1. Abstract - Introduction We propose a decentralized reputation system that can replace the word-of-mouth, stars- and review-based systems. The basic idea is that a member A trusts her friends with a certain value (with a 1/2 multisig), thus risking to lose their value. When A wants to transfer value V to a (maybe previously unknown) member B, A asks the system if she trusts B enough to transfer this value to B. The system will search throughout the network for trust paths that begin from A and reach B and add up to V and will answer whether the proposed transaction is within the trust capabilities of A towards B. If the answer is positive, it means that transferring value V to B will not raise the risk for A to lose their value. Note: we use Bitcoin terminology.

2. Related Work

3. Key points

Definitions

- Direct trust from A to B, $DTr_{A \to B}$
  Total amount of value that exists in 1/{A,B} multisigs in the utxo, where the money is deposited by A
- B steals x from A
  B steals value x from A when B reduces the $DTr_{A \to B}$ by x. This makes sense when $x \leq DTr_{A \to B}$.
- Honest (passive) strategy
  A member A is said to follow the honest (passive) strategy if for any value x that is stolen from her, she substitutes it by stealing from others that trust her:

$$\begin{cases} x \text{ if } \sum_{B \in members} DTr_{B \to A} \geq x \\ \sum_{B \in members} DTr_{B \to A} \text{if} \sum_{B \in members} DTr_{B \to A} < x \end{cases}$$

  or simply $min(x, \sum_{B \in members} DTr_{B \to A})$.
- Indirect trust from A to B $Tr_{A \to B}$
  Value that A will lose if B steals the maximum amount she can steal (all her incoming trust) and everyone else follows the honest (passive) strategy.

Theorems

- $Tr_{A \to B} = MaxFlow_{A \to B}$ (Treating trusts as capacities)
- Trust transfer theorem (flow terminology)
  Let s source, t sink,
  $X_s = \{x_{s \to 1}, ..., x_{s \to n}\}$ outgoing flows from s,
  $X_t = \{x_{1 \to t}, ..., x_{m \to t}\}$ incoming flows to t,
  $U_s = \{u_{s \to 1}, ..., u_{s \to n}\}$ outgoing capacities from s,
  $U_t = \{u_{1 \to t}, ..., u_{m \to t}\}$ incoming capacities to t,
  V the value to be transferred.
  Nodes apart from s, t cannot create or consume flow.
  Obviously $maxFlow = F = \sum_{i=1}^{n} x_{t \to i}$.

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     /                    ....                  \
    / x_s1/u_s1                    x_1t/u_1t \
   /                                               \
  /                                                 \
 / x_s2/u_s2                         x_2t/u_2t \
s-------------            ....       ------------t
 \      .                                  .    /
  \     .                                  .   /
   \    .                                  .  /
    \ x_sn/u_sn           ....     x_mt/u_mt /
     \                                         /
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We create a new graph where

(a) $\sum_i u'_{s \to i} = F - V$
(b) $u'_{s \to i} \leq x_{s \to i}$

We will now prove that $maxFlow' = F' = F - V$.

(a) It is impossible to have $F' > F - V$ because $F' \leq \sum u'_{s \to i} = F - V$.
(b) It is impossible to have $F' < F - V$.
Let i be a node such that $x_{s \to i} > 0$ and $I = \{(i, j) \in E\}$ the set of direct trusts outgoing from i. In the initial graph we have $x_{s \to i} = \sum_j x_{i \to j}, F = \sum_i x_{s \to i}$ and in the new graph we have $x'_{s \to i} = u'_{s \to i} \leq x_{s \to i}, F' = \sum_i x'_{s \to i}, x_{i \to j} \leq u_{i \to j} = u'_{i \to j} \forall j, i.$ We can construct a set $X'_i = \{x'_{i \to j}\}$ of flows such that $x'_{i \to j} \leq x_{i \to j}$ and $\sum_j x'_{i \to j} = x'_{s \to i}$. This shows that there is a possible flow such that $F' = F - V$, so the maxFlow algorithm will not return a flow less than $F - V$.
Example construction:
$x'_{i \to j} = x_{i \to j} \forall j \in \{1, ..., k\}$ with k such that
   i. $\sum_{j=1}^{k} x_{i \to j} \leq x'_{s \to i}$ and
   ii. $\sum_{j=1}^{k+1} x_{i \to j} > x'_{s \to i}$
$x'_{i \to (k+1)} = x'_{s \to i} - \sum_{j=1}^{k} x'_{i \to j}$
$x'_{i \to j} = 0 \forall j \in \{k + 2, ..., |X'_i|\}$

4. Further Research

5. References

6. Tags/Keywords decentralized, trust, reputation, web-of-trust, bitcoin, multisig, line-of-credit, trust-as-risk, flow