

## Knowledge Representation Technique

Logic are formal language with well defined rules for manipulation of representation as well as to draw conclusion

Propositional logic

First order Logic (Predicate logic)

Second order logic

Properties of these KR techniques

- 1.Representational Adequacy
- 2.Clear syntax and semantics
- 3.Inferencial Adequacy
- 4.Inferencial efficiency
5. Naturalness

# Resolution Techniques to derive conclusion

## Steps for Resolution

- Convert the given statements in Predicate/Propositional Logic
- Convert these statements into Conjunctive Normal Form
- Negate the Conclusion (Proof by Contradiction)
- Resolve using a Resolution Tree (Unification)

Propositional logic is mathematical system for reasoning

Proposition is variable and connection/relation between them

P: It is hot

Q: It is humid

R: It is raining

connective: And  $\wedge$

OR  $\vee$



$P \rightarrow$  can also be written as  $\neg P \vee Q$

If it is hot and humid then it is raining  $P \wedge Q \rightarrow R$

## First Order logic (Predicate logic)

Predicate logic(object, function and quantifier)

$P(x,y,....)$

More expressive than propositional logic  
syntax and semantics are more clear

All students are smart  
 $\forall x \text{ Student}(x) \longrightarrow \text{Smart}(x)$

All P's are Q's  $\forall x P(x) \longrightarrow Q(x)$

Some P's are Q's  $\exists x P(x) \wedge Q(x)$

conversion to CNF: conjunctive normal form

1: eliminate implication sign  $\longrightarrow$

2. eliminate existential and universal quantifier  $\exists$   $\forall$

3. eliminate And  $\wedge$

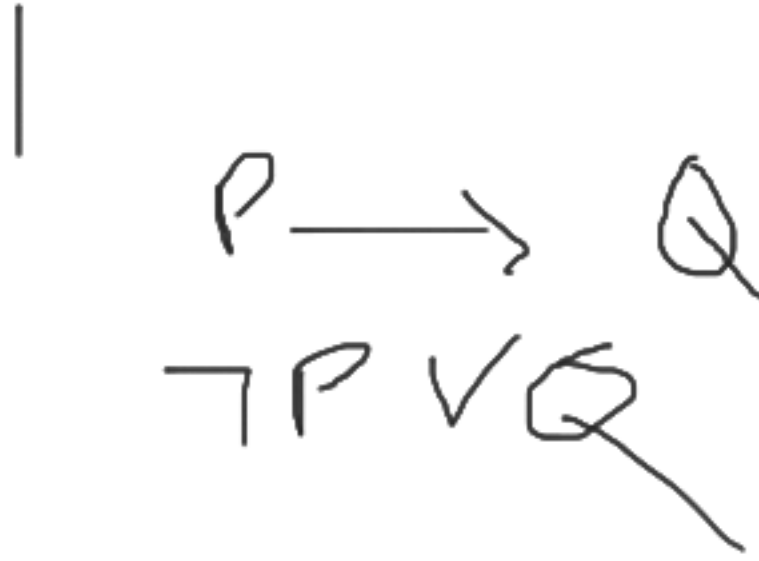
Resolution to negate conclusion

# Resolution

Problem Statement:

1. Ravi likes all kind of food.
  2. Apples and chicken are food
  3. Anything anyone eats and is not killed is food
  4. Ajay eats peanuts and is still alive
  5. Rita eats everything that Ajay eats
- Prove by resolution that Ravi likes peanuts using resolution.

Solution:



Step 1: Converting the given statements into Predicate/Propositional Logic

- i.  $\forall x : \text{food}(x) \wedge \text{likes}(\text{Ravi}, x)$
- ii.  $\text{food}(\text{Apple}) \wedge \text{food}(\text{chicken})$
- iii.  $\forall a : \forall b : \text{eats}(a, b) \wedge \neg \text{killed}(a) \rightarrow \text{food}(b)$
- iv.  $\text{eats}(\text{Ajay}, \text{Peanuts}) \wedge \text{alive}(\text{Ajay})$
- v.  $\forall c : \text{eats}(\text{Ajay}, c) \rightarrow \text{eats}(\text{Rita}, c)$
- vi.  $\forall d : \text{alive}(d) \wedge \neg \text{killed}(d)$
- vii.  $\forall e : \neg \text{killed}(e) \wedge \text{alive}(e)$

Conclusion:  $\text{likes}(\text{Ravi}, \text{Peanuts})$

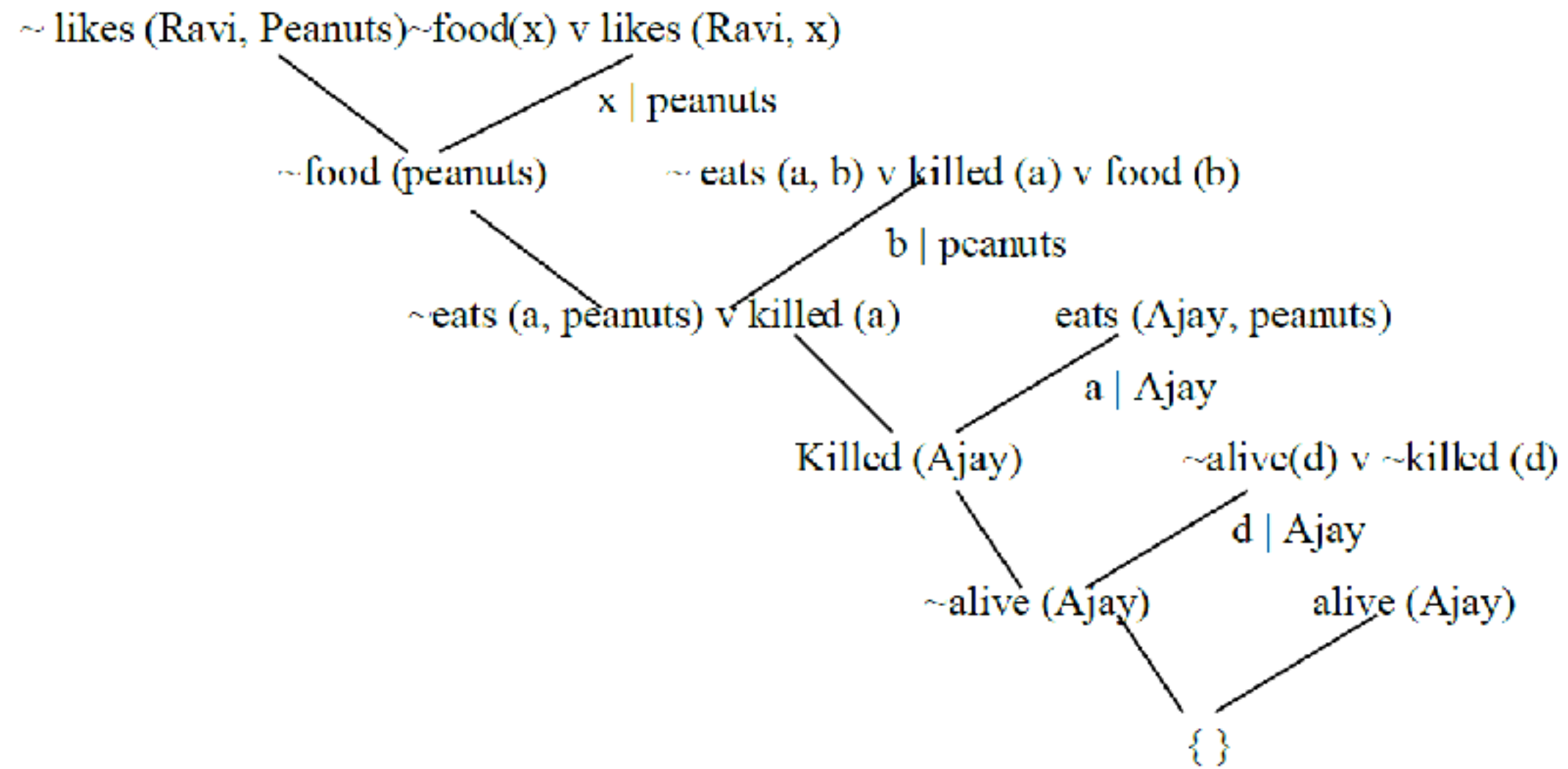
Step 2: Convert into CNF

- i.  $\neg \text{food}(x) \vee \text{likes}(\text{Ravi}, x)$
- ii.  $\text{Food}(\text{apple})$
- iii.  $\text{Food}(\text{chicken})$
- iv.  $\neg \text{eats}(a, b) \vee \text{killed}(a) \vee \text{food}(b)$
- v.  $\text{Eats}(\text{Ajay}, \text{Peanuts})$
- vi.  $\text{Alive}(\text{Ajay})$
- vii.  $\neg \text{eats}(\text{Ajay}, c) \vee \text{eats}(\text{Rita}, c)$
- viii.  $\neg \text{alive}(d) \vee \neg \text{killed}(d)$
- ix.  $\text{Killed}(e) \vee \text{alive}(e)$

Conclusion:  $\text{likes}(\text{Ravi}, \text{Peanuts})$

Step 3: Negate the conclusion  
 $\neg \text{likes}(\text{Ravi}, \text{Peanuts})$

Step 4: Resolve using a resolution tree



<https://www.cs.utexas.edu/users/novak/resosol.html>

All SGSITS  
students are  
intelligent



1. All people who are not poor and are smart are happy.
2. Those People who read are not stupid.
3. John can read and is healthy.
4. Happy People have exciting life

1.  $\forall x: \neg \text{poor}(x) \wedge \text{smart}(x) \longrightarrow \text{happy}(x)$
2.  $\forall x: \text{read}(x) \longrightarrow \neg \text{stupid}(x)$
3.  $\text{read}(\text{John}) \wedge \text{healthy}(\text{John})$
4.  $\forall x: \text{Happy}(x) \longrightarrow \text{Exciting}(x)$
1.  $\neg \text{stupid}(x) \equiv \text{smart}(x)$

1.  $\text{poor}(x) \vee \neg \text{smart}(x) \vee \text{happy}(x)$
  2.  $\neg \text{read}(x) \vee \text{smart}(x)$
  3.  $\neg \text{read}(\neg \text{john}) \wedge \text{smart}(\neg \text{john})$
  4.  $\neg \text{poor}(\neg \text{john})$
  5.  $\neg \text{happy}(x) \vee \text{exciting}(x)$
- Some people has exciting life:  $\exists x: \text{exciting}(x)$

$\neg \text{exciting}(x)$

happy

$\text{poor} \vee \neg \text{smart}(x) / x / \neg \text{john}$

$\neg \text{poor}(\neg \text{john}) \vee 4$