

# Constraint Satisfaction Problems

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## Problem 1: Backtracking

*How many calls does your algorithm need (on average) for  $n=10$ ? Is there a lot of variation in the number of calls when you try this multiple times?*

Run	Calls	Run	Calls	Run	Calls	Run	Calls	Run	Calls
0	128	20	16	40	60	60	24	80	77
1	59	21	201	41	109	61	85	81	163
2	17	22	26	42	29	62	17	82	19
3	74	23	74	43	144	63	168	83	93
4	33	24	12	44	45	64	22	84	80
5	16	25	27	45	238	65	11	85	32
6	183	26	306	46	150	66	48	86	62
7	42	27	47	47	439	67	47	87	196
8	97	28	23	48	168	68	124	88	302
9	23	29	656	49	244	69	16	89	46
10	13	30	51	50	207	70	75	90	15
11	11	31	298	51	231	71	97	91	11
12	135	32	117	52	11	72	31	92	34
13	22	33	49	53	664	73	12	93	20
14	37	34	137	54	228	74	18	94	267
15	52	35	45	55	39	75	62	95	296
16	213	36	32	56	11	76	41	96	218
17	40	37	22	57	57	77	151	97	301
18	104	38	69	58	23	78	124	98	29
19	35	39	348	59	29	79	15	99	15

This is a report of one hundred runs of the backtracking algorithm.

The mean is 104.8.

The standard deviation is 121.7.

For further insight, the minimum and maximum of the calls number are 11 and 664.

So, on average the algorithm needs 104.8 calls for  $n = 10$ , and there is a lot of variation in the number of calls, since the standard deviation is 121.7, but also encouraged by the staggering difference between the minimum number of calls (11) and the maximum (664).

## Problem 2: Forward Checking

The following statistics are gathered from 10 runs with  $n = 50$ .

Configuration	Mean	Standard Deviation
No MRV or LCV	4724.4	6315.95
Only LCV	2643.1	3172.38
Only MRV	67.0	0.0
Both (MRV and LCV)	73.0	0.0

The functions `selectVariable` and `orderDomain` make the algorithm faster and more stable, because they enforce an order to selecting the next value to be assigned (the `selectVariable` function) and which is the best domain to choose next (the `orderDomain` function). So now, we no longer leave things to chance. Every run will be the same for the same starting variables list and domains.

## Problem 3: AC3

The following statistics are gathered from 10 runs with  $n = 50$ .

Configuration	Mean	Standard Deviation
No MRV or LCV	986.4	2264
Only LCV	76.6	24.44
Only MRV	60	0.0
Both (MRV and LCV)	55	0.0

AC3 is more efficient than normal Forward Checking because it enforces arc consistency on every arc in the graph instead of only neighbouring arcs to the assigned variable. Again, enforcing an order to selecting the next variable to be assigned and the next domain to be chosen ensures an efficient route without (much) backtracking.

## Problem 4: Sudoku

Can you solve the hard puzzle with any of your algorithms?

The hard sudoku puzzle was solvable with AC3 and Forward Checking

**AC3: 3382 calls.**

**Forward Checking: 5855 calls**