

SMIT vector:

vector-rotation for product

$$\cos(\angle) \vec{v}_1^T \vec{v}_2 = \frac{\vec{v}_2^T \vec{v}_1}{\|\vec{v}_2\| \|\vec{v}_1\|} \sim \|\vec{v}_2\| (\cos \theta - 1)$$

$$\vec{c} = \vec{v}_1^T \vec{v}_2 + \vec{v}_1^T \vec{v}_2 = \frac{\vec{v}_2^T \vec{v}_2}{\|\vec{v}_2\|}$$

$$\vec{c} = \left[ \vec{v}_2^T \Delta v_1 + \vec{v}_1^T \Delta v_2 - \frac{\vec{v}_2^T}{\|\vec{v}_2\|} \Delta v_2 \right] \vec{v}_2$$

$$\vec{c} = \vec{v}_2^T \Delta v_1 + \vec{v}_2^T \Delta v_2 + \vec{v}_1^T \Delta v_2 - \frac{\vec{v}_2^T}{\|\vec{v}_2\|} \Delta v_2 - \left( \frac{\vec{v}_2^T}{\|\vec{v}_2\|} - \frac{\vec{v}_2^T \vec{v}_2}{(\vec{v}_2^T \vec{v}_2)^{3/2}} \right) \Delta v_2$$