```
Protocol \Pi_{\mathrm{Chan}}
 1: Initialisation:
         State \leftarrow \text{INIT}
 3: On top up, check top up by \mathcal{E}, act as \mathcal{F}_{\mathrm{Chan}} (Fig. 3, lines 4-8 and 9-15
     respectively)
 4: On (OPEN, c_F, pk_{A,out}, pk_{B,out}) by \mathcal{E}:
         ensure State = \text{TOPPED UP}
         State \leftarrow \text{Opening base channel}
 6:
         do LN (other box)
 7:
 8: On (CHECK FUNDING) by \mathcal{E}:
 9:
         ensure State = WAITING FOR LEDGER
         send (READ) to \mathcal{G}_{\text{Ledger}} and assign reply to \Sigma
10:
         ensure F\in \varSigma
11:
12:
         c_A \leftarrow c; c_B \leftarrow 0 // c received in OPEN
13:
         State \leftarrow \text{OPEN BASE}
14:
         output (OPEN SUCCESS) to {\cal E}
15: On (PAY, x) by \mathcal{E}:
16:
         ensure State \in \{\text{OPEN BASE}, \text{OPEN VIRTUAL}\}
17:
         ensure c_A \geq x
         do LN payment (these channels won't be async) (balance change here)
18:
19:
         output (OK) to \mathcal{E}
20: On (BALANCE) by \mathcal{E}:
         ensure State \in \{\text{OPEN BASE}, \text{OPEN VIRTUAL}\}
22:
         output (BALANCE, (c_A, c_B, locked_A, locked_B)) to \mathcal{E}
23: On (CLOSE) by \mathcal{E}:
         \mathbf{if} \ \mathit{State} = \mathtt{OPEN} \ \mathtt{BASE} \ \mathbf{then}
24:
25:
              prepare C TODO
26:
              send (SUBMIT, C) to \mathcal{G}_{Ledger}
27:
          else if State = OPEN VIRTUAL then
28:
              TODO
29:
         end if
```

Fig. 1.

```
Protocol \Pi_{\mathrm{Chan}} – virtual
 1: // notification to funder
 2: // trust that Alice has c in her channel
3: On (FUND YOU, c, Bob) by Charlie as input:
       {\rm ensure}\ State = {\rm init}
 5:
        State \leftarrow \text{Opening virtual channel}
 6:
        do LN with Bob – TODO
        output (OK) to Charlie
8: On (FUND, c, hops, sub_parties = (fundee, counterparty), outer_parties =
    (Charlie, Dave) by \mathcal{E}:
        ensure State \in \{\text{OPEN BASE}, \text{OPEN VIRTUAL}\}
        do the same as in \mathcal{F}_{Chan}, Fig. 6, lines 9-18 TODO: make sure it makes sense
10:
        do VChan() with hops – TODO //P_{i-1}P_i, P_iP_{i+1} and all P_1P_n held by
11:
    BOTH R_{i-1} and L_i. P_{i-1}P_i held only by R_{i-1}, P_iP_{i+1} held only by L_i. This
    (probably) ensures that only relevant parties can close their channels (with the
    exception of honest R_{i-1} wanting to leave channels virtual but corrupted L_i
    demoting them to base, which however doesn't cost funds to anyone), but that
    they have minimal impact to the decisions of ajdacent channels. All P_{i-1}P_i
    inputs must be signed by R_{i-1} and all P_iP_{i+1} inputs by L_i.
12:
        do the same as in \mathcal{F}_{Chan}, Fig. 6, lines 20-24
13:
        output (OK) to \mathcal{E}
14: // notification to fundee
15: On (ALLOW FUND, ...) by Charlie, act as \mathcal{F}_{Chan} (Fig 6, line 26):
```

Fig. 2.

```
Functionality \mathcal{F}_{\operatorname{Chan}} - \operatorname{init} \, \& \, \operatorname{top} \, \operatorname{up}
 1: Initialisation: // runs on first activation
 2:
           State \leftarrow \texttt{INIT}
           (\operatorname{locked}_A, \operatorname{locked}_B) \leftarrow (0, 0)
3:
 4: On (top up, c_{\min}) by Alice:
           ensure State = INIT
           State \leftarrow \text{sent key}
 7:
           (sk, pk) \leftarrow \text{KeyGen}()
           output (Public Key, pk) to Alice
9: On (CHECK TOP UP) by Alice:
10:
           ensure State = SENT KEY
11:
           send (READ) to \mathcal{G}_{\text{Ledger}} as Alice and assign reply to \Sigma
12:
           ensure \exists \mathsf{tx} \in \Sigma, c_{\mathsf{on}} : c_{\mathsf{on}} \geq c_{\mathsf{min}} \land (c_{\mathsf{on}}, pk) \in \mathsf{tx.outputs}
13:
           \texttt{base\_output} \leftarrow (c_{\text{on}}, pk) \text{ of } tx
14:
            State \leftarrow \texttt{topped up}
15:
           output (TOPPED UP) to Alice
```

Fig. 3.

```
Functionality \mathcal{F}_{\operatorname{Chan}} - \operatorname{base}
 1: On (OPEN, c_F, pk_{A,out}, pk_{B,out}) by Alice:
 2:
         ensure State = TOPPED UP
 3:
         ensure c_F \geq c_{\rm on}
 4:
         (sk_{A,F}, pk_{A,F}) \leftarrow \text{KeyGen}(); (sk_{B,F}, pk_{B,F}) \leftarrow \text{KeyGen}()
         F \leftarrow TX \{\text{input: base\_output, output: } (c_F, 2/\{pk_{A,F}, pk_{B,F}\})\}
 6:
         F \leftarrow F.\operatorname{sign}(sk)
 7:
         State \leftarrow \text{Waiting for ledger}
 8:
         send (OPEN, c_F, pk_{A,\text{out}}, pk_{B,\text{out}}, F, Alice) to A and ensure reply is OK
         output ok to Alice
10: On (CHECK FUNDING) by Alice:
         ensure State = \text{Waiting for Ledger}
11:
12:
         send (READ) to \mathcal{G}_{Ledger} as Alice and assign reply to \Sigma
         ensure F\in \varSigma
13:
14:
         c_A \leftarrow c; c_B \leftarrow 0
15:
         State \leftarrow \text{OPEN BASE}
16:
         output (OPEN SUCCESS) to Alice
17: On (PAY, x) by Dave \in \{Alice, Bob\}:
18:
         ensure State \in \{\text{OPEN BASE}, \text{OPEN VIRTUAL}\}
19:
         ensure c_D - \operatorname{locked}_D \ge x
20:
         send (PAY, x, Dave) to A and expect reply (OK)
21:
         c_D \leftarrow c_D - x; c_{\bar{D}} \leftarrow c_{\bar{D}} + x //\bar{D} is Alice if D is Bob and vice-versa
22:
         output (PAY SUCCESS) to Dave
23: On (BALANCE) by Dave \in \{Alice, Bob\}:
24:
         ensure State \in \{\text{OPEN BASE}, \text{OPEN VIRTUAL}\}
25:
         output (BALANCE, (c_A, c_B, locked_A, locked_B)) to Dave
```

Fig. 4.

```
Functionality \mathcal{F}_{\mathrm{Chan}} - \mathrm{close}
 1: On (CLOSE) by Alice:
 2:
          if State = OPEN base then
 3:
              C \leftarrow \text{TX {input: }} F.\text{out, outputs: } (c_A, pk_{A,\text{out}}), (c_B, pk_{B,\text{out}}) \}
 4:
              C \leftarrow C.\mathrm{sign}(\mathrm{sk}_{\mathrm{A,F}}, \mathrm{sk}_{\mathrm{B,F}})
 5:
              State \leftarrow \text{CLOSED}
              input (SUBMIT, C) to \mathcal{G}_{Ledger}
 6:
 7:
          else if State = OPEN VIRTUAL then
 8:
              State \leftarrow \text{CLOSED}
 9:
              output (CLOSING, c_A, c_B) to opener
          end if
10:
11: On (CLOSING, c_{\text{left}}, c_{\text{right}}) by \mathcal{F}_{\text{Chan}}:
          ensure State \in \{\text{OPEN BASE}, \text{OPEN VIRTUAL}\}
12:
          ensure ((c_L, c_R), hops, (Charlie, Dave), (Frank, George), id) \in funded with
13:
     Frank \in \{Alice, Bob\}
14:
          ensure c_{\text{left}} \leq c_L + c_R
15:
          remove entry from funded
16:
          output (CLOSED VIRTUAL, c_{\text{right}}, id) to Frank
17: On (CLOSED VIRTUAL, c_{\text{right}}, id) by \mathcal{F}_{\text{Chan}}:
          ensure State \in \{\text{OPEN BASE}, \text{OPEN VIRTUAL}\}
19:
          ensure (virtual, c, \mathcal{F}_{Chan}, Dave, id) \in funded
20:
          ensure c_{\text{right}} \leq c
21:
          send (CLOSED) to virtual and expect reply YES
22:
          c_D \leftarrow c_D + c_{\text{right}}
23:
          remove entry from funded
24: On (CLOSED) by P:
25:
          if State = CLOSED then
26:
              send (YES) to P
27:
          else
28:
              send (NO) to P
29:
          end if
```

Fig. 5.

```
Functionality \mathcal{F}_{Chan} – virtual
 1: On (FUND YOU, c, Dave) by Charlie as input to Alice: // Alice is funded by
     Charlie
 2:
        ensure State = INIT
 3:
        Bob \leftarrow Dave
        send (FUND YOU, c, Bob, Charlie, Alice) to A and ensure reply is (OK)
 4:
        c_A \leftarrow c; c_B \leftarrow 0
 5:
 6:
        \mathtt{opener} \leftarrow \mathit{Charlie}
 7:
        State \leftarrow \text{OPEN VIRTUAL}
        output (OK) to Charlie
 9: On (FUND, c, hops, sub_parties = (fundee, counterparty), outer_parties =
     (Charlie, Dave)) by Alice: // we fund another channel
10:
        ensure State \in \{\text{OPEN BASE}, \text{OPEN VIRTUAL}\}
11:
        ensure c_A - \operatorname{locked}_A \geq c
12:
        input (FUND YOU, c, counterparty) to fundee as Alice, ensure output is (OK)
13:
         (L_0, R_0) \leftarrow (Alice, Bob)
        generate random id
14:
         for all (L_i, R_i) \in \text{hops do } // i \in \{1, \dots, |\text{hops}|\}
15:
16:
            ensure R_{i-1} = L_i
            send (ALLOW FUND, c, sub_parties, local_funder = L_i, id, i \stackrel{?}{=} |\text{hops}|)
17:
    to L_i as Alice and ensure reply is (OK)
18:
        end for
        send (FUND c, hops, sub_parties = (fundee, counterparty), outer_parties
19:
    = (Charlie, Dave), funder = Alice) to A and ensure reply is OK
20:
        for all (L_i, R_i) \in \text{hops do } // i \in \{1, \dots, |\text{hops}|\}
21:
            send (FUND DONE, id) to L_i as Alice and ensure reply is (OK)
22:
         end for
23:
        c_A \leftarrow c_A - c
24:
        add ((c, 0), hops, sub_parties, outer_parties, id) to funded
25:
        output (OK) to Alice
26: On (ALLOW FUND, c, sub_parties, Dave, id, is_last) by Charlie:
27:
        ensure State \in \{\text{OPEN BASE}, \text{OPEN VIRTUAL}\}
28:
        ensure Dave \in \{Alice, Bob\}
29:
        ensure c_D - \operatorname{locked}_D \ge c
30:
        output received message to Dave and ensure reply is (OK)
31:
        locked_D \leftarrow locked_D + c
32:
        add (id, is_last, sub_parties, c, Dave) to pending
33:
        send (OK) to Charlie
34: On (FUND DONE, id) by Charlie:
        ensure State \in \{\text{OPEN BASE}, \text{OPEN VIRTUAL}\}
35:
36:
        ensure (id, is_last, sub_parties, c, Dave) \in pending
37:
        remove (id, is_last, sub_parties, c, Dave) from pending
38:
         if is_last then
39:
            add ((0, c), \perp, \text{sub\_parties.reverse}(), (Dave, \perp), id) to funded
40:
         end if
41:
        send (OK) to Charlie
```

```
Simulator \mathcal{S}
 1: On (OPEN, c_F, pk_{A,out}, pk_{B,out}, F, Alice) by \mathcal{F}_{Chan}:
 2:
        simulate Alice receiving input (OPEN, c_F, pk_{A,out}, pk_{B,out}) by \mathcal{E}
 3:
        ensure simulated Alice outputs ok
 4:
        send ok to \mathcal{F}_{Chan}
 5: On (PAY, x, Dave) by \mathcal{F}_{Chan}:
        simulate Dave receiving input (PAY, x) by \mathcal{E}
        ensure simulated Dave outputs ok
 7:
        send ok to \mathcal{F}_{Chan}
9: On (FUND YOU, c, Bob, Charlie, Alice) by \mathcal{F}_{Chan}:
        simulate Alice receiving input (FUND YOU, c, Bob) by Charlie
11:
        ensure simulated Alice outputs ok to Charlie
12:
        send ok to \mathcal{F}_{Chan}
13: On (FUND c, hops, sub_parties = (fundee, counterparty), outer_parties =
    (Charlie, Dave), funder = Alice) by \mathcal{F}_{Chan}:
        simulate receiving the message without the last element with Alice,
14:
    executing only line 11 of Fig. 2
15:
        ensure VChan() is successful
16:
        send (OK) to \mathcal{F}_{Chan}
```

Fig. 7.

1 Security Proof

When \mathcal{E} sends (FUND, c, hops, sub_parties = (fundee, counterparty), outer_parties = (Charlie, Dave)) to Alice in the real world, the same thing as in the ideal world happens first, then VChan() takes place, then again the same as in the ideal world. On the other hand, in the ideal world the same thing as in the real world happens first, then VChan() is simulated by \mathcal{S} , then again the same as in the real world. TODO: double-check that the above argument makes sense

References