. Execute the test
4. Make a decision



# HYPOTHESIS TEST

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A hypothesis test is simply comparing reality to an assumption and asking, “Did things change?”

## Null Hypothesis ( $H_o$ )

Represents no change, no effect, or the status quo.

## Alternative Hypothesis ( $H_a$ )

Represents the possibility that things did change or that there is a significant difference.



# EXERCISE

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A fitness tracker company claims their device measures heart rate with **95%** accuracy compared to medical-grade monitors. An independent lab wants to verify this claim.

Null Hypothesis

$$H_o: \mu_o = 95$$

The average accuracy is 95%.

Alternative Hypothesis

$$H_a: \mu_o \neq 95$$

The average accuracy differs from 95%.



# EXERCISE

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A manufacturer claims that their new energy-efficient LED bulbs have an average lifespan of **at least 25,000 hours**. A consumer group suspects that the actual lifespan is shorter and decides to test this claim.

Null Hypothesis

$$H_o: \mu_o = 25,000$$

The average lifespan of the LED is 25,000 hours.

Alternative Hypothesis

$$H_a: \mu_o < 25,000$$

The average lifespan of the LED is less than 25,000 hours.



# EXERCISE

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A study suggests that storing apples in a controlled atmosphere **extends** their shelf life beyond **30 days**. A food scientist wants to verify if this method truly increases shelf life compared to conventional storage.

Null Hypothesis

$$H_o: \mu_o = 30$$

Controlled-atmosphere storage shelf life is 30 days.

Alternative Hypothesis

$$H_a: \mu_o > 30$$

Controlled-atmosphere storage increases shelf life beyond 30 days.





# SIGNIFICANCE LEVEL



# SIGNIFICANCE LEVEL

The significance level ( $\alpha$ ) determines the threshold for deciding whether to reject the null hypothesis ( $H_o$ ).

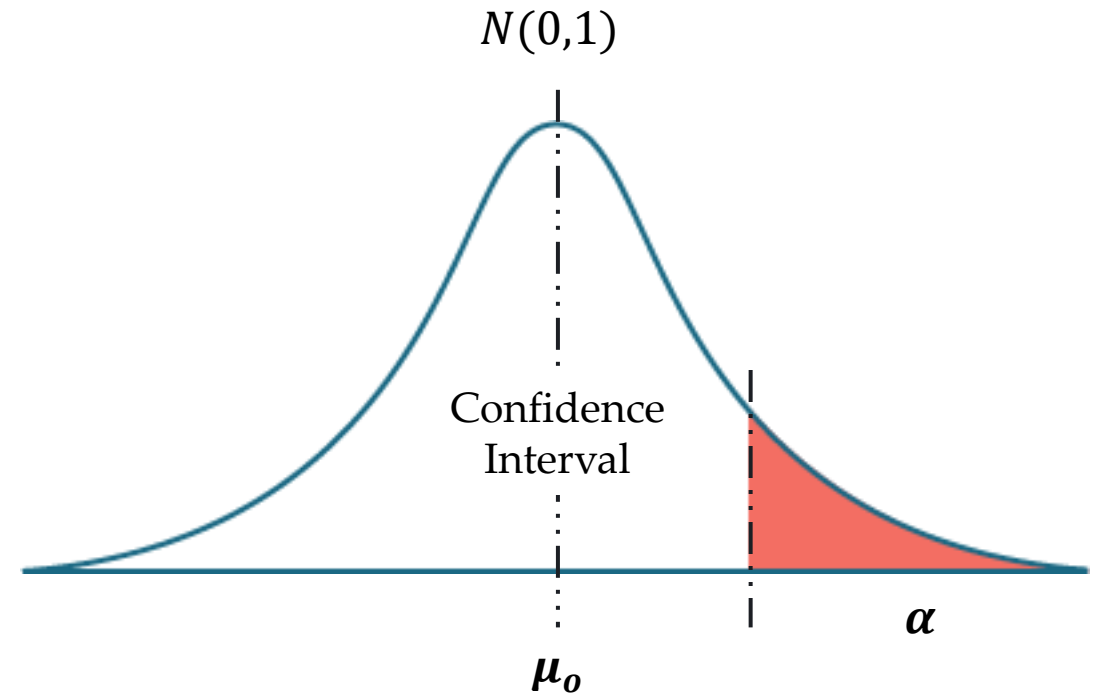
Typical values for  $\alpha$ :

0.01

0.05

0.1

Standard Normal Distribution

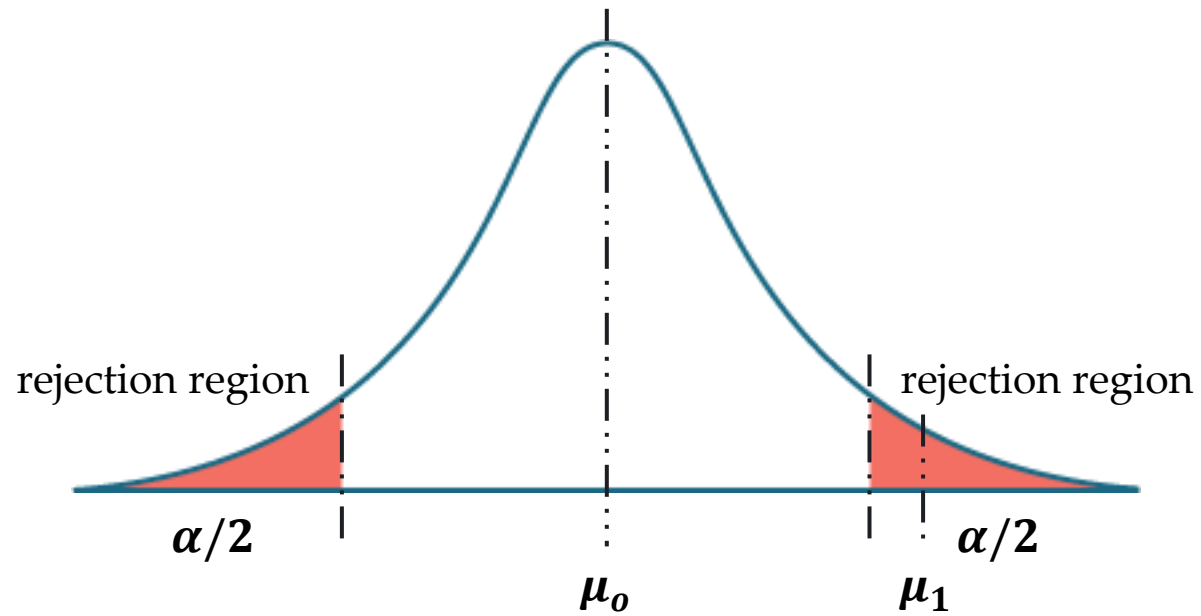


# REJECTION REGION



# REJECTION REGION

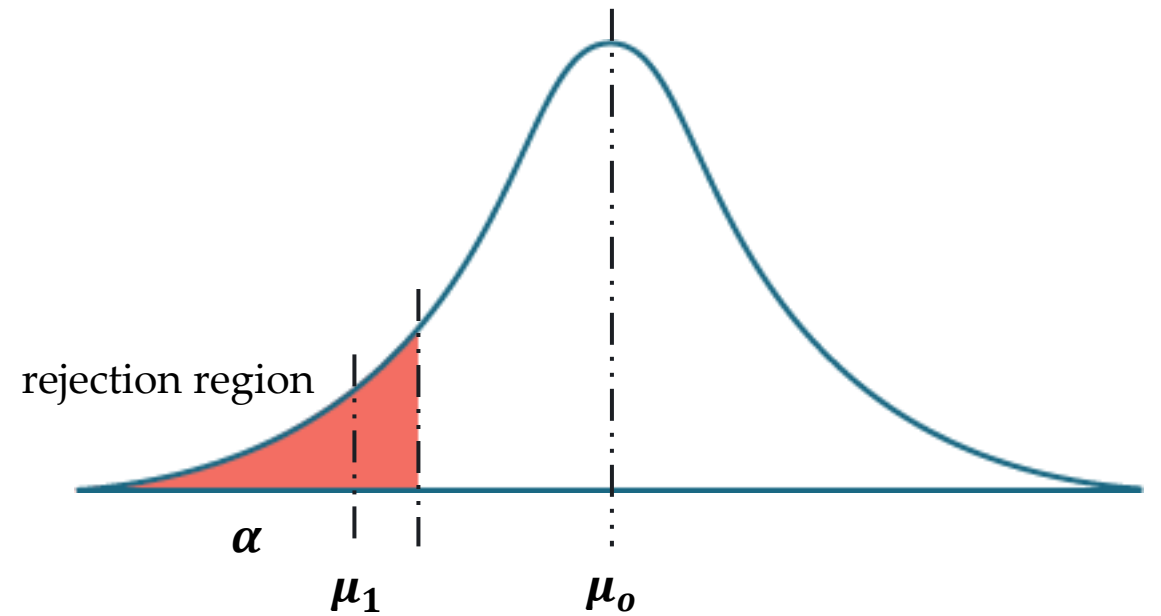
## Two-Tailed Test



$$H_o: \mu_1 = \mu_o$$

$$H_a: \mu_1 \neq \mu_o$$

## One-Tailed Test

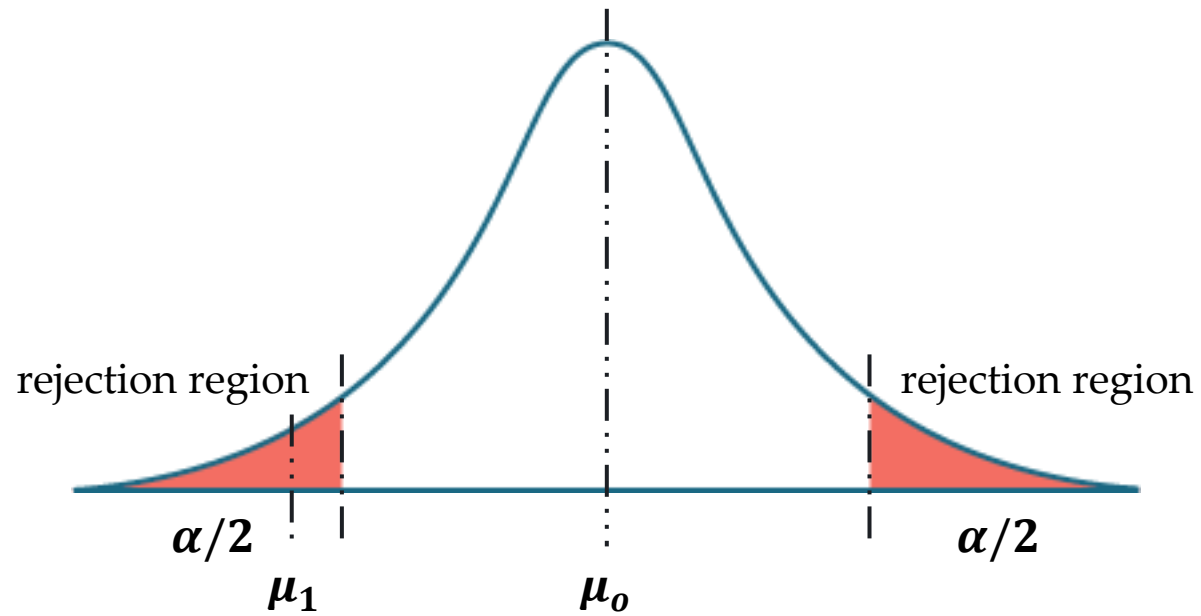


$$H_o: \mu_1 = \mu_o$$

$$H_a: \mu_1 < \mu_o$$

# REJECTION REGION

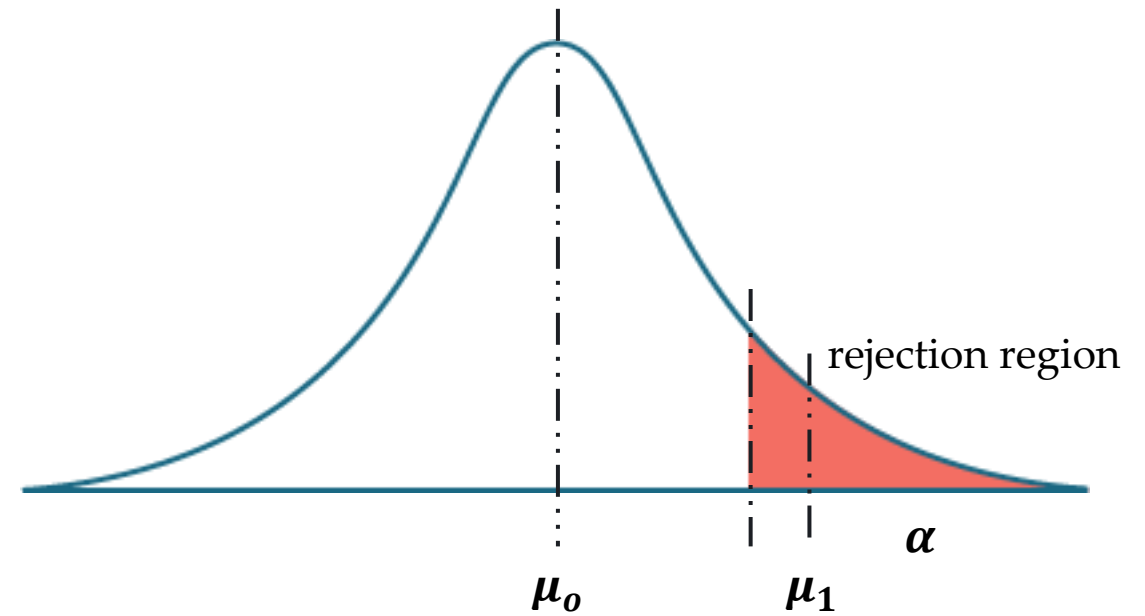
## Two-Tailed Test



$$H_o: \mu_1 = \mu_o$$

$$H_a: \mu_1 \neq \mu_o$$

## One-Tailed Test



$$H_o: \mu_1 = \mu_o$$

$$H_a: \mu_1 > \mu_o$$



# CRITICAL VALUE AND Z-SCORE



# CRITICAL VALUE AND Z-SCORE

## One-Tailed Test

lowercase z

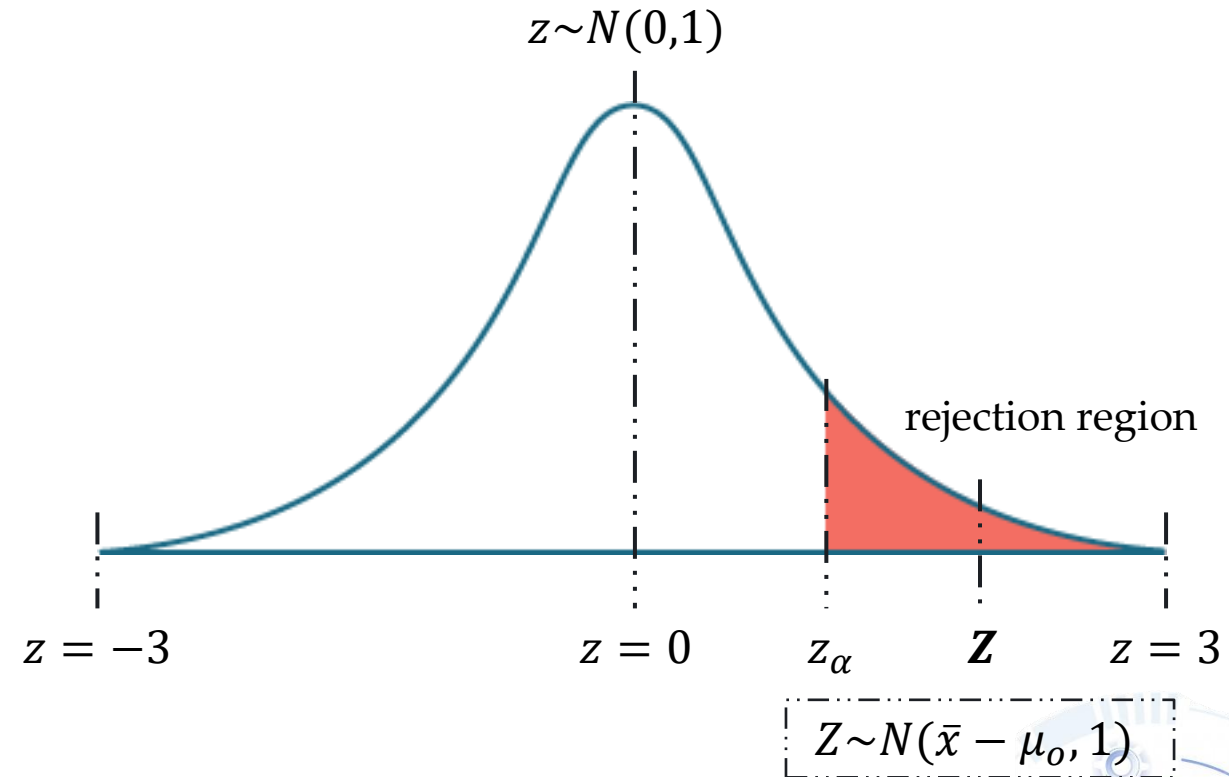
z refers to the critical value obtained from the standard normal distribution table (z-table).

uppercase Z

Z is a standardized variable associated with the test called the Z-score.

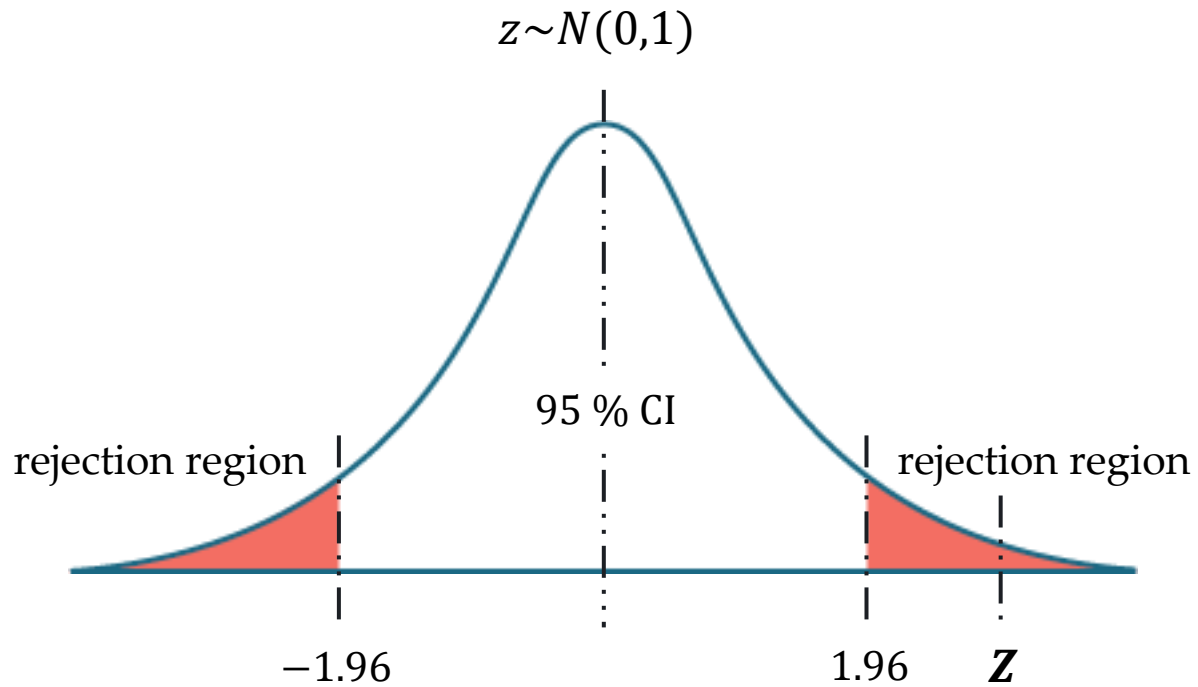
Formula:

$$Z = \frac{\bar{x} - \mu_o}{\sigma/\sqrt{n}}$$



# EXERCISE

## Two-Tailed Test



$$\alpha = 0.05$$

$$z_{0.025} = 1.96$$

## Null Hypothesis

$$H_o: \mu_o = 95$$

The average accuracy is 95%.

## Alternative Hypothesis

$$H_a: \mu_o \neq 95$$

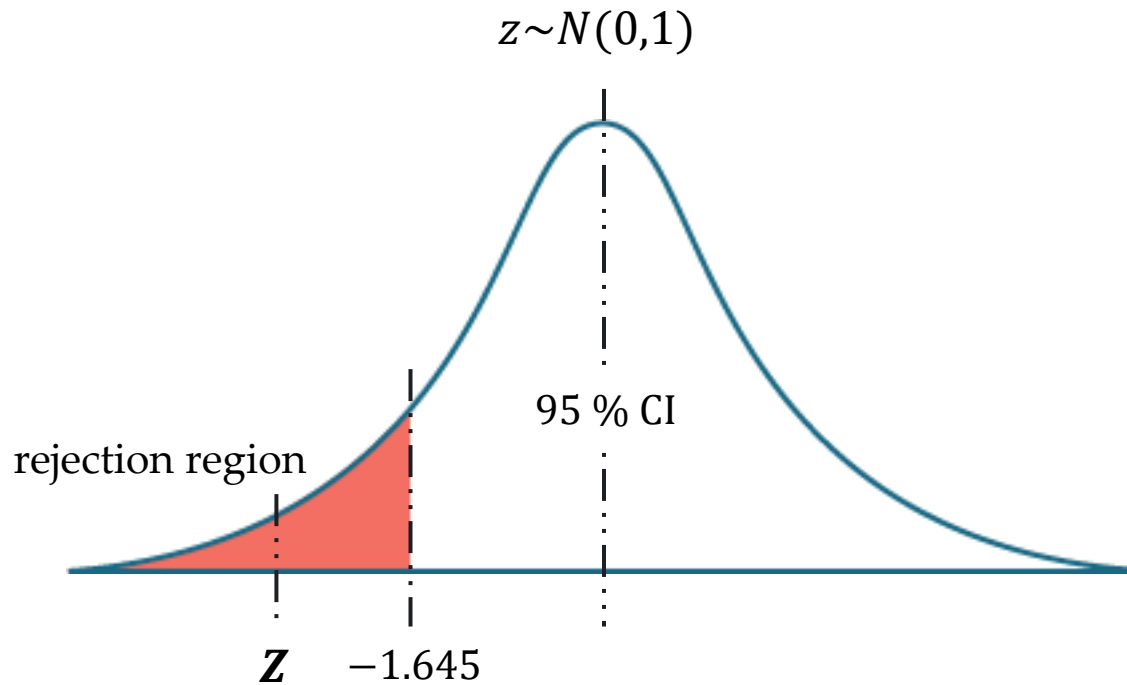
The average accuracy differs from 95%.





# EXERCISE

## One-Tailed Test



$$\alpha = 0.05$$

$$z_{0.05} = 1.645$$

## Null Hypothesis

$$H_o: \mu_o = 25,000$$

The average lifespan of the LED is 25,000 hours.

## Alternative Hypothesis

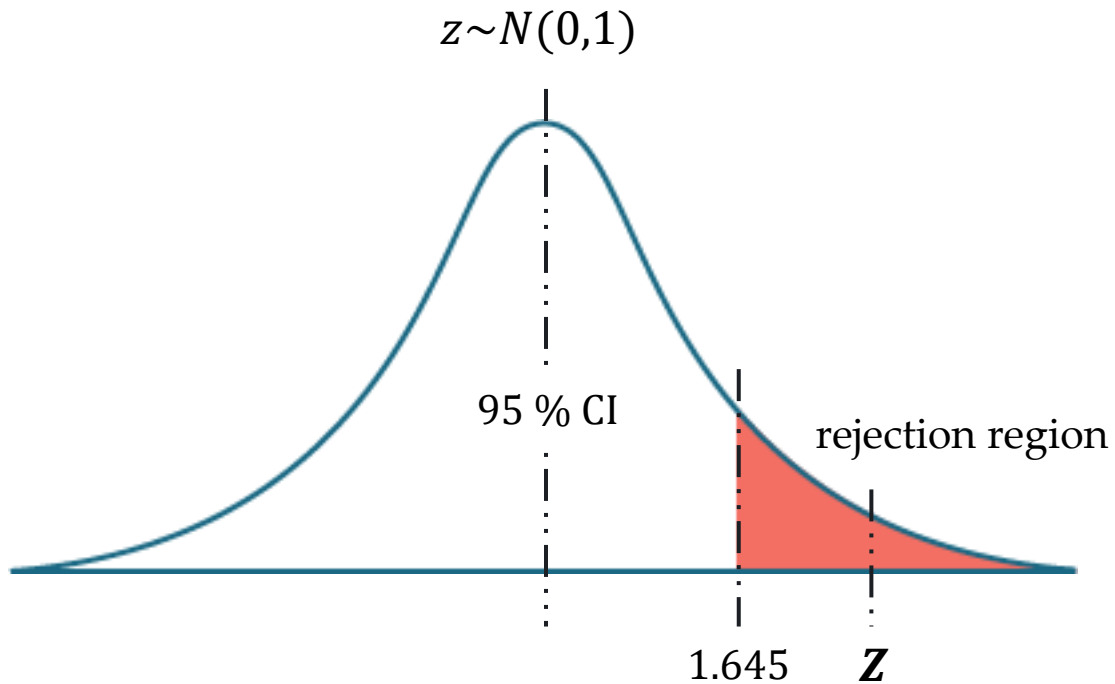
$$H_a: \mu_o < 25,000$$

The average lifespan of the LED is less than 25,000 hours.



# EXERCISE

## One-Tailed Test



$$\alpha = 0.05$$

$$z_{0.05} = 1.645$$

## Null Hypothesis

$$H_o: \mu_o = 30$$

Controlled-atmosphere storage shelf life is 30 days.

## Alternative Hypothesis

$$H_a: \mu_o > 30$$

Controlled-atmosphere storage increases shelf life beyond 30 days.



# EXERCISE

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A manufacturing process is claimed to have an average defect rate of **10.32** units, with a known standard deviation of **3.17** units. The Statistical Process Control (SPC) department suspects this claim may no longer be valid and collects a **random sample** of **30** production units to test whether the true average **defect rate differs** significantly from **10.32**.

Dataset:

defects-data-30-samples.csv

Solution:



# LABORATORY

