



$$A(x, y, z) \Rightarrow A'(x', y', z')$$

绕Z轴:

$$\begin{cases} x' = r \cdot \cos(\alpha - \theta) \\ y' = r \cdot \sin(\alpha - \theta) \\ z' = z \end{cases}$$

$$\Rightarrow \begin{cases} x' = r \cdot (\cos\alpha \cos\theta + \sin\alpha \sin\theta) \\ y' = r \cdot (\sin\alpha \cos\theta - \cos\alpha \sin\theta) \\ z' = z \end{cases}$$

$$\Rightarrow \begin{cases} x' = \cos\theta \cdot x + \sin\theta \cdot y \\ y' = -\sin\theta \cdot x + \cos\theta \cdot y \\ z' = z \end{cases}$$

$$\Rightarrow \begin{pmatrix} \cos\theta & \sin\theta & 0 \\ -\sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} \cos\theta x + \sin\theta y \\ \cos\theta y - \sin\theta x \\ z \end{pmatrix}$$

绕Y轴:

$$\begin{cases} x' = r \cdot \cos(\alpha - \theta) \\ y' = y \\ z' = r \cdot \sin(\alpha - \theta) \end{cases}$$

$$\Rightarrow \begin{cases} x' = r(\cos\theta \cos\alpha + \sin\alpha \sin\theta) \\ y' = y \\ z' = r(\sin\alpha \cos\theta - \sin\theta \cos\alpha) \end{cases}$$

$$\Rightarrow \begin{cases} x' = \cos\theta \cdot x + z \cdot \sin\theta \\ y' = y \\ z' = z \cos\theta - x \sin\theta \end{cases}$$

$$\Rightarrow \begin{pmatrix} \cos\theta & 0 & \sin\theta \\ 0 & 1 & 0 \\ -\sin\theta & 0 & \cos\theta \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix}$$