

Fig. 1: Circuit Schematic

Questions:

- a) To find the maximum value of the load resistor, continuous mode will be considered with the boundary case where $i_L(0)=0$. The equation is given below.

$$I_o = \frac{V_o}{R} \geq I_{OB}$$

$$I_{OB} = \frac{T_s V_d}{2L} \times (D - D^2) = 0.208A$$

$$I_o = \frac{5.5}{R} \geq 0.208 \rightarrow R \leq 26.45\Omega$$

To find the minimum value of the load resistance where $i_{Lpeak} \leq 1.5A$, I used the following equation.

$$I_{OB} = \frac{i_{Lpeak}}{2} = 0.75A$$

$$I_o = \frac{5.5}{R} = 0.75 \rightarrow R = 7.3\Omega$$

- b) The load resistances in the range $7.3\Omega < R_{L1} < 26.45\Omega$ are 8.2Ω , 10Ω , and 15Ω . I choose 10Ω as the load resistance. Because $I_o \geq I_{OB}$, continuous mode is considered. Duty cycle can be calculated by the equation below.

$$D = \frac{V_o}{V_d} = 0.458$$

- c) To estimate the diode current, I need to find the i_{Lpeak} value.

$$i_L(0) = \frac{V_o}{R} - 0.5 * \frac{V_d - V_o}{L} * t_{ON} = 0.326A$$

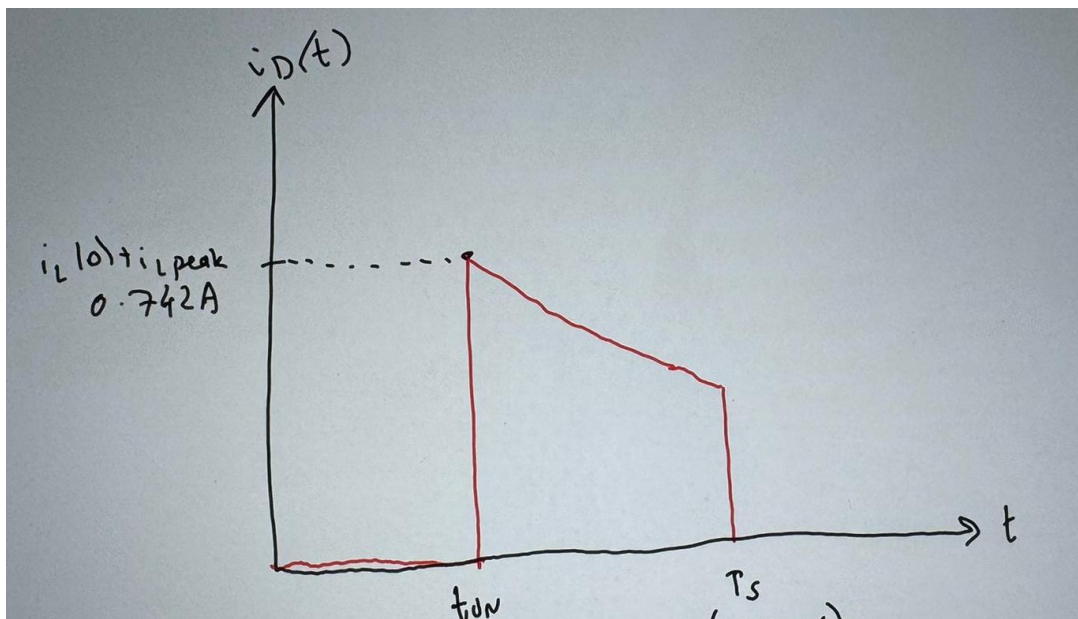


Fig. 2: Estimated diode current with $R_L=10$

$$\Delta i_L = \frac{V_d - V_o}{L} = 0.416A$$

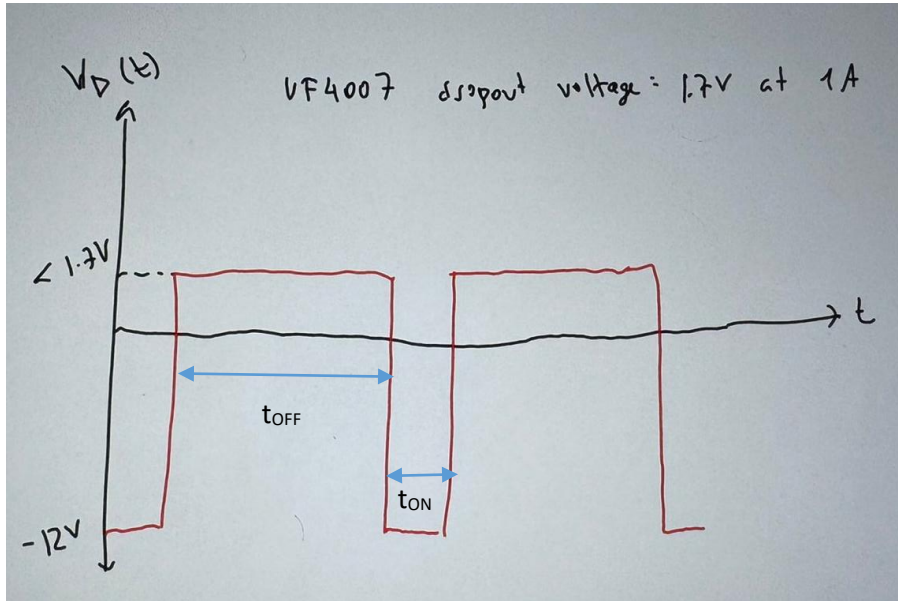


Fig. 3: Estimated Diode voltage with $R_L=10$

To show the diode voltage, t_{ON} time period is shown too short, however t_{ON} is greater than t_{OFF} normally.

- d) When a single $100\mu F$ capacitor with $ESR=0.25\Omega$ used, output ripple is measured around $0.052V$. To lower the output ripple, two $100\mu F$ capacitors are connected in series to lower the equivalent ESR value. Because ESR is the dominant mechanism for the output ripple, following equation will be used.

$$\Delta i_L = i_{Lpeak} - i_L(0) = 0.416A$$

$$\Delta V_{ESR} = \Delta i_L * R_{ESR} = 0.052V$$

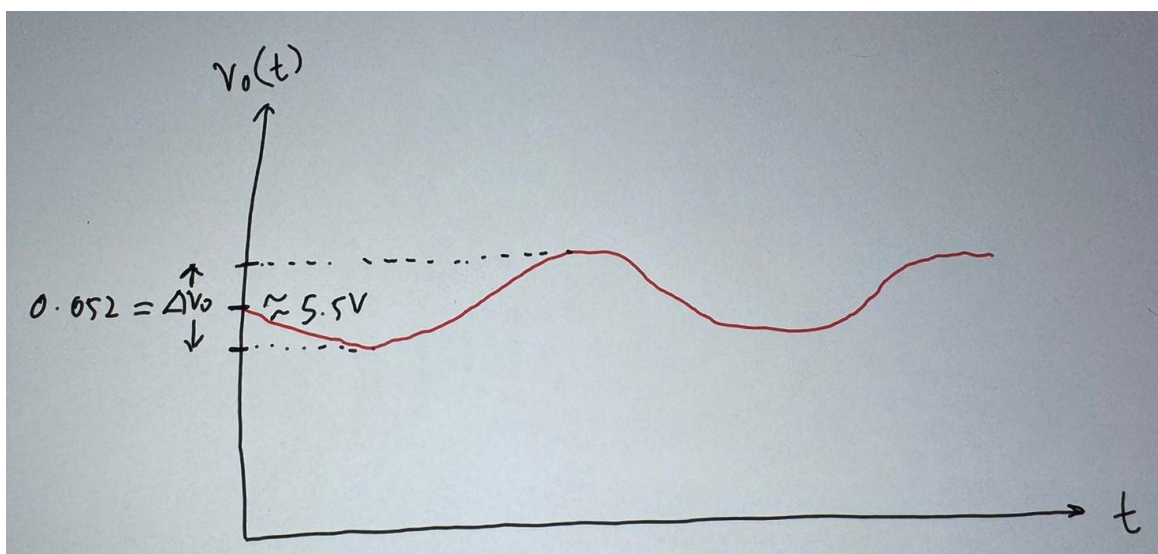


Fig. 4: Estimated output ripple voltage (positive valued)

- e) R_{\max} value calculated as 26.45Ω . R_{L2} value is choosed as 47Ω . As a result, because the output current will be less than I_{OB} , discontinuous mode is going to be considered.

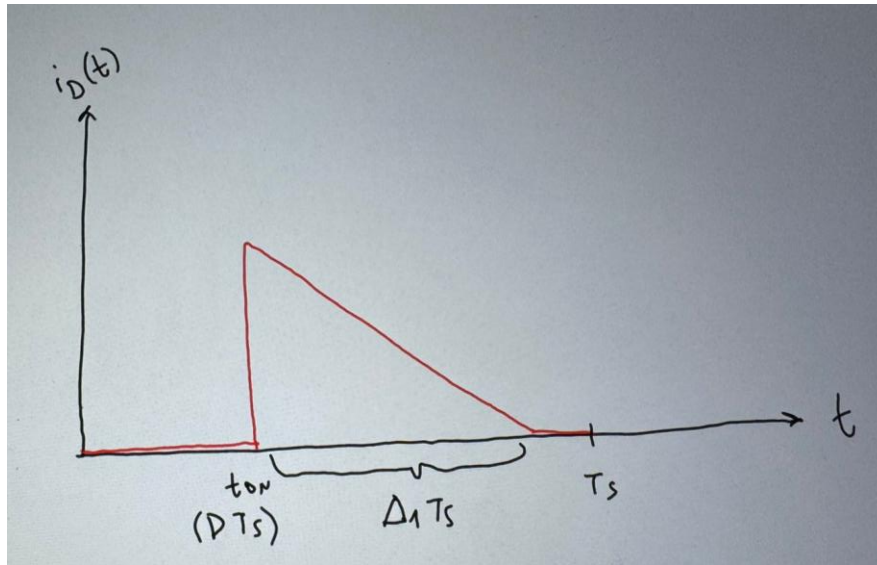


Fig. 5: Estimated diode current with $R_L=47$

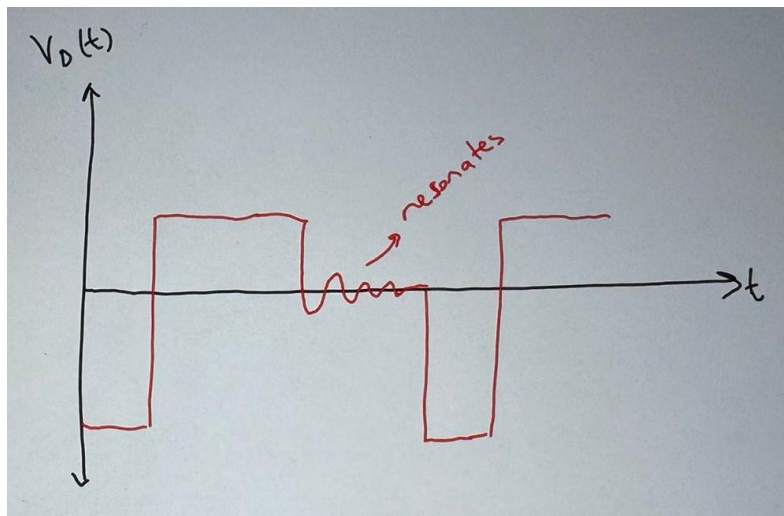


Fig. 6: Estimated diode voltage with $R_L=47$

- f) Initially, duty cycle value is 0.458, which gives the output voltage as -7.1V. To make this output voltage value -5.5V, a change in duty cycle has to be made. The equation for the duty cycle calculation is given below.

$$D = \frac{V_o}{V_d} * \sqrt{\frac{I_o}{I_{OBmax} * \left(1 - \frac{V_o}{V_d}\right)}} = 0.388$$

$$I_{OBmax} = \frac{T_s * V_0}{2 * L} = 0.3A$$

- g) Duty cycle is measured from the inductor current. Figure below shows the inductor current waveform and t_{ON} value.

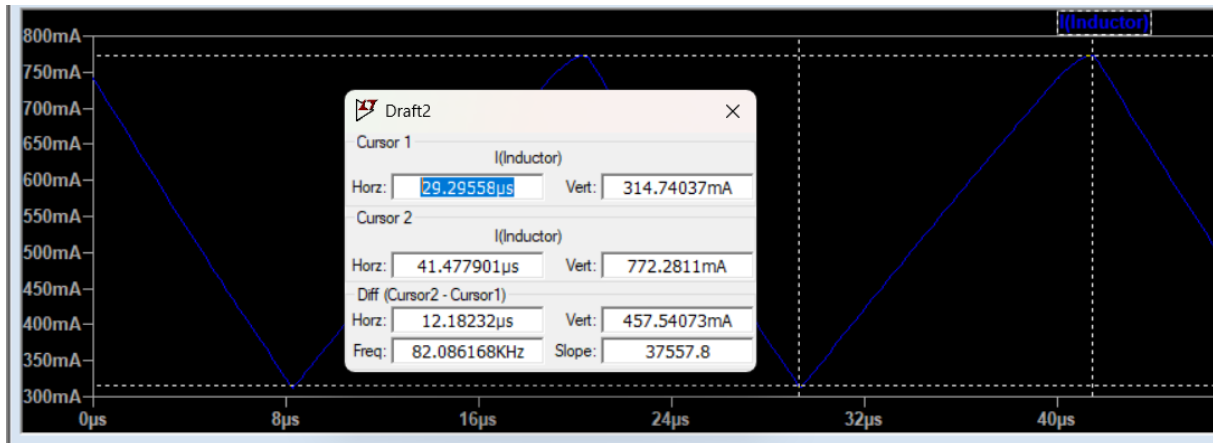


Fig. 7: t_{ON} value from the inductor current waveform

T_s value is 21.4μs. Corresponding duty cycle $D=0.57$. Value found at b) is 0.458. As expected, duty cycle in the simulation is greater than the calculated value because of the voltage drops across the diode and resistors.

h) Figures below shows the diode current $i_D(t)$ and diode voltage $v_x(t)$ respectively.

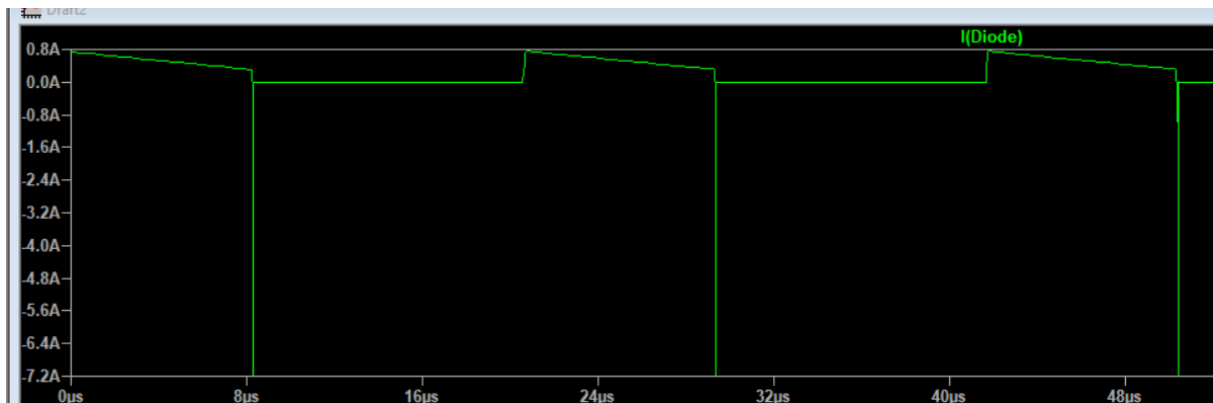


Fig. 8: Diode current waveform

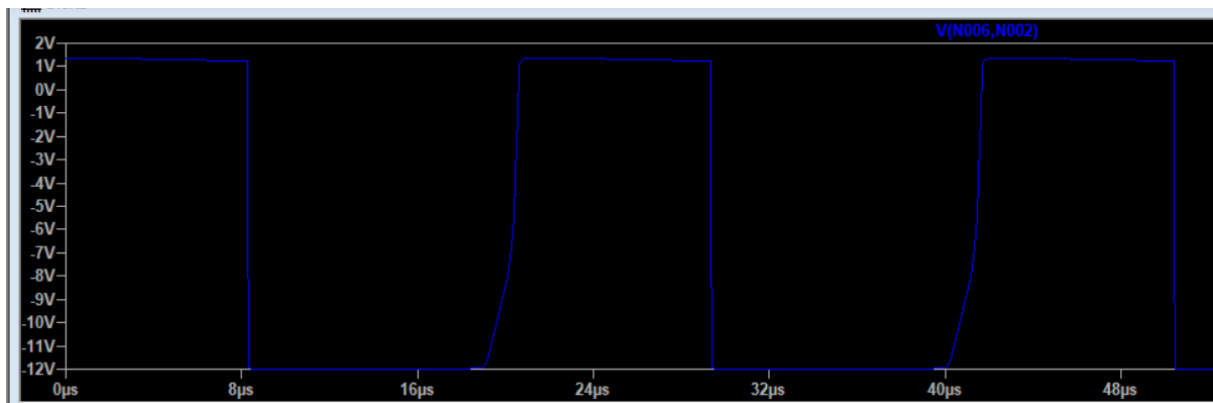


Fig. 9: Diode voltage waveform

i) The output voltage waveform is given below. The pk-to-pk ripple is measured as 56mV. The average value of the output voltage is -5.49V. V_o value is calculated as -5.5V at the beginning.

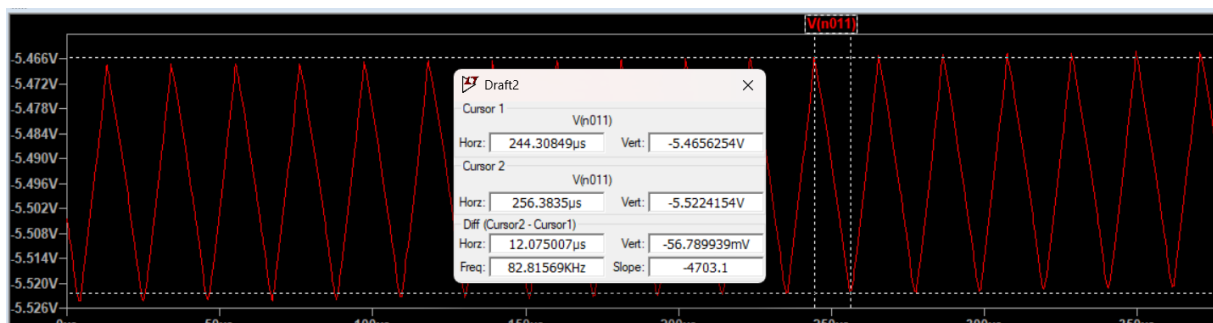


Fig. 10: Output voltage in PSS and p-p ripple value

j) To find the converter's efficiency, following equations are going to be used.

$$P_{in} = V_d * I_d = 4.21W$$

$$P_{out} = \frac{V_o^2}{R_L} = 3.02W$$

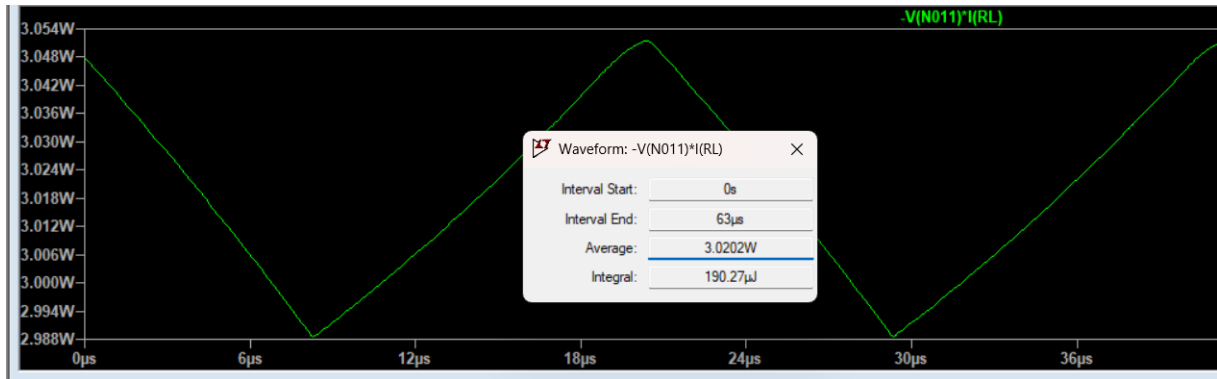


Fig. 11: Input power

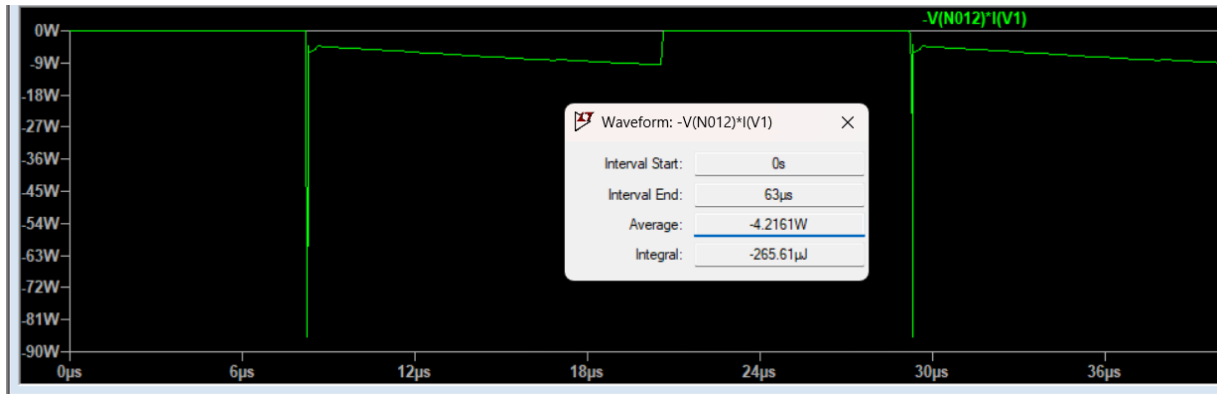


Fig. 12: Output power

$$\eta = \frac{P_{out}}{P_{in}} = 72\%$$

The efficiency of the system is calculated as 72%.

k) In part f), duty cycle is calculated as 0.388. Therefore a value near to this is going to be obtained in the simulation and the output voltage will be checked. Fig. 13 shows the T_S value of the circuit and Fig. 14 shows the t_{ON} value with $R_L=47\Omega$. To get a value close to $D=0.388$, R_A value is set to $9K\Omega$ and R_B value is set to $1K\Omega$.

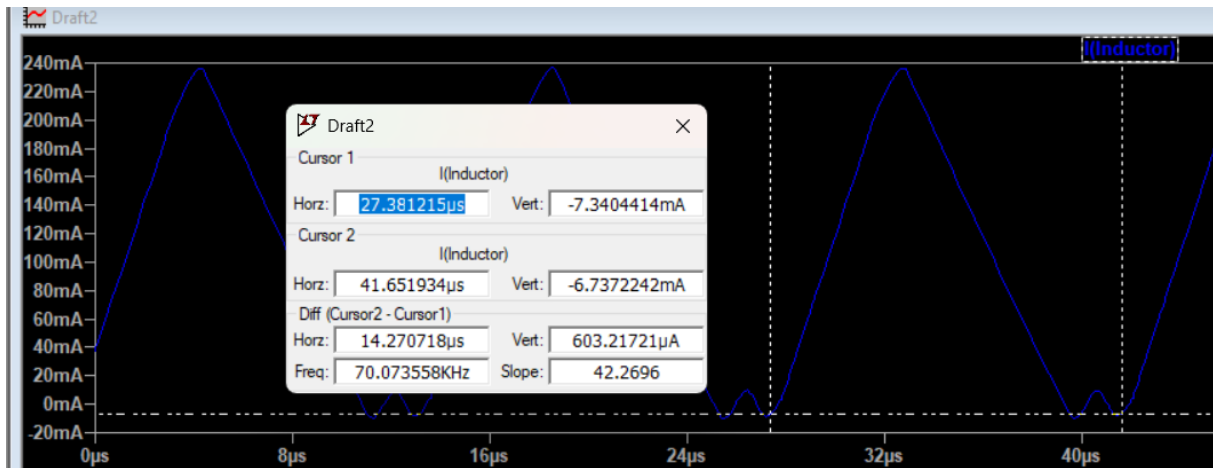


Fig. 14: T_s value with $R_L=47\Omega$

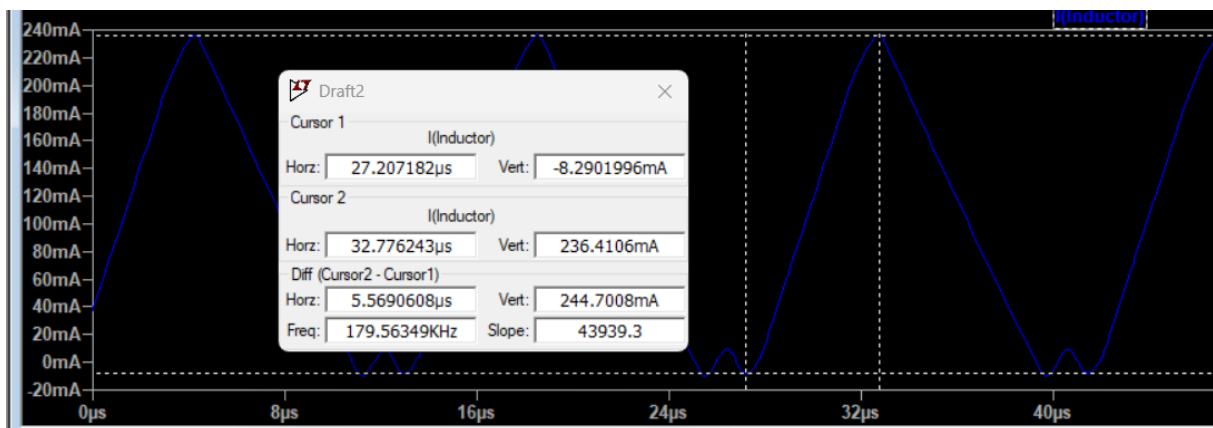


Fig. 13: t_{ON} value with $R_L=47\Omega$

Corresponding duty cycle value is calculated as 0.389. The duty cycle value in part f) is 0.388. Fig. 15 shows the output voltage waveform. The output voltage is around -4.12V.

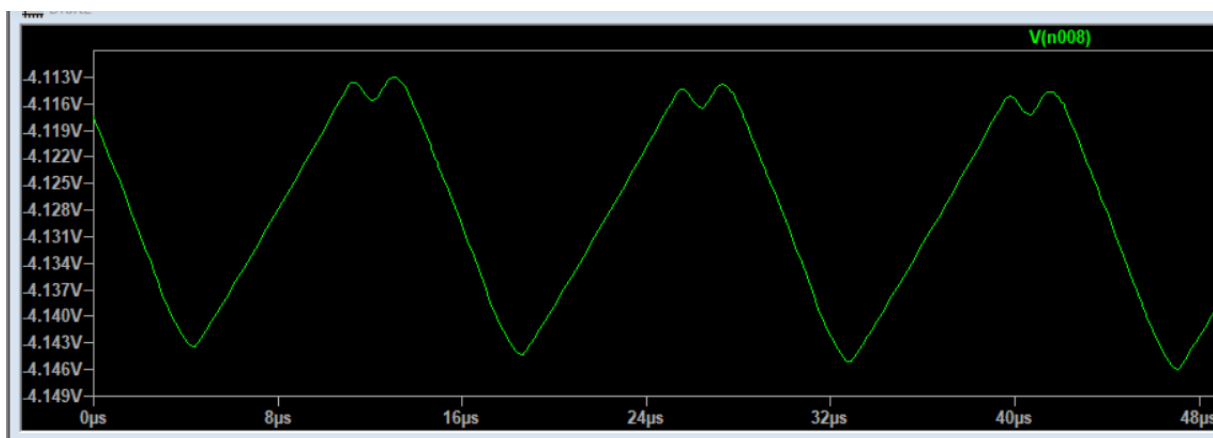


Fig. 15: Output voltage with $D=0.389$ and $R_L=47\Omega$

- l) In order to get the previous voltage at the output which is 5.5V, some adjustments need to be done. Currently, with $R_L=47\Omega$, $V_o=7.1V$. To reduce this value to 5.5V, I swapped the R_A and R_B values. As a result, both T_s and duty cycle values are changed. New T_s value is $16.36\mu s$ (Fig. 16) and duty cycle value measured $D=0.462$ ($t_{ON}=7.54\mu s$) (Fig. 17). The value found at f) for duty cycle is 0.388, and here is 0.462. It is seen that due to voltage drops across diode and resistors, duty cycle has increased. Output voltage can be observed from Fig. 17, which is measured as around -5.5V.

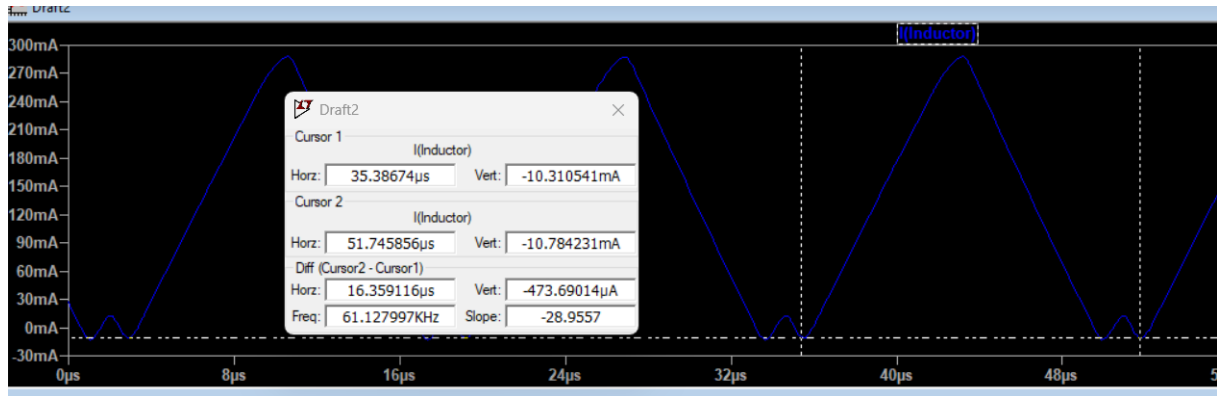


Fig. 16: New T_s value with $R_L=47$

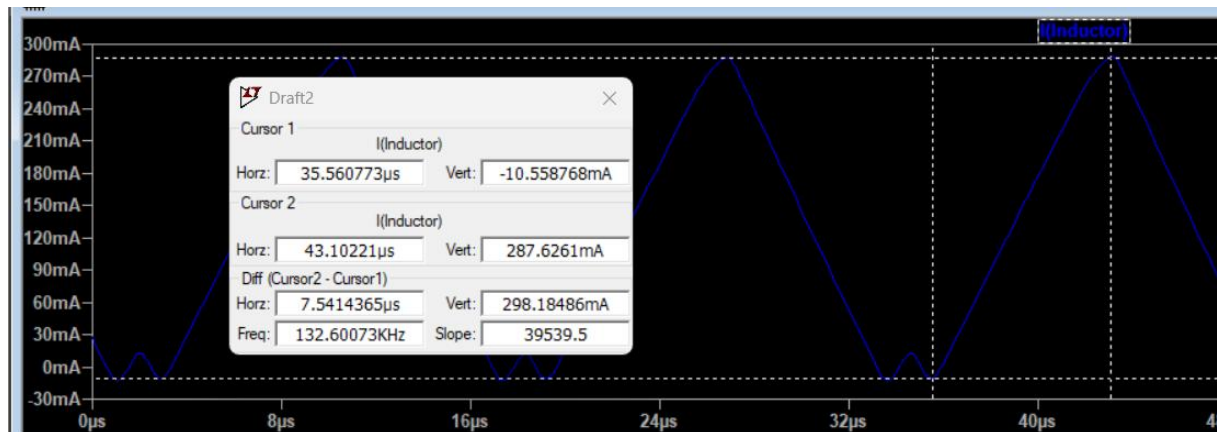


Fig. 18: t_{ON} value with $R_L=47$

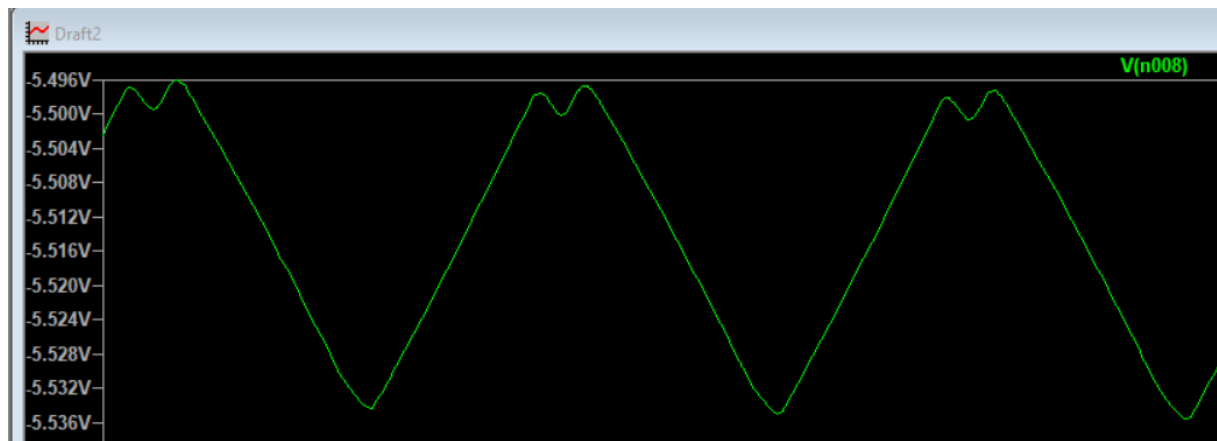


Fig. 17: Output voltage with $R_L=47\Omega$