#### Contents

cardinal.hpp	1
dijkstra.hpp	4
dinic.hpp	4
EK.hpp	5
fft.hpp	6
floyd.hpp	7
graph.hpp	8
kdbitree.hpp	8
kmp.hpp	8
math.hpp	9
matrix.hpp	10
mfset.hpp	11
mint.hpp	11
network.hpp	12
prime.hpp	12
segtree.hpp	13
$\operatorname{sgttree.hpp}$	15
splay.hpp	17
vector.hpp	19

## cardinal.hpp

```
#include <bits/stdc++.h>
using namespace std;
3 using INT=int;
4 //#define int long long
5 #define pb push_back
   #define eb emplace_back
7 #define all(a) (a).begin(),(a).end()
_{8} template<class T>
9 using refT=reference_wrapper<T>;
10 template < class T>
using crefT=reference_wrapper<const T>;
12 auto &_=std::ignore;
using ll=long long;
   template<class T>
14
using vec=vector<T>;
_{16} \quad \textbf{template} \small{<} \textbf{bool} \  \, \textbf{B}, \textbf{class} \  \, \textbf{T} \small{=} \textbf{void} \small{>}
using enableif_t=typename enable_if<B,T>::type;
```

```
18
    #define DEF_COULD(name,exp) \
19
   template<class U> \
20
   struct name{\
21
        template<class T>\
        constexpr static auto is(int i)->decltype(exp,true){return true;}\
23
        template<class T>\
24
        constexpr static bool is(...){return false;}\
25
        static const bool value=is<U>(1);\
26
   };
27
    #define DEF_CAN(name,exp) DEF_COULD(can##name,exp)
28
    #define ENABLE(T,name) enableif_t<can##name<T>::value>(1)
29
    #define ENABLEN(T,name) enableif_t<!can##name<T>::value>(1)
    #define FOR_TUPLE enableif_t<i!=tuple_size<T>::value>(1)
31
    #define END_TUPLE enableif_t<i==tuple_size<T>::value>(1)
32
33
    #define DEF_INF(name,exp)\
34
    constexpr struct{\
35
        template < class T > \setminus
36
        constexpr operator T()const {return numeric_limits<T>::exp();}\
37
38
    } name;
39
   DEF CAN(Out, (cout <<*(T*)(0))) DEF CAN(For, begin(*(T*)(0)))
40
   DEF_INF(INF,max) DEF_INF(MINF,min)
41
42
    template<size_t i,class T>
43
    auto operator>>(istream% is,T &r)->decltype(END_TUPLE,is){
44
        return is;
45
46
    template<size_t i=0,class T>
47
    auto operator>>(istream& is,T &r)->decltype(FOR_TUPLE,is){
48
        is>>get<i>(r);
        return operator>> <i+1>(is,r);
50
    }
51
   template<class T>
52
    auto __format(ostream &os,const char *c,const T& cv)->decltype(ENABLE(T,Out),c+1){
53
        os << cv;
54
        while (*c!='}') c++;
55
        return c+1;
56
   }
57
   template<size_t i,class T>
58
    auto format(ostream &os,const char *c,const T&
59

→ cv) ->decltype (ENABLEN(T, For), END_TUPLE, c+1) {
        return c;
60
61
    template<size_t i=0,class T>
62
    auto __format(ostream &os,const char *c,const T&

¬ cv) ¬>decltype (ENABLEN(T, For), FOR_TUPLE, c+1) {

        while (*c!='\{') os <<*c++;
64
        c=__format(os,c,get<i>(cv));
65
        return __format<i+1>(os,c,cv);
67
    template < class T>
68
   auto __format(ostream &os,const char *c,const T&
69

→ cv) ->decltype(ENABLEN(T,Out),ENABLE(T,For),c+1){
        const char *ct=c+1;
70
```

```
if (cv.size()==0){
71
              while (*ct!='}') ct++;
73
              while (*ct!='}') ct++;
         }else{
              for (auto &i:cv){
76
                   const char *cc=c+1;
77
                  while (*cc!='\{') os << *cc++;
78
                  cc=__format(os,cc,i);
                  while (*cc!='}') os << *cc++;
80
                   ct=cc;
81
              }
         }
         return ct+1;
84
85
     void _format(ostream &os,const char *c){
86
87
         while (*c!='\{'\&\&*c!='\setminus0'\}) os<< *c++;
     }
88
     template<class T,class ...Args>
89
     void _format(ostream &os,const char *c,const T &a,Args&& ...rest){
         while (*c!='\{'\&\&*c!='\setminus0'\}) os<< *c++;
91
         if (*c=='{') c= format(os,c,a);
92
         _format(os,c,forward<Args>(rest)...);
93
     }
94
     template<class ...Args>
95
     string format(const char *c, Args&& ...rest){
96
         ostringstream os;
97
         _format(os,c,forward<Args>(rest)...);
         return os.str();
99
100
     template<class ...Args>
101
     ostream& print(const char *c, Args&& ...rest){return
102
         _format(cout,c,forward<Args>(rest)...),cout;}
103
     #ifdef LOCAL
104
     #define debug(...) cerr<<format(__VA_ARGS__)</pre>
105
106
     #define debug(...) cerr
107
    #endif
108
    template<class T,class ...Args>
109
     struct Rtar{
110
         T& a; tuple < Args...> n;
111
         Rtar(T& a, tuple Args...>n):a(a),n(n){}
112
113
     template<class T,class ...Args>
114
     Rtar<T,Args&...> rtar(T &a,Args&... rest){
115
         return Rtar<T,Args&...>(a,tie(rest...));
116
     }
117
     template<size_t i,class U,class ...Args,class T=tuple<Args&...>>
118
     auto operator>>(istream& is,Rtar<U,Args&...> r)->decltype(END_TUPLE,is){
119
         return is>>r.a;
120
121
     template<size_t i=0,class U,class ...Args,class T=tuple<Args&...>>
122
     auto\ operator >> (istream \&\ is, Rtar < U, Args \& \ldots >\ r) -> decltype(FOR\_TUPLE, is) \{ auto\ operator >> (istream \&\ is, Rtar < U, Args & \ldots >\ r) -> decltype(FOR\_TUPLE, is) \} 
123
         r.a=typename decay<U>::type(get<i>(r.n));
124
         for (auto &w:r.a)
125
```

```
operator>> <i+1>(is,Rtar<decltype(w),Args&...>(w,r.n));
126
        return is;
127
    }
128
    template < class T1, class T2>
129
    bool cmin(T1 &a,const T2 b){return a>b?a=b,1:0;}
130
    template < class T1, class T2>
131
    bool cmax(T1 &a,const T2 b){return a<b?a=b,1:0;}</pre>
132
    template<class T1,class T2,class ...T3>
133
    bool cmin(T1 &a,const T2 b,const T3 ...rest){return cmin(a,b)|cmin(a,rest...);}
    template<class T1,class T2,class ...T3>
135
    bool cmax(T1 &a,const T2 b,const T3 ...rest){return cmax(a,b)|cmax(a,rest...);}
136
    bool MULTIDATA=true;
137
    dijkstra.hpp
    template < class vT = int, class GT >
    vector<vT> dijkstra(const GT &G,int i){
        using P=pair<vT,int>;
        const auto n=G.size();
        vector<vT> dis(n,(vT)INF);
 5
        vector<bool> book(n,true);
 6
        dis[i]=0;
        set<P> p;
        p.insert(make_pair(0,i));
        int now=i;
10
        while (p.size()){
             now=p.begin()->second;p.erase(p.begin());
12
             if (!book[now]) continue;
13
             book[now]=false;
14
             for (auto &e:G[now])
                 if (book[e.v]&&dis[e.v]>dis[now]+e.w){
16
                     p.erase(make_pair(dis[e.v],e.v));
17
                     dis[e.v]=dis[now]+e.w;
                     p.insert(make_pair(dis[e.v],e.v));
                 }
20
21
22
        return dis;
    }
    dinic.hpp
    template < class vT, class T, class lT>
    vT dinic_dfs(T &G, int s, int t, lT &level, vT maxf=INF){
 2
        if (s==t||maxf==0) return maxf;
        vT flow=0;
 4
        for (auto &e:G[s]){
 5
             int v=e.v;
             if (level[v] == level[s] + 1 \% \&e.flow < e.cap) {
                 vT f=dinic_dfs(G,v,t,level,min(e.cap-e.flow,maxf));
 8
                 if (f>0){
 9
                     e.flow+=f;
10
                     e.iedge->flow-=f;
11
                     flow+=f;
12
                     maxf-=f;
13
                     if (maxf==0) break;
```

```
}
15
            }
16
        }
17
        if (flow==0) level[s]=0;
18
        return flow;
19
20
21
   template<class vT,class T>
22
    vT dinic(T &G, int s, int t){
23
        const size_t n=G.size();
24
        vT ans=0;
25
        vector<int> level;
        while([&](){
            level=vector<int>(n,0);
28
            queue<int> q;
29
            level[s]=1;
            q.push(s);
31
            while(!q.empty()){
32
                 int x=q.front();q.pop();
33
                 for(auto &e:G[x]){
                     int v=e.v;
                     if(!level[v])
36
                         if(e.flow<e.cap){</pre>
37
                              level[v]=level[x]+1;
                              q.push(v);
39
                         }
40
                 }
41
            }
            return level[t];
43
44
            while(vT tmp=dinic_dfs<vT>(G,s,t,level)) ans+=tmp;
45
        return ans;
47
   }
48
   EK.hpp
    template < class vT, class GT>
    vT EK(GT &G, int source, int sink){
2
        vector<typename GT::value_type::value_type*> path(G.size());
3
        vT totflow=0;
        while (true){
5
            vector<vT> flow(G.size());
6
            queue<int> q;
            flow[source] = INF;
            q.push(source);
            while (q.size()){
10
                 int x=q.front();q.pop();
11
                 for (auto &e:G[x])
                     if (!flow[e.v]&&e.cap>e.flow){
13
                         path[e.v]=&e;
14
                         flow[e.v]=min(flow[e.u],e.cap-e.flow);
15
                         q.push(e.v);
17
                 if (flow[sink]) break;
```

18

```
}
19
             if (!flow[sink]) break;
20
             for (auto i=path[sink];i!=path[source];i=path[i->u]){
21
                  i->flow+=flow[sink];
                  i->iedge->flow-=flow[sink];
24
             totflow+=flow[sink];
25
26
        return totflow;
27
   }
28
    fft.hpp
    template < class T>
1
    struct Complex{
2
        T x, y;
3
        Complex(T x=0,T y=0):x(x),y(y){}
        operator T(){return x;}
    };
6
    template < class T>
    Complex<T> operator+(const Complex<T> a,const Complex<T> b){return
     \leftarrow Complex<T>(a.x+b.x,a.y+b.y);}
    template < class T>
    Complex<T> operator-(const Complex<T> a,const Complex<T> b){return
10
     \rightarrow Complex<T>(a.x-b.x,a.y-b.y);}
    template < class T>
    Complex<T> operator*(const Complex<T> a,const Complex<T> b){return
12
     \rightarrow Complex<T>(a.x*b.x-a.y*b.y,a.x*b.y+a.y*b.x);}
    template < class T>
13
    Complex<T> operator/(const Complex<T> a,const Complex<T> b){return
     \leftarrow Complex<T>(a.x*b.x+a.y*b.y,a.x*b.y-a.y*b.x)/(b.x*b.x+b.y*b.y);}
    template < class T>
15
    Complex<T>& operator+=(Complex<T> &a,const Complex<T> b) {a.x+=b.x;a.y+=b.y;return a;}
16
    template < class T>
    Complex<T>& operator = (Complex<T> &a,const Complex<T> b) {a.x-=b.x;a.y-=b.y;return a;}
18
    template < class T>
19
    Complex<T>& operator*=(Complex<T> &a,const Complex<T>
     \rightarrow b){tie(a.x,a.y)=make_tuple(a.x*b.x-a.y*b.y,a.x*b.y+a.y*b.x);return a;}
    template < class T>
21
    Complex<T>& operator/=(Complex<T> &a,const Complex<T>
     \Rightarrow b) \{ \texttt{tie}(\texttt{a.x},\texttt{a.y}) = \texttt{make\_tuple}((\texttt{a.x*b.x+a.y*b.y},\texttt{a.x*b.y-a.y*b.x}) / (\texttt{b.x*b.x+b.y*b.y})) ; \texttt{return}(\texttt{b.x+b.x+b.y*b.y}) \} 
    template < class U > class complexT = Complex >
23
    struct fft{
24
        static constexpr T Pi=M_PI;
25
        int size,1,n;
        vector<int> r;
27
        vector<complexT<T>> W[2];
28
        int floorintlog2(int i){
             int k=0;
30
             while (i) i >>= 1, k++;
31
             return k;
32
33
        fft(int size):size(size){
34
             l=floorintlog2(size);
35
```

```
n=1 << 1;
36
             r.resize(n,0);
37
             W[0].resize(n, \{0,0\});
38
             W[1].resize(n, \{0,0\});
39
             for (int i=0;i<n;i++)</pre>
                  r[i]=(r[i>>1]>>1)|((i\&1)<<(1-1));
41
             for (int type:{0,1})
42
                  for (int i=0;i<n;i++)</pre>
43
                      W[type][i] = {cos(Pi/i), (type?1:-1)*sin(Pi/i)};
44
        }
45
        template<int type, class U>
46
        valarray<complexT<T>>> _FFT(const U& B)const{
             using cT=complexT<T>;
             valarray<cT> A(n);
49
             copy(std::begin(B),std::end(B),begin(A));
50
             for (int i=0;i<n;i++)</pre>
                  if(i<r[i]) swap(A[i],A[r[i]]);
52
             for (int mid=1;mid<n;mid<<=1){</pre>
53
                  const cT Wn=W[type][mid];
54
                  for (int R=mid<<1, j=0; j<n; j+=R){</pre>
                      cT w(1,0);
56
                      for (int k=0; k<mid; k++, w=w*Wn){</pre>
57
                           const cT x=A[j+k],y=w*A[j+mid+k];
58
                           A[j+k]=x+y;
59
                           A[j+mid+k]=x-y;
60
61
                  }
62
             }
             return A;
64
65
        template<class U>
66
        valarray<complexT<T>> FFT(const U& A)const{return _FFT<0>(A);}
        template<class vT>
68
        valarray<vT> DFT(const valarray<complexT<T>>& A)const{
69
             auto b=_FFT<1>(A);
             valarray<vT> a(size);
             if (is_integral<vT>::value)
72
                  for (int i=0;i<size;i++)</pre>
73
                      a[i]=llround(b[i]/n);
74
             else
                  for (int i=0;i<n;i++)</pre>
76
                      a[i]=b[i]/n;
77
             return a;
    };
80
    floyd.hpp
    template < class vT = int, class GT>
    vector<vector<vT>>> floyd(const GT &G){
2
        const auto n=G.size();
3
        \verb|vector| < \verb|vector| < \verb|vT>> | dp(n, \verb|vector| < \verb|vT>(n, INF)|);
4
        for (size_t i=0;i<n;i++) dp[i][i]=0;
6
        for (size_t k=0; k< n; k++)
             for (auto &e:G[k])
```

```
cmin(dp[k][e.v],e.w);
       for (size_t k=0;k<n;k++)</pre>
            for (size_t i=0;i<n;i++)</pre>
10
                for (size_t j=0; j<n; j++)
11
                    cmin(dp[i][j],dp[i][k]+dp[k][j]);
13
       return dp;
   }
14
   graph.hpp
   template <class vT>
   struct wedge{int u,v;vT w;};
   template <class vT>
   struct sedge{int u,v;const constexpr static vT w=1;};
   template <template <class vT> class etT,class vT>
   struct graph:public vector<vector<etT<vT>>>{
       using eT=etT<vT>;
       using esT=vector<eT>;
       using GT=vector<esT>;
       using vector<vector<etT<vT>>>::vector;
10
       void addEdge(const eT &a){GT::operator[](a.u).push_back(a);}
11
       void add2Edge(eT a){addEdge(a);swap(a.u,a.v);addEdge(a);}
   };
13
   kdbitree.hpp
   template<class T>
   T lowbit(T a) {return a&(-a);}
   template<class T,size_t n,size_t d,size_t i=0>
   struct kdbitree{
       kdbitree<T,n,d,i+1> a[n];
       void add(const array<int,d>& ax,T v){
            auto x=ax[i];
            while (x < n) a[x].add(ax,v),x+=lowbit(x);
8
9
       T sum(const array<int,d>& ax){
```

```
auto x=ax[i];
12
            while (x>0) ans+=a[x].sum(ax),x-=lowbit(x);
13
            return ans;
15
16
    template < class T, size_t n, size_t d>
17
    struct kdbitree<T,n,d,d>{
18
        Ta;
19
        kdbitree():a(0){}
20
        void add(const array<int,d>& ax,T v){a+=v;}
        T sum(const array<int,d>& ax){return a;}
```

# kmp.hpp

```
template < class T>
vector < int > to_next(T s) {
```

T ans=0;

11

23

```
vector<int> next(s.size(),-1);
3
        next[0]=-1;
        for (int i=1;i<s.size();i++){</pre>
5
            int w=next[i-1];
6
            while (w!=-1\&\&s[w+1]!=s[i]) w=next[w];
            next[i] = (s[w+1] == s[i]) + w;
8
9
        return next;
10
    }
11
    template<class T>
12
    vector<int> kmp(T a,T b){
13
        vector<int> pos;
14
        auto bn=to_next(b);
15
        int ai=0,bi=0;
16
        while (ai<=a.size()){</pre>
17
            if (bi!=b.size()&&a[ai]==b[bi]){
                 ai++;bi++;
19
            }else{
20
                if (bi==b.size()){
21
                     pos.push_back(ai-bi);
                 }
                 if (bi!=0){
24
                     bi=bn[bi-1]+1;
25
                }else{
                     ai++;
27
28
            }
29
        }
        return pos;
31
32
    math.hpp
    #define ATL_MATH
    constexpr ll gcd(ll a,ll b){return b?gcd(b,a%b):a;}
2
    constexpr ll lcm(ll a,ll b){return a*b/gcd(a,b);}
3
    template<class T>
    T power(T a,size_t b,const T &unit=1){
        if (b==0) return unit;
6
        if (b&1) return a*power(a*a,b>>1,unit);
        return power(a*a,b>>1,unit);
    }
9
    constexpr ll ceildiv(const ll a,const ll b){return a/b+(a%b?1:0);}
10
    tuple<11,11,11> exgcd(11 a,11 b){//a1+b2=gcd(a,b)}
11
        if (b==0) return \{a,1,0\};
12
        11 g,x,y;
13
        tie(g,x,y)=exgcd(b,a\%b);
14
        return make_tuple(g,y,x-a/b*y);
15
16
    tuple<11,11,11> Fexgcd(11 a,11 b){\frac{1}{a1+b2=gcd(a,b),ensure}}
17
        auto k=exgcd(a,b);
18
```

if (get<1>(k)<0) {

get<1>(k)+=b;get<2>(k)-=a;

19

21

22

}

```
23     return k;
24 }
```

### matrix.hpp

```
template < class T, size_t n, size_t m>
   struct matrix:public valarray<valarray<T>>{
2
        using base1=valarray<T>;
3
        using base2=valarray<base1>;
        using base2::base2;
       matrix(const T &a):base2(base1(a,m),n){}
        matrix():base2(base1(m),n){}
7
   };
8
9
   template<class T,size_t n,size_t m>
   matrix<T,n,n> operator*(const matrix<T,n,m> &a,const matrix<T,m,n> &b){
11
       matrix<T,n,n> x;
12
        for (size_t i=0;i<n;i++)</pre>
            for (size_t j=0; j<n; j++)</pre>
14
                for (size_t k=0; k<m; k++)</pre>
15
                    x[i][j]+=a[i][k]*b[k][j];
16
        return x;
   }
18
19
   template < class T, class U>
20
   auto operator*(const valarray<T> &a,const U &b)->decltype(b+=1,a){
21
22
        valarray<T> x(a);
        for (auto &i:x) i*=b;
23
       return x;
24
   }
25
26
   template < class T, class U>
27
   auto operator*=(valarray<T> &a,const U &b)->decltype(b+=1,a){
28
        for (auto &i:a) i*=b;
        return a;
30
31
32
   template < class T, size_t n>
33
   matrix<T,n,n> unitmatrix(){
34
       matrix<T,n,n> m;
35
        for (int i=0;i<n;i++) m[i][i]=1;
37
        return m;
38
39
   template<class T,size_t n>
40
   pair<bool, matrix<T,n,n>> inverse(matrix<T,n,n> a){
41
        auto b=unitmatrix<T,n>();
42
        for (int i=0;i<n-1;i++){</pre>
43
            int k=-1;
            45
            if (k!=-1){
46
                swap(b[i],b[k]);swap(a[i],a[k]);
47
                for (int j=i+1; j<n; j++)</pre>
                    if (a[k][i]!=0){
49
                         T d=a[j][i]/a[k][i];
50
```

```
a[j]-=a[k]*d;
51
                         b[j]-=b[k]*d;
52
53
            }else return {false,b};
        }
        for (int i=n-1; i>=0; i--){
56
            b[i]/=a[i][i];a[i]/=a[i][i];
57
            for (int j=i-1; j>=0; j--){}
58
                b[j]-=b[i]*a[j][i];
                a[j]-=a[i]*a[j][i];
60
61
        }
62
        return {true,b};
63
64
   mfset.hpp
   struct mfset:protected vector<int>{
       mfset(){}
2
        mfset(int size){resize(size);}
3
        void resize(int size){
            vector<int>::resize(size);
            iota(this->begin(),this->end(),0);
6
        }
        int find(int a){
            int &b=this->operator[](a);
            return a==b?a:b=find(b);
10
11
        void merge(int a,int b){
12
            int aa=find(a),bb=find(b);
            if (aa!=bb)
14
                this->operator[](bb)=aa;
15
16
   };
   mint.hpp
   #define op_mint(op)\
    _mint operator op (const _mint a)const{_mint k(*this);k op##=a;return k;}
2
   #define cmp_mint(op)\
   bool operator op (const _mint a)const{return v op a.v;}
   template < class T>
5
   struct _mint{
       T v;
        static T mod;
        _mint()=default;
9
        _mint(const T &a){(v=a%mod)<0&&(v+=mod);}
10
        _{\min} operator+=(const _{\min} a){return (v+=a.v)>=mod\&\&(v-=mod),*this;}
        \verb|_mint& operator=(const _mint a){return (v-=a.v)<0&&(v+=mod),*this;}|
12
        _mint& operator*=(const _mint a){return (v*=a.v)%=mod,*this;}
13
        op_mint(+) op_mint(-) op_mint(*)
14
        cmp_mint(<) cmp_mint(>) cmp_mint(<=) cmp_mint(>=) cmp_mint(!=) cmp_mint(==)
15
        #ifdef ATL MATH
16
        _mint inverse(){_mint a;a.v=get<1>(Fexgcd(v,mod));return a;}
17
        _mint& operator/=(const _mint a){return (*this)*=a.inverse()%=mod,*this;}
```

```
op_mint(/)
19
        #endif
20
   };
21
   template<class T>
22
   T _mint<T>::mod;
   template < class T>
24
   ostream& operator<<(ostream& os,const _mint<T>& a){return os<<a.v;}
25
   template<class T>
26
   istream \& operator >> (istream \& os, \_mint < T > \& a) \\ \{T \ k; os >> k; a = \_mint < T > (k); return \ os; \}
27
   using mint=_mint<int>;
28
   using mll=_mint<ll>;
29
    network.hpp
   template <class vT>
    struct fedge{int u,v;vT cap,flow;fedge* iedge;};
   template <class vT>
    struct cfedge{int u,v;vT cap,cost,flow;cfedge* iedge;};
    template <class edgeT>
    struct network:public vector<list<edgeT>>{
6
        using vector<list<edgeT>>::vector;
        using eT=edgeT;
        using esT=list<eT>;
        using GT=vector<esT>;
10
        eT* addFlow(const eT &a){
11
            auto &l=GT::operator[](a.u);
13
            return &*1.insert(l.end(),a);
14
        void add2Flow(eT a){
15
            a.flow=0;
            auto b=addEdge(a);
17
            swap(a.u,a.v);a.cap=0;
18
            auto c=addEdge(a);
19
            tie(b->iedge,c->iedge)=make_tuple(c,b);
21
   };
22
    prime.hpp
    template <size_t n>
    struct Primes{
2
        bitset<n> book;
3
        array<size_t,n> phi;
        vector<size_t> pri;
5
        Primes(){
6
            phi[1]=1;
            for (size_t i=2;i<n;i++){</pre>
                 if (!book[i]) {
                     phi[i]=i-1;
10
                     pri.pb(i);
11
                 }
12
                 for (size_t j=0; j<pri.size();++j) {</pre>
13
                     size_t w=i*pri[j];
14
                     if (w>=n) break;
15
                     book [w]=1;
```

```
if (i%pri[j]) {
17
                         phi[w]=phi[i]*(pri[j]-1);
18
                     } else {
19
                         phi[w]=phi[i]*pri[j];
20
                         break;
                     }
22
                }
23
            }
24
        }
25
        template <class T>
26
        bool is(const T &a)const{return book[a];}
27
        11 operator[](const size_t &i)const{return pri[i];}
   Primes<100000> primes;
30
    segtree.hpp
    template<class T>
    struct segtree{
2
        T fsum;
3
        virtual ~segtree(){}
4
        virtual void dadd(const T &nadd)=0;
        virtual void add(const ll &1,const ll &r,const T &nadd)=0;
6
        virtual void dmul(const T &nadd)=0;
        virtual void mul(const ll &1,const ll &r,const T &nadd)=0;
        virtual T sum(const ll &1,const ll &r)=0;
9
   };
10
    template < class T, class U>
11
    unique_ptr<segtree<T>> make_seg(const U% op,const U% ed);
12
    template < class T>
13
    struct segtreec:public segtree<T>{
14
        using segtree<T>::fsum;
15
        unique_ptr<segtree<T>> lson,rson;
16
        11 count,mid;
        T fadd, fmul;
18
        template<class U>
19
        segtreec(const U% op,const U% ed):fadd(0),fmul(1){
20
            mid=(count=ed-op)>>1;
21
            lson=make_seg<T>(op,op+mid);
22
            rson=make_seg<T>(op+mid,ed);
23
            pushup();
        }
25
        void pushdown(){
26
            lson->dmul(fmul);
27
            rson->dmul(fmul);
28
            fmul=1;
            lson->dadd(fadd);
30
            rson->dadd(fadd);
31
            fadd=0;
33
        void pushup(){
34
            fsum=lson->fsum+rson->fsum;
35
36
        void dadd(const T &nadd){
37
            fadd+=nadd;
38
```

```
fsum+=nadd*count;
39
        }
40
        void add(const ll &1,const ll &r,const T &nadd){
41
            if (1<=1&&count<=r)</pre>
42
                 dadd(nadd);
            else{
44
                 pushdown();
45
                 if (1 \le mid) lson \ge add(1,r,nadd);
46
                 if (r>mid) rson->add(l-mid,r-mid,nadd);
47
                 pushup();
48
49
        }
        void dmul(const T &nmul){
            fmul*=nmul;
52
            fadd*=nmul;
53
            fsum*=nmul;
        }
55
        void mul(const ll &1,const ll &r,const T &nmul){
56
            if (1<=1&&count<=r)</pre>
57
                 dmul(nmul);
            else{
                 pushdown();
60
                 if (l<=mid) lson->mul(l,r,nmul);
61
                 if (r>mid) rson->mul(l-mid,r-mid,nmul);
62
                 pushup();
63
64
65
        T sum(const ll &1,const ll &r){
            if (l<=1&&count<=r) return fsum;</pre>
67
            pushdown();
68
            T ans=0;
69
            if (1 \le mid) ans +=1 \le n-> sum(1,r);
            if (r>mid) ans+=rson->sum(l-mid,r-mid);
71
            return ans;
72
        }
    };
74
    template < class T>
75
    struct segtreen:public segtree<T>{
76
        using segtree<T>::fsum;
77
        template<class U>
        segtreen(const U% op,const U% ed){fsum=*op;}
79
        void dadd(const T &nadd){fsum+=nadd;}
80
        void add(const 11 &1,const 11 &r,const T &nadd){fsum+=nadd;}
        void dmul(const T &nmul){fsum*=nmul;}
        void mul(const ll &1,const ll &r,const T &nmul){fsum*=nmul;}
83
        T sum(const ll &1,const ll &r){return fsum;}
84
    };
85
    template < class T, class U>
86
    unique_ptr<segtree<T>> make_seg(const U& op,const U& ed){
87
        if (ed-op==1) return unique_ptr<segtree<T>>(new segtreen<T>(op,ed));
88
        else return unique_ptr<segtree<T>>(new segtreec<T>(op,ed));
    }
90
```

### sgttree.hpp

```
template < class T, class iT>
    struct sgttree{
2
        constexpr static double s_alpha=0.724;
3
        constexpr static double s_beta=0.35;
        struct Tnode{
            static Tnode nilnode;
            static Tnode* nil;
            T val;
8
            iT cnt,size,cover,rsize;
9
            Tnode *ch[2];
10
            Tnode (T v,iT c){val=v;cnt=size=c;rsize=(c!=0);cover=1;}
11
            ~Tnode(){
12
                if (ch[0]!=Tnode::nil) delete ch[0];
                if (ch[1]!=Tnode::nil) delete ch[1];
14
15
            void maintain(){
16
                             size=cnt+ch[0]->size+ch[1]->size;
                             rsize=(cnt!=0?1:0)+ch[0]->rsize+ch[1]->rsize;
18
                             cover=1+ch[0]->cover+ch[1]->cover;}
19
            void rmaintain(){maintain();cover=rsize;}
20
            bool isBad(){return max(ch[0]->cover,ch[1]->cover)>=
                                  (s_alpha*cover);}
            char cmp(T v){
23
                if (v==val) return -1;
24
                return v>=val;
25
            }
26
            char cmpkth(iT &k){
27
                iT p=k-ch[0]->size;
                if (p<=0) return 0;</pre>
                k=p; p-=cnt;
30
                if (p \le 0) return -1;
31
                k=p;return 1;
32
        };
34
        Tnode *head;
35
        sgttree():head(Tnode::nil){}
37
        ~sgttree(){if (head!=Tnode::nil) delete head;}
38
        int ci;
39
        void toArr(Tnode *e,vector<Tnode*> &g){
40
            if (e==Tnode::nil) return ;
            if (e->ch[0]!=Tnode::nil) toArr(e->ch[0],g);
42
            if (e->cnt) g.pb(e);
43
            if (e->ch[1]!=Tnode::nil) toArr(e->ch[1],g);
            if (!e->cnt) delete e;
45
46
47
        Tnode* toTree(int 1,int r,vector<Tnode*> &g){
            if (l>=r) return Tnode::nil;
49
            int mid=(l+r)>>1;
50
            Tnode &e=*(g[mid]);
51
            e.ch[0]=toTree(1,mid,g);
            e.ch[1] = toTree(mid+1,r,g);
53
            e.maintain();
54
```

```
return &e;
55
         }
56
57
         void reBuild(Tnode *&e){
             if (e!=Tnode::nil){
                  vector<Tnode*> g;
60
                  g.reserve(e->cover);
61
                  toArr(e,g);
62
                  e=toTree(0,g.size(),g);
             }
64
         }
65
         Tnode **to;
         T v;iT s;
68
         void insert(Tnode *&e){
69
             if (e==Tnode::nil){
                  e=new Tnode(v,s);
71
                  e->ch[0]=e->ch[1]=Tnode::nil;
72
                  return ;
73
             }
             char d=e->cmp(v);
             if (d==-1)
76
                  e->cnt+=s;
77
             else insert(e->ch[d]);
             e->maintain();
79
             if (e->isBad()) to=&e,e->rmaintain();
80
         }
81
         void erase(Tnode *&e){
83
             if (e==Tnode::nil) return ;
84
             char d=e->cmp(v);
85
             if (d==-1)
                  e \rightarrow cnt = max(0, e \rightarrow cnt - s);
             else erase(e->ch[d]);
88
             e->maintain();
         }
90
91
         void insert(T vs,iT ss=1){
92
             v=vs; s=ss;
93
             to=&Tnode::nil;
             insert(head);
95
             reBuild(*to);
96
         }
98
         void erase(T vs,iT ss=1){
99
             v=vs;s=ss;
100
101
             erase(head);
             if ((head->cover-head->rsize)>head->cover*s_beta)
102
                  reBuild(head);
103
         }
104
         iT rank(T v){
106
             Tnode *e=head;iT k=1;char d;
107
             while (e!=Tnode::nil\&\&(d=e->cmp(v))!=-1){
108
                  if (d==1) k+=e->ch[0]->size+e->cnt;
109
                  e=e->ch[d];
110
```

```
111
                                               return k+e->ch[0]->size;
112
113
114
                                Tnode* kth(iT k){
                                               Tnode *e=head; char d;
116
                                               while ((d=e->cmpkth(k))!=-1) e=e->ch[d];
117
                                               return e;
118
                                }
119
                };
120
                template < class T, class IT>
121
                typename sgttree<T,IT>::Tnode sgttree<T,IT>::Tnode::nilnode=[](){
122
                                Tnode nil(0,0);
123
                                nil.rsize=nil.cover=0;
124
                                nil.ch[0]=nil.ch[1]=&sgttree<T,IT>::Tnode::nilnode;;
125
                                return nil;
127
                }();
               template < class T, class IT>
128
                \texttt{typename sgttree} < \texttt{T,IT} > : : \texttt{Tnode} * \; \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nil} = \& \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT} > : : \texttt{Tnode} : : \texttt{nilnode} ; \\ \texttt{sgttree} < \texttt{T,IT
129
                splay.hpp
                template < class T, class iT>
                struct splay{
    2
                                struct Tnode{
    3
                                               T val;
                                               iT cnt,size;
                                               Tnode *ch[2];
    6
                                               Tnode (T v,iT c){val=v;size=cnt=c;}
                                               void maintain(){
                                                               size=ch[0]->size+ch[1]->size+cnt;
  10
                                               char cmp(const T& v){
                                                                if (v==val) return -1;
                                                               return val<v;
  13
  14
                                               char cmpkth(iT &k){
  15
                                                               iT p=k-ch[0]->size;
  16
                                                               if (p<=0) return 0;</pre>
  17
                                                               k=p; p-=cnt;
                                                               if (p \le 0) return -1;
                                                               k=p;return 1;
  20
                                               }
  21
                                };
  22
                                static Tnode nilnode;
  23
                                static Tnode* nil;
                                Tnode *head;
  25
  26
                                splay(){
                                               head=nil;
  29
  30
                                void rotate(Tnode *&e,const char d){
  32
                                               if (e==nil) return ;
                                               Tnode *&a=e, *&b=e->ch[d], *&c=e->ch[d]->ch[d^1];
  33
```

```
swap(a,b);swap(b,c);
34
            e->ch[d^1]->maintain();
35
            e->maintain();
36
37
        void Splay(Tnode *&e,const T& v){
39
             if (e==nil) return ;
40
            char d1=e->cmp(v);
41
            if (d1==-1 \mid \mid e->ch[d1]==ni1){
42
                 return ;
43
            }else{
44
                 \begin{array}{ll} \textbf{char} & \texttt{d2=n1->cmp(v);} \end{array}
                 if (d2==-1 || n1->ch[d2]==nil) {rotate(e,d1);return ;}
47
                 else{
48
                     Splay(n1->ch[d2],v);
49
                     if (d1==d2) {rotate(e,d1);rotate(e,d1);}
50
                     else {rotate(n1,d2);rotate(e,d1);}
51
                 }
52
            }
        }
55
        void splaykth(Tnode *&e,iT& k){
56
            if (e==nil) return ;
57
             char d1=e->cmpkth(k);
58
            if (d1==-1 | e->ch[d1]==nil)
59
                 return ;
            }else{
                 Tnode *&n1=e->ch[d1];
62
                 char d2=n1->cmpkth(k);
63
                 if (d2==-1 || n1->ch[d2]==nil) {rotate(e,d1);return ;}
64
                 else{
                     splaykth(n1->ch[d2],k);
66
                     if (d1==d2) {rotate(e,d1);rotate(e,d1);}
67
                     else {rotate(n1,d2);rotate(e,d1);}
                 }
            }
70
71
72
        void _insert(const T& vs,const iT& ss,Tnode *&e){
            if (e==nil){
74
                 e=new Tnode(vs,ss);
                 e->ch[0]=e->ch[1]=nil;
                 return ;
78
            char d=e->cmp(vs);
79
            if (d==-1){
                 e->cnt+=ss;
            }else _insert(vs,ss,e->ch[d]);
82
        }
        void insert(const T& vs,const iT& ss=1){
85
             _insert(vs,ss,head);
86
            Splay(head, vs);
87
        }
89
```

```
void erase(const T& vs,const iT& ss=1){
90
             Splay(head, vs);
             if (ss<head->cnt){
92
                 head->cnt-=ss;
                 head->size-=ss;
                 return ;
95
96
             Tnode *l=head->ch[0], *r=head->ch[1];
97
             delete head;
             if (r!=nil){
99
                 Splay(r,vs+1);
100
                 r->ch[0]=1;
101
                 r->maintain();
102
                 head=r;
103
             }else head=1;
104
        }
105
106
        iT rank(T v){
107
             Splay(head, v);
108
             return head->ch[0]->size+(head->val<v?head->cnt:0)+1;
109
        }
110
111
        Tnode* kth(iT k){
112
             splaykth(head,k);
113
             return head;
114
115
116
117
    template < class T, class IT>
118
    typename splay<T,IT>::Tnode splay<T,IT>::nilnode(0,0);
119
    template < class T, class IT>
120
    typename splay<T,IT>::Tnode* splay<T,IT>::nil=&splay<T,IT>::nilnode;
    vector.hpp
    #define op_array(x) \
    template<class T,size_t d> \
 2
    array<T,d>\& operator x##=(array<T,d>\& a,const array<T,d>\& b)\{for (size_t i=0;i<d;i++) a[i]\}

    x##=b[i];return a;}
\
    template<class T,class U,size_t d>\
    auto operator x##=(array<T,d>& a,const U& b)->decltype(T(declval<U>()),a){for (size_t
     \rightarrow i=0;i<d;i++) a[i] x##=b;return a;}\
    template<class T,size_t d,class U>\
    auto operator x (const array<T,d>% a,const U%
     a b)->decltype(T(declval<U>()),array<T,d>()){array<T,d> k(a);k x##=b;return k;}
    op_array(+) op_array(-) op_array(*) op_array(/)
    template < class T>
 9
    using vec2=array<T,2>;
10
    template < class T>
12
    using vec3=array<T,3>;
    template < class T, size t d>
13
    T dot(const array<T,d>& a,const array<T,d>& b){
14
15
        T ans=0;
        for (size_t i=0;i<d;i++) ans+=a[i]*b[i];</pre>
16
        return ans;
17
```

```
}
18
   template<class T,size_t d>
19
^{20} \quad \text{T abs(const array<T,d>& a){return sqrt(dot(a,a));}}
_{21} template<class T>
   T crs(const vec2<T> &a,const vec2<T> &b){return a[0]*b[1]-a[1]*b[0];}
   template<class T>
23
   vec3<T> crs(const vec3<T> &a,const vec3<T> &b){return
24
    \  \, \leftrightarrow \  \, \{a[1]*b[2]-a[2]*b[1],a[2]*b[0]-a[0]*b[2],a[0]*b[1]-a[1]*b[0]\};\}
   template<class T,size_t d>
   bool operator<(const array<T,d>& a,const array<T,d>& b){for (size_t i=0;i<d;i++) if
26

  (a[i] < b[i]) return true; else if (a[i] < b[i]) return false; return false;}</pre>
   template<class T,size_t d>
27
    istream& operator>>(istream& is,array<T,d> &p){
        for (size_t i=0;i<d;i++) is>>p[i];
29
        return is;
30
   }
31
```