## What is Trust

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 $\bf Abstract.$  We will try to define all the abstract properties that we would like "Trust" to have.

# 1 High-level idea

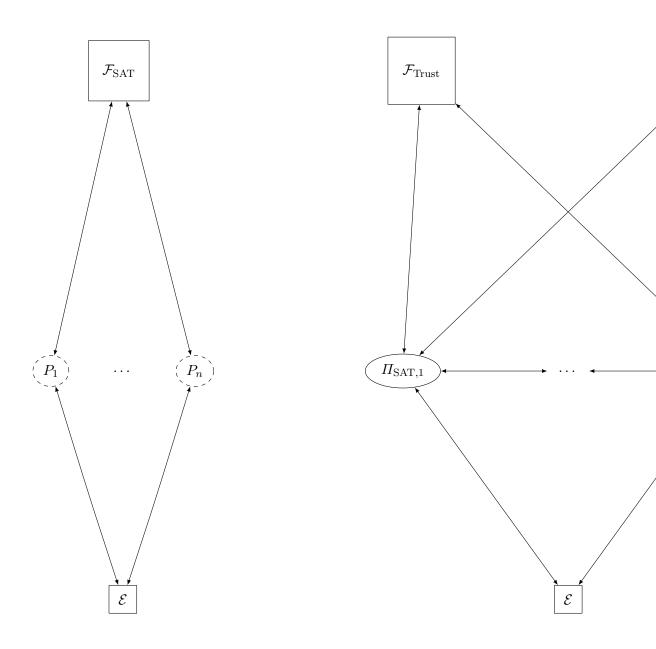


Fig. 1: (Almost) all functionalities

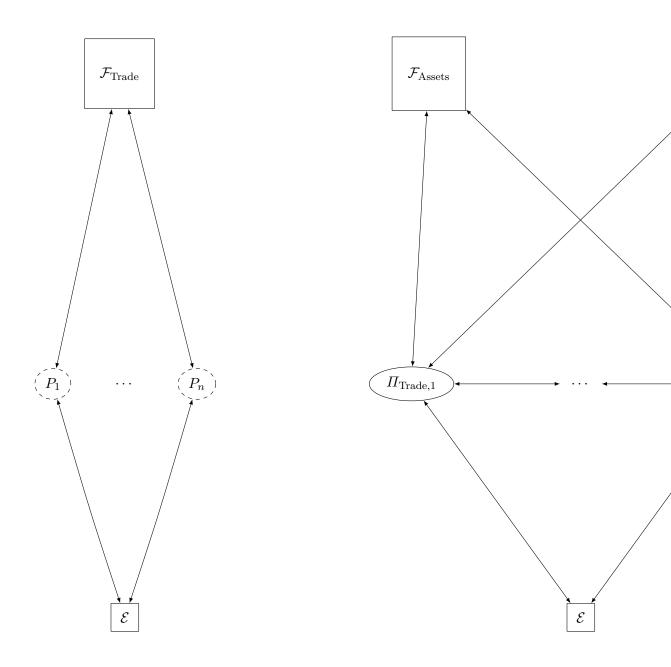


Fig. 2: Trade functionality and protocol

## 2 Utility Function Properties

Before Alice (an ITM that executes  $\Pi_{SAT}$ ) can take any action, she must be assigned a utility function,  $U_{Alice}$ , and a discount function,  $\lambda_{Alice}$ , by  $\mathcal{E}$ .

**Definition 1 (Utility Function).**  $U_{Alice}: Money \times multiset (Asset) \times Rep \rightarrow Utility, where <math>Money, Rep \in \mathbb{N}, Utility \in \mathbb{R}$ .

The utility function is strictly increasing with respect to the integer Money and may do anything with respect to the quantity of any single Asset or combination of Assets. It is also strictly increasing with respect to the integer Rep.

**Definition 2 (Reputation function).** Reputation :  $\mathcal{P} \times Time \times 2^{Asset} \rightarrow Rep$ , where  $Time, Rep \in \mathbb{N}$ 

$$Rep\left(Alice,t,set\right) > Rep\left(Bob,t,set\right) \stackrel{\text{def}}{\Longleftrightarrow}$$
 
$$\Pr\left[Alice \text{ receives message (canYouSatisfy},d) \text{ at time t}\right] >$$
 
$$\Pr\left[Bob \text{ receives message (canYouSatisfy},d) \text{ at time t}\right]$$
 
$$\text{where } d \in set$$

Rep is an integer that corresponds to Alice's perceived rank in a partial ordering of all the players where Alice assumes that she has a higher rank than Bob if the average probability of third players choosing her before Bob when they want to buy something amongst a list of Assets that Alice is interested in selling is higher than Bob's corresponding probability for the same Assets, as perceived by Alice.

**Definition 3 (Discount function).**  $\lambda_{Alice} : Time \rightarrow [0, 1], where Time \in \mathbb{N}$  and  $\lambda$  is strictly decreasing.

**Definition 4 (State).** Let  $state_{Alice} : Time \rightarrow Money \times multiset (Asset) \times Rep.$ 

Alice's target is to maximise

$$\sum_{t=1}^{\infty} \lambda_{Alice}\left(t\right) \left( \sum_{\substack{(m,a,r) \in \\ Money \times mset(Asset) \times Rep}} U_{Alice}\left(m,a,r\right) \cdot \Pr\left[state_{Alice}\left(t\right) = (m,a,r)\right] \right) \ .$$

#### 3 Protocol

In this section we will describe the real protocol executed by the players in the absence of the  $\mathcal{F}_{SAT}$  ideal functionality. The description of this protocol does not need any utility function; all the "important" decisions are taken by the environment.

Consider an environment  $\mathcal{E}$ , and adversary  $\mathcal{A}$  and n players executing copies of the same protocol  $\Pi_1, \ldots, \Pi_n$ .  $\mathcal{E}$  can send the following messages to  $\Pi_i$ :

- 1. Manage player desires
  - (a) Satisfy  $d \in \mathcal{D}$  through a player in  $L \subseteq [n]$
  - (b) Abort attempt to satisfy  $d \in \mathcal{D}$
- 2. Manage offered desires satisfaction
  - (a) Gain the ability to satisfy  $d \in \mathcal{D}$  for players in  $L \subseteq [n]$  for a price  $x \in \mathbb{N}$
  - (b) Lose the ability to satisfy  $d \in \mathcal{D}$  for players in  $L \subseteq [n]$  for a price  $x \in \mathbb{N}$
- 3. Satisfy another player's desire
  - (a) Satisfy player's  $i \in [n]$  desire  $d \in \mathcal{D}$  with the corresponding satisfaction string s
  - (b) Satisfy player's  $i \in [n]$  desire  $d \in \mathcal{D}$  with the satisfaction string s' (normally suitable for satisfying  $d' \neq d, d' \in \mathcal{D}$ )
  - (c) Ignore player's  $i \in [n]$  desire  $d \in \mathcal{D}$
- 4. Manage direct trusts
  - (a) Increase direct trust to player  $i \in [n]$  by  $x \in \mathbb{N}$
  - (b) Decrease direct trust to player  $i \in [n]$  by  $x \in \mathbb{N}$
  - (c) Steal direct trust  $x \in \mathbb{N}$  from player  $i \in [n]$

Some of these messages (e.g. 1b) are meaningful only when some other messages have been delivered previously (e.g. 1a).  $\mathcal{E}$  may send such messages even when they are not meaningful; the protocol should take care to reject/ignore such messages.

Let  $i \in [n]$ .  $\Pi_i$  can send the following messages to  $\mathcal{E}$ :

- 1. No player in L can satisfy my desire  $d \in \mathcal{D}$
- 2. Desire  $d \in \mathcal{D}$  made available for satisfaction amongst  $L \subseteq [n]$  for price  $x \in \mathbb{N}$
- 3. Desire  $d \in \mathcal{D}$  made unavailable for satisfaction amongst  $L \subseteq [n]$  for price  $x \in \mathbb{N}$
- 4. Payment  $x \in \mathbb{N}$  has been sent to player  $j \in [n]$  for the satisfaction of desire  $d \in \mathcal{D}$

- 5. Correct Payment  $x \in \mathbb{N}$  from player  $j \in [n]$  for the satisfaction of desire  $d \in \mathcal{D}$  has been received
- 6. Wrong Payment  $x \in \mathbb{N}$  from player  $j \in [n]$  for the satisfaction of desire  $d \in \mathcal{D}$  has been received
- 7. Player  $j \in [n]$  has satisfied my desire  $d \in \mathcal{D}$  with satisfaction string s
- 8. Player  $j \in [n]$  has partially satisfied my desire  $d \in \mathcal{D}$  with satisfaction string s' (normally suitable for satisfying  $d' \neq d, d' \in \mathcal{D}$ )
- 9. Player  $j \in [n]$  has ignored my desire  $d \in \mathcal{D}$
- 10. Direct trust to player  $i \in [n]$  increased by  $x \in \mathbb{N}$
- 11. Direct trust to player  $i \in [n]$  decreased by  $x \in \mathbb{N}$
- 12. Stole  $x \in \mathbb{N}$  from player's  $i \in [n]$  direct trust

 $\Pi_i$  should only send these messages when  $\mathcal{E}$  is expecting them.

Let  $i, j \in [n]$  The messages that can be sent between  $\Pi_i$  and  $\Pi_j$  are the following:

- 1. Can you satisfy  $d \in \mathcal{D}$ ?
- 2. I can satisfy  $d \in \mathcal{D}$  for a price  $x \in \mathbb{N}$
- 3. I cannot satisfy  $d \in \mathcal{D}$
- 4. Payment of  $x \in \mathbb{N}$  for satisfaction of  $d \in \mathcal{D}$  sent
- 5. Satisfaction string s', response to payment of  $x \in \mathbb{N}$  for  $d \in \mathcal{D}$

 $\Pi_i$  is supposed to send 4 when it has already paid through  $\mathcal{F}_{Ledger}$ . Similarly, it is supposed to send 5 when it has verified that the other party has sent the corresponding payment on  $\mathcal{F}_{Ledger}$ .

Going in more detail, the actual protocol is as follows:

```
\Pi_{\text{SAT}}
    Initalization:
      util = \bot
2
   Upon receiving (type, t) from \mathcal{E}:
      util = t
    Upon receiving message (satisfy, d, L) from \mathcal{E}:
      If util == \bot:
         send message (utilityNotSet) to {\mathcal E}
         go to Idle state
10
      aux = L
11
      While (aux \neq \emptyset):
         send message (chooseBestSeller, d, aux) to \mathcal{F}_{\mathrm{Trust}}
13
         wait for response1 from \mathcal{F}_{\mathrm{Trust}}
14
```

```
If response1 == (bestSeller, d, L, Bob):
           send message (canYouSatisfy, d) to Bob
16
           wait for response2 from Bob
17
           If response2 == (IcanSatisfy, d, x, s):
18
             If util(state \cup s - x) > util(state) and s \in d
19
               send message (trade, x, s, Bob) to \mathcal{F}_{\mathrm{Trade}}
20
               wait for response3 from \mathcal{F}_{\mathrm{Trade}}
                  If response3 == (traded, x, s, Bob):
                    send message (satisfied, d, x, s, Bob) to \mathcal{F}_{Trust}
23
                    # maybe send only utility difference to \mathcal{F}_{\mathrm{Trust}}
24
                    send message (satisfied, d, L) to \mathcal{E}
25
                    go to Idle state
26
                  Else If response3 == (cheated, x, s, Bob):
27
                    send message (cheated, d, x, s, Bob) to \mathcal{F}_{Trust}
                    send message (cheated, d, L) to \mathcal{E}
                    go to Idle state
30
        Else: # if response1 == \bot
31
           send message (unsatisfied, d, L) to \mathcal{E}
32
           go to Idle state
33
         aux = aux \setminus \{Bob\} # only when response2 is not good
34
      send message (unsatisfied, d, L) to \mathcal{E}
35
36
    Upon receiving message (obtain, s) from \mathcal{E}:
37
      send message (obtain, s) to \mathcal{F}_{\mathrm{Trade}}
38
      wait for response from \mathcal{F}_{\mathrm{Trade}}
39
      If response == (obtained, s):
40
         send message (obtained, s) to {\cal E}
41
      Else:
42
         send message (notObtained, s) to {\cal E}
43
    Upon receiving message (lose, s) from \mathcal{E}:
45
      send message (lose, s) to \mathcal{F}_{\mathrm{Trade}}
46
      wait for response from \mathcal{F}_{\mathrm{Trade}}
47
      If response == (lost, s):
48
        send message (lost, s) to {\cal E}
49
      Else:
50
         send message (notLost, s) to {\cal E}
51
    Upon receiving message (canYouSatisfy, d) from Alice:
53
      If util == \bot:
54
```

```
ignore request, go to Idle state
55
      If (util(state + x + badRep) > util(state) or
56
          \mathtt{util}(state \setminus s + x + qoodRep) > \mathtt{util}(state)) and s \in d:
57
        send message (IcanSatisfy, d, x, s) to Alice \# x is the
58
             price
      Else:
59
        send message (IcannotSatisfy, d) to Alice
60
61
    Upon receiving message (willWeCheat, x, s, Alice) from \mathcal{F}_{Trade}:
62
      If util == \perp: # (Unreachable since we've already engaged)
63
        ignore request, go to Idle state
64
      If util(state \setminus s + x + goodRep) \geq util(state + x + badRep):
65
        send message (doNotCheat, x, s, Alice) to \mathcal{F}_{\mathrm{Trade}}
66
      Else:
67
        send message (cheat, x, s, Alice) to \mathcal{F}_{Trade}
```

### 4 Desire Satisfaction Ideal Functionality

Following the UC paradigm, in this section we define the ideal functionality for desire satisfaction,  $\mathcal{F}_{SAT}$ . In this setting, all the desires that are generated by the environment and are input to the players are immediately forwarded to  $\mathcal{F}_{SAT}$ ; the functionality decides which desires to satisfy. Since the players are dummy and all desires are satisfied by the functionality, no trust semantics amongst the players are necessary.

Nevertheless, given that all desires have a minimum cost, the cost semantics are still necessary, as we show with the following example: Consider a set of desires D with more elements than the total number of tokens all players have. D could never be satisfied by the players because of the high total cost, but a  $\mathcal{F}_{\text{SAT}}$  with no consideration for cost could in principle satisfy all desires in D.

The functionality can calculate the properties and functions defined in ??, ?? and ?? for all inputs at any moment in time.

Without knowledge of the utilities the environment is going to give to each satisfied desire, the functionality may fail spectacularly. So knowledge of the utility of each desire, or at least some function of the utility given the desires is needed. We can assume that  $\mathcal{F}_{SAT}$  knows U or an approximation of it.

Going into more detail,  $\mathcal{F}_{SAT}$  is a stateful process that acts as a market and as a bank for the players. The market does not offer a particular product for the same price to all users; For some users it may be cheaper

than for others, reflecting the fact that some players can realize some desires more efficiently than others.

 $\mathcal{F}_{\mathrm{SAT}}$  stores a number for each player that represents the amount of tokens this player has and a table with the price of each desire for each player. It provides the functions cost(u,d) which returns the cost of the desire d for player u with no side effects, sat(u,d) that returns the string that satisfies the desire d to u and reduces the amount of the tokens belonging to u by cost(u,d). There exists also the function  $transfer(u_1,u_2,t)$  which reduces the amount of tokens  $u_1$  has by t and increases the tokens of  $u_2$  by t, given that initially the tokens belonging to  $u_1$  were equal or more than t. This function is private to the functionality, thus can be used only internally.

```
\mathcal{F}_{\mathrm{SAT}}
    Initialisation:
      \forall Alice \in \mathcal{P},
         util(Alice) = \bot
3
         assets(Alice) = \bot
4
    Upon receiving (type, t) from Alice:
      util(Alice) = t
    Upon receiving (satisfy, d, L) from Alice:
       If util(Alice) == \bot:
10
         send message (utilityNotSet) to Alice
11
         go to Idle state
12
       find list = \{(Bob, x, s) \in L \times \mathbb{R} \times Assets : 
13
         s \in \mathtt{assets}(Bob) and s \in d and x \ge 0 and
         Alice has at least x coins available and
15
         \mathtt{util}(Alice) (state_{Alice} \cup s - x) > \mathtt{util}(Alice) (state_{Alice})
16
         and
17
         util(Bob)(state_{Bob} \setminus s + x) \ge util(Bob)(state_{Bob})
18
       send (chooseBestSeller, list, d, Alice) to {\cal A}
19
       wait for response from {\cal A}
20
       If response \neq (bestSeller, list, Bob, x, s),
21
           Bob \in \mathcal{P}, x \in Money, s \in Asset:
         # e.g. Bob = \bot
22
         (Bob, x, s) =
                             \operatorname{argmax} \{\operatorname{util}(Alice)(\operatorname{state}_{Alice} \cup s - x)\}
23
                          (Bob,x,s) \in list
       Else:
24
         parse response as (bestSeller, list, Bob, x, s)
25
```

```
pay x from Alice to Bob
     assets(Bob) = assets(Bob) \setminus \{s\}
27
     assets(Alice) = assets(Alice) \cup \{s\}
28
     send message (satisfied, d, L) to Alice
29
30
   Upon receiving (obtain, s) from Alice:
31
     assets(Alice) = assets(Alice) \cup \{s\}
     send message (obtained, s) to Alice
34
   Upon receiving (lose, s) from Alice:
35
     assets(Alice) = assets(Alice) \setminus \{s\}
36
     send message (lost, s) to Alice
37
   \mathcal{F}_{\mathrm{Trade}}
   Initialisation:
     \forall Alice \in \mathcal{P},
        assets(Alice) = \bot
   Upon receiving (trade, ours, theirs, Bob) from Alice:
     If not isAvailable(ours, Alice):
        send message (youDontHave, ours) to Alice
        go to Idle state
     If transfer(ours, Alice, Bob) == True:
        send message (willWeCheat, ours, theirs, Alice) to Bob
10
        wait for response from Bob
11
        If (response == (complete, x, s, Alice) and
12
          not is Available (s, Bob)) or
13
          response \neq (complete, x, s, Alice):
14
            send message (youDontHave, s) to Bob
            send message (cheated, ours, theirs, Bob) to Alice
            go to Idle state
       Else If (transfer, theirs, Bob, Alice) == True:
          send message (traded, ours, theirs, Bob) to Alice
19
     Else # failed to give (Unreachable for a good \mathcal{F}_{\mathrm{Ledger}})
20
        send message (failed, ours, theirs, Bob) to Alice
21
22
   isAvailable(object, player):
23
     If object is money:
        send (doIhaveBalance, object) to \mathcal{F}_{\mathrm{Ledger}} as player
        wait for response from \mathcal{F}_{\mathrm{Ledger}}
26
```

```
return response
     Else: # object is asset
28
        If object \in assets(player):
29
          return True
30
        Else:
31
          return False
32
   transfer(object, sender, receiver):
      If isAvailable(object):
35
        If object is money:
36
          send (pay, object, receiver) to \mathcal{F}_{\mathrm{Ledger}} as sender
37
          wait for response from \mathcal{F}_{\mathrm{Ledger}}
38
          Upon receiving (paymentDone, object, receiver):
39
            return True
        Else: # object is asset
          assets(sender) = assets(sender) \ { object }
42
          assets(receiver) = assets(receiver) ∪{object}
43
          return True
44
      return False
45
46
   Upon receiving (obtain, s) from Alice:
47
      assets(Alice) = assets(Alice) \cup \{s\}
      send message (obtained, s) to Alice
49
   Upon receiving (lose, s) from Alice:
51
      assets(Alice) = assets(Alice) \setminus \{s\}
52
      send message (lost, s) to Alice
   \mathcal{F}_{\mathrm{Assets}}
   Initialisation:
     \forall Alice \in \mathcal{P},
        assets(Alice) = \bot
   Upon receiving (add, asset) from Alice:
      assets(Alice) = assets(Alice) \cup \{asset\}
      send (added, asset) to Alice
   Upon receiving (remove, asset) from Alice:
      If asset \in assets(Alice):
        assets(Alice) = assets(Alice) \setminus \{asset\}
11
```

```
send (removed, asset) to Alice
     Else:
13
       send (unableToRemove, asset) to Alice
14
15
   Upon receiving (howManyDoIhave, asset) from Alice:
16
     send (youHave, assets(Alice).count(asset)) to Alice
   Upon receiving (transfer, asset, Bob) from Alice:
     If asset \in assets(Alice):
       assets(Alice) = assets(Alice) \setminus \{asset\}
21
       assets(Alice) = assets(Bob) \cup \{asset\}
22
       send (transferred, asset, Bob) to Alice
23
     Else:
24
       send (unableToTransfer, asset, Bob) to Alice
25
   \Pi_{\text{Trade}}
   Upon receiving (trade, ours, theirs, Bob) from \mathcal{E}:
     Send (letsTrade, ours, theirs) to Bob
     If transfer(ours, Bob) == True:
       Send (transferred, ours, Bob) to Bob and {\cal E}
       Wait for response from Bob
       If response == (transferred, theirs, Bob):
         send message (traded, ours, theirs, Bob) to {\mathcal E}
       Else:
          send message (cheated, ours, theirs, Bob) to {\cal E}
10
   Upon receiving (letsTrade, theirs, ours) from Bob:
11
     Send (willWeCheat, theirs, ours, Bob) to \mathcal{E}
12
     Wait for response from {\mathcal E}
13
     If response is (doNotCheat, theirs, ours, Bob):
       If (transfer, ours, Bob) == True:
         Send (transferred, ours, Bob) to Bob and {\cal E}
17
   transfer(object, receiver):
18
     If isAvailable(object):
19
       If object is money:
20
         send (pay, object, receiver) to \mathcal{F}_{\mathrm{Ledger}}
21
         wait for response from \mathcal{F}_{\mathrm{Ledger}}
22
         Upon receiving (paymentDone, object, receiver):
            return True
24
```

```
Else: # object is asset
           send (transfer, object, receiver) to \mathcal{F}_{\mathrm{Assets}}
26
           wait for response from \mathcal{F}_{\mathrm{Assets}}
           Upon receiving (transferDone, object, receiver):
2.8
              return True
29
       return False
30
    isAvailable(object):
       If object is money:
33
         send (doIhaveBalance, object) to \mathcal{F}_{\mathrm{Ledger}}
34
         wait for response from \mathcal{F}_{\mathrm{Ledger}}
35
         return response
36
       Else: # object is asset
37
         Send (doIHave, object) to \mathcal{F}_{\mathrm{Assets}}
         wait for response from \mathcal{F}_{\mathrm{Assets}}
         If response == (youHave, object):
           return True
         Else:
42
           return False
43
44
    Upon receiving message (obtain, s) from \mathcal{E}:
45
       send message (add, s) to \mathcal{F}_{\mathrm{Assets}}
       wait for response from \mathcal{F}_{\mathrm{Assets}}
47
       If response == (added, s)
         send message (obtained, s) to {\cal E}
49
       Else
50
         send message (notObtained, s) to {\mathcal E}
51
52
    Upon receiving message (lose, s) from \mathcal{E}:
       send message (remove, s) to \mathcal{F}_{\mathrm{Assets}}
       wait for response from \mathcal{F}_{\mathrm{Assets}}
55
       If response == (removed, s)
56
         send message (lost, s) to \mathcal{E}
57
      Else
58
         send message (notLost, s) to {\cal E}
59
```

## 5 $\mathcal{F}_{\mathrm{SAT}}$ and $\Pi_{\mathrm{SAT}}$ are potentially distinguishable

Consider the hybrid world of Fig. 1 (right) with n ITMs executing  $\Pi_{SAT}$ , where  $\mathcal{F}_{Trust}$  is replaced by  $\mathcal{F}'_{Trust}$ :

```
Upon receiving (chooseBestSeller, d, L) from Alice:
      Bob \stackrel{R}{\leftarrow} L \cup \{\bot\}
      send message (bestSeller, d, L, Bob) to Alice
    We will show here that \mathcal{E} can distinguish between \mathcal{F}_{SAT} and \Pi_{SAT}^{\mathcal{F}'_{Trust}}.
    Distinguishability. Consider the following adversary and environment:
    \mathcal{A}
   Upon receiving (chooseBestSeller, list, d, Alice):
      If |\text{list}| \neq 1 \lor |d| \neq 1:
         go to Idle State
      Bob = p : p \in list
      s = asset : asset \in d
      return (bestSeller, list, Bob, 1, s)
    \mathcal{E} distinguisher
    Alice \stackrel{R}{\leftarrow} \mathcal{P}
   Bob \xleftarrow{R} \mathcal{P} \setminus \{Alice\}
  util(Alice)(\{assets\}, x, r) = 2|\{assets\}| + x
   \mathtt{util}(Bob)(\{assets\}, x, r) = |\{assets\}| + 2x
   \lambda \left(Alice\right)(t) = \lambda \left(Bob\right)(t) = \frac{1}{t^2}
   \forall p \in \{Alice, Bob\}:
      send message (type, util(p), \lambda(p)) to p
    s \stackrel{R}{\leftarrow} Asset
    send message (obtain, 1 coin) to (*$Alice$@*)
    send message (obtain, s) to Bob
    send message (satisfy, \{s\}, \{Bob\}) to Alice
11
12
    Upon receiving message (x, \{s\}, \{Bob\}) from Alice:
13
      If x == satisfied:
14
         return 1 # functionality
15
      Else: # if x \in \{\text{cheated, unsatisfied}\}\
         return 0 # protocol
```

Because of the way  $\mathcal{E}$  is built, there always exists a seller (Bob, line 2) who has an asset (line 10) that can satisfy the desire (line 11) of the buyer (Alice, line 1).

In case  $\mathcal{E}$  interacts with  $\mathcal{F}_{SAT}$ , let  $\mathcal{S}$  simulator that tries to simulate  $\mathcal{A}$ .  $\mathcal{F}_{SAT}$  will always send the message (chooseBestSeller,  $\{Bob, 1, s\}$ ,  $\{s\}$ , Alice) to  $\mathcal{S}$  because:

- 1. Alice has one coin according to  $\mathcal{E}$ , line 9, as required by  $\mathcal{F}_{SAT}$ , line 15.
- 2. It is in *Alice*'s benefit for the trade to go through, since she values acquiring one asset more than one coin (util(*Alice*) ( $\{s\}$ , 0) = 2 > 1 = util(*Alice*) ( $\emptyset$ , 1) as can be seen in  $\mathcal{E}$ , lines 3 and 7), as required in  $\mathcal{F}_{SAT}$ , line??.
- 3. It is in Bob's benefit for the trade to go through, since he values acquiring one coin more than one asset (util(Bob)( $\{s\}$ ,0) = 1 < 2 = util(Bob)( $\{\emptyset$ ,1) as can be seen in  $\mathcal{E}$ , lines 4 and 7), as required in  $\mathcal{F}_{SAT}$ , line??.

 $\mathcal{S}$  should always match the buyer and the seller because of the way  $\mathcal{A}$  is built. More precisely,  $\mathcal{S}$  must always respond to (chooseBestSeller,  $\{Bob\}$ ,  $\{s\}$ , \_) with (bestSeller,  $\{Bob\}$ , Bob, 1, s) in order to correctly simulate  $\mathcal{A}$  (lines 4-6). Additionally, the price of 1 is cheap enough for Alice to want to buy the asset, since she values acquiring one asset more than one coin (util(Alice) ( $\{s\}$ , 0) = 2 > 1 = util(Alice) ( $\emptyset$ , 1) as can be seen in  $\mathcal{E}$ , lines 3 and 7).

Furthermore,  $\mathcal{F}_{SAT}$  never cheats on a trade and always chooses a suitable seller, price and asset (given that there exists one, which is the case here as we saw earlier), thus the exchange will always complete correctly and  $\mathcal{E}$  will receive satisfied as response.  $\mathcal{E}$  will always correctly output 1 (which corresponds to the functionality, line 15).

On the other hand, in case  $\mathcal{E}$  interacts with  $\Pi_{SAT}$ , then we observe that  $\mathcal{F}'_{Trust}$  does not choose players depending on their reputation (line 2), thus in this particular setting the utility of the players does not depend on their reputation. Thus, if  $\mathcal{F}'_{Trust}$  does not respond with  $\bot$ , it is always in Bob's interest to cheat, since keeping the asset is preferrable to giving it ( $\mathcal{E}$ , lines 4 and 7). Thus Alice's response to  $\mathcal{E}$  will always be cheated. If  $\mathcal{F}'_{Trust}$  responds with  $\bot$  (line 2), the trade will not go through ( $\Pi_{SAT}$ , lines 31-32) and  $\mathcal{E}$  will receive unsatisfied as a response. In all cases  $\mathcal{E}$  will correctly output 0 (which corresponds to the protocol, line 17).

#### References