



$$e = \alpha \cos(\theta_1, \theta_2) - d$$

$$\dot{e} = - \frac{v_2^T \dot{v}_1 + v_1^T \dot{v}_2}{\sqrt{1 - (v_1^T v_2)^2}}$$



$$\dot{e} = - \frac{1}{\sqrt{1 - (v_1^T v_2)^2}} \underbrace{\left[v_2^T v_1 \dot{q}_1 + v_1^T v_2 \dot{q}_2 \right]}_{\dot{J}^T \dot{q}}$$

$$J^T = [k_1 \times v_{f1} \quad \dots \quad k_n \times v_{fn}]$$

$$\dot{J}^T = - \frac{1}{\sqrt{1 - (v_1^T v_2)^2}} \left[\dot{v}_2^T v_1 + v_2^T \dot{v}_1 + v_1^T \dot{v}_2 + v_1^T \dot{v}_2 \right]$$

$$- \left[v_2^T v_1 + v_1^T v_2 \right] \frac{v_1^T v_2 (\dot{v}_1^T v_2 + v_1^T \dot{v}_2)}{(1 - (v_1^T v_2)^2)^{3/2}}$$

$$\dot{J}^T = - \frac{1}{\sqrt{1 - (v_1^T v_2)^2}} \dot{J}^T - \frac{v_1^T v_2 \dot{J}^T}{(1 - (v_1^T v_2)^2)^{3/2}} \dot{J}^T$$