

Programming Ex.4

ML:Programming Exercise 4:Neural Networks Learning

This is the toughest exercise so far, mainly because you have to implement a series of steps, each subject to error, before you get any feedback. These techniques may help:

See the tutorial below (developed for the Spring 2014 session).

Use the command `help`. The command line is your friend. Run enough of `eval` to initialize x_0 , Θ_{init1} , and Θ_{init2} , then write one statement or operation at a time to get the results you want, when you get a statement working, transfer it to `initialize` and save the file.

Use `size` functions. Use `size` to check the dimensions of vectors and matrices to determine order of multiplication and whether a transpose is needed. This is especially valuable for the gradients. Graders need that the gradient matrices are the same size as Θ_{init1} and Θ_{init2} . Also note that `zeros` needs to do some things that `ones` and `size` cannot. See multiplying an $n \times 1$ vector by a $1 \times n$ vector `ones` on `m` columns.

You may find it helpful to note the dimensions of each matrix in a comment on the line of code, as you define it, such as `R = zeros(n, n)`.

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1

train1 = reshape(.....) % (dim x (n+1))

2

x = x + 1; % distibute (dim x (n+1)) = (dim x n) + (dim x (n+1))

- Do not hard code. Specifically, do not hard code the size of the 1d array y vector to 10. It will work fine for the test set, but will blow up with eight error message arrays.
- If you get stuck on gradients, try working on a smaller, easier to grasp problem. You can take code from deepNN2 and paste it into the command line to get a 5-5 network that's a bit more manageable.
- Full vectorization of backprop.

If you want to get rid of the loop over the training samples in back propagation algorithm, you are facing the problem to create a logical vector for y for all training examples. Some smart guy from the spring 2013 instance of this course came up with the following elegant solution for this task

```
1  g = (1 / max_labels) * y
2
```

(This does not seem to work in Octave 3.2.4. I use 3.6.4. Doesn't work on 3.4 either.)

After getting this, it was pretty straightforward to vectorize the loop - I could transform each line from my for loop 1.1 to the vectorized code.

Note, the above expression relies on the broadcasting feature of Octave: see <https://www.coursera.org/learn/machine-learning/resources/Uuxg6>

[Broadcasting](#)

A call to `bsxfun` is an equivalent solution that explicitly apply a broadcast:


```
1 y = zeros(n, num_labels);
2 for i = 1:n
3     y(i,:) = f;
4 end
```

Using vectorization speeds up the code considerably.

Another method for generating the y matrix, this time looping over the labels:

```
1  U_matrix = []  # create a null matrix
2  for i in range(M):
3      U_matrix = [0]*M
4  return U_matrix
5
```

Another vectorized concave method (using vectorized indexing of an eye matrix) - Spring 2014 session.

```
1 y_matrix = eye(num_labels)(y,:); % works for Octave
2 ...or
3 all_combos = eye(num_labels);
4 y_matrix = all_combos(y,:); % works for Matlab
5
```

This method uses an indexing trick to vectorize the creation of 'y_matrix', where each element of 'y' is mapped to a single-value row vector copies from an *array* matrix.

FYI: Misleading Formula in Ex4 pdf for regularization term of cost

Tutorial for Ex.4 Forward and Backpropagation (Spring 2014 session)

[illegible]

A note regarding the sizes of these data objects: See the Appendix at the bottom of the tutorial for information on the sizes of the data objects. **Note regarding bias units, regularisation, and back-propagation:** There are 2 methods for handling the bias units in the back-propagation gradient calculations. I've described only one of them here, it's the one that I understood the best. Both methods work, choose the one that makes sense to you and avoid dimension errors. It matters not a whit whether the bias unit is dropped before or after it is calculated. Both methods give the same results, though the order of operations and transpositions required may be different. Those with contrary opinions are welcome to join our own ever-nucleated **Propagation** list by outlining the forward propagation process. Though this was already accomplished once upon Exercise 3, you'll need to duplicate some of that work because computing the gradients requires some of the intermediate results from

Step 1 - Expand the 'y' output values into a matrix of single values (see [v04.pdf](#) Page 5). This is most easily done using an `eye()` matrix of size `num_labels`, with vectorized indexing by 'y', as in `eye(num_labels)[y,:]`. Discussions of this and other methods are available in the Course Wiki - [Prostatectomy Exercises](#) section. A typical variable name would be `'y_matrix'`.

Step 2 - perform the forward propagation on \mathbf{a}_1 equals the \mathbf{X} input matrix with a column of 1's added (\mathbf{a}_1 units) \mathbf{z}_2 equals the product of \mathbf{a}_1 and \mathbf{Q}_1 is the result of passing \mathbf{z}_2 through \mathbf{g}_1 \mathbf{a}_2 then has a column of 1's added (\mathbf{a}_2 units) \mathbf{z}_3 equals the product of \mathbf{a}_2 and \mathbf{Q}_2 \mathbf{a}_3 is the result of passing through \mathbf{g}_2 Cost Function, non-regularized

Step 3 - Compute the unregularized cost according to eq.4.pdf (top of Page 5). I had a hard time understanding this equation mainly that I had a misconception that $y^{(i)}$ is a vector, instead it is just simply one number/using X , your θ matrix, and m (the number of training examples). Cost should be a scalar value. If you give a vector of cost values, you can turn that vector to get the cost. Remember to use element-wise multiplication with the last function. Moreover, you can see in which the θ matrix is used to compute the cost. I am not sure if this is the case.

Cost Regularization

Step 4 - Compute the regularized component of the cost according to eq4.pdf Page 6, using O1 and O2 ignoring the columns of bias units, along with λ and m . The easiest method to do this is to compute the regularization terms separately, then add them to the unregularized cost from Step 3. You can run `evl.m` to check the regularized cost, then you can submit Part 2 to the grader. **Sigmoid Gradient and Random Initialization**

Step 6 - Implement the random initialization function as instructed on ex6.pdf, top of Page 8. You do not submit this function to the grader.

Step 7 - Now we work from the output layer back to the hidden layer, calculating how bad the errors are. See [ex4.pdf](#) Page 9 for reference. δ_3 equals the difference between a_3 and the $y_{\text{matrix}}[2]$ equals the product of δ_5 and δ_2 (ignoring the δ_2 bias units), then multiplied element-wise by the $g'(z)$ of z_2 computed back in Step 2). Note that at this point, the instructions in [ex4.pdf](#) are specific to looping implementations, so the notation there is different. δ_2 equals the product of δ_3 and δ_1 . This step calculates the product and sum of the errors. δ_1 equals the product of δ_2 and a_1 . This step calculates the product and sum of the errors.

Gradient, non-regularized

Step 8 - Now we calculate the normalized these gradients, using the sums of the errors we just computed (see [ex4.pdf](#) bottom of Page 119). gradient equals its scaled by 1/m (2 gradient equals scaled by 1/m). The `ex4.m` script will also perform gradient checking for you, using a small test case than the full character classification example. So if you're debugging your `nnCostFunction()` using the `'keyboards'` command during this, you'll suddenly be seeing some much smaller sizes of `X` and the `Gradients`. Do not be alarmed if the feedback provided to you by `ex4.m` for gradient checking seems OK, you can now submit Part 4 to the grader. **Overfitting/Regularization**

[illegible]

Appendix

Here are the sizes for the character recognition example, using the method described in this tutorial. a1: 5000x400x2; 5000x25x2; 5000x26x3; 5000x10x3; 5000x10x2; 5000x25xtheta1; Delta1 and Theta1_grad: 25x4017theta2; Delta2 and Theta2_grad: 10x26 (note that the ex4m script uses a several test cases of different sizes, and the subnet grader uses yet another different test case).

Debugging Tip

The submit script, for all the programming assignments, does not report the line number and location of the error when it crashes. The following method can be used to make it do so which makes debugging easier.

Open `ex64\src\mainWithConfiguration.m` and replace line

```
1 print("I Please try again later, lol")
2
```

Output 20 with


```
1  @param() Vector from FileIOCollectionFileIO.readLine() , s, stack(1,1), FileIOCollectionFileIO.readLine(), s, stack(1,1), line 1}
2
```

That top line says "I Photo by again later" on stack, instead of that, the bottom line will give the location and the number of the error. This change can be applied to all the programming assignments.

Tips for classifying your own images:

There's no documentation on how the images were prepared for this course. These tips may be helpful.

- The images must be 10x10 pixels with 255/255 pixels.
- The image plots are subplots (not to plot -1.0 is black, 0.0 is gray, and +1.0 is white. However, nearly all of the plots are in the 0.0 to +1.0 range. The backgrounds are gray, and the image "open screen" are white.
- Your images must use the same value range as the training data, otherwise the NN will not be able to classify them.
- Center the digit image so it does not use the top pixels around the borders.

Bonus: Neural Network does not need order in pixels of an image as humans do

The pixels order (as a human sees them) is not necessary (or relevant) for a Neural Network.

You can test it with a modified ex3.m program below (you can call it ex3_rand.m)

The program has a randomize pixel position step "scrambling" the 400 vector positions BEFORE the training. As long as you keep the same pixel position when predicting, the results are the same.

It is interesting to "see" how good your perfectly results with a scrambled picture.

You can test it once you have submitted ON the ex3.m program (warning that you have the **correct** function working ON Error).

ex3_rand.m is a modified version of ex3.m

```
1 # ex1_grad.m (is a modified version of ex1.m to scramble pixels/features)
2 #
3 # Machine Learning Online Class - Exercise 3 | Randomize Features
4
5 % Initialization
6 clear; close all; clc
7
8 % Setup the parameters you will use for this part of the exercise
9 randLayerSize = 400; % Initial Depth: Number of digits
10 numLabels = 10; % 10 labels, from 1 to 10
11 % Note that we have mapped '0' to label 10!
12
13 % ===== Part 1: Loading and Visualizing Data =====
14 % We start the exercise by first loading and visualizing the dataset.
15 % You will be working with a dataset that contains handwritten digits.
16 %
17
18 % Load Training Data
19 fprintf('Loading and Visualizing Data ... \n');
20
21 % Load the data
22 x = load('ex1data1.mat'); % Training data stored in arrays X, y
23 n = size(X, 1);
24
25 % Randomly select 100 data points to display
26 rand_indices = randperm(n, 100);
27 x1 = X(rand_indices, :);
28 displayData(x1);
29
30 fprintf('Program paused. Press enter to continue.\n');
31 pause;
32
33 % ===== Part 2: Vectorize Logistic Regression =====
34 % In this part of the exercise, you will reuse your logistic regression
35 code from the last exercise. We take here 4s to make sure that your
36 % regularized logistic regression implementation is vectorized. After
37 % that, you will implement one-vs-all classification for the handwritten
38 % digit dataset.
39 %
40
```

Why the order is irrelevant for the Neural-Network

You can use that the order of the points is irrelevant as long as you are consistent in two ways:

1. Between samples. Each feature should mean the same thing. You can not change the pixel location for one sample and not for the others. You can not decide from left to right how to name the "training" data for the entire dataset.

2. Between labels. Each label should represent the same digit for its group of samples. Mapping a digit four is a four for all of the samples you loaded in that and can not change it, it does not matter if the pixels are scrambled, it is a four.

Equivalent example of order irrelevancy

An equivalent example is the order of variable names when solving a system of equations, it does not matter how you call a variable or the order in which you are considering through out the solution.

For example this:

$$3x_1 + 4x_2 = 36$$

$$2x_1 - 3x_2 = 11$$

$$\text{Solves } x_1 = 3, \quad x_2 = 5$$

...is equivalent to:

$$3x_1 + 4x_2 = 36$$

$$2x_2 - 3x_1 = -11$$

$$\text{Solves } x_1 = 3, \quad x_2 = 5$$

...also you can "normalize" the terms and labels:

$$-3x_1 + 2x_2 = -11$$

$$4x_1 + 3x_2 = 36$$

$$\text{Solves } x_1 = 3, \quad x_2 = 5$$

It has to do with convention. Any convention as long as it is the same all the way through.

