

```
(*                      CSS221 Computer Graphics with Applications
                        Lab 1
                        Introduction into Mathematica
*)
```

```
SetOptions[EvaluationNotebook[], ShowCellLabel → False]
```

```
SetOptions[{Plot, Plot3D, ContourPlot, DensityPlot, ParametricPlot,
  ParametricPlot3D, ListPlot, ListLinePlot}, ImageSize → Small];
```

```
(* Comments are in (**) In order to see the output run
  the Mathematica Notebook: Evaluation Evaluate Cells (OR) press
  Shift Enter In order to evaluate the entire notebook run Evaluation→
  Evaluate Notebook. To start a new cell press down arrow and press
  Enter. To evaluate the cell press Shift+Enter.
*)
```

```
(* Note. Sometimes there are too many mistakes in the Lab solution. IN this
  case save your work. Quit Mathematica. Load your file again and run it *)
```

```
(* Basics of Mathematical Calculations *)
```

```
(* Problem(1) Define a variable x equal to 3 and y equal to 2. Find x+y,
  x^2+y^2, x*y, x/y. Type every line in a different cell *)
```

```
x = 3 (* press shift +enter to run the cell *)
```

```
3
```

```
y = 2
```

```
2
```

```
x + y
```

```
5
```

```
13
```

```
6
```

```
3
```

```
2
```

```
(* Problem(2) First letters of the built in
functions are capitalized. Use[] around the arguments Find
Sqrt[5],Sqrt[5.],Exp[3.],Sin[Pi/3],
ArcTan[Sqrt[3]] Assign these numerical values to variables.
Type them in different cells *)
```

```
xs1 = Sqrt[5]
```

$$\sqrt{5}$$

```
xs2 = Sqrt[5.]
```

```
2.23607
```

```
xe1 = Exp[3.]
```

```
20.0855
```

```
xs3 = Sin[Pi/3]
```

$$\frac{\sqrt{3}}{2}$$

```
xa1 = ArcTan[Sqrt[3]]
```

$$\frac{\pi}{3}$$

```
(* Find xs1+xs2+xe1+xs3+xa1 *)
```

```
26.4709
```

```
(* Functions. 2D plots *)
```

```
(* Problem(3) Define f[x_]:=
x^2+0.8 Note the underscore x_ denotes the argument. Call f[x] with x=3,
x=Pi.x=(1+t) and x=Sin[t*Pi]. Find f[f[4.5]] *)
```

```
f[x_] := x^2 + 0.8
```

```
f[3]
```

```
9.8
```

```
f[Pi]
```

```
10.6696
```

```
f[1 + t]
```

```
0.8 + (1 + t)^2
```

```
f[Sin[t * Pi]]
```

```
0.8 + Sin[ $\pi$  t]^2
```

```
f[f[4.5]]
```

```
443.903
```

```
(* Problem(4) Define a function given by f[a_]:=
Sin[a^2]+ Cos[a] and call with a=1 , a=1. and a=1.*Pi *)
```

```
Cos[1] + Sin[1]
```

```
1.38177
```

```
-1.4303
```

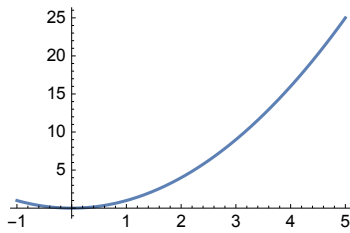
```
(* Problem(5) A function with more than one argument. Define the Function,
f5[u_,v_]:= u/v
Call f5[21, 5] *)
```

```
4.2
```

```
(* Problem(6) Plot f6[a_]:=a^2 as Plot[ function,{x,xmin,xmax}, Options] ,
the argument x ranges from xmin to xmax. *)
```

```
f6[a_] := a^2
```

```
Plot[f6[a], {a, -1, 5}]
```

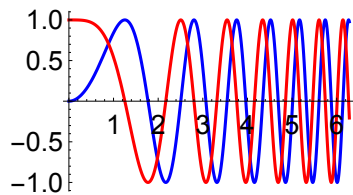
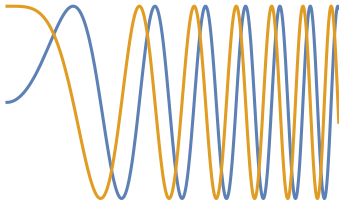


(* Problem (6)

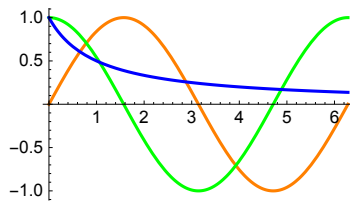
Plotting several functions. 1) Plot the function $\text{Sin}[x^2]$ and $\text{Cos}[x^2]$ with the range $\{0, 2\pi\}$, and with $\text{Axes} \rightarrow \text{False}$. 2) Use Options $\text{Axes} \rightarrow \text{True}$, use $\text{PlotStyle} \rightarrow \{\text{Blue}, \text{Red}\}$ $\text{BaseStyle} \rightarrow \{\text{FontSize} \rightarrow 14\}$ and observe the difference *)

```
f82[x_] := Cos[x^2]
```

```
Plot[{f81[x], f82[x]}, {x, 0, 2 Pi}, Axes -> False]
```



(* Problem (7) Plot three functions: $\text{Sin}[x]$, $\text{Cos}[x]$, $1/(x+1)$ on interval $\{x, 0, 2\pi\}$ using $\{\text{Orange}, \text{Green}, \text{Blue}\}$ *)



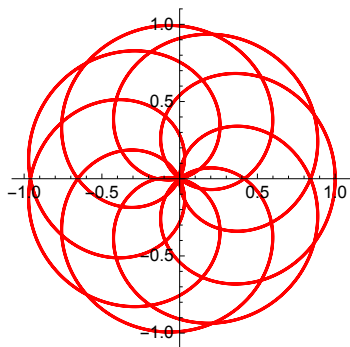
(* Problem(8) Plot a parametric function using the ParametricPlot *)
 (* Parametric function is specified
 by a pair $\{x(t), y(t)\}$ of a parametric variable t .
 Define $x[t_]:=Cos[7t]Cos[11t]$, $y[t_]:=Cos[7t]Sin[11t]$, t ranges from 0 to 2π ,
 Use AspectRatio→1. It specifies the ratio of height to width for a plot. *)

```
x10[t_] := Cos[7 t] Cos[11 t]
```

```
y10[t_] := Cos[7 t] Sin[11 t]
```

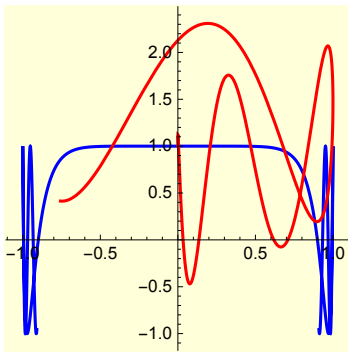
```
p10[t_] := {x10[t], y10[t]}
```

```
ParametricPlot[p10[t], {t, 0, 2 Pi}, PlotStyle -> Red, AspectRatio -> 1]
```



(* Problem(9) Plot the following two parametric functions
 $x_{111}[t]:=Sin[t]$; $y_{111}[t]:=Cos[t^4]$ and $x_{112}[t]:=Sin[t^2]$;
 $y_{112}[t]:=Cos[11*t]+Sqrt[t]$ on one graph, $\{t, -2, 2\}$, use PlotStyle→ {Blue, Red}
 Background→LightYellow AspectRatio→1 *)



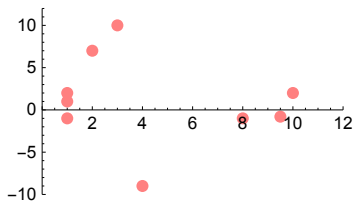


(*2D Plotting lists *)

(* Problem(10) ListPlot is designed for plotting a discrete data. The list is composed of the x and y coordinates. The size and color of the points are controlled by the PlotStyle Options. Practice with the following list *)

```
G = {{1, 1}, {1, 2}, {1, -1}, {2, 7}, {3, 10}, {4, -9}, {8, -1}, {9.5, -0.8}, {10, 2}}
{{1, 1}, {1, 2}, {1, -1}, {2, 7}, {3, 10}, {4, -9}, {8, -1}, {9.5, -0.8}, {10, 2}}
```

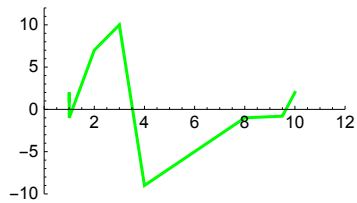
```
Plot1 = ListPlot[G, PlotStyle -> {PointSize[0.04], Pink}, PlotRange -> {{0, 12}, {-10, 12}}]
```



(* Note that the above plot has been now associated with the variable Plot1 *)

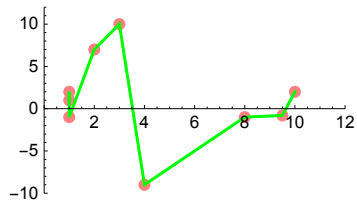
(* Problem(11) Plot list G again with options PlotJoined->True, PlotStyle->{Green ,Thickness[0.01]}, PlotRange->{{0,12},{-10,12}} and superimpose Plot1 and Plot2 *)

```
Plot2 = ListPlot[G, Joined → True,
  PlotStyle → {Green, Thickness[0.01]}, PlotRange → {{0, 12}, {-10, 12}}]
```



(* Superimpose Plot1 and Plot2 *)

```
Show[Plot1, Plot2]
```

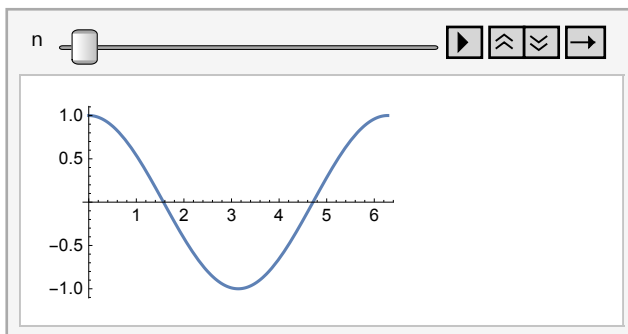


(* Animating 2D Plots *)

```
(* Problem(12) Use Animate[Plot[function],{parameter,pmin,pmax,step}]
to animate Cos[n x] {x,0,2Pi} {n,1,6,1}
from 1 to 6 with the step 1 *)
```

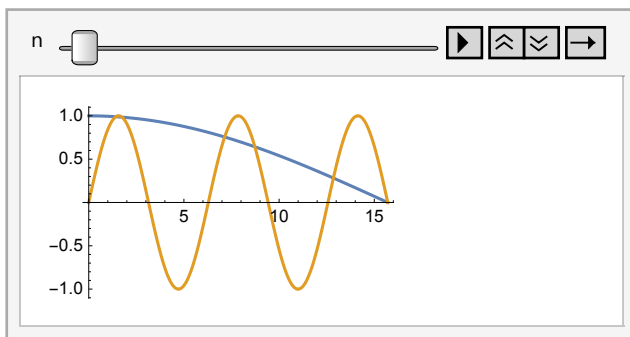
```
f16[x_, n_] := Cos[n x]
```

```
Animate[Plot[f16[x, n], {x, 0, 2 Pi}], {n, 1, 6, 1}, AnimationRunning → False]
```

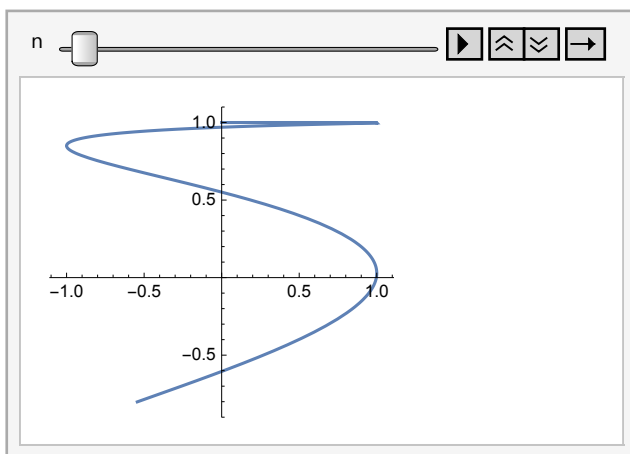


```
(* Problem(13) Use Animate[Plot[function],{parameter,pmin,pmax,step}] to animate
two explicit functions Cos[n x/10] and Sin[n^2 x] {x,0,5Pi} {n,1,10,1} *)
```





(* Problem(14) Use ParametricPlot to
animate a parametric plot of a function given by
 $x_p[t_, n_] := \sin[2t \cdot n]$, $y_p[t_, n_] := \cos[t^2 \cdot n/10]$,
{t, 0, 5} {n, 1, 10, 1}. Use PlotPoints \rightarrow 100 *)

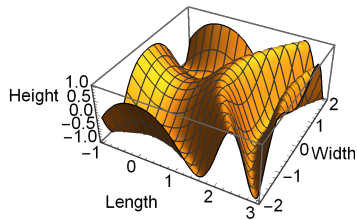


(* 3D Plots *)

(* Problem(15) Plot a 3D function given by $\sin[x^2 - y^2]$
on {x, -1, 3} {y, -2, 2} and note options such as AxesLabel and
the number of points in each direction given by PlotPoints. *)

f19[x_, y_] := Sin[x^2 - y^2]

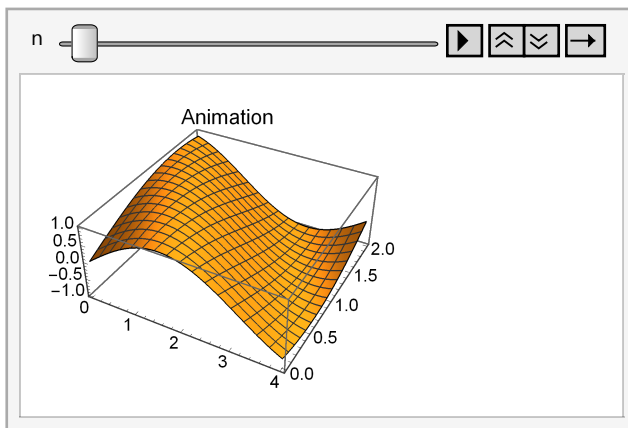

```
Plot3D[f19[x, y], {x, -1, 3}, {y, -2, 2},
  PlotPoints → {20, 20}, AxesLabel → {"Length", "Width", "Height"}]
```



```
(* Problem(16) Animate a family of surfaces given by Sin[x+y*n] on {x,0,4},
{y,0,2} {n,1,15,2} *)
```

```
f21[x_, y_, n_] := Sin[x + y * n]
```

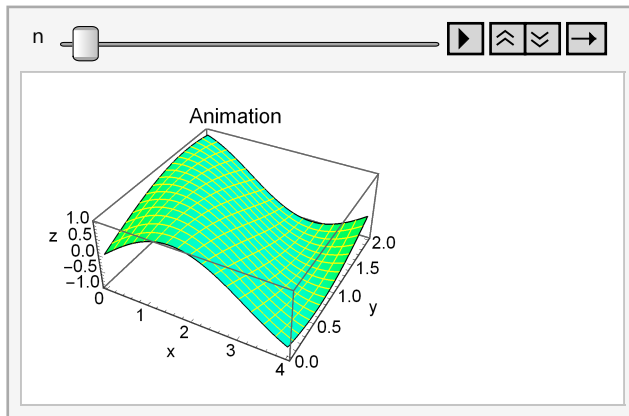
```
Animate[Plot3D[f21[x, y, n], {x, 0, 4}, {y, 0, 2}, PlotPoints → 40, PlotLabel → "Animation"],
  {n, 1, 15, 2}, AnimationRunning → False]
```



```
(* The entire set of options is given using: *)
```

```
Options[Plot3D];
```

```
(* Problem(17) Beautify the graph above. Select 3 additional options or change
the existing ones and animate the result. Your graph may look different *)
```



(* Your graph may look different *)

(* Problem (18) Using ParametricPlot3D plot a spiral below *)

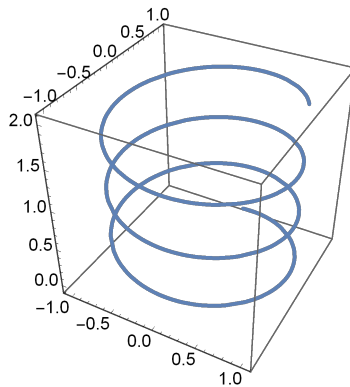
```
x22[u_] := Sin[u]
```

```
y22[u_] := Cos[u]
```

```
z22[u_] := u/10
```

```
spiral[u_] := {x22[u], y22[u], z22[u]} (*vector function *)
```

```
ParametricPlot3D[spiral[u], {u, 0, 20}]
```

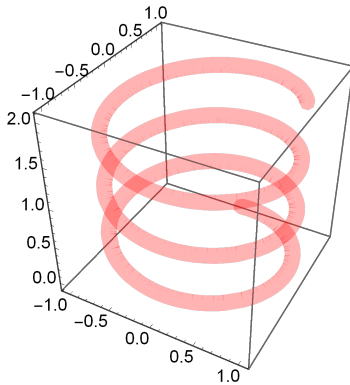


(* Problem (19) Beautify the graph using 3 new options. Use Options[ParametricPlot3D] and Mathematica help, for example, change PlotStyle→ AxesLabel→ and Opacity. *)

(* The entire set of options is given using: *)

```
Options[ParametricPlot3D];
```

```
(* your graphs may look different *)
```



```
(* Problem(20) Animate a parametric function
```

```
  x23[u_,v_] := u
```

```
  y23[u_,v_] := v
```

```
  z23[u_,v_,n_] := n*(u^2 + v^2)/10
```

```
on 1 graph , n is the animation parameter {n,1,3,0.5}. Fix the PlotRange →
```

```
{{-5, 5}, {-5, 5}, {0, 10}}) to
```

```
avoid changing the graphics box. Use PlotPoints→20 *)
```

```
{u, -5, 5},  
{v, -5, 5}    {{-5, 5}, {-5, 5}, {0, 15}}
```

