

KIRCHHOFF'S CURRENT AND VOLTAGE LAW

BASIC CIRCUIT ANALYSIS METHOD

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TOPIC OUTLINE

Circuit Convention

Kirchhoff's Current Law (KCL)

Kirchhoff's Voltage Law (KVL)



CIRCUIT CONVENTION



CONVENTION

A convention is a widely accepted practice, method, or behavior that is followed by common agreement or tradition, rather than by formal rules.

example

Color coding in Offices

red – urgent documents

blue – general files

green – financial records

This is a common practice but not formally regulated.



STANDARD

A standard is a formal, established guideline, rule, or specification that is often mandatory and enforced by an authoritative body or organization.

example

IEC 60062 Resistor Color Code

black – 0

brown – 1

red – 2

.

.

.

white – 9

Resistors have colored bands that represent specific digits, multipliers, and tolerance values.



LABELING VARIABLES

Steps in Labeling Variables

1. Label the Reference Node (ground)

Select a reference node with the most connections or the negative (-) terminal of a voltage source.

2. Label Node Voltages

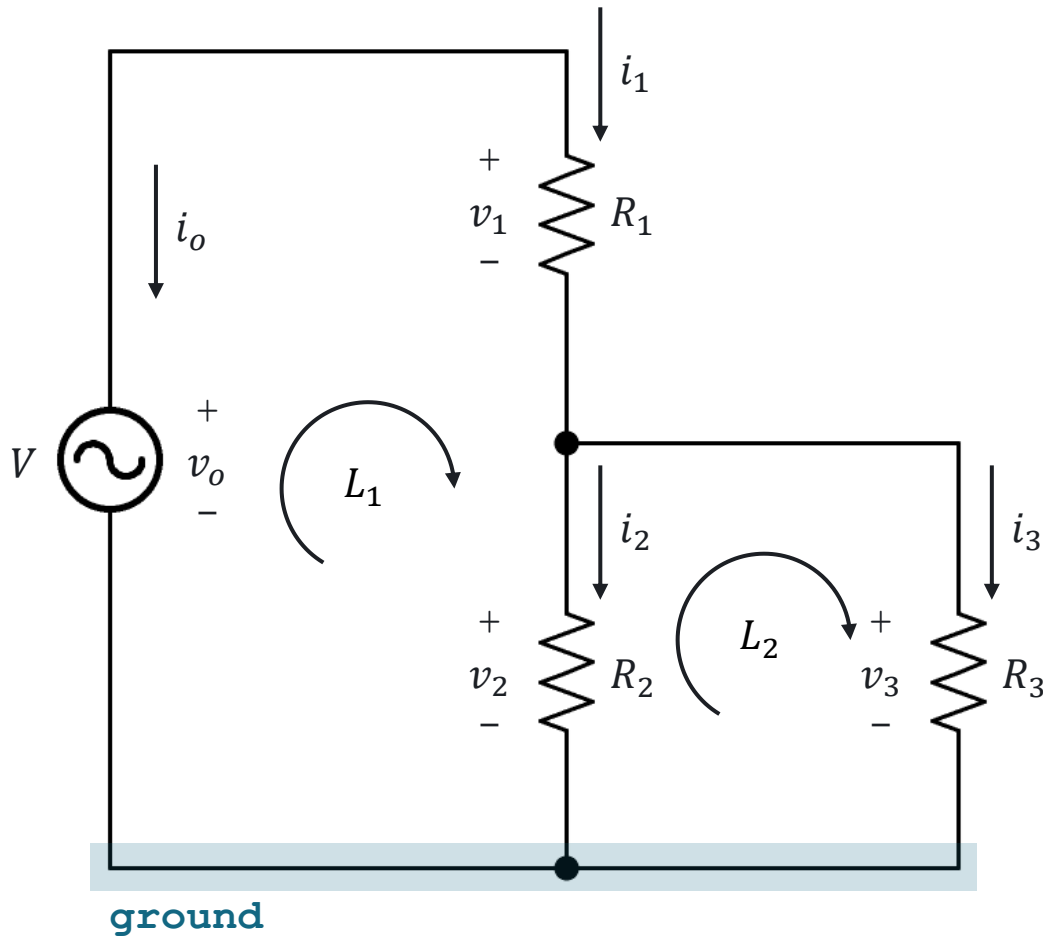
Mark higher potentials as positive (+) relative to the reference node.

3. Label Currents

Entering the positive (+) terminal of a component.

4. Create a voltage loop

Follow the defined current directions.



CIRCUIT CONVENTION

Current Flow Convention

- Current entering a node is negative $(-)$
- Current leaving a node is positive $(+)$

@a

$-i_1$

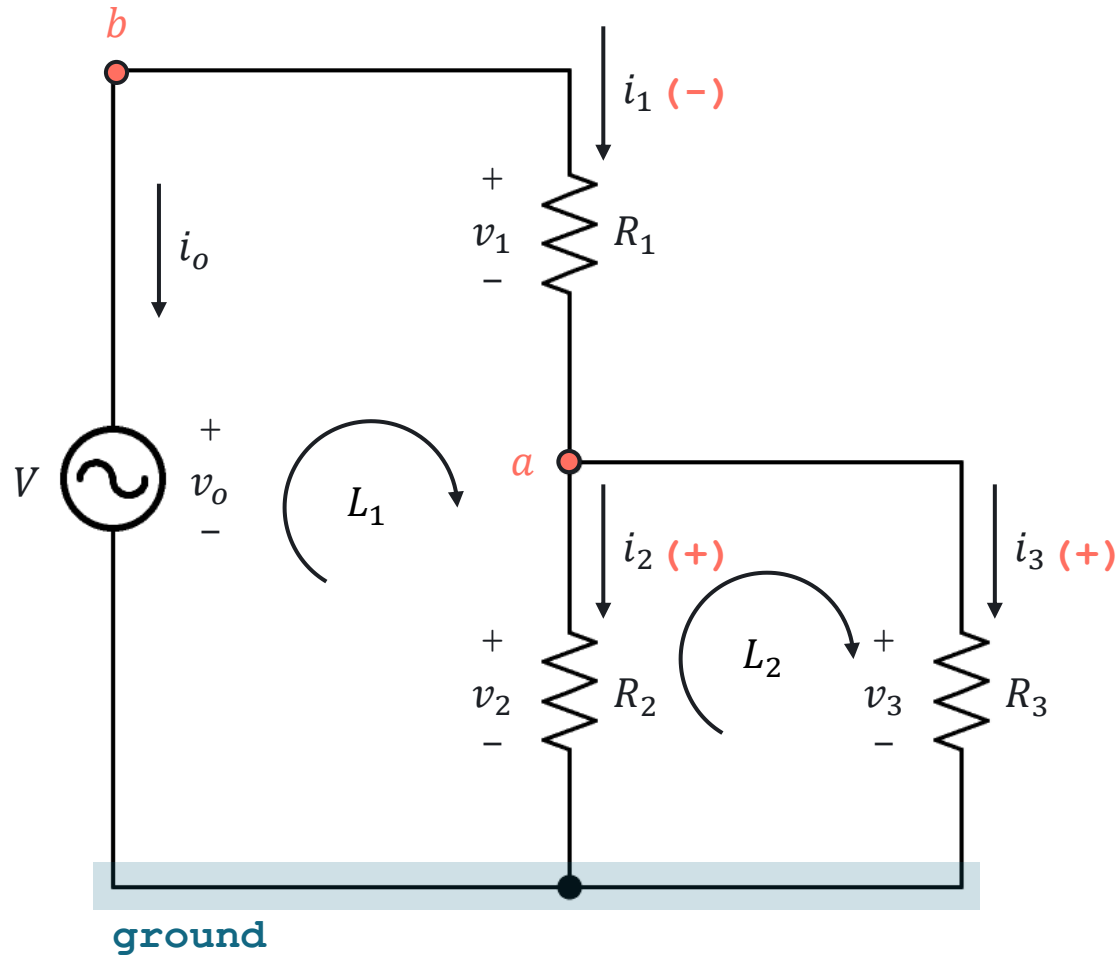
$+i_2$

$+i_3$

@b

$+i_o$

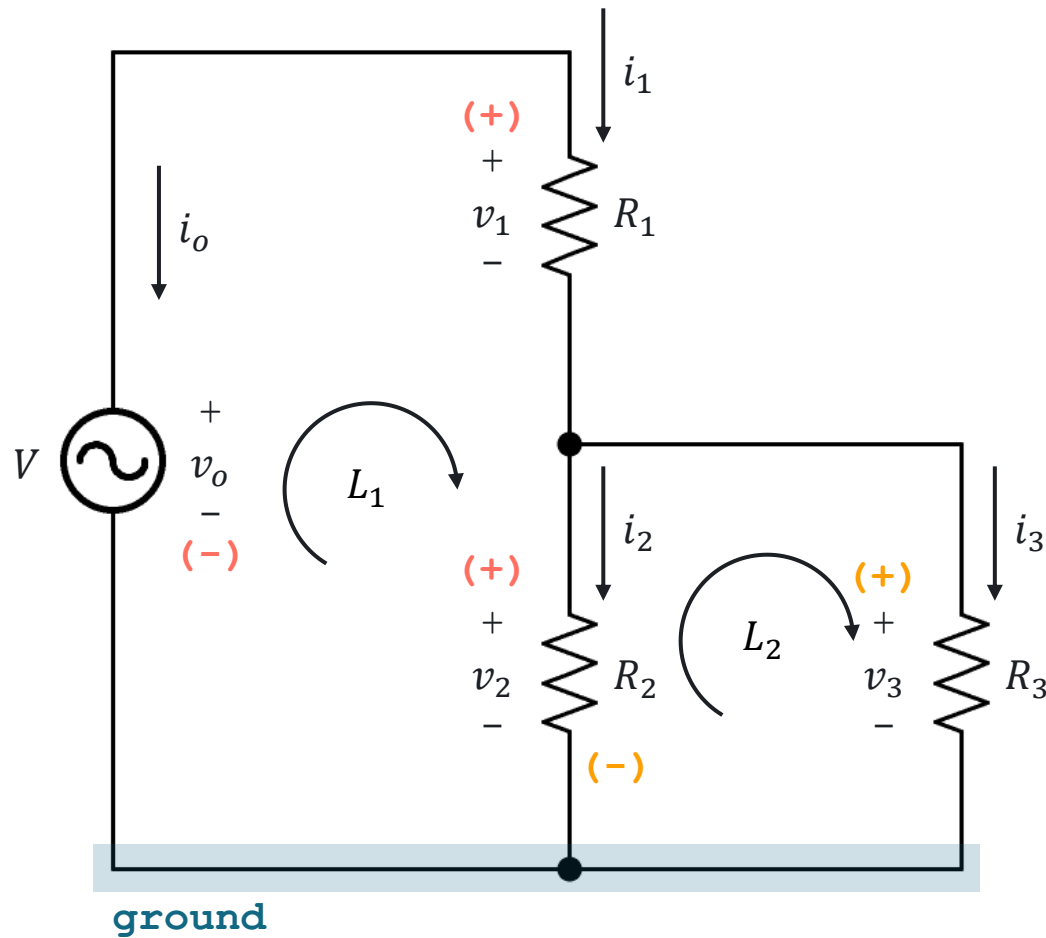
$+i_1$



CIRCUIT CONVENTION

Voltage Loop Convention

The “sign” of voltage of the element is the first sign the loop encounters.



@ L_1

$-v_o$

$+v_1$

$+v_2$

@ L_2

$-v_2$

$+v_3$



KIRCHHOFF'S CURRENT AND VOLTAGE LAW



KIRCHHOFF'S CURRENT LAW

Kirchhoff's current law states that summation of currents going-in and going-out a node is zero.

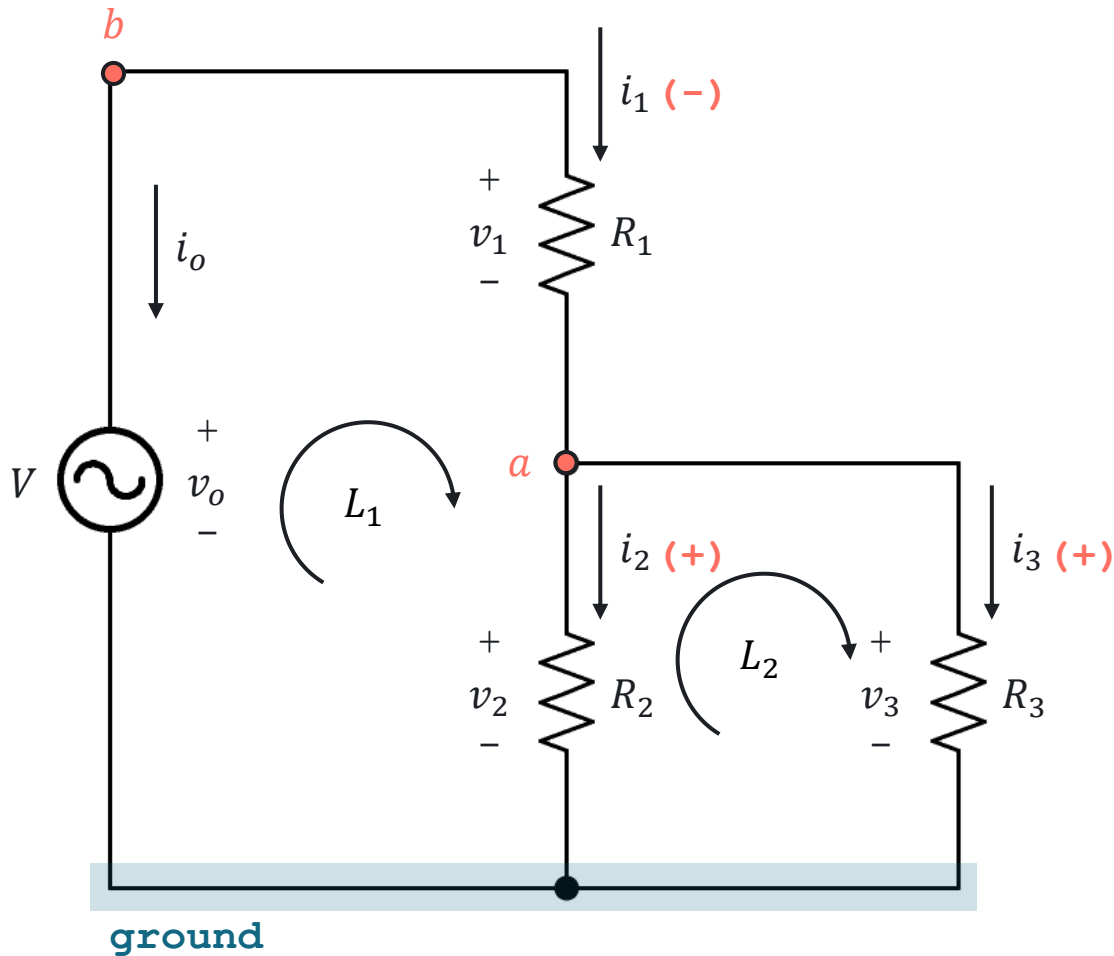
$$\sum i_j = 0$$

KCL @a

$$-i_1 + i_2 + i_3 = 0$$

KCL @b

$$i_o + i_1 = 0$$



KIRCHHOFF'S VOLTAGE LAW

Kirchhoff's voltage law states that the summation of voltages in a closed-loop is zero.

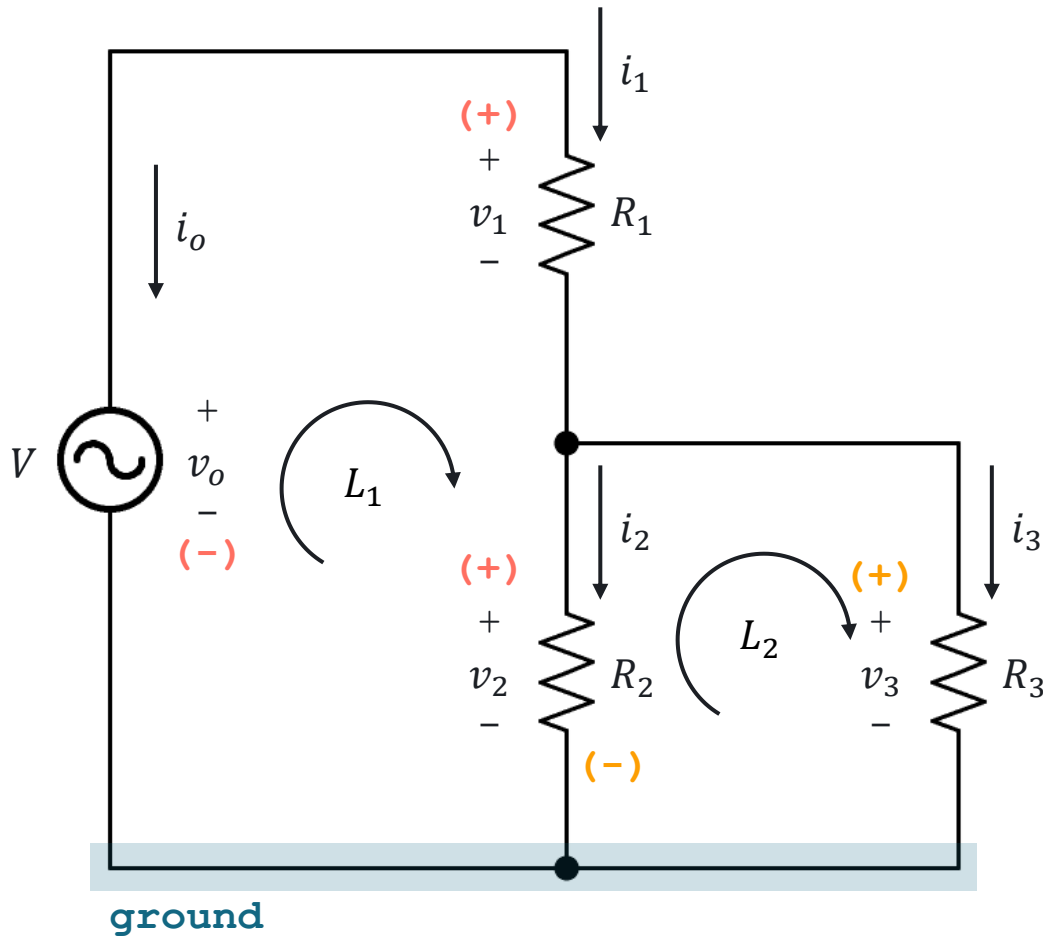
$$\sum v_j = 0$$

KVL @ L_1

$$-v_o + v_1 + v_2 = 0$$

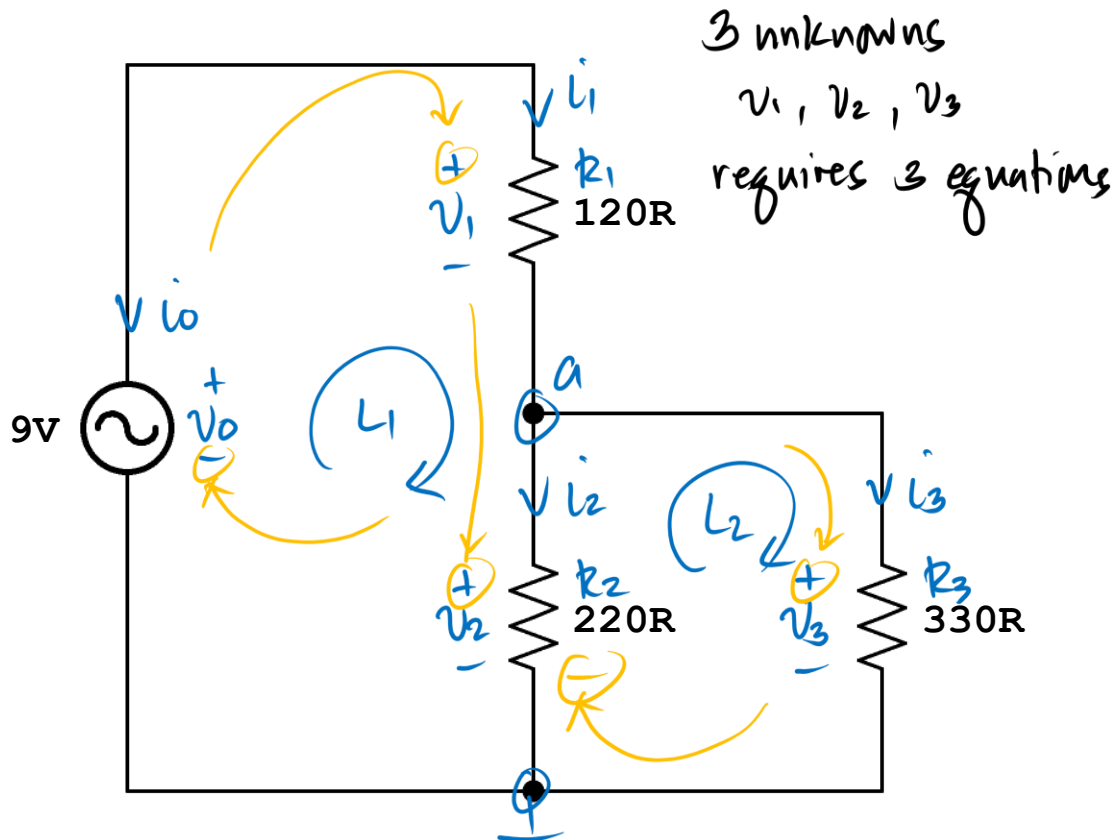
KVL @ L_2

$$-v_2 + v_3 = 0$$



EXERCISE

Analyze the given circuit to determine both the current through and the voltage drop across each resistor.



Solution

KCL @ a

$$-i_1 + i_2 + i_3 = 0$$

$$-\frac{v_1}{R_1} + \frac{v_2}{R_2} + \frac{v_3}{R_3} = 0$$

$$-v_1 G_1 + v_2 G_2 + v_3 G_3 = 0 \quad \text{eq ①}$$

KVL @ L1

$$-v_0 + v_1 + v_2 = 0$$

$$v_1 + v_2 = v_0 \quad \text{eq ②}$$

KVL @ L2

$$-v_2 + v_3 = 0 \quad \text{eq ③}$$

EXERCISE

Gaussian elimination method

| v_1 | v_2 | v_3 | |
|--|---------------------------------------|---------------------------------------|---------|
| $-\frac{1}{120}$ | $\frac{1}{220}$ | $\frac{1}{330}$ | 0 r_1 |
| ① | 1 | 0 | 9 r_2 |
| 0 | -1 | 1 | 0 r_3 |

System of linear equations

$$\underline{-v_1 G_1 + v_2 G_2 + v_3 G_3 = 0} \quad \text{eq ①}$$

$$\underline{v_1 + v_2 = v_0} \quad \text{eq ②}$$

$$\underline{-v_2 + v_3 = 0} \quad \text{eq ③}$$

$$-v_1 \frac{1}{120} + v_2 \frac{1}{220} + \frac{1}{330} = 0 \quad \text{①}$$

$$v_1 + v_2 = 9 \quad \text{②}$$

$$-v_2 + v_3 = 0 \quad \text{③}$$



EXERCISE

Gaussian elimination method

| v_1 | v_2 | v_3 | |
|------------------|-----------------|-----------------|----------------------------------|
| $-\frac{1}{120}$ | $\frac{1}{220}$ | $\frac{1}{390}$ | 0 r_1 |
| 1 | 1 | 0 | 9 $r_2 \leftarrow 120 r_1 + r_2$ |
| 0 | -1 | 1 | 0 r_3 |

System of linear equations

| v_1 | v_2 | v_3 | |
|------------------|-----------------|-----------------|---------|
| $-\frac{1}{120}$ | $\frac{1}{220}$ | $\frac{1}{390}$ | 0 r_1 |
| 0 | $\frac{17}{11}$ | $\frac{4}{11}$ | 9 r_2 |
| 0 | -1 | 1 | 0 r_3 |



EXERCISE

Gaussian elimination method

| v_1 | v_2 | v_3 | |
|------------------|-----------------|-----------------|---------|
| $-\frac{1}{120}$ | $\frac{1}{220}$ | $\frac{1}{330}$ | 0 r_1 |
| 0 | $\frac{17}{11}$ | $\frac{4}{11}$ | 9 r_2 |
| 0 | 0 | $\frac{21}{11}$ | 9 r_3 |

System of linear equations

| v_1 | v_2 | v_3 | |
|------------------|-----------------|-----------------|---|
| $-\frac{1}{120}$ | $\frac{1}{220}$ | $\frac{1}{330}$ | 0 r_1 |
| 0 | $\frac{17}{11}$ | $\frac{4}{11}$ | 9 r_2 |
| 0 | -1 | 1 | 0 $r_3 \leftarrow \frac{17}{11}r_3 + r_2$ |



EXERCISE

Gaussian elimination method

| v_1 | v_2 | v_3 | |
|--|---------------------------------------|---------------------------------------|---------|
| $-\frac{1}{120}$ | $\frac{1}{220}$ | $\frac{1}{330}$ | 0 r_1 |
| 0 | $\frac{17}{11}$ | $\frac{4}{11}$ | 9 r_2 |
| 0 | 0 | $\frac{21}{11}$ | 9 r_3 |

System of linear equations

from r_3

$$\frac{21}{11} v_3 = 9$$

$$v_3 = \frac{9(11)}{21}$$

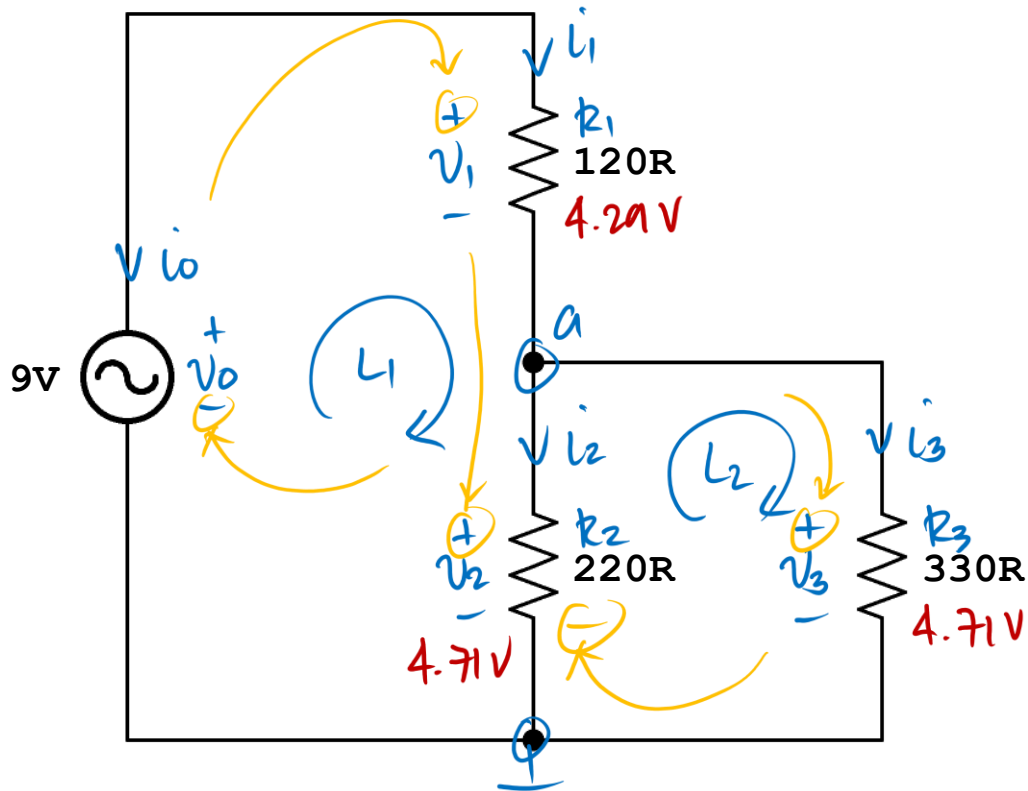
$$v_3 = 4.71 \text{ V}$$

ans



EXERCISE

Analyze the given circuit to determine both the current through and the voltage drop across each resistor.



Solution

KVL @ L_2

$$-V_2 + V_3 = 0$$

$$V_2 = V_3$$

$$V_2 = 4.71 \text{ V}$$

ans

KVL @ L_1

$$-V_0 + V_1 + V_2 = 0$$

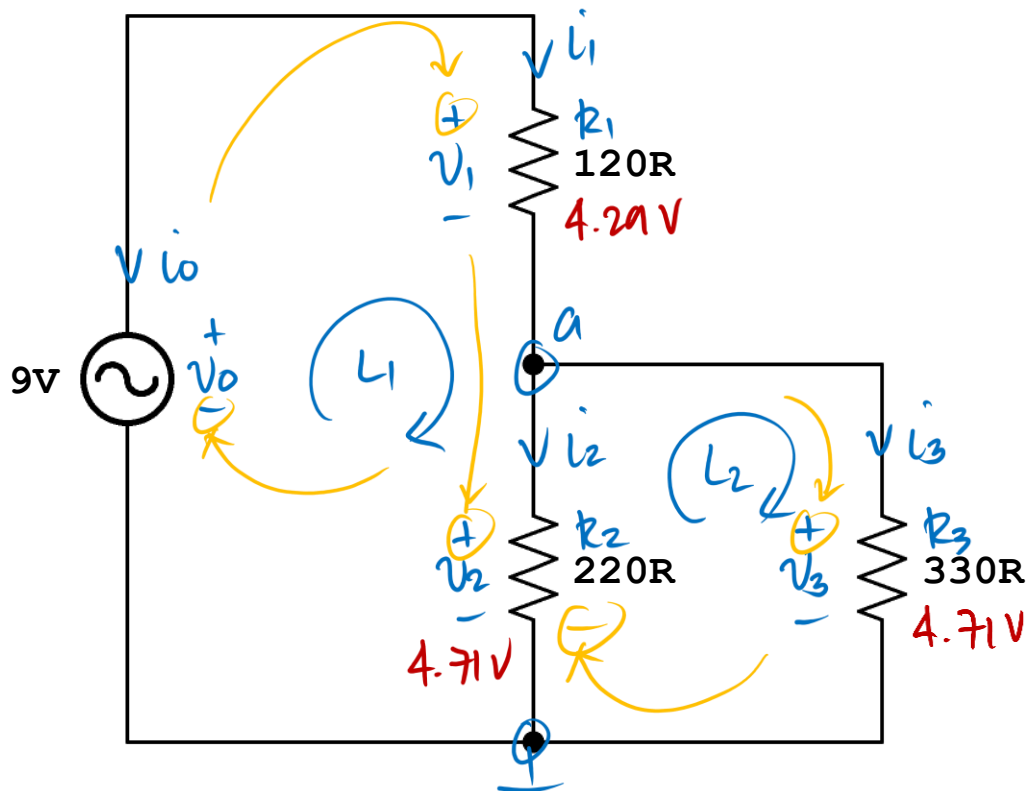
$$V_1 = V_0 - V_2$$
$$= 9 - 4.71$$

$$V_1 = 4.29 \text{ V}$$

ans

EXERCISE

Analyze the given circuit to determine both the current through and the voltage drop across each resistor.



Solution

$$i_1 = \frac{v_1}{R_1} = \frac{4.29}{120}$$

$$i_1 = 35.75 \text{ mA}$$

ans

$$i_2 = \frac{v_2}{R_2} = \frac{4.71}{220}$$

$$i_2 = 21.41 \text{ mA}$$

ans

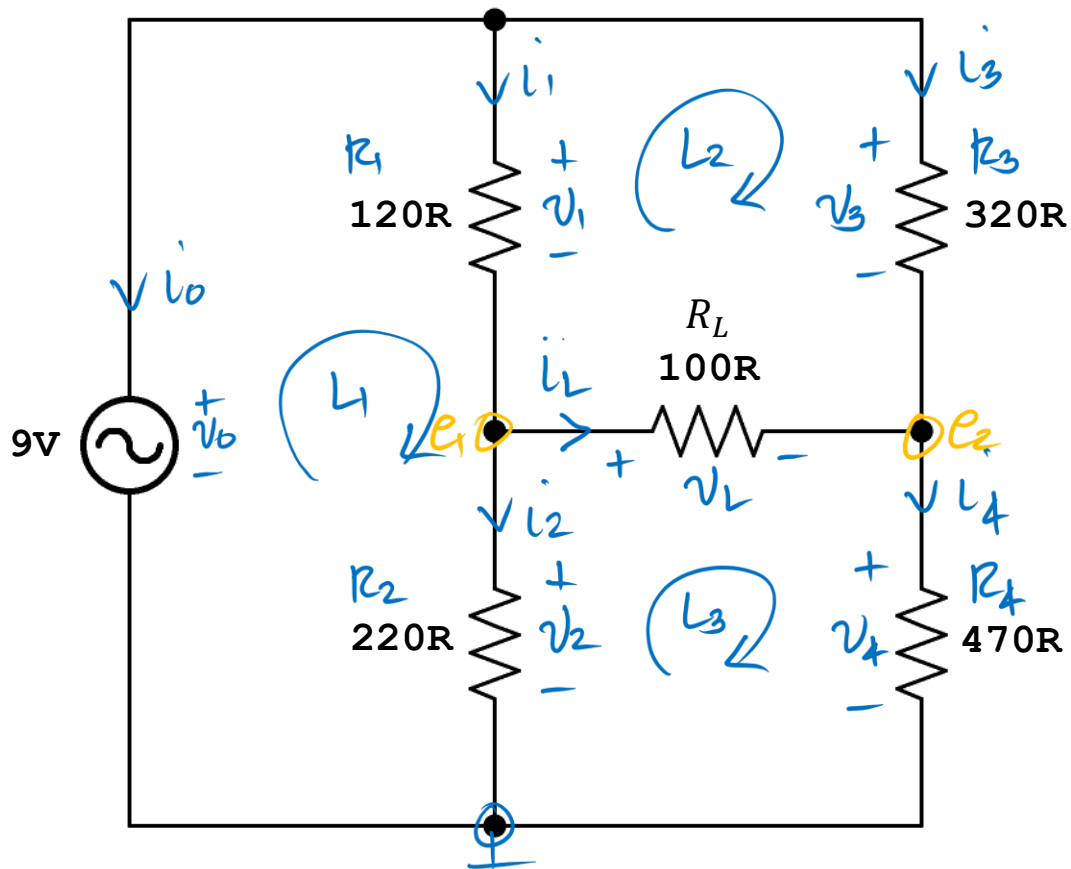
$$i_3 = \frac{v_3}{R_3} = \frac{4.71}{330}$$
$$i_3 = 14.27 \text{ mA}$$

ans



EXERCISE

Determine the voltage drop across the load resistor and the current flowing through it.



Solution

KCL @ e1

$$-i_1 + i_2 + i_L = 0$$

$$-\frac{v_1}{R_1} + \frac{v_2}{R_2} + \frac{v_L}{R_L} = 0$$

$$-v_1 G_1 + v_2 G_2 + v_L G_L = 0 \quad (\text{eq.1})$$

KCL @ e2

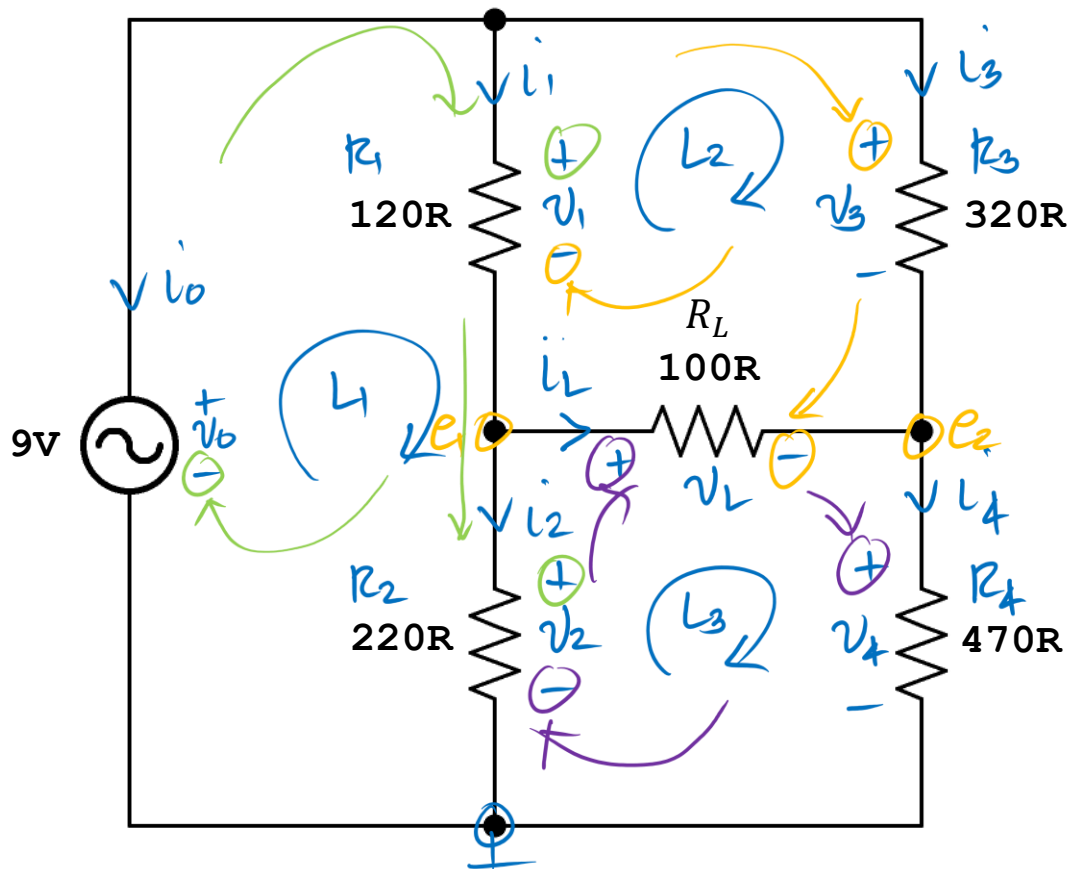
$$-i_3 + i_4 - i_L = 0$$

$$-\frac{v_3}{R_3} + \frac{v_4}{R_4} - \frac{v_L}{R_L} = 0$$

$$-v_3 G_3 + v_4 G_4 - v_L G_L = 0 \quad (\text{eq.2})$$

EXERCISE

Determine the voltage drop across the load resistor and the current flowing through it.



Solution

KVL @ L1

$$-v_0 + v_1 + v_2 = 0$$

$$v_1 + v_2 = v_0 \quad (\text{eq. 3})$$

KVL @ L2

$$-v_1 + v_3 - v_L = 0 \quad (\text{eq. 4})$$

KVL @ L3

$$-v_2 + v_4 + v_L = 0 \quad (\text{eq. 5})$$



EXERCISE

Gaussian Elimination Method

| v_1 | v_2 | v_3 | v_4 | v_L | | |
|------------------|-----------------|------------------|-----------------|------------------|---|-------|
| $-\frac{1}{120}$ | $\frac{1}{220}$ | 0 | 0 | $\frac{1}{100}$ | 0 | r_1 |
| 0 | 0 | $-\frac{1}{320}$ | $\frac{1}{470}$ | $-\frac{1}{100}$ | 0 | r_2 |
| 1 | 1 | 0 | 0 | 0 | 9 | r_3 |
| -1 | 0 | 1 | 0 | -1 | 0 | r_4 |
| 0 | -1 | 0 | 1 | 1 | 0 | r_5 |

System of Linear Equations

$$-\cancel{v_1 \frac{1}{120}} + \cancel{v_2 \frac{1}{220}} + \cancel{v_L \frac{1}{100}} = 0 \quad (\text{eq.1})$$

$$-\cancel{v_3 \frac{1}{320}} + \cancel{v_4 \frac{1}{470}} - \cancel{v_L \frac{1}{100}} = 0 \quad (\text{eq.2})$$

$$v_1 + v_2 = \cancel{20}^9 \quad (\text{eq.3})$$

$$-v_1 + v_3 - v_L = 0 \quad (\text{eq.4})$$

$$-v_2 + v_4 + v_L = 0 \quad (\text{eq.5})$$



LABORATORY

