

ROTATE-VECTORS FUNCTION

cross product: $a \times b = \|a\| \|b\| \sin \alpha$

$$e = (v_1 \times v_2)^T (v_1 \times v_2) \sim (\|a\| \|b\|)^2 \sin^2 \alpha$$

$$\dot{e} = 2(v_1 \times v_2)^T (v_1 \times \dot{v}_2 - v_2 \times \dot{v}_1)$$

$$\dot{e} = \underbrace{2(\hat{S}_{v_1} \cdot v_2)^T (\hat{S}_{v_1} \Delta v_2 - \hat{S}_{v_2} \Delta v_1)}_{J_T} \dot{q}$$

$$\begin{aligned} J_T &= 2[\dot{v}_1 \times v_2 + v_1 \times \dot{v}_2](\hat{S}_{v_1} \Delta v_2 - \hat{S}_{v_2} \Delta v_1) + \\ &+ 2(\hat{S}_{v_1} \cdot v_2)^T [\hat{S}_{v_1} \Delta v_2 + \hat{S}_{v_1} \dot{v}_2 - \hat{S}_{v_2} \Delta v_1 - \hat{S}_{v_2} \dot{v}_1] \end{aligned}$$