Analysis and Attacks of decentralized content curation platforms

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Abstract. We will attack Steem.

1 Introduction

Steem is not incentive-compatible.

2 Related Work

Several research efforts have aimed to model the mechanics and incentives for users in crowdsourced content curation systems. Motivated by the widespread adoption of crowdsourced aggregation sites such as Reddit or Digg, they have aimed to model crowdsourced curation of Usergenerated content (UGC) [1]. Most of the academic work in the field have analyzed content curation from an incentives and game-theoretic standpoint [2,3,4]. We recognize the value of these past efforts and we adopt some of the components used in these models such as the quality distribution of the articles and the user's attention span(askalidis,ghosh). However, our approach is fundamentally different as we describe the mechanics of post-voting systems from a computational angle. More specifically, we draw inspiration from the real-ideal world paradigm of Cryptography [5] in the definition of convergence.

We are aware of the limitations imposed by Arrow's impossibility theorem [6]. Nevertheless, since we avoid a general game-theoretic approach, these limitations do not impact the outcomes of our work. In particular, we restrict the behavior of agents to a specific set of choices and we do not permit strategic decisions. Only a subset of players is endowed with a payoff function. This keeps the computational analysis of post-voting systems tractable whilst highlighting. In the present work, we develop a general framework for the analysis of decentralized content curation platforms. After that, we particularize our analysis on Steemit as we recognize that the explicit financial incentives present in its blockchain-based platform are better suited to our analysis than traditional sites such as Reddit or Hacker News, studied in the previous literature. The governance of online communities such as Wikipedia has been thoroughly studied in previous academic work [7,8]. However, the financially incentivized governance processes in blockchain systems, where the voters are at the same time equity-holders have still many open research questions [?,?]. Beyond the Steem blockchain, coinholder voting systems are present in decentralized platforms as DAOs [9] or in other blockchain protocols such as EOS(cite) or Tezos(cite) (not sure if including this). Our analysis of Steemit's post-voting system aims to provide a better framework for the better design of future decentralized curation platforms.

3 Model

1 Notation

- We denote the set of all probability distributions on set A as $\mathcal{D}(A)$.
- We denote the powerset of a set A with 2^A .
- -a||b| denotes the concatenation of a and b.
- Let $n \in \mathbb{N}^*$. [n] denotes $\{1, 2, \ldots, n\}$.

2 Properties of Post Voting Systems

A post voting system has the objective to arrange the posts according to the preferences of the participants. The ideal order is defined based on the likeability matrix for the posts.

Definition 1 (Post). Let $N \in \mathbb{N}^*$. A post is defined as p = (i, l), with $i \in [N], l \in [0, 1]^N$.

- Author. The first element of a post is the index of its creator, i.
- **Likeability.** The likeability of a post is defined as $l \in [0,1]^N$.

Let $M \in \mathbb{N}^*$ the number of posts. Then $\forall j \in [M]$, let $\operatorname{creator}_j \in [N]$, $l_j \in [0,1]^N$ and $p_j = (\operatorname{creator}_j, l_j)$. The set of all posts is $\mathcal{P} = \bigcup_{j=1}^M \{p_j\}$.

Definition 2 (Ideal Score of a post). Let post p = (m, l). We define the ideal score of p as idealSc $(p) = \sum_{i=1}^{N} l_i$.

The ideal score of a post is a single number that represents its overall worth to the community. By using simple summation, we assume that the opinions of all players have the same weight. In an ordered list of posts where higher posts are more visible, the "common interest" would require that a post with higher ideal score appear before another post with a lower score.

Definition 3 (t-Ideal Post Order). Let \mathcal{P} a list of posts. We say that \mathcal{P} is in t-ideal order and that the property IDEAL^t (\mathcal{P}) holds if

$$\forall i < j \in |t|, \text{idealSc}\left(\mathcal{P}\left[i\right]\right) \geq \text{idealSc}\left(\mathcal{P}\left[j\right]\right)$$
.

Definition 4 (Post-Voting System). A tuple S = (INIT, AUX, HANDLEVOTE, VOTE) of four algorithms. The four algorithms parametrize the following two ITMs:

 $\mathcal{G}_{\mathrm{Feed}}$ is a global functionality that accepts two messages: **read**, which responds with the current list of posts and **vote**, which can take various arguments and does whatever is defined in HANDLEVOTE.

 Π_{honest} is a protocol that sends read and vote messages to $\mathcal{G}_{\text{Feed}}$ whenever it receives (activate) from \mathcal{E} .

Algorithm 1 $\mathcal{G}_{\text{Feed}}$ (Init, Aux, HandleVote) (\mathcal{P} , initArgs)

```
1: Initialization:

2: \mathcal{U} \leftarrow \emptyset

3: INIT (initArgs)

4:

5: Upon receiving (read) from u_{\text{pid}}:

6: \text{aux} \leftarrow \text{Aux} (u_{\text{pid}})

7: Send (posts, \mathcal{P}, aux) to u_{\text{pid}}

8:

9: Upon receiving (vote, ballot) from u_{\text{pid}}:

10: HANDLEVOTE(ballot)
```

Algorithm 2 Π_{honest} (Vote)

```
1: Upon receiving (activate) from \mathcal{E}:
```

- 2: Send (read) to $\mathcal{G}_{\text{Feed}}$
- 3: Wait for response (posts, P, aux)
- 4: ballot \leftarrow Vote (\mathcal{P}, aux)
- 5: Send (vote, ballot) to \mathcal{G}_{Feed}

Definition 5 (Post-Voting System Activation Message). We define act_{pid} as the message (activate), sent to u_{pid} .

Definition 6 (Execution Pattern). Let $N, R \in \mathbb{N}^*$.

$$\text{ExecPat}_{N,R} = \left\{ \left(\texttt{act}_{\text{pid}_1}, \dots, \texttt{act}_{\text{pid}_{NR}} \right) : \forall i \in [R] \,, \forall k \in [N] \,, \exists j \in [N] : \text{pid}_{(i-1)N+j} = k \right\} \,,$$

i.e. activation messages are grouped in R rounds and within each round each player is activated exactly once. The order of activations is not fixed.

Let Environment \mathcal{E} that sends messages msgs = $(\mathtt{act}_{\mathrm{pid}_1}, \ldots, \mathtt{act}_{\mathrm{pid}_n})$ sequentially. We say that \mathcal{E} respects $\operatorname{ExecPat}_{N,R}$ if $\operatorname{msgs} \in \operatorname{ExecPat}_{N,R}$. (Note: this implies that n = NR.)

Definition 7 ((N, R, M, t)-convergence under honesty). We say that a post-voting system S = (INIT, AUX, HANDLEVOTE, VOTE) (N, R, M, t)converges under honesty (or t-converges under honesty for N players, R rounds and M posts) if, for every input \mathcal{P} such that $|\mathcal{P}| = M$, for every \mathcal{E} that respects ExecPat_{N,R} and given that all protocols execute Π_{honest} , it holds that after $\mathcal E$ completes its execution pattern, $\mathcal G_{\mathrm{Feed}}$ contains a post list \mathcal{P} such that IDEAL^t (\mathcal{P}) is true.

TODO: Discuss: Is R missing from Steem system? Maybe add "Let $N, R \in \mathbb{N}^*, ...,$ controlled by an Environment that respects ExecPat_{N,R} and the following ...".

Definition 8 (Steem system). The Steem system is the post voting system S with parameters $SP \in \mathbb{N}^{*N}$, a, b, regen $\in [0,1]: a+b < 1$, attSpan \in \mathbb{N}^* and the following parametrizing procedures:

Algorithm 3 INIT (SP, attSpan, a, b, regen)

- 1: Store input parameters as constants
- $2 \colon\thinspace r \leftarrow 1$
- 3: lastVoted $\leftarrow (0, \dots)$

4:
$$\mathbf{VP} \leftarrow \underbrace{(1,\ldots,1)}^{I}$$

4:
$$\mathbf{VP} \leftarrow \underbrace{(1, \dots, 1)}_{N}$$
5: $\mathbf{scores} \leftarrow \underbrace{(0, \dots, 0)}_{|\mathcal{P}|}$

Algorithm 4 Aux

1: **return** (**SP**, attSpan, a, b, r, regen)

Algorithm 5 HandleVote (ballot, u_{pid})

```
1: if lastVoted<sub>pid</sub> \neq r then
                                                                                                          \triangleright One vote per player per round
 2:
                                                                                                                                                  \, \triangleright \, \text{For proofs} \,
              \mathbf{VP}_{\mathrm{pid},r} \leftarrow \mathbf{VP}_{\mathrm{pid}}
              \mathbf{VP}_{\mathrm{pid}} \leftarrow \max \left\{ \mathbf{VP}_{\mathrm{pid}} + \mathrm{regen} \cdot \left(r - \mathrm{lastVoted}_{\mathrm{pid}}\right), 1 \right\}
 3:
                                                                                                                                      \triangleright TODO: Remove
       (r - lastVoted_{pid})?
 4:
              \mathbf{VPreg}_{\mathrm{pid},r} \leftarrow \mathbf{VP}_{\mathrm{pid}}
                                                                                                                                                 ⊳ For proofs
              if ballot \neq null then
 5:
 6:
                     Parse ballot as (p, weight)
 7:
                     \mathrm{cost} \leftarrow a \cdot \mathbf{VP}_{\mathrm{pid}} \cdot \mathrm{weight} + b
                     if \mathbf{VP}_{\mathrm{pid}} - \mathrm{cost} \geq 0 then
 8:
                            score \leftarrow cost \cdot \mathbf{SP}_{pid}
 9:
                            \mathbf{VP_{\mathrm{pid}}} \leftarrow \mathbf{VP_{\mathrm{pid}}} - \mathrm{cost}
10:
11:
                     else
                            \mathrm{score} \leftarrow \mathbf{V} \mathbf{P}_{\mathrm{pid}} \cdot \mathbf{S} \mathbf{P}_{\mathrm{pid}}
12:
13:
                            \mathbf{VP}_{\mathrm{pid}} \leftarrow 0
                     end if
14:
                     \mathsf{scores}_p \leftarrow \mathsf{scores}_p + \mathsf{score}
15:
16:
              end if
17:
              lastVoted_{pid} \leftarrow r
18: end if
19: if \forall i \in [N], lastVoted<sub>i</sub> = r then
                                                                                                                                                 ▷ round over
20:
              \mathcal{P} \leftarrow \text{Order}\left(\mathcal{P}, \text{scores}\right)
                                                                                                                             \triangleright order posts by votes
21:
              \mathcal{P}_r \leftarrow \mathcal{P}
                                                                                                                                                  \triangleright For proofs
22:
23: end if ▷ TODO: count rounds? simplify with set of voted and check of length?
```

Algorithm 6 Vote (\mathcal{P}, aux)

```
1: Store aux contents as constants
 2: if VoteThisRound (r) = yes then
 3:
         top \leftarrow ChooseTopPosts (attSpan, P, votedPosts)
         (i,l) \leftarrow \operatorname{argmax} \left\{ l_{\text{pid}} \right\} [1]
 4:
                    (i,l) \in top
         votedPosts \leftarrow votedPosts \ \cup \ (i,l)
 5:
 6:
         return ((i, l), l_{pid})
 7: else
         return null
 8:
9: end if
10:
11: function ChooseTopPosts(attSpan, \mathcal{P}, votedPosts)
12:
         res \leftarrow \emptyset
13:
         idx \leftarrow 1
14:
         while |res| < attSpan & idx \le |\mathcal{P}| do
15:
             if \mathcal{P}[idx] \notin votedPosts then
                                                                       ⊳ One vote per post per player
16:
                  res \leftarrow res \cup \{ \mathcal{P} [idx] \}
17:
              end if
18:
             idx \leftarrow idx + 1
19:
         end while
20:
         \mathbf{return} \ \mathrm{res}
21: end function
22:
23: function VoteThisRound(r, |\mathcal{P}|)
24:
         if R < |\mathcal{P}| then
25:
             \mathbf{return} yes
         else if \left| (r-1) \mod \frac{R-1}{|\mathcal{P}|-1} \right| = 0 then
                                                                      ▷ TODO: if Discussion above is
26:
    accepted, change |\mathcal{P}| to M and don't input |\mathcal{P}|.
27:
             return yes
28:
         else
29:
              return no
         end if
30:
31: end function
```

Theorem 1. The Steem system (N, R, M, M)-converges if and only if SP is constant and $R-1 \ge (M-1) \left\lceil \frac{a+b}{\text{regen}} \right\rceil$.

Discussion

- If players have attention span smaller than the full list and do not have the rounds to vote for every post, make a \mathcal{P} with the best post at the end and it will stay there.

Proof. $- (\Leftarrow)$ Suppose that

$$R-1 \ge (M-1) \left\lceil \frac{a+b}{\text{regen}} \right\rceil$$
 and $\forall i \in [N], \mathbf{SP}_i = c$.

Let pid \in [N]. In this case it is $R \ge M$ and according to VOTETHIS-ROUND in Algorithm 6, u_{pid} votes non-null in rounds (r_1, \ldots, r_M) with $r_i = \left| (i-1) \frac{R-1}{M-1} \right| + 1$. Observe that:

$$(1) \Rightarrow \frac{R-1}{M-1} \ge \left\lceil \frac{a+b}{\text{regen}} \right\rceil \stackrel{\text{rhs}}{\underset{\text{integer}}{\Rightarrow}} \left\lfloor \frac{R-1}{M-1} \right\rfloor \ge \left\lceil \frac{a+b}{\text{regen}} \right\rceil , \qquad (2)$$

$$\forall i \in [M] \setminus \{1\}, r_i \in \left\{r_{i-1} + \left\lfloor \frac{R-1}{M-1} \right\rfloor, r_{i-1} + \left\lceil \frac{R-1}{M-1} \right\rceil \right\} . \tag{3}$$

From (2) and (3) we have that $\forall i \in [M-1], r_{i+1} - r_i \ge \left\lceil \frac{a+b}{\text{regen}} \right\rceil$. We will now prove by induction that $\forall i \in [M], \mathbf{VP}_{\text{pid},r_i} = 1$.

- For i = 1, $\mathbf{VP}_{\text{pid},1} = 1$ by (Algorithm 3, line 4).
- Let $\mathbf{VP}_{\mathrm{pid},r_i} = 1$. Until r_{i+1} , a single non-null vote is cast by u_{pid} , which reduces $\mathbf{VP}_{\mathrm{pid}}$ by at most a+b (Algorithm 5, line 7) and at least $\left\lceil \frac{a+b}{\mathrm{regen}} \right\rceil$ regenerations, each of which replenishes $\mathbf{VP}_{\mathrm{pid}}$ by regen. Thus

$$\mathbf{VP}_{\mathrm{pid},r_{i+1}} \ge \min \left\{ \mathbf{VP}_{\mathrm{pid},r_i} - a - b + \mathrm{regen} \left[\frac{a+b}{\mathrm{regen}} \right], 1 \right\} \ge 1$$
.

But \mathbf{VP}_{pid} cannot exceed 1 (line 4), thus $\mathbf{VP}_{pid,r_{i+1}} = 1$.

Since the above holds for every pid $\in [N]$, we have that at the end of the execution, all votes have been cast with full voting power, thus $\forall p = (i, l) \in \mathcal{P}_R$, scores_p = $c\left(Nb + a\sum_{\text{pid}=1}^N l_{\text{pid}}\right)$ and the posts in \mathcal{P}_R are sorted by decreasing score (Algorithm 5, line 20). We observe that

$$\forall p_1 = \left(j^1, l^1\right) \neq p_2 = \left(j^2, l^2\right) \in \mathcal{P}_R, \text{idealSc}\left(p_1\right) > \text{idealSc}\left(p_2\right) \Rightarrow$$

$$\sum_{i=1}^N l_i^1 > \sum_{i=1}^N l_i^2 \Rightarrow c\left(Nb + a\sum_{i=1}^N l_i^1\right) > c\left(Nb + a\sum_{i=1}^N l_i^2\right).$$

Thus all posts will be ordered according to their ideal scores; put otherwise, IDEALSCORE^M (\mathcal{P}_R) holds.

- (**SP** variable \Rightarrow no convergence) Let $\mathcal{P} = ((1, (a_1, \ldots, a_N)), (2, (b_1, \ldots, b_N)))$ such that the following linear constraints are simultaneously feasible:

$$\sum_{i=1}^{N} a_i > \sum_{i=1}^{N} b_i$$
$$\sum_{i=1}^{N} \mathrm{SP}_i a_i < \sum_{i=1}^{N} \mathrm{SP}_i b_i$$

I think that's always possible if SP is not constant.

- (inequality doesn't hold \Rightarrow no convergence) Suppose that

$$R-1 < (M-1) \left\lceil \frac{a+b}{\text{regen}} \right\rceil$$
 and $\forall i \in [N], \mathbf{SP}_i = c$.

$$\operatorname{Let} \mathcal{P} = \left[\left(1, \underbrace{(1, 0.5 + \epsilon, 0, \dots, 0)}_{N} \right), \left(1, \underbrace{(0, 0.5, 0, \dots, 0)}_{N} \right), \left(1, \underbrace{(0, \dots, 0)}_{N} \right), \dots, \left(1, \underbrace{(0, \dots, 0)}_{N} \right), \dots \right]$$

Observe that idealSc $(\mathcal{P}[1]) = 1$, idealSc $(\mathcal{P}[2]) = 1 + \epsilon$ and $\forall i \in [M] \setminus \{1, 2\}$, idealSc $(\mathcal{P}[i]) = 0$, thus $\forall \mathcal{P}'$ that contains the same posts as \mathcal{P} and IDEAL¹ (\mathcal{P}') holds, it is $\mathcal{P}'[1] = \mathcal{P}[2]$.

• R = 1, attSpan = 1 In the first round, u_1 casts

In the first round, u_1 casts a vote of weight 1 and the rest of the players cast a vote of weight 0 for $\mathcal{P}[1]$, thus at the end of the execution, $scores_1 = c(a+b) + (N-1)cb$. No other votes are cast, thus $scores_2 = 0$. Thus at the end of the execution $scores_1 > scores_2$.

• R = 1, attSpan > 1

In the first round, u_1 casts a vote of weight 1 for $\mathcal{P}[1]$, u_2 casts a vote of weight 0.5 for $\mathcal{P}[2]$ and all other players cast a vote of weight 0 for $\mathcal{P}[1]$. No other votes are cast. Thus at the end of the execution, $scores_1 = c(a+b) + (N-2)cb$ and $scores_2 = c(0.5a+b)$. We deduce that $scores_1 > scores_2$.

• R > 1, attSpan = 1

In the first round, the votes are identical to the previous case. As we saw in eq. (3), the next vote will be cast not earlier than round $\left\lceil \frac{R-1}{M-1} \right\rceil$ and not later than round $\left\lceil \frac{R-1}{M-1} \right\rceil + 1$, thus $\left\lceil \frac{R-1}{M-1} \right\rceil \leq r_2 \leq \left\lceil \frac{R-1}{M-1} \right\rceil + 1 \Rightarrow \mathbf{VPreg}_{1,r_2} \leq \min \left\{ 1 - a - b + \operatorname{regen} \left\lceil \frac{R-1}{M-1} \right\rceil, 1 \right\}$

• R > 1, attSpan > 1

In every case, \mathcal{P}_R is ordered in descending post score (Algorithm 5, line 20), thus $\mathcal{P}_R[1] \neq \mathcal{P}[2]$ and the property $\mathrm{Ideal}^1(\mathcal{P}_R)$ does not hold.

• $R < M \land \operatorname{attSpan} < M$

At the end of the execution all players will have voted for $\mathcal{P}[1]$ in the first round, and thus $\text{scores}_{\mathcal{P}[1]} = Nc(0.5a + b)$. On the other hand, $\mathcal{P}[M]$ will have been voted by at most u_N with voting power $\text{VP} \leq 1 - (0.5a + b) + \text{regen}$, thus

 $\operatorname{scores}_{\mathcal{P}[M]} \leq c \left(\left(1 - (0.5a + b) + \operatorname{regen} \right) \left(0.5 + \epsilon \right) a + b \right) \overset{\operatorname{regen} < b}{<} c \left(\left(0.5 + \epsilon \right) a + b \right).$ Thus $\operatorname{scores}_{\mathcal{P}[1]} > \operatorname{scores}_{\mathcal{P}[M]} \Leftrightarrow (N - 1) \left(0.5 + \frac{b}{a} \right) > \epsilon$. TODO: choose ϵ and show non-convergence

• $R < M \land \operatorname{attSpan} = M$

At the end of the execution, all players except for u_N will have voted for $\mathcal{P}[1]$ in the first round, and thus $\mathrm{scores}_{\mathcal{P}[1]} \geq (N-1) \, c \, (0.5a+b)$. On the other hand, $\mathcal{P}[M]$ will have been voted by exactly u_N and this vote will have been cast on the first round, thus $\mathrm{scores}_{\mathcal{P}[M]} = c \, ((0.5+\epsilon) \, a+b)$. Thus $\mathrm{scores}_{\mathcal{P}[1]} > \mathrm{scores}_{\mathcal{P}[M]} \Leftrightarrow (N-2) \, \left(0.5+\frac{b}{a}\right) > \epsilon$. TODO: choose ϵ and show non-convergence

• $R > M \land \operatorname{attSpan} < M$

In this case, all players vote for all posts. At the end of the execution all players will have voted for $\mathcal{P}[1]$ in the first round, and thus $\mathrm{scores}_{\mathcal{P}[1]} = Nc\,(0.5a+b)$. As far as $\mathcal{P}[M]$ is concerned, we first observe that the distance between to voting rounds is $\left\lceil \frac{R-1}{M-1} \right\rceil$ at most: $\forall i \in [M-1], r_{i+1} - r_i \leq \left\lceil \frac{R-1}{M-1} \right\rceil$. Thus the voting power of all players will be at most regen $\left\lfloor \frac{R-1}{M-1} \right\rfloor$ before voting for the last post. We deduce that $\mathrm{scores}_{\mathcal{P}[M]}$ will have been voted by all players except for u_N with voting power at most

• $R \ge M \land \operatorname{attSpan} = M$

On the other hand,

- Let attSpan < M.
 - * If R < M, then

the first post $\mathcal{P}[1]$ is voted by all players at round 1 and its score becomes Nc(0.5a+b). Given (4), all subsequent votes are cast with voting power strictly less than 1, thus the last post will have a score of $(N-1)c(0.5a?+b)+c((0.5+\epsilon)a?+b)$ at the end of the execution.

• If attSpan = M,

The above result is tight. If the conditions are violated the above theorem is not true.

4 Results

Steem won't achieve high quality posts.

5 Further Work

Posts at any time

6 Conclusion

Keep inventing new decentralized content curation platforms.

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