1 Payment Network Functionality

```
Functionality \mathcal{F}_{\mathrm{PayNet}} – interface
  from \overline{\mathcal{E}}:
   • (REGISTER, delay, relayDelay)
   • (TOPPEDUP)
   • (OPENCHANNEL, Alice, Bob, x, tid)
   • (CHECKFORNEW, Alice, Bob, tid)
     (PAY, Bob, x, \overrightarrow{path}, receipt)
      (CLOSECHANNEL, receipt, pchid)
     (FORCECLOSECHANNEL, receipt, pchid)
     (POLL)
     (PUSHFULFILL, pchid)
   • (PUSHADD, pchid)
   • (COMMIT, pchid)
   • (FULFILLONCHAIN)
   • (GETNEWS)
- to \mathcal{E}:
   • (REGISTER, Alice, delay(Alice), relayDelay(Alice), pubKey)
     (REGISTERED)
   • (NEWS, newChannels, closedChannels, updatesToReport)
– from S:
     (REGISTERDONE, Alice, pubKey)
     (CORRUPTED, Alice)
     (CHANNELANNOUNCED, Alice, p_{Alice,F}, p_{Bob,F}, fchid, pchid, tid)
     (UPDATE, receipt, Alice)
     (CLOSEDCHANNEL, channel, Alice)
   • (RESOLVEPAYS, payid, charged)
– to S:
   • (REGISTER, Alice, delay, relayDelay)
   • (OPENCHANNEL, Alice, Bob, x, fchid, tid)
     (CHANNELOPENED, Alice, fchid)
     (PAY, Alice, Bob, x, \overrightarrow{path}, receipt, payid)
     (CONTINUE)
     (CLOSECHANNEL, fchid, Alice)
     (FORCECLOSECHANNEL, fchid, Alice)
     (POLL, \Sigma_{Alice}, Alice)
     (PUSHFULFILL, pchid, Alice)
     (PUSHADD, pchid, Alice)
     (COMMIT, pchid, Alice)
   • (FULFILLONCHAIN, t, Alice)
```

Fig. 1.

All players need to register in order to use channels. The registration of *Alice* works as follows: *Alice* inputs her desired delay and relayDelay that will be used for all her future channels. The first denotes how often she has to check the blockchain for revoked commitments and the second defines the minimum time distance between incoming and outgoing CLTV expiries. $\mathcal{F}_{\text{PayNet}}$ then informs \mathcal{S} , who sends back a long-lived public key for *Alice*. This key represents *Alice*'s account, from where $\mathcal{F}_{\text{PayNet}}$ can get coins to open new channels on her behalf and to place coins of closed channels. The key is sent to *Alice* who moves some initial funds to it and notifies $\mathcal{F}_{\text{PayNet}}$. She is now registered. The exact logic is found in Fig. 2, which also contains the actions of $\mathcal{F}_{\text{PayNet}}$ related to corruptions.

Additionally, the procedure checkClosed() is called after READing from \mathcal{G}_{Ledger} , with the received state Σ as input. This call happens every time \mathcal{F}_{PayNet} READs from \mathcal{G}_{Ledger} . The formal definition of checkClosed() can be found in Fig. 9, along with a discussion of its purpose.

```
Functionality \mathcal{F}_{PayNet} – registration and corruption
 1: Initialisation:
        \texttt{channels}, \texttt{pendingPay}, \texttt{pendingOpen}, \texttt{corrupted}, \varSigma \leftarrow \emptyset
 2:
 3: Upon receiving (REGISTER, delay, relayDelay) from Alice:
        delay(Alice) \leftarrow delay // Must check chain at least once every
    delay(Alice) blocks
        \texttt{relayDelay} \ (Alice) \leftarrow \texttt{relayDelay}
 6:
        updatesToReport (Alice), newChannels (Alice) \leftarrow \emptyset
        polls(Alice) \leftarrow \emptyset
 7:
        focs(Alice) \leftarrow \emptyset
 8:
        send (READ) to \mathcal{G}_{Ledger} as Alice, store reply to \Sigma_{Alice}, add \Sigma_{Alice} to \Sigma and
    add largest block number to polls(Alice)
10:
         checkClosed(\Sigma_{Alice})
11:
         send (REGISTER, Alice, delay, relay Delay) to S
12: Upon receiving (REGISTERDONE, Alice, pubKey) from S:
        pubKev(Alice) \leftarrow pubKev
13:
        send (REGISTER, Alice, delay(Alice), relayDelay(Alice), pubKey) to Alice
14:
15: Upon receiving (TOPPEDUP) from Alice:
16:
        send (READ) to \mathcal{G}_{Ledger} as Alice and store reply to \Sigma_{Alice}
         \mathtt{checkClosed}(\Sigma_{Alice})
17:
        assign the sum of all output values that are exclusively spendable by Alice
18:
    to onChainBalance
19:
        send (REGISTERED) to Alice
20: Upon receiving any message (M) except for (REGISTER) or (TOPPEDUP) from
        if if haven't received (REGISTER) and (TOPPEDUP) from Alice (in this
21:
    order) \mathbf{then}
22:
            send (INVALID, M) to Alice and ignore message
23:
         end if
24: Upon receiving (CORRUPTED, Alice) from S:
25:
         add Alice to corrupted
         for the rest of the execution, upon receiving any message for Alice, bypass
    normal execution and simply forward it to \mathcal{S}
```

Fig. 2.

The process of Alice opening a channel with Bob is as follows: First Alice asks \mathcal{F}_{PayNet} to open and \mathcal{F}_{PayNet} informs \mathcal{S} . \mathcal{S} provides the necessary keys and IDs for the new channel to \mathcal{F}_{PayNet} . Alice asks \mathcal{F}_{PayNet} to check if \mathcal{G}_{Ledger} contains

the funding transaction from Alice's point of view. If it does, \mathcal{F}_{PayNet} activates \mathcal{S} , who in turn returns control to \mathcal{F}_{PayNet} . Now \mathcal{F}_{PayNet} checks that the funding transaction is in the \mathcal{G}_{Ledger} also from Bob's point of view and in case it does, it notifies \mathcal{S} . \mathcal{S} then confirms that to \mathcal{F}_{PayNet} that the channel is open and \mathcal{F}_{PayNet} finally stores the channel as open. This last exchange is needed to match the real-world interaction.

```
Functionality \mathcal{F}_{\mathrm{PayNet}} – open
 1: Upon receiving (OPENCHANNEL, Alice, Bob, x, tid) from Alice:
 2:
        ensure tid hasn't been used by Alice for opening another channel before
 3:
        choose unique channel ID fchid
 4:
        pendingOpen (fchid) \leftarrow (Alice, Bob, x, tid)
 5:
        send (OPENCHANNEL, Alice, Bob, x, fchid, tid) to S
 6: Upon receiving (CHANNELANNOUNCED, Alice, p<sub>Alice,F</sub>, p<sub>Bob,F</sub>, fchid, pchid, tid)
    from S:
        ensure that there is a pendingOpen(fchid) entry with temporary id tid
        add p_{Alice,F}, p_{Bob,F}, pchid and mark "Alice announced" to
    pendingOpen(fchid)
9: Upon receiving (CHECKFORNEW, Alice, Bob, tid) from Alice:
10:
        ensure there is a matching channel in pendingOpen(fchid), marked with
    "Alice announced"
11:
        (funder, fundee, x, p_{Alice,F}, p_{Bob,F}) \leftarrow pendingOpen(fchid)
12:
        send (READ) to \mathcal{G}_{\text{Ledger}} as Alice and store reply to \Sigma_{Alice}
13:
        \mathtt{checkClosed}(\varSigma_{Alice})
        ensure that there is a TX F \in \Sigma_{Alice} with a (x, (p_{\text{funder},F} \land p_{\text{fundee},F}))
14:
    output
15:
        mark channel with "waiting for FUNDINGLOCKED"
        send (FUNDINGLOCKED, Alice, \Sigma_{Alice}, fchid) to S
16:
17: Upon receiving (FundingLocked, fchid) from S:
        ensure a channel is in pendingOpen(fchid), marked with "waiting for
    FUNDINGLOCKED" and replace mark with "waiting for CHANNELOPENED"
19:
        send (READ) to \mathcal{G}_{Ledger} as Bob and store reply to \Sigma_{Bob}
20:
        \mathtt{checkClosed}(\varSigma_{Bob})
        ensure that there is a TX F \in \Sigma_{Bob} with a (x, (p_{\text{funder},F} \land p_{\text{fundee},F}))
21:
    output
22:
        add receipt(channel) to newChannels(Bob)
23:
        send (FUNDINGLOCKED, Bob, \Sigma_{Bob}, fchid) to S
24: Upon receiving (Channel Opened, fchid) from S:
        ensure a channel is in pendingOpen(fchid), marked with "waiting for
25:
    CHANNELOPENED" and remove mark
26:
        offChainBalance (funder) \leftarrow offChainBalance (funder) + x
27:
        onChainBalance (funder) \leftarrow onChainBalance (funder) -x
28:
        \texttt{channel} \leftarrow (\text{funder}, \text{fundee}, x, 0, 0, fchid, pchid})
29:
        add channel to channels
30:
        add receipt(channel) to newChannels(Alice)
31:
        clear pendingOpen(fchid) entry
```

Fig. 3.

When instructed to perform a payment, \mathcal{F}_{PayNet} simply takes note of the message and forwards it to \mathcal{S} . It also remembers to inform the payer that the payment has been completed when \mathcal{S} says so. Observe here that \mathcal{F}_{PayNet} trusts \mathcal{S} to correctly carry out channel updates. While counterintuitive, it allows \mathcal{F}_{PayNet} to ignore the details of channel updates, signatures, key and transaction handling. Nevertheless, as we will see \mathcal{F}_{PayNet} keeps track of requested and ostensibly carried out updates and ensures that upon channel closure the balances are as expected, therefore ensuring funds security.

```
Functionality \mathcal{F}_{\text{PayNet}} - pay

1: Upon receiving (PAY, Bob, x, path) from Alice:

2: choose unique payment ID payid

3: add (Alice, Bob, x, path, payid) to pendingPay

4: send (PAY, Alice, Bob, x, path, payid, STATE, Σ) to S

5: Upon receiving (UPDATE, receipt, Alice) from S:

6: add receipt to updatesToReport(Alice) // trust S here, check on RESOLVEPAYS

7: send (CONTINUE) to S
```

Fig. 4.

The message RESOLVEPAYS, sent by S, is supposed to contain a list of resolved payments, along with who was charged for each payment after all. For each entry there are four "happy paths" that do not lead to \mathcal{F}_{PayNet} halting (\mathcal{F}_{PayNet} halts when it cannot uphold its security guarantees anymore): if the payment failed and no balance is changed, if the charged player is the one who initiated the payment, if the charged player is corrupted or if she has not checked the blockchain at the right times, i.e. was negligent (as discussed in Section ?? and formally defined in Figures 5 and 6). In case the payment was completed in a legal manner, the balance of all channels involved is updated accordingly (Fig. 7). Conversely, \mathcal{F}_{PayNet} halts if the charged player was not on the payment path (Fig. 5, l. 8), if a signature forgery has taken place (Fig. 5, l. 16), if the charged player has not been negligent (Fig. 5, ll. 19 and 27), or if any one of the individual channel updates needed to carry out the whole payment has not been previously reported with an UPDATE message by S (Fig. 7, l. 10).

```
Functionality \mathcal{F}_{\mathrm{PayNet}} – resolve payments
 1: Upon receiving (RESOLVEPAYS, charged) from S: // after first sending PAY,
    PUSHFULFILL, PUSHADD, COMMIT
 2:
        for all Alice \text{ keys} \in \text{charged do}
            \mathbf{for} \ \mathbf{all} \ (Dave, payid) \in \mathtt{charged} \ (Alice) \ \mathbf{do}
 3:
                retrieve (Alice, Bob, x, \overrightarrow{path}) with ID payid and remove it from
 4:
    pendingPay
                if Dave = \bot then // Payment failed
 5:
                    continue with next iteration of inner loop
 6:
 7:
                else if Dave \notin path then
 8:
                    halt // Only players on path may be charged
 9:
                else if Dave \in \text{corrupted then}
10:
                    run code of Fig. 7
                    \mathtt{offChainBalance}\,(Bob) \leftarrow \mathtt{offChainBalance}\,(Bob) + x
11:
12:
                else // Dave honest
13:
                    send (READ) to \mathcal{G}_{Ledger} as Dave and store reply to \Sigma_{Dave}
                    \mathtt{checkClosed}(\varSigma_{Dave})
14:
                    if \Sigma_{Dave} contains a tx that is not a localCom_n or a remoteCom_n
15:
    and spends a funding tx for an open channel that contains Dave then
16:
                        halt // DS forgery
                    else if \Sigma_{Dave} contains in block h_{tx} an old remoteCom<sub>m</sub> that does
17:
    not contain the HTLC and a tx that spends the delayed output of remoteCom_m
    then
18:
                        if polls(Dave) contains an element in
    [h_{\mathsf{tx}}, h_{\mathsf{tx}} + \mathtt{delay}\,(Dave) - 1] then
19:
                            halt // Dave Polled, but successful malicious closure
20:
21:
                            negligent(Dave) \leftarrow true
22:
                         end if
23:
                    else if Dave \neq Alice then
                        calculate IncomingCltvExpiry, OutgoingCltvExpiry of Dave
    (as in Fig. ??, l. ??)
25:
                        if \Sigma_{Dave} does not contain an old remoteCom_m then
26:
                            if failure condition of Fig. 6 is true then
27:
                                halt // Dave POLLed and fulfilled, but charged
28:
29:
                                negligent(Dave) \leftarrow true
30:
                            end if
31:
                        end if
32:
                    end if
33:
                    run code of Fig. 7
34:
                    \texttt{offChainBalance} \ (Dave) \leftarrow \texttt{offChainBalance} \ (Dave) - x
35:
                    offChainBalance(Bob) \leftarrow offChainBalance(Bob) + x
36:
                end if
            end for
37:
38:
        end for
```

Fig. 5. r, windowSize as in Proposition ??

```
Absolute delay failure condition

IncomingCltvExpiry — OutgoingCltvExpiry < relayDelay(Alice) + (2+r) windowSize \lor (polls(Dave) contains two elements in

[OutgoingCltvExpiry, IncomingCltvExpiry — (2+r) windowSize] that have a difference of at least (2+r) windowSize \land focs(Dave) contains IncomingCltvExpiry — (2+r) windowSize \land the element in polls(Dave) was added before the element in focs(Dave))
```

Fig. 6.

```
Loop over payment hops for update and check
1: for all open channels \in \overline{path} that are not in any closedChannels, starting
   from the one where Dave pays do
       in the first iteration, payer is Dave. In subsequent iterations, payer is the
   unique player that has received but has not given. The other channel party is
   payee
       if payer has x or more in channel then
          update channel to the next version and transfer x from payer to payee
4:
5:
          revert all updates done in this loop
6:
7:
       end if
8: end for
9: for all updated channels in the previous loop do
       ensure that a corresponding element has been added to the
   updatesToReport of each honest counterparty, otherwise halt
11: end for
```

Fig. 7.

Similarly to payment instructions, when \mathcal{F}_{PayNet} receives a message instructing it to close a channel (Fig. 8), it takes a note of the pending closure, it stops serving any more requests for this channel and it forwards the request to \mathcal{S} . In turn \mathcal{S} notifies \mathcal{F}_{PayNet} of a closed channel with the corresponding message, upon which \mathcal{F}_{PayNet} takes a note to inform the corresponding player. Depending on whether the message instructed for a unilateral or a cooperative close, \mathcal{F}_{PayNet} will either put or not a time limit respectively to the service of the request. In particular, in case of cooperative close, the time limit is infinity (l. 4). As we will see, in case a unilateral close request was made and the time limit for servicing it is reached, \mathcal{F}_{PayNet} halts (Fig. 9, l. 27). Once more \mathcal{F}_{PayNet} trusts \mathcal{S} , but later checks that the chain contains the correct transactions with checkClosed() (Fig. 9).

```
Functionality \mathcal{F}_{PayNet} – close
1: Upon receiving (CLOSECHANNEL, receipt, pchid) from Alice
       ensure that there is a channel \in channels : receipt (channel) = receipt
   with ID pchid
       retrieve fchid from channel
       add (fchid, receipt(channel), \infty) to pendingClose(Alice)
       do not serve any other (PAY, CLOSECHANNEL) message from Alice for this
   channel
       send (CLOSECHANNEL, receipt, pchid, Alice) to {\cal S}
7: Upon receiving (FORCECLOSECHANNEL, receipt, pchid) from Alice
8:
       retrieve fchid from channel
       add (fchid, receipt(channel), \perp) to pendingClose(Alice)
9:
       do not serve any other (PAY, CLOSECHANNEL, FORCECLOSECHANNEL)
   message from Alice for this channel
       send (FORCECLOSECHANNEL, receipt, pchid, Alice) to \mathcal{S}
11:
12: Upon receiving (CLOSEDCHANNEL, channel, Alice) from S:
       remove any (fchid of channel, receipt(channel), \infty) from
   pendingClose(Alice)
14:
       add (fchid of channel, receipt(channel), \perp) to closedChannels(Alice) /
   trust S here, check on checkClosed()
15:
       send (CONTINUE) to {\cal S}
```

Fig. 8.

After every READ \mathcal{F}_{PayNet} sends to \mathcal{G}_{Ledger} and its response is received, checkClosed() (Fig. 9) is called. \mathcal{F}_{PayNet} checks the input state Σ for transactions that close channels and, in case no security violation has taken place, it updates the on- and off-chain balances of the player accordingly (ll. 6-15). The possible security violations are: signature forgery (l. 17), malicious closure even though the player was not negligent (l. 20), no closing transaction in Σ even though the player asked for channel closure a substantial amount of time before (l. 27) and incorrect on- or off-chain balance after the closing of all of the player's channels (l. 32).

```
Functionality \mathcal{F}_{\text{PayNet}} - checkClosed()
 1: function checkClosed(\Sigma_{Alice}) // Called after every (READ), ensures requested
    closes eventually happen
 2:
       if there is any closing/commitment transaction in \Sigma_{Alice} with no
    corresponding entry in pendingClose(Alice) \cup closedChannels(Alice) then
 3:
           add (fchid, receipt, \bot) to closedChannels(Alice), where fchid is the ID
    of the corresponding channel, receipt comes from the latest channel state
       end if
 4:
       for all entries
 5:
    (fchid, \mathtt{receipt}, h) \in \mathtt{pendingClose}(Alice) \cup \mathtt{closedChannels}(Alice) \ \mathbf{do}
           if there is a closing/commitment transaction in \Sigma_{Alice} for open channel
    with ID fchid with a balance that corresponds to receipt then
 7:
               let x, y Alice's and channel counterparty Bob's balances respectively
               offChainBalance (Alice) \leftarrow offChainBalance (Alice) -x
 8:
9:
               onChainBalance (Alice) \leftarrow onChainBalance (Alice) + x
10:
               offChainBalance (Bob) \leftarrow offChainBalance (Bob) - y
11:
               onChainBalance (Bob) \leftarrow onChainBalance (Bob) + y
12:
               remove channel from channels & entry from pendingClose(Alice)
13:
               if there is an (fchid, _, _) entry in pendingClose(Bob) then
14:
                   remove it from pendingClose(Bob)
15:
               end if
16:
           else if there is a tx in \Sigma_{Alice} that is not a closing/commitment tx and
    spends the funding tx of the channel with ID fchid then
17:
               halt // DS forgery
           else if there is a commitment transaction in block of height h in \Sigma_{Alice}
18:
    for open channel with ID fchid with a balance that does not correspond to the
    receipt and the delayed output has been spent by the counterparty then
19:
               if polls(Alice) contains an entry in [h, h + delay(Alice) - 1] then
20:
                   halt
21:
               else
22:
                   negligent(Alice) \leftarrow true
               end if
23:
24:
           else if there is no such closing/commitment transaction \wedge h = \bot then
25:
               assign largest block number of \Sigma_{Alice} to h of entry
26:
           else if there is no such closing/commitment transaction \land h \neq \bot \land
    (largest block number of \Sigma_{Alice}) \geq h + (2+r) windowSize then
27:
               halt
28:
           end if
29:
        end for
30:
        if Alice has no open channels in \Sigma_{Alice} AND negligent(Alice) = false then
           if offChainBalance(Alice) \neq 0 OR onChainBalance(Alice) is not equal
31:
    to the total funds exclusively spendable by Alice in \Sigma_{Alice} then
32:
               halt
33:
           end if
        end if
34:
35: end function
```

Fig. 9.

POLL is a request that every player has to make to \mathcal{F}_{PayNet} periodically (once every delay blocks, as set on registration) in order to remain non-negligent. In a software implementation, such a request would be automatically sent at safe time intervals. When receiving POLL (Fig. 10), \mathcal{F}_{PayNet} checks the ledger for maliciously closed channels and halts in case of a forgery (l. 6) or in case of a successful malicious closing of a channel whilst the offended player was non-negligent (l. 11). If on the other hand a channel has been closed maliciously but the offended player did not POLL in time, she is marked as negligent (l. 13).

```
Functionality \mathcal{F}_{\mathrm{PayNet}} – poll
 1: Upon receiving (POLL) from Alice:
        send (READ) to \mathcal{G}_{Ledger} as Alice and store reply to \Sigma_{Alice}
        add largest block number in \Sigma_{Alice} to polls(Alice)
3:
4:
        \mathtt{checkClosed}(\Sigma_{Alice})
        if \existschannel \in \Sigma_{Alice} that contains Alice and is closed by a tx that is not a
    commitment transaction then
6:
            halt // DS forgery
7:
        end if
        for all channels \in \Sigma_{Alice} that contain Alice and are maliciously closed by
    a remote commitment tx (one with an older channel version than the
    irrevocably committed one) in block with height h_{tx} do
9:
            if the delayed output (of the counterparty) has been spent then
10:
                if polls(Alice) has an element in [h_{tx}, h_{tx} + \text{delay}(Alice) - 1] then
11:
                    halt // Alice wasn't negligent but couldn't punish
                else
12:
13:
                    negligent(Alice) \leftarrow true
                end if
14:
            end if
15:
16:
        end for
17:
        send (POLL, \Sigma_{Alice}, Alice) to \mathcal{S}
```

Fig. 10.

The last part of \mathcal{F}_{PayNet} (Fig. 11) contains some additional "daemon" messages that help various processes carry on. PUSHFULFILL, PUSHADD and COMMIT are simply forwarded to \mathcal{S} . They exist because the "token of execution" in the protocol does not follow the strict order required by UC, and thus some additional messages are needed for the protocol to carry on. In other words, they are needed due to the incompatibility of the serial execution of UC and the asynchronous nature of LN.

FULFILLONCHAIN has to be sent by a multi-hop payment intermediary that has not been paid by the previous player off-chain in order to close the chan-

nel. The request is noted and forwarded to \mathcal{S} . GETNEWS requests from \mathcal{F}_{PayNet} information on newly opened, closed and updated channels.

```
Functionality \mathcal{F}_{PayNet} – daemon messages
1: Upon receiving (PUSHFULFILL, pchid) from Alice:
       send (PUSHFULFILL, pchid, Alice, STATE, \Sigma) to S
3: Upon receiving (PUSHADD, pchid) from Alice:
       send (PUSHADD, pchid, Alice, STATE, \Sigma) to S
5: Upon receiving (COMMIT, pchid) from Alice:
       send (COMMIT, pchid, Alice, STATE, \Sigma) to \mathcal{S}
7: Upon receiving (FULFILLONCHAIN) from Alice:
       send (READ) to \mathcal{G}_{Ledger} as Alice, store reply to \Sigma_{Alice} and assign largest
   block number to t
9:
       add t to focs(Alice)
       \mathtt{checkClosed}(\varSigma_{Alice})
10:
       send (FULFILLONCHAIN, t, Alice) to \mathcal S
11:
12: Upon receiving (GETNEWS) from Alice:
       clear newChannels(Alice), closedChannels(Alice),
   updatesToReport(Alice) and send them to Alice with message name NEWS,
   stripping fchid and h from closedChannels(Alice)
```

Fig. 11.

References