

(forward converter)

HW #4

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Q1) i. When S is ON, $V_L = V_d \cdot \frac{N_2}{N_1} - V_o$

When S is OFF, $V_L = -V_o$

$$\Rightarrow \left(N_2 \cdot \frac{N_1}{N_1} - V_o \right) D - V_o (1-D) = 0 \Rightarrow V_o = \frac{N_1}{N_1} D V_d \quad \text{for } i_L > 0$$

$$\text{so, } \frac{V_o}{V_d} = \frac{1}{5} \times \frac{N_2}{N_1} \cdot D \quad \frac{N_1}{N_2} \cdot \frac{1}{D} = 25 \Rightarrow \text{choose}$$

$$\boxed{\begin{aligned} D &= 0.2 \\ N_1 &= 5 \\ N_2 &= 1 \end{aligned}}$$

ii. $I_o = \frac{V_o}{R_L} \geq I_{OB} \Rightarrow R_L = R_{L\max}$

$$i_{avg} = I_o + \frac{i_{peak}}{2} = \frac{\left(\frac{V_o}{R_L} D V_d - V_o \right)}{L}, \quad D T_p = i_{peak} = 3.84 A$$

$$i_{avg} = 1.92 A \Rightarrow R_{L\max} = \frac{12}{1.92} = \boxed{6.25 \Omega}$$

iii. $(D + \Delta m) T_S = 36 \mu s$ wanted. D is chosen as 0.2, so $\Delta m T_S = 28 \mu s$.

$$\boxed{\Delta m = 0.7} \Rightarrow D = \frac{N_1}{N_2}, \quad \Delta m \Rightarrow N_2 = \frac{N_1}{D}, \quad \Delta m = \frac{25}{2} = \boxed{17.5 \text{ turns}}$$

iv. $i_{avg} = \frac{V_o}{R_L}$ choose $R_L = 10 \Omega$

$$V_o = \frac{N_2}{N_1} \cdot V_d ; \quad \sqrt{\frac{2}{1 + \frac{E \cdot L}{R_L \cdot T_S}}} = \boxed{16.8 V}$$

(push-pull converter)

$$Q2) \left(\frac{N_2}{N_1} V_d - V_o \right) D T_S - V_o \left(\frac{T_S}{2} - D T_S \right) = 0$$

$$\hookrightarrow \frac{V_o}{V_d} = 2D \cdot \frac{N_2}{N_1} \Rightarrow \frac{18}{200} = 2 \cdot \frac{N_2}{N_1} \cdot D$$

$N_2 = 9$
$N_1 = 20$
$D = 0.1$

iii. $I_{oB} = \frac{V_o (1-D) T_S}{2L}$ $\Rightarrow \frac{1}{2}$ multiplier due to 4 states ($\frac{T_S}{2}$).

$$\frac{V_o}{I_{oB}} = R_{MAX} \Rightarrow I_{oB} = 3.24 A \Rightarrow R_{MAX} = 5.55 \Omega$$

