

Solving Simultaneous Equation using Parametric form of a line:

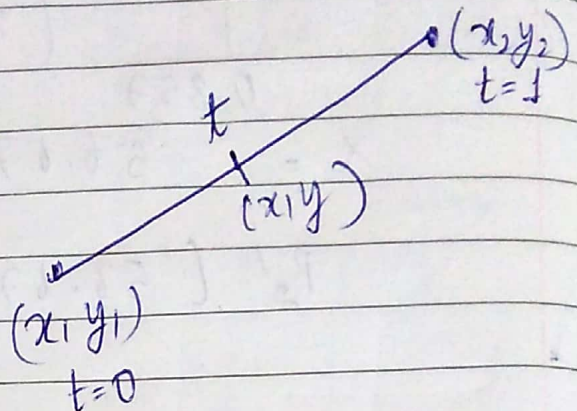
$$x = tx_2 + (1-t)x_1$$

$$x = t \cdot x_2 + x_1 - x_1 t$$

$$x = x_1 + t(x_2 - x_1)$$

$$\boxed{x = x_1 + t \cdot \Delta x}$$

$$0 < t < 1$$



$$\boxed{y = y_1 + t \cdot \Delta y}$$

$$0 < t < 1$$

$$x_{wmin} \leq x \leq x_{wmax}$$

$$y_{wmin} \leq y \leq y_{wmax}$$

$$x_{wmin} \leq x_1 + t \Delta x \leq x_{wmax}$$

$$y_{wmin} \leq y_1 + t \Delta y \leq y_{wmax}$$

$$x_1 + t \Delta x \geq x_{wmin}$$

$$x_1 + t \Delta x \leq x_{wmax}$$

$$y_1 + t \Delta y \geq y_{wmin}$$

$$y_1 + t \Delta y \leq y_{wmax}$$

$$t \Delta x \geq x_{wmin} - x_1 \quad \text{--- (1)}$$

$$t \Delta x \leq x_{wmax} - x_1 \quad \text{--- (2)}$$

$$t \Delta y \geq y_{wmin} - y_1 \quad \text{--- (3)}$$

$$t \Delta y \leq y_{wmax} - y_1 \quad \text{--- (4)}$$

There are the two different w-ordinates at particular time $t=0$ & $t=1$.

x, y w-ordinates must lie between window boundaries i.e. $(x_{min}, x_{max}, y_{min}, y_{max})$

$$t \cdot P_k \leq q_k$$

$$k = 1, 2, 3, 4.$$

In order to convert these equations in above form, we need to multiply eqⁿ ① & ③ with -1 .

$$\begin{aligned} -t \Delta x &\leq x_1 - x_{wmin} \\ t \Delta x &\leq x_{wmax} - x_1 \\ -t \Delta y &\leq y_1 - y_{wmin} \\ t \Delta y &\leq y_{wmax} - y_1 \end{aligned}$$

Based upon these 4 conditions we need to find out whether line lies inside or outside window boundary.

$$P_1 = -\Delta x$$

$$q_1 = x_1 - x_{wmin}$$

$$P_2 = \Delta x$$

$$q_2 = x_{wmax} - x_1$$

$$P_3 = -\Delta y$$

$$q_3 = y_1 - y_{wmin}$$

$$P_4 = \Delta y$$

$$q_4 = y_{wmax} - y_1$$

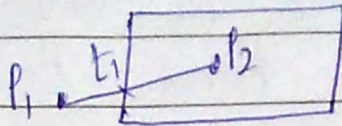
If $P_k = 0$ - Line is parallel to window

$q_k < 0$ - Line outside

$q_k > 0$ - line is inside / partial

$q_k = 0$ - within boundary / partially.

If $P_k < 0 \rightarrow t_1$



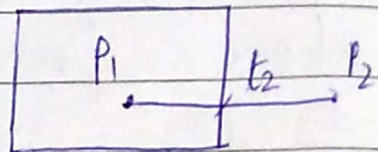
$$t_1 = \max\left(0, \frac{q_k}{P_k}\right)$$

At what interval the point is intersecting with the window boundary

$$x = x_1 + t_1 \cdot \Delta x$$

$$y = y_1 + t_1 \cdot \Delta y$$

If $P_k > 0 \rightarrow t_2$



$$t_2 = \min\left(1, \frac{q_k}{P_k}\right)$$

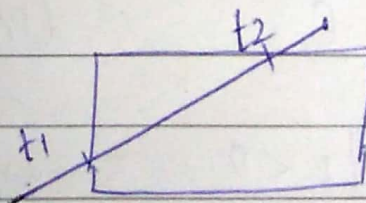
$$x = x_1 + t_2 \cdot \Delta x$$

$$y = y_1 + t_2 \cdot \Delta y$$

If t_1 changes \rightarrow starting position is outside the window

If t_2 changes \rightarrow end point is outside the window

If both changes \rightarrow both initial & final point lies outside the window.



Ques.

$$x_{wmin} = 5$$

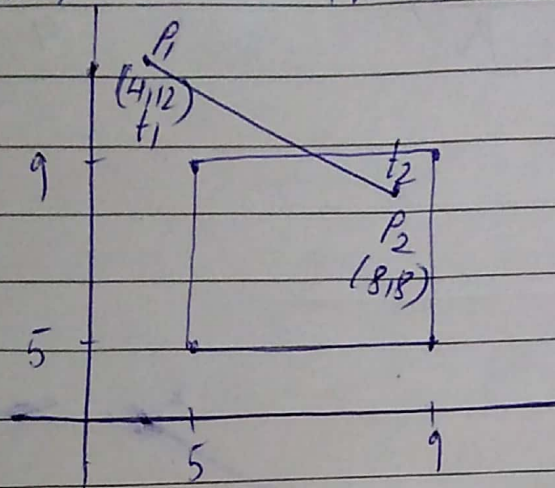
$$y_{wmin} = 5$$

$$\text{Line } P_1 (4, 12)$$

$$x_{wmax} = 9$$

$$y_{wmin} = 9$$

$$P_2 (8, 8)$$



$$\begin{aligned} P_1 &= -\Delta x & q_1 &= x_1 - x_{wmin} \\ P_2 &= \Delta x & q_2 &= x_{wmax} - x_1 \\ P_3 &= -\Delta y & q_3 &= y_1 - y_{wmin} \\ P_4 &= \Delta y & q_4 &= y_{wmax} - y_1 \end{aligned}$$

$$\Delta x = x_2 - x_1 = 8 - 4 = 4$$

$$\Delta y = y_2 - y_1 = 8 - 12 = -4$$

$$\begin{aligned} P_1 &= -4 & q_1 &= -1 \\ P_2 &= 4 & q_2 &= 5 \\ P_3 &= 4 & q_3 &= 7 \\ P_4 &= -4 & q_4 &= -3 \end{aligned}$$

$$P_k < 0 \quad (P_1, P_4)$$

Here, we need to find time interval (t_1)

$$t_1 = \max\left(0, \frac{q_k}{P_k}\right)$$

$$t_1 = \max\left(0, \frac{q_1}{P_1}, \frac{q_4}{P_4}\right) = \max\left(0, \frac{1}{-4}, \frac{-3}{-4}\right) = \boxed{t_1 = 3/4}$$

$$p_k > 0 \quad (p_2, p_3)$$

$$t_2 = \min\left(1, \frac{q_2}{p_2}, \frac{q_3}{p_3}\right) = \min\left(1, \frac{5}{4}, \frac{7}{4}\right)$$

$$t_2 = 1$$

$$\text{for } t_1 = 3/4$$

$$\begin{aligned} x &= x_1 + t_1 \cdot \Delta x \\ &= 4 + (3/4) \cdot 4 \\ &= 7 \end{aligned}$$

$$\begin{aligned} y &= y_1 + t_1 \cdot \Delta y \\ &= 12 + (3/4) \cdot -4 \\ &= 9 \end{aligned}$$

$$t_1 = 3/4 \quad (7, 9)$$

Ques. Window A (20,20) B (90,20) C (90,70) D (20,70)
Line P₁ (10,30) P₂ (80,90)