```
Protocol \Pi_{\mathrm{Chan}}
 1: Initialisation:
         State \leftarrow \text{INIT}
 3: On top up, check top up by \mathcal{E}, act as \mathcal{F}_{\mathrm{Chan}} (Fig. 3, lines 4-8 and 9-15
     respectively)
 4: On (OPEN, c_F, pk_{A,out}, pk_{B,out}) by \mathcal{E}:
         ensure State = \text{TOPPED UP}
         State \leftarrow \text{Opening base channel}
 6:
         do LN (other box)
 7:
 8: On (CHECK FUNDING) by \mathcal{E}:
 9:
         ensure State = WAITING FOR LEDGER
         send (READ) to \mathcal{G}_{\text{Ledger}} and assign reply to \Sigma
10:
         ensure F\in \varSigma
11:
12:
         c_A \leftarrow c; c_B \leftarrow 0 // c received in OPEN
13:
         State \leftarrow \text{OPEN BASE}
14:
         output (OPEN SUCCESS) to {\mathcal E}
15: On (PAY, x) by \mathcal{E}:
16:
         ensure State \in \{\text{OPEN BASE}, \text{OPEN VIRTUAL}\}
17:
         ensure c_A \geq x
         do LN payment (these channels won't be async) (balance change here)
18:
19:
         output (OK) to \mathcal{E}
20: On (BALANCE) by \mathcal{E}:
         ensure State \in \{\text{OPEN BASE}, \text{OPEN VIRTUAL}\}
22:
         output (BALANCE, (c_A, c_B, locked_A, locked_B)) to \mathcal{E}
23: On (CLOSE) by \mathcal{E}:
         \mathbf{if} \ \mathit{State} = \mathtt{OPEN} \ \mathtt{BASE} \ \mathbf{then}
24:
25:
              prepare C TODO
26:
              send (SUBMIT, C) to \mathcal{G}_{Ledger}
27:
          else if State = OPEN VIRTUAL then
28:
              TODO
29:
         end if
```

Fig. 1.

```
Protocol \Pi_{\mathrm{Chan}} – virtual
 1: // notification to funder
2: // trust that Alice has c in her channel
3: On (FUND YOU, c, Bob) by Charlie as input:
        ensure State = INIT
 5:
        State \leftarrow \text{Opening virtual channel}
        do LN with Bob – TODO
        output (OK) to Charlie
8: On (FUND, c, hops, sub\_parties = (fundee, counterparty), outer\_parties = (fundee, counterparty)
    (Charlie, Dave) by \mathcal{E}:
        ensure State \in \{\text{OPEN BASE}, \text{OPEN VIRTUAL}\}
        do the same as in \mathcal{F}_{Chan} (Fig. 6, lines 9-20) TODO: make sure it makes
10:
        do VChan() with hops - TODO
11:
12:
        output (OK) to \mathcal{E}
13: // notification to fundee
14: On (ALLOW FUND, ...) by Charlie, act as \mathcal{F}_{Chan} (Fig 6, line 22):
```

Fig. 2.

```
Functionality \mathcal{F}_{\mathrm{Chan}} - \mathrm{init}
 1: Initialisation: // runs on first activation
 2:
           State \leftarrow \text{init}
           (\operatorname{locked}_A, \operatorname{locked}_B) \leftarrow (0, 0)
3:
4: On (top up, c_{\min}) by Alice:
          ensure State = INIT
 6:
           State \leftarrow \text{sent key}
 7:
           (sk, pk) \leftarrow \text{KeyGen}()
          output (Public Key, pk) to Alice
9: On (CHECK TOP UP) by Alice:
10:
           ensure State = SENT KEY
11:
           send (READ) to \mathcal{G}_{\text{Ledger}} as Alice and assign reply to \Sigma
12:
           ensure \exists \mathsf{tx} \in \Sigma, c_{\mathsf{on}} : c_{\mathsf{on}} \geq c_{\mathsf{min}} \land (c_{\mathsf{on}}, pk) \in \mathsf{tx.outputs}
           \texttt{base\_output} \leftarrow (c_{\text{on}}, pk) \text{ of } \mathsf{tx}
13:
           State \leftarrow \texttt{topped up}
14:
15:
           output (TOPPED UP) to Alice
```

Fig. 3.

```
Functionality \mathcal{F}_{\operatorname{Chan}} - \operatorname{base}
 1: On (OPEN, c_F, pk_{A,out}, pk_{B,out}) by Alice:
 2:
         ensure State = TOPPED UP
 3:
         ensure c_F \geq c_{\rm on}
 4:
         (sk_{A,F}, pk_{A,F}) \leftarrow \text{KeyGen}(); (sk_{B,F}, pk_{B,F}) \leftarrow \text{KeyGen}()
         F \leftarrow TX \{\text{input: base\_output, output: } (c_F, 2/\{pk_{A,F}, pk_{B,F}\})\}
 6:
         F \leftarrow F.\operatorname{sign}(sk)
 7:
         State \leftarrow \text{Waiting for ledger}
 8:
         send (OPEN, c_F, pk_{A,\text{out}}, pk_{B,\text{out}}, F, Alice) to A and ensure reply is OK
         output ok to Alice
10: On (CHECK FUNDING) by Alice:
         ensure State = \text{Waiting for Ledger}
11:
12:
         send (READ) to \mathcal{G}_{Ledger} as Alice and assign reply to \Sigma
         ensure F\in \varSigma
13:
14:
         c_A \leftarrow c; c_B \leftarrow 0
15:
         State \leftarrow \text{OPEN BASE}
16:
         output (OPEN SUCCESS) to Alice
17: On (PAY, x) by Dave \in \{Alice, Bob\}:
18:
         ensure State \in \{\text{OPEN BASE}, \text{OPEN VIRTUAL}\}
19:
         ensure c_D - \operatorname{locked}_D \ge x
20:
         send (PAY, x, Dave) to A and expect reply (OK)
21:
         c_D \leftarrow c_D - x; c_{\bar{D}} \leftarrow c_{\bar{D}} + x //\bar{D} is Alice if D is Bob and vice-versa
22:
         output (PAY SUCCESS) to Dave
23: On (BALANCE) by Dave \in \{Alice, Bob\}:
24:
         ensure State \in \{\text{OPEN BASE}, \text{OPEN VIRTUAL}\}
25:
         output (BALANCE, (c_A, c_B, locked_A, locked_B)) to Dave
```

Fig. 4.

```
Functionality \mathcal{F}_{\mathrm{Chan}} - \mathrm{close}
 1: On (CLOSE) by Alice:
 2:
          if State = OPEN base then
 3:
              C \leftarrow \text{TX {input: } } F.\text{out, outputs: } (c_A, pk_{A,\text{out}}), (c_B, pk_{B,\text{out}}) \}
 4:
              C \leftarrow C.\mathrm{sign}(\mathrm{sk}_{\mathrm{A,F}}, \mathrm{sk}_{\mathrm{B,F}})
 5:
              State \leftarrow \text{CLOSED}
              input (SUBMIT, C) to \mathcal{G}_{Ledger}
 6:
 7:
          else if State = OPEN VIRTUAL then
 8:
              State \leftarrow \text{CLOSED}
 9:
              output (CLOSING, c_A, c_B) to opener
          end if
10:
11: On (CLOSING, c_{\text{left}}, c_{\text{right}}) by \mathcal{F}_{\text{Chan}}:
          ensure State \in \{\text{OPEN BASE}, \text{OPEN VIRTUAL}\}
12:
          ensure ((c_L, c_R), hops, (Charlie, Dave), (Frank, George), id) \in funded with
13:
     Frank \in \{Alice, Bob\}
14:
          ensure c_{\text{left}} \leq c_L + c_R
15:
          remove entry from funded
16:
          output (CLOSED VIRTUAL, c_{\text{right}}, id) to Frank
17: On (CLOSED VIRTUAL, c_{\text{right}}, id) by \mathcal{F}_{\text{Chan}}:
          ensure State \in \{\text{OPEN BASE}, \text{OPEN VIRTUAL}\}
19:
          ensure (virtual, c, \mathcal{F}_{Chan}, Dave, id) \in funded
20:
          ensure c_{\text{right}} \leq c
21:
          send (CLOSED) to virtual and expect reply YES
22:
          c_D \leftarrow c_D + c_{\text{right}}
23:
          remove entry from funded
24: On (CLOSED) by P:
25:
          if State = CLOSED then
26:
              send (YES) to P
27:
          else
28:
              send (NO) to P
29:
          end if
```

Fig. 5.

```
Functionality \mathcal{F}_{\operatorname{Chan}} - \operatorname{virtual}
 1: On (FUND YOU, c, Dave) by Charlie as input to Alice: // Alice is funded by
    Charlie
 2:
        ensure State = INIT
 3:
        Bob \leftarrow Dave
        send (FUND YOU, c, Bob, Charlie, Alice) to A and ensure reply is (OK)
 4:
 5:
        c_A \leftarrow c; c_B \leftarrow 0
 6:
        \mathtt{opener} \leftarrow \mathit{Charlie}
 7:
        State \leftarrow \texttt{OPEN VIRTUAL}
        output (OK) to Charlie
9: On (FUND, c, hops, sub_parties = (fundee, counterparty), outer_parties =
    (Charlie, Dave)) by Alice: // we fund another channel
10:
        ensure State \in \{\text{OPEN BASE}, \text{OPEN VIRTUAL}\}
11:
        ensure c_A - \operatorname{locked}_A \ge c
        input (FUND YOU, c, counterparty) to fundee as Alice, ensure output is (OK)
12:
13:
        (L_0, R_0) \leftarrow (Alice, Bob)
14:
        generate random id
        for all (L_i, R_i) \in \text{hops do } // i \in \{1, \dots, |\text{hops}|\}
15:
16:
            ensure R_{i-1} = L_i
            send (ALLOW FUND, c, sub_parties, local_funder = L_i, id, i \stackrel{?}{=} |\text{hops}|)
17:
    to L_i as Alice and ensure reply is (OK)
18:
        end for
19:
        c_A \leftarrow c_A - c
20:
        add ((c, 0), hops, sub_parties, outer_parties, id) to funded
21:
        output (OK) to Alice
22: On (ALLOW FUND, c, sub_parties, D, id, is_last) by Charlie:
        ensure State \in \{\text{OPEN BASE}, \text{OPEN VIRTUAL}\}
23:
24:
        ensure D \in \{Alice, Bob\}
25:
        ensure c_D - \operatorname{locked}_D \ge c
26:
        output received message to D and ensure reply is (OK)
27:
        locked_D \leftarrow locked_D + c
28:
        if is_last then
29:
            add ((0, c), \perp, sub\_parties.reverse(), (Dave, \perp), id) to funded
30:
        end if
31:
        send (OK) to Charlie
```

Fig. 6.

## Simulator ${\cal S}$

- 1: On (OPEN,  $c_F$ ,  $pk_{A,\text{out}}$ ,  $pk_{B,\text{out}}$ , F, Alice) by  $\mathcal{F}_{\text{Chan}}$ :
- 2: simulate Alice receiving input (OPEN,  $c_F$ ,  $pk_{A,\text{out}}$ ,  $pk_{B,\text{out}}$ ) by  $\mathcal{E}$
- 3: ensure simulated *Alice* outputs ok
- 4: send ok to  $\mathcal{F}_{Chan}$
- 5: On (PAY, x, Dave) by  $\mathcal{F}_{Chan}$ :
- 6: simulate Dave receiving input (PAY, x) by  $\mathcal{E}$
- 7: ensure simulated Dave outputs OK
- 8: send ok to  $\mathcal{F}_{Chan}$
- 9: On (FUND YOU, c, Bob, Charlie, Alice) by  $\mathcal{F}_{Chan}$ :
- 10: simulate Alice receiving input (fund you, c, Bob) by Charlie
- 11: ensure simulated Alice outputs OK to Charlie
- 12: send ok to  $\mathcal{F}_{Chan}$

Fig. 7.

## References