Congestion-Aware Routing for Multi-Class Mobility-on-Demand Service

Semester 8 Project Thesis

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Candidate's Declaration

I declare that the project work titled "Congestion-Aware Routing for Multi-Class Mobility-on-Demand Service" done at the Singapore University of Technology and Design, Singapore and submitted at the Indian Institute of Information Technology, Allahabad is the bonafide work of Niharika Shrivastava(IIT2016501). It is a genuine record of my study carried out from January 2020 till present under the guidance of Prof. Malika Meghjani and Prof O.P. Vyas. Due acknowledgements have been made in the text to all the materials used.

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Abstract

Recent developments in urban mobility have demonstrated the potential capacity of road networks to accommodate increasing traffic demand. However, all of the approaches are either sub-optimal or computationally inefficient. This paper addresses the problem of customer routing in a congested network. First, our aim is to provide congestion-aware routes for mobility-on-demand services that operate using a combination of a heterogeneous multi-class fleet. Every customer trip is distributed into multiple legs, i.e., walking or cycling for the first and last leg of the trip; cars or public transport for the middle leg of the trip. Second, we provide optimal transit points from one leg to another for this inter-modal (multi-class) service, such that the overall travel time is least within a capacity-bound transportation network. Finally, we build this framework into a social model by fulfilling all trip demands in a system-optimal way. We showcase the effectiveness of our framework by using Singapore's network data from OpenStreetMap coupled with its real-time traffic data. We achieve 0% congestion for 1000 customers for different peak times along with a 64.79% reduction in the overall network cost by using a multi-class setup. Our proposed algorithm to find optimal transit points within trips saves 70.1% queries with an average delay of 4 secs. Moreover, our solution also recommends alternate paths that are user-optimal.

Contents

1   Introduction

1.1   Motivation

Traffic congestion on urban road networks has become increasingly problematic since the 1950s [1]. With an increase in vehicles on the road and capacity of the roads remaining approximately constant, the speed of the traffic stream slows [2]. This results in higher travel times and increased pollution. With the increasing popularity of on-demand mobility services [3, 4, 5] like Uber, Grab, Yulu and Lyft, the traffic demand has started to reach road capacities more often, thereby enabling congestion to set in. All passengers inherently opt for the shortest route in the network in order to save travelling time, which ultimately results in blocked roads and very slow traffic movements [6]. All these factors lead to under-utilization of a city's intricately-built road network.

Many countries adopt the "odd-even rule" [7] that allows only a section of the vehicles to operate on a given day, for e.g., vehicles with odd number plate on Monday. In the UK, they reduced congestion by creating "out of town" [8] commercial areas and pedestrianising city centres, thereby reducing drive-able routes in the most populated areas. Many works involving autonomous systems, where a central operator can manage system-wide actions, have tried to increase the throughput of a network. [9, 10] have shown that autonomous vehicles may be able to drive faster and follow other vehicles at closer distances without compromising safety, thereby effectively increasing the capacity of a road. Others have suggested ride-sharing services such as UberPool and LyftLine, or public transport to lessen the traffic burden of the [11, 12, 13]. Rerouting empty vehicles to potential regions of higher customer requests based on historical data has also shown to lessen region-wise network congestion [14, 15].

Multi-class fleets [16] allow breaking a customer trip into 3 classes: first mile, middle mile and last mile. The customer can choose to either walk on foot on pedestrian paths, use dedicated cycle-ways, or on-demand scooters for their first and last mile. The middle mile will cover at least 90% of the customer trip using the main road networks of a city and make use of fast-speed cars or public transports as per convenience. By using all three classes in an optimal combination, customers can maneuver through crowded paths and congested roads with ease. This also gives customers flexibility in choosing their preferred mode of transport based on accessibility and cost.

1.2   Problem Definition

In this paper, we present an efficient algorithm to route customer trips in a congestion-aware manner using a multi-class fleet of vehicles. The trip is divided into multiple legs in order to decrease the overall travel-time of the customer. Each leg of the trip is served by a different mode of transport depending on travel time and ease of the customer. The algorithm provides optimal transit points for each trip, i.e., till what point should a person walk/cycle and then take a car/public transport, in order to get the least travel time for the entire trip. All customer requests are routed into system-optimal paths in order to get the least travel time for the entire system. The optimal points are however user-centric and can therefore, act as a recommendation or alternate path.
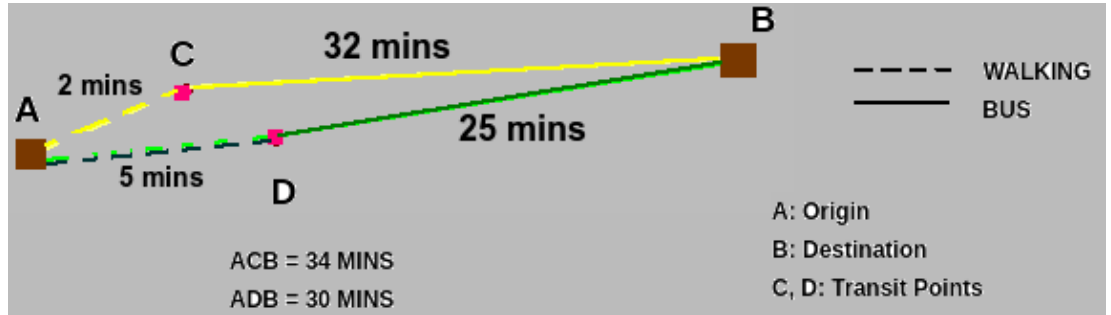

Figure 1: A multi-class combination of walking and bus, where D is the optimal transit point for minimum trip time.

2   Literature Review

1. In [11], car-pooling with 2-3 riders per vehicle was introduced in order to serve more customers with lesser vehicles on the road. [12] presented a more general model for real-time high-capacity ride-sharing that had rider-capacity of up to 10 simultaneous customers per vehicle. Their results showed that 98% of the taxi rides currently served by over 13,000 taxis (of capacity one) could be served with just 3,000 taxis (of capacity four). This can result in greater traffic throughput for increasing demand or lesser congestion for constant demand.

2. [17] tackled the problem of congestion-aware routing for a network consisting of Autonomous Mobility on Demand (AMoD) systems as they allow for system-wide coordination. It showed that intelligently routing and re-balancing each vehicle on capacitated roads did not increase congestion for small demand sizes. However, customer trips were considered event-based and routed greedily using an A* approach. This results in a Wardrop User equilibrium [18] which is considered sub-optimal. Moreover, the solutions could not be used for a real-time analysis [19].

3. [20] proposes congestion-aware route-planning policies for AMoD systems under mixed traffic conditions. Customer and re-balancing flows are routed in a system-centric fashion. However, for high levels of demand, pure AMoD travel can be detrimental due to the additional traffic stemming from its rebalancing flows. Private vehicles are routed in a user-centric way in order to adapt to the AMoD flows, which in turn, hampers systems to reach an optimal solution. By combining AMoD rides with moderate levels of walking, the overall system performance improved by 50%. However, there are no optimal transit points present to guide when to stop walking and start using an AMoD system. It also did not provide any route-recovery strategies for the flow solution.

4. In [16], multi-class fleets were introduced that serviced a request using a combination of heterogeneous vehicles (cars, buggies, scooter, walking). However, there was a constraint on the fleet size due to its cost. Different vehicles were assigned to each customer sequentially and with the objective of minimizing travel time for each mile. Due to this greedy approach, when the demand is much greater than the expected demand used to optimize the fleet size, the total average travel time for multi-class is worse than that of single-class.

5. Many works demonstrated new computationally efficient ways to replace the traditional process of the Traffic Assignment Problem (TAP). Frank Wolfe optimization [21] and Contraction Hierarchies [22] were used in [23] in order to achieve a system-optimal solution to the congestion-aware routing problem. There was a 20% improvement in computational time over the traditional TAP assignments. Even though the convergence rate of Frank Wolfe is known to be slow, its sub-steps could be easily made faster with parallel computing. In [24], shortest distances in a network are found using a hybrid algorithm that uses Euclidean distances as a comparative base line. The time complexity for this is $O(n^2)$. It's highly useful in cases of large cities where the total number of possible routes is huge.

6. in [20], various cost functions such as the Bureau of Public roads (BPR), 2-line approximation, 3-line approximation, and Davidson's heuristics were compared. In case of convex problems, BPR was an effective choice.

7. In [14], the network is optimally partitioned into re-balancing regions. Real-time demand estimate for every region is determined using incoming requests based on which idle vehicles are optimally assigned to these regions. There was a reduction in the average travel delay by 86%, the average waiting time by 37%, and the amount of ignored requests by 95% compared to [12] at the expense of an increased distance travelled by the fleet. The algorithm could not incorporate the existing public transportation infrastructure and congestion information of the network.

8. In [25], ride-sharing was explored in terms of how many vehicles were needed, where they should be initialized, and how they should be routed to service all the demand. There was a reduction in the fleet size by 69% and travel delay of 1.7 mins (for up to 2 customers per vehicle) and by 77% and 2.8 mins (for up to 4 passengers per vehicle). However, it's computationally expensive for online adaptation.

9. [13] computed future demands of passenger requests, based on historical data. The predictions improved the positioning of the vehicles towards satisfying future requests, reduced waiting and travel time. This lessened region-wise congestion by performing re-balancing of the network. However, seasonal changes was not taken into account while predicting future requests and the analysis was static in nature.

3 Proposed Methodology

3.1 Timeline

Timeline	Tasks
15 - 31 January	Study the previous work on ride-sharing, congestion-management, fleet sizing, assignment and re-balancing.
1 - 14 February	Build a road network from existing opensource GIS (e.g. open street maps)
15 - 29 February	Develop tools for querying APIs for public transport schedules and dynamic congestion flow information.
1 - 14 March	Integrate existing tools for graph queries and path planning algorithms.
15 March - 30 June	Develop novel algorithms for congestion-aware routing of multi-class fleet.

3.2 Method Overview

3.2.1 Phase 1

1. Setting up of Singapore city's road network (GIS) using the OpenStreetMap (OSM) database [26]. It consists of pedestrian paths, cycle-ways, and driveable roads, all interconnected via nodes.

2. Collection of Traffic Speed Band dataset using LTA Datamall [27], an API for retrieving static and dynamic network information of Singapore.

3.2.2 Phase 2

1. Integrate the traffic speed band dataset with our OSM GIS and calculate congestion information for the entire network, time-wise.

2. Propose an algorithm that finds optimal transit points for each mile (first, middle, last) for every customer request, such that the overall travel time for each customer is least.

3. Formulate a linear programming problem (LPP) that satisfies all origin-destination (OD) demands along with its capacity constraints, while minimizing travel time of the entire system.

3.2.3   Phase 3

1. Create a set of OD trip demands and run the proposed algorithm to find optimal transit points from the first to the middle mile, and from the middle to the last mile.

2. Solve the LPP using Frank-Wolfe algorithm to get system-optimal flows for all demands for the middle mile.

3. Decompose these flows into dedicated routes for each OD trip using an efficient shortest successive path algorithm [28].
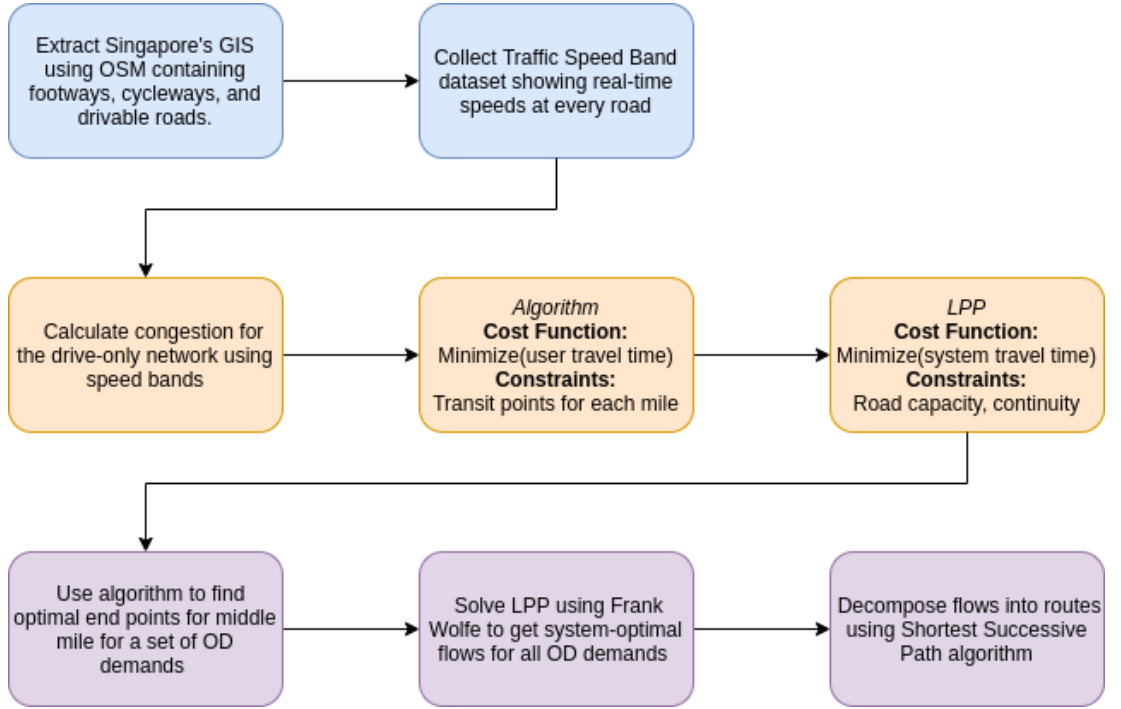

Figure 2: Project life cycle

4   Requirements

4.1   Data set

1. **Singapore's GIS:** Open Street Map (OSM) was used to extract Singapore's geographic information system (GIS) using the Overpass API.

   (a) The network is tagged with different types of roads or edges like pedestrian, cycle-ways, and drive-able routes. They constitute of corridors, cycle lanes, highways, service roads, etc.

   (b) The network is tagged with different types of nodes like bus stops, elevators, residential areas, parking lots, motorway junctions, etc.

   (c) Routing is possible from one node to another using a series of edges.

2. **Traffic Speed Band Data set:** It was collected from Land Transport Authority (LTA) Datamall owned by the Singapore Government.

   (a) It is a dynamic data set that updates itself every five minutes.

   (b) It shows speed bands (maximum and minimum observed speed) for every road link in Singapore giving real-time information about congestion on that link.

   (c) It was collected for two weeks including weekends, for time intervals of 09:00 A.M., 12:00 P.M., 03:00 P.M., 06:00 P.M., 09:00 P.M. .

4.2   Hardware and Software Requirements

1. A GPU with 12 GB RAM for fast computation .

2. **OSMnx 0.11.4:** Used to download, model, project, visualize, and analyze complex street networks from OpenStreetMap.

3. **NetworkX 2.4:** Used for path planning, routing and studying the structure and functions of Singapore's complex networks.

4. **Rtree 0.9.4:** Provided advanced spatial indexing features like Nearest neighbors search and Intersection search.

5. **Open Source Routing Machine(OSRM):** Its an open source router designed to compute the shortest path using contraction hierarchies or multi-level Dijkstra's.

6. **Python 3.6:** Interpreter language on top of which all these libraries would function.

5   Implementation

1. **Collect and combine data:** Extract Singapore's GIS using OpenStreetMap with the place name as *"Singapore, Central, Singapore"*. We get a drive-only network by specifying the network type as *"drive"*, and a pedestrian/cycle-way network by specifying the network type as *"walk"* or *"bike"*. Integrate the drive-only network with the traffic speed band data set for three slices of time: 12:00 A.M., 3:00 P.M., and 6:00 P.M. The entire Singapore network can be visualized as a densely-connected directed graph $G(V, E)$ with V vertices (nodes) and E edges.

Figure 3: Nodes (V)

Figure 4: Edges (E)

2. **Compute congestion:** Calculate congestion information for the entire drive-only network. It is calculated in terms of how much travel time is required to cross a road link in the network.

   (a) If vehicles present on a road link (u, v) are within the link capacity $c(u, v)$, they are assumed to be operating at free flow speed. Thus, the time taken for vehicles to cross a road link at free flow speed is called the free flow time $t(u, v)$. However, if vehicles present on a road link exceed the link capacity, congestion starts to set in. This lowers the the speed at which they are operating and hence, travel time to cross that link increases.

   (b) The travel time $t_d(u, v)$ along each edge is computed using a heuristic delay function that is related to the current volume of traffic on each edge. We use the Bureau of Public Roads (BPR) delay model [29], which computes the travel time on each edge (u, v) $\in$ edges (E) as:

   $$t_d(u, v) := t(u, v) \left(1 + \alpha \left(\frac{f(u, v)}{c(u, v)} \right)^{\beta} \right)$$

   where $f(u, v) := \sum_{m=1}^{M} f_m(u, v)$ is the total flow on edge (u, v), and α and β are usually set to 0.15 and 4 respectively.

3. **Compute middle mile transit nodes:** We now propose an efficient algorithm [1,2] that will be used to find optimal transit points for each mile (first, middle, last) for every customer request. Each customer request is composed of multiple legs(in this case, 3) served by different transportation modes (walking, cycle, taxi, public transport). The first and last miles can use only micro-mobility options like walking, cycling, or scooters. Whereas only private taxis or public transport can be used for the middle mile.

   For example, a customer will walk (for 250m) to a certain node in the graph for the first mile, after which they would alight a taxi (for 15 mins) till another node in the graph for the middle mile, and would cycle further (for 400m) until their destination for the last mile. These transit points would be selected such that the overall travel time for each customer is the least. Thus, every customer trip would be like:

   $$\mathbf{X} \longrightarrow \mathbf{A} \longrightarrow \mathbf{B} \longrightarrow \mathbf{Y}$$

   X: Origin of customer request, start node of the first mile
   A: End node of the first mile, start node of the middle mile

B: End node of the middle mile, start node of the last mile

Y: End node of the last mile, destination of customer request

X and **Y** are constant for every customer request. Therefore, we only need to compute **A** and **B**. In order to exercise maximum flexibility in choosing our combination of transit points while minimizing the travel times for every mile, we first route for the middle mile, i.e., $(\mathbf{A} \longrightarrow \mathbf{B})$ such that the overall travel time for each customer is least.
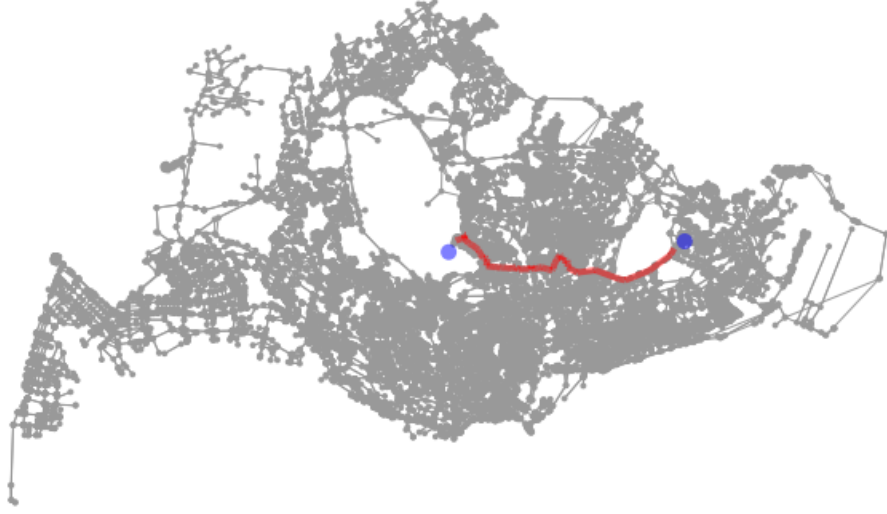

Figure 5: Routing shown for the middle mile (A —> B)

Algorithm 1: Find optimal transit nodes: A,B

Result: Demand set containing middle mile transit nodes

1: $Demand \leftarrow EmptyList()$;

2: $OD \leftarrow \{S, T\}$ {OD is set of all demands};

3: **for** $\{s, t\} \in OD$ **do**

4:     $CandidateSources \leftarrow$ `GetNearestNodes(s, 720m)`;

5:     $CandidateTargets \leftarrow$ `GetNearestNodes(t, 720m)`;

6:     $EuclideanDict \leftarrow$
        `SortLengthDict`$(CandidateSources, CandidateTargets)$;

7:     $AB \leftarrow$ `ModifiedHybridSearch`$(EuclideanDict)$;

8:     `Append` AB `to` $Demand$;

9: **end for**

10: $FirstMile \leftarrow$ `ShortestPath`(X, A);

11: $LastMile \leftarrow$ `ShortestPath`(B, Y);

12: **return** $Demand$

(a) To find an optimal starting **A** and ending node **B** for the middle mile, an assumption cum flexibility for the customer is made. According to it, all nodes within a 720 metre radius (euclidean distance) from the customer's starting and ending coordinates (**X**, **Y** respectively), are considered as potential sources and targets for the middle mile. This means that a customer is allowed to walk or cycle to/from their middle mile endpoints.

$$PotentialSources(X) = \{s_1, s_2, \ldots, s_n\}$$
$$PotentialTargets(Y) = \{t_1, t_2, \ldots, t_m\}$$

A total of $m * n$ combinations of {source, target} pairs are made. We choose that {source, target} pair as **A** and **B** which takes the least travelling time from *source* to *target*.

(b) We use a modified version of the hybrid algorithm [2] used in [24] to query through the set of {source, target} pairs. The algorithm uses a base distance with which it compares all other distances to find the shortest path, in order to save time on querying. We impose an extra cutoff on the shortest path search by using an extension of the Secretary problem [30], i.e., we stop the search for the shortest path after at most 37% of {source, target} pairs have been seen.

(c) We use euclidean lengths as base distances for comparison with real lengths. Since our parameter is travel time, we calculate the euclidean length between each {source, target} pair and divide it by the permissible average speed of vehicles in Singapore (50 km/hr).

(d) To calculate the real-time travel time of each {source, target} pair route, we use Contraction Hierarchies with edge weights/cost as the Bureau of Public Roads delay heuristic. This outputs a {source, target} pair with the least travel time between them, given real-time

congestion information.

Algorithm 2: Modified Hybrid Search

Data: Dictionary X with key:(A,B); value: Euclidean distance, sorted in increasing order of value

Result: Nodes (A,B) s.t. travel time between them is least

$Cutoff \leftarrow$ `Floor(n/e)`; // Only search till first 37% of entries

$Source \leftarrow$ First source of X ;

$Dest \leftarrow$ First destination of X ;

$minTime \leftarrow \infty$;

for $i \leftarrow 1$ *to Length(X)* **do**

    $travelTime \leftarrow$ `ContractionHierarchies(`$Source, Dest$`)`;

    if $i > Cutoff$ **then**

        if $travelTime < minTime$ **then**

            Return current (A,B) pair as its optimal;

        else

            Return (A,B) pair optimal till now;

        end

    else

        if $travelTime < minTime$ **then**

            Current (A,B) pair is optimal till now;

            if $i < N$ **then**

                if $travelTime < Euclidean\ distance\ of\ next\ pair$ **then**

                    Return current (A,B) pair as its optimal;

                else

                    Assign next pair as $Source, Dest$;

                end

            else

                Return current (A,B) pair as its optimal;

            end

        else

            if $i < N$ **then**

                if $minTime < Euclidean\ distance\ of\ next\ pair$ **then**

                    Return (A,B) pair optimal till now;

                else

                    Assign next pair as $Source, Dest$;

                end

            else

                Return (A,B) pair optimal till now;

            end

        end

    end

end

end

4. **Compute system-optimum flows for middle mile:** In order to convert this framework into a social model and satisfy all OD demands, we formulate a linear programming problem. The objective or cost function is to minimize the travel time of the entire network, given a set of customer requests M such that, $m \in M$, where $m := (start, target)$. The capacity of the roads is used as a constraint for the upper bound on number of vehicles that can be at an edge E at the same time. Hence, the LP problem formulates as:

$$
\text{minimize:} \quad \sum_{m \in M} \sum_{(u,v) \in E} t(u,v) f_m(u,v)
$$

$$
\text{subject to:} \quad \sum_{u \in V} f_m(u, s_m) + \lambda_m = \sum_{w \in V} f_m(s_m, w), \qquad \forall m \in M
$$

$$
\sum_{u \in V} f_m(u, t_m) = \lambda_m + \sum_{w \in V} f_m(t_m, w), \qquad \forall m \in M
$$

$$
\sum_{u \in V} f_m(u, v) = \sum_{w \in V} f_m(v, w), \qquad \forall m \in M, v \in V \backslash \{s_m, t_m\}
$$

$$
\sum_{m \in M} f_m(u, v) \leq c(u, v), \qquad \forall (u, v) \in E
$$

Constraints (2), (3) and (4) enforce continuity of each trip (i.e., flow conservation) across nodes. Finally, constraint (5) enforces the capacity constraint on each link.

Solving this LPP is NP-Hard. Hence we make use of a conditional gradient descent algorithm, Frank-Wolfe Optimization [31] using PyTrans. The OSM GIS is converted into *.tntp* [32] format. The solution of Frank-Wolfe optimization is feasible integral customer flows on congestion-free road links satisfying all demand. It is to note that these customer flows belong solely on the drivable network, since congestion is being monitored only for vehicles and public transport. These flows can be then decomposed into routes using a flow routing algorithm.

5. **Decompose system flows into path:** In order to decompose customer flows into dedicated routes:

   (a) The system-optimal flows act as the new capacity of the network. These capacities are used as an upper bound on the number of vehicles allowed on a road at once in the network.

   (b) All demand is added in a FIFO queue as per their time of arrival. Each customer is routed using a capacity-constrained weighted Dijkstra algorithm. [28] [3].

Algorithm 3: Capacity-bound weighted Dijkstra

Data: source, target

Result: System-optimal route for an OD trip

$paths \leftarrow$ {source: [source], target: emptyList()};

$Q \leftarrow$ Node Priority Queue;

for *each vertex v in Graph* **do**

   | $dist[v] \leftarrow \infty$;

end

$dist[source] \leftarrow 0$;

Q.add_with_priority($source, dist[source]$);

while *Q is not empty* **do**

   | $u \leftarrow$ Q.pop_min();

   | **for** *each neighbor v of u* **do**

   | | **if** *capacity(u, v) > 0* **then**

   | | | $dist\_vu \leftarrow$ weight(u, v);

   | | | $alt \leftarrow dist[u] + dist\_vu$;

   | | | **if** *alt < dist[v]* **then**

   | | | | $dist[v] \leftarrow alt$;

   | | | | Q.add_with_priority($v, dist[v]$);

   | | | | $paths[v] \leftarrow path[u] + [v]$

   | **end**

end

return $paths[target]$

---

6. **Compute first and last miles:** To compute the first and last mile routes, only pedestrian roads and cycle-ways are used for routing. The customer is expected to travel these routes by either walking, cycling, or using on-demand scooters (like Yulu). These distances are calculated keeping in mind that a customer may want to (i) walk for a maximum of 10 minutes or 720 metres (assuming walking speed as 1.2 m/s), or (ii) cycle for a maximum of 15 minutes or 2 Km (assuming cycling speed as 5.4 m/s).

  (a) For the first mile, the starting node is **X**. The customer is expected to reach from **X** $\longrightarrow$ **A** as part of their first mile journey. This route is calculated using weighted-Dijkstra using edge weights as length of the paths.

  (b) For the last mile, the starting node is **B**. A route from **B** to **Y** is calculated using weighted-Dijkstra using edge weights as length of the paths. The customer is expected to reach from **B** $\longrightarrow$ **Y** in order to finish their entire trip.

6   Results

All numerical experiments are done on 3 time slices keeping in mind the traffic patterns of Singapore: 12:00 A.M. (off-peak), 3:00 P.M. (moderately-peak), and 6:00 P.M. (high-peak). These experiments showcase the spatial as well as the temporal aspects of our proposed framework.

1. **Minimum distance path V.S. Minimum travel-time path:**

    A set of 1000 OD trips is taken. (i) The blue bars represent the time taken to travel on its shortest-distance path, and (ii) The orange bars represent the time taken to travel on the least congested path.
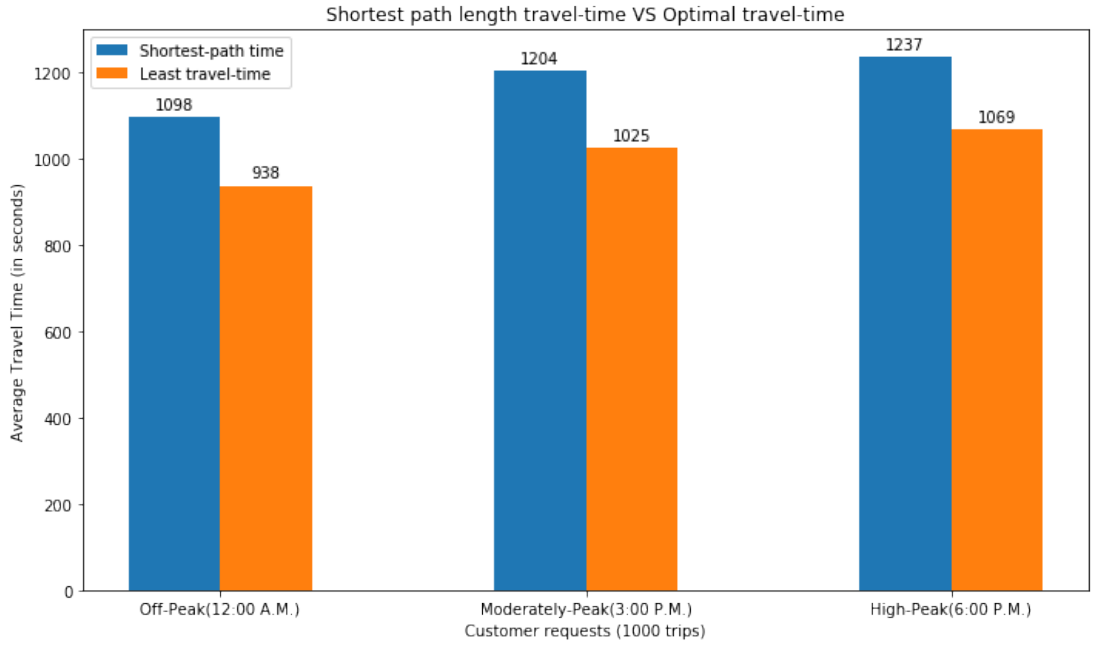
Figure 6

    The capacities of roads decrease with increasing peak times due to the increasing number of vehicles in the network. Hence, this results in increase in travel times for the same routes. Majority of customers inherently opt for the shortest-distance route because of lack of congestion information, thereby increasing their trip times drastically. The average increase in trip times by taking a shortest-distance path instead of the least congested path is 14.34%. Therefore, the shortest-distance paths don't always correspond to minimum travel-time paths.

$$\textbf{\% Average travel-time increase}$$
$$= \textbf{14.57} + \textbf{14.87} + \textbf{13.58}$$
$$= \textbf{14.37\%}$$

2. **Modified Hybrid Search V.S. Hybrid search V.S. Exhaustive search:**

Given a set of OD pairs of size N, such that,

$$OD = \{(s_1, t_1), (s_2, t_2), \ldots, (s_n, t_n)\}$$

we seek to find an origin-destination pair (s, t) such that the travel-time between them is minimum. A set of 100 customer trips is taken and 3 different search methodologies are compared in terms of accuracy and performance.

(i) Exhaustive Search looks at the travel times of every $(s_i, t_i) \in OD$. (ii) Hybrid Search uses euclidean distances as a base comparison for different (s_i, t_i). (iii) Modified Hybrid Search extends on the concept of Hybrid Search but adds a depth cutoff on its search strategy. This cutoff is taken to be as (N/e) [30], thereby always having an optimal win probability of at least 37%.
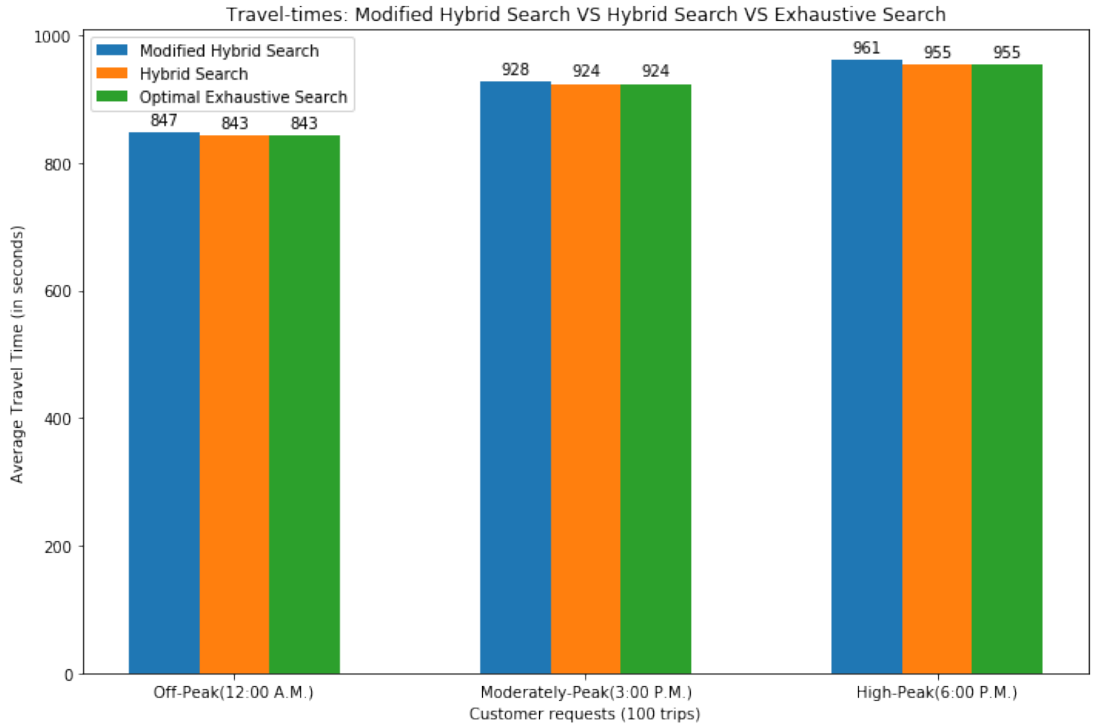
(a) **Travel-time deviations:**

Figure 7

It shows that Exhaustive Search and Hybrid Search both output an OD pair having minimum travel time. Hence, both of these searches are optimal. However, Modified Hybrid Search doesn't always output an optimal OD pair. The average deviation in travel times between the 3 searches is 4.67 seconds.

16

Average travel-time deviation (in secs)
$$= (4 + 4 + 6)/3$$
$$= 4.67 \text{ seconds}$$

(b) **Number of queries:**

We tabulate the number of queries required to give an output by each of the 3 search strategies.
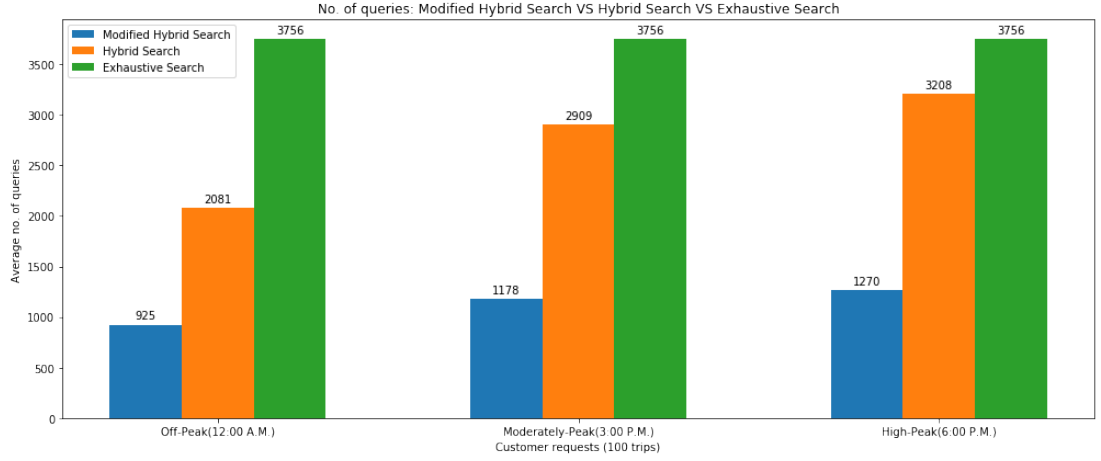

Figure 8

i. Exhaustive search iterates through every $(s_i, t_i) \in OD$, thereby finding a solution in $O(N)$.

ii. Hybrid search stops its iterations if the current (s_i, t_i) pair's distance is lesser than its next base distance, or if it has reached the end of the set. Hence, sometimes it takes $< N$ iterations to find a solution. Thus, its worst-case time complexity is also $O(N)$.

% queries saved (Hybrid, Exhaustive)
$$= 44.6 + 22.55 + 14.59$$
$$= 22.25\%$$

iii. Modified Hybrid search stops its iterations if the current (s_i, t_i) pair's distance is lesser than its next base distance, or if it has reached the depth cutoff. Hence, sometimes it takes $< (N/e)$ iterations to find a solution. Thus, its worst-case time complexity is $O(N/e)$.

% queries saved (Modified Hybrid, Exhaustive)
$$= 75.37 + 68.64 + 66.19$$
$$= 70.07\%$$

Hence, it shows that Modified Hybrid Search outperforms the traditional

17

Exhaustive Search and Hybrid Search, and is highly efficient with negligible average delay for this use case.

3. **Multi-Class V.S. Single-Class Fleet:**

A set of 500 OD trips is taken. All of these are routed either using a single class of vehicle (e.g. only taxi), or a combination of walking and taxi (multi-class). We try to see the effect of incorporating micro-mobility options in one's journey for reasonable distances (maximum 1 KM) with respect to the overall system cost.
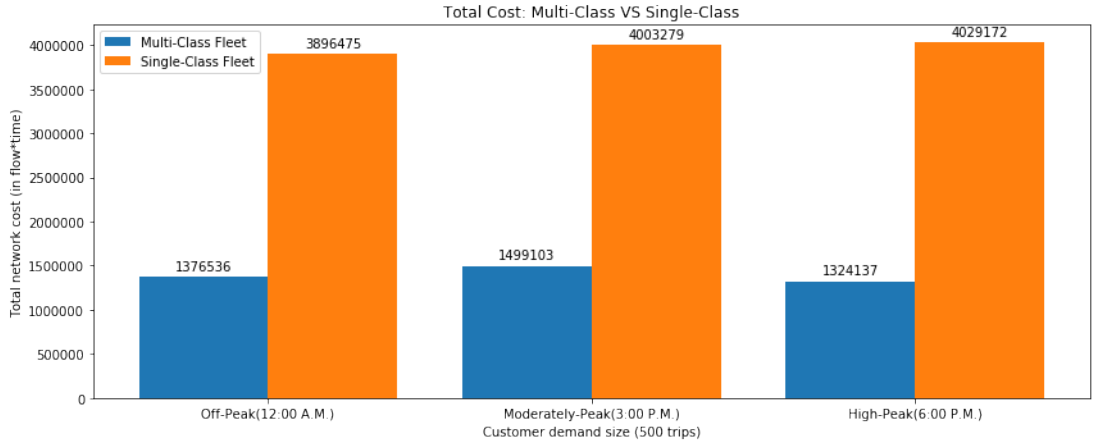

Figure 9

We see that the average reduction in the overall system cost by using a multi-class fleet of vehicles over just a single vehicle is 64.79%. This shows a drastic potential decrease in congestion in the entire network by pedestrianizing a very small % of the entire trip (in this case up to 1KM).

$$\textbf{\% Average Cost Reduction}$$
$$= \textbf{64.67} + \textbf{62.55} + \textbf{67.14}$$
$$= \textbf{64.79\%}$$

4. **System Equilibrium Flows V.S. User Equilibrium Flows:**

To evaluate congestion, we take a demand set of 1000 OD trips. All demands originate and end in Downtown Singapore, which is the busiest region of the city for majority of the day. After decomposing the system optimal flows into routes using capacity-constrained Dijkstra, we record if all demands are satisfied or not. Since, all the decomposed routes follow system-optimal flow constraints, they are bound to be within capacity. This means they all travel in a congestion-free network.

(a) **Total Network Cost:**

All demands are fed into the Frank-Wolfe algorithm to find flows that correspond to either system equilibrium or user equilibrium. Current frameworks opt for user equilibrium flows as it tends to compute shortest routes greedily. However, this does not adhere to a social framework as it does not take into account the flows originating from other customer demands. Whereas, a system equilibrium keeps in mind the current congestion information, and future possible congestion from current customer demands. We seek to see the effect of these equilibriums on the overall cost of the network.
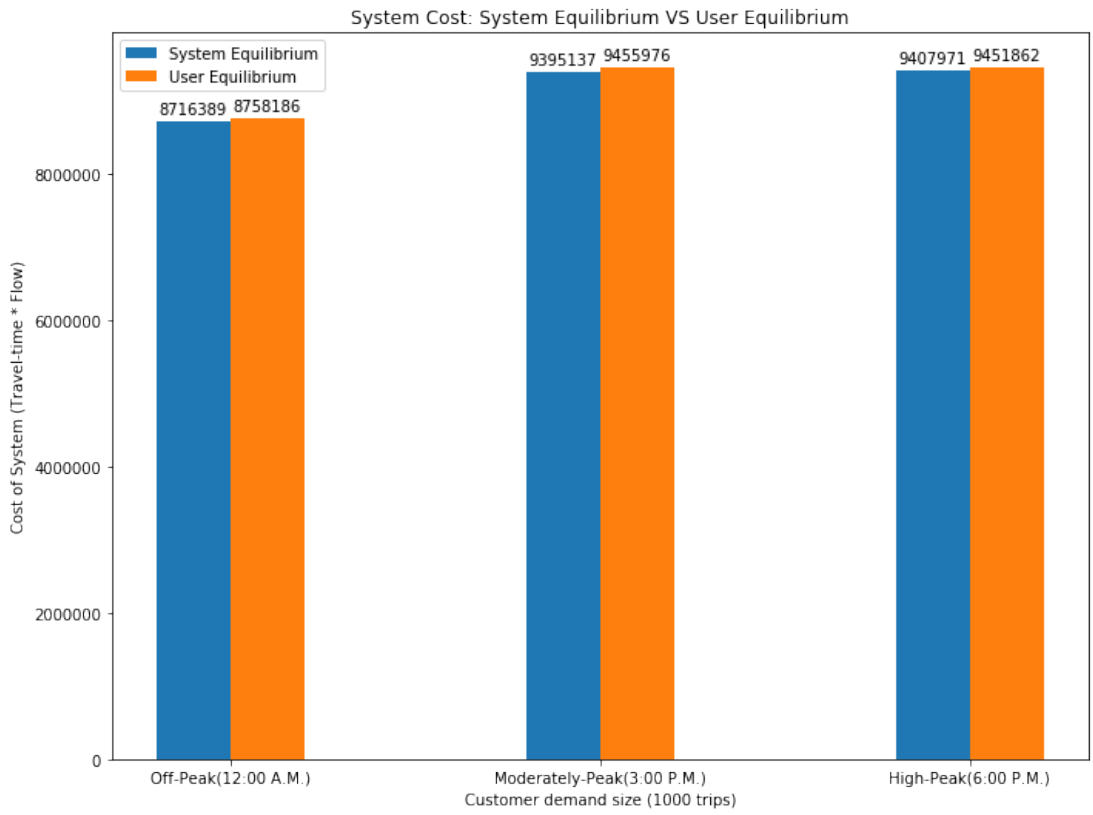

Figure 10

The average reduction in the cost for the entire network is 0.53%, i.e., system-optimal flows could have accommodated 4887 more vehicles. Hence, system equilibrium flows are optimal and user equilibrium flows are sub-optimal.

$$\textbf{\% Average Cost Reduction}$$
$$= \textbf{0.48} + \textbf{0.64} + \textbf{0.46}$$
$$= \textbf{0.53\%}$$

19

(b) **Waiting Queue Size:**

We seek to evaluate the congestion by assigning routes to all 1000 customers using different flow equilibrium(s). After decomposing the flows into routes for every demand, network capacities were reached early, thereby leaving some user demands as infeasible. Hence, these trips are added to a waiting queue and would be served in the next batch-process.
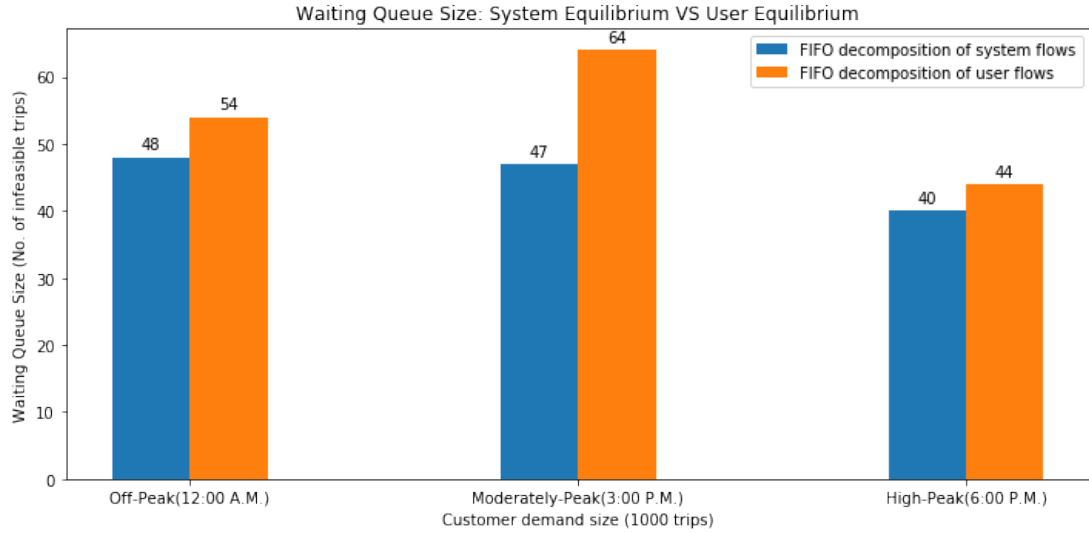

Figure 11

Since all routes follow capacity bounds, all feasible demands correspond to congestion-free demands. Hence, there is 0% congestion at all times in the network. The figure shows that there are greater infeasible trips for user equilibrium flows than system equilibrium. This means that network capacities are reached faster in user equilibrium, thereby resulting in higher travel times for a larger fraction of user demands.

% Average Waiting Queue Size Reduction
$$= 11.11 + 26.56 + 9.09$$
$$= 15.59\%$$

This shows that traffic assignment should follow a System-Equilibrium as its optimal.

7   Conclusion and Future Scope

We have successfully built a social framework that performs traffic assignment in a congestion free manner and does customer-routing using a multi-class fleet of vehicles. The framework is computationally efficient than the current state-of-the-art.

It can be adapted to an Autonomous Mobility-on-Demand (AMoD) system. Machine Learning techniques can be used to predict travel times based on historic congestion data in the future.

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