

```
(*      Computer Graphics with Applications of Dr. Makhanov.
      Lab 3
      "Flying" Objects and Rotations. *)
```

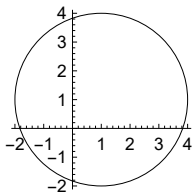
```
SetOptions[EvaluationNotebook[], ShowCellLabel → False];
```

```
SetOptions[{Graphics, Plot, Plot3D, ContourPlot, ContourPlot3D, DensityPlot, ParametricPlot,
  ParametricPlot3D, ListPlot, ListLinePlot, VectorPlot, VectorPlot3D, StreamPlot,
  ListPointPlot3D, RegionPlot, RegionPlot3D, Graphics, Graphics3D}, ImageSize → Small];
```

```
(* This introduces graphics primitives such as Circle[{x,y},Rc],
Sphere[{x,y,z},Rs], Cuboid[{xc,yc,zc}] (there are many others) where {x,y} and
{x,y,z} is the center of the circle and sphere/cuboid respectively and Rc
Rs the radius. Cuboid[{xc,yc,zc}] represents a unit cuboid with a corner at
{xc,yc,zc}. These functions must be called with displaying functions Graphics
and Graphics3D. See the examples below (you do not need to replicate them) *)
```

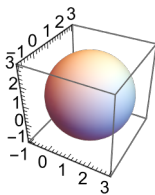
```
(* Circle, radius 3 and the center at {1,1} use Graphics *)
```

```
Graphics[Circle[{1, 1}, 3], Axes → True, ImageSize → Tiny]
```



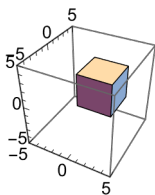
```
(* Sphere radius 2 and the center at {1,1,1} use Graphics3D*)
```

```
Graphics3D[Sphere[{1, 1, 1}, 2], Axes → True, ImageSize → Tiny]
```



```
(* Cube, centered at {1,1,1} with the side 4 *)
```

```
Graphics3D[Cube[{1, 1, 1}, 4], Axes → True,
ImageSize → Tiny, PlotRange → {{-5, 5}, {-5, 5}, {-5, 5}}]
```



(* ----- PART 2 -----*)

(* Problem (8) Rotations in 2D are performed by rotation matrices given by `RotationMatrix[θ]`. Using the rotation matrix to `R[a]` to rotate a curve `c[t]` is accomplished by `R[a].c[t]`, where `.` denotes the matrix-vector multiplication
 Let us rotate the curve given by `x8[t_]:=0.1*Sin[t]` `y8[t_]:=0.3*Cos[t]`
 for `{t,0,5}` by 45 deg around
 the origin. Show the original and the rotated curve *)

```
x8[t_] := 0.1 * Sin[t]
```

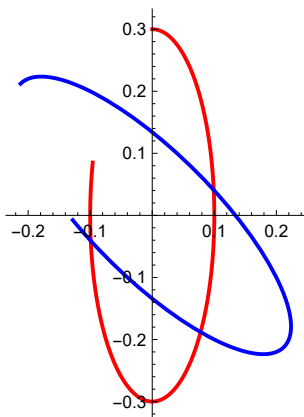
```
y8[t_] := 0.3 * Cos[t]
```

```
RM[a_] := RotationMatrix[a]
```

```
s8[t_] := {x8[t], y8[t]}
```

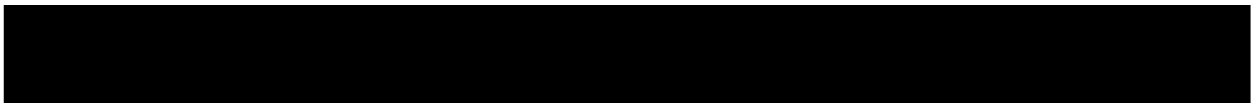
```
srotated8[t_] := RM[45 * Degree].s8[t]
```

```
ParametricPlot[{s8[t], srotated8[t]}, {t, 0, 5}, PlotStyle -> {{Red, Thick}, {Blue, Thick}}]
```

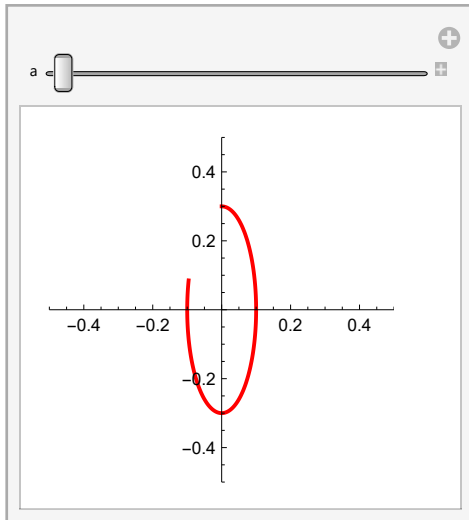


(* Problem (9). Animate a curve from
 Problem 8 rotating continuously around the origin *)

```
srotated91[t_, a_] := RM[a].s8[t]
```



```
Manipulate[plotg91[a], {a, 0, 360 * Degree, 1 * Degree}]
```



(* Problem (10). Rotating Pold around a point Paround=
 $\{x,y\}$ is performed by the following transformation
 $P_{\text{new}} = \text{RM}[a] \cdot (P_{\text{old}} - \text{Paround}) + \text{Paround}$.
 Using the transformation above animate rotation of the parametric curve from
 problem 9 around $\text{Paround} = \{1, 0.5\}$. On animation plot display Paround using
 $\text{ListPlot}[\{\text{Paround}\}, \text{PlotStyle} \rightarrow \{\text{Blue}, \text{PointSize}[0.05]\}]$
 Fix the PlotRange *)

```
Paround = {1, 0.5}
```

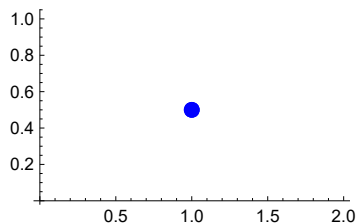
```
{1, 0.5}
```

```
srotated10[t_, a_] := RM[a] . (s8[t] - Paround) + Paround
```

```
plotg10[a_] := ParametricPlot[srotated10[t, a],  

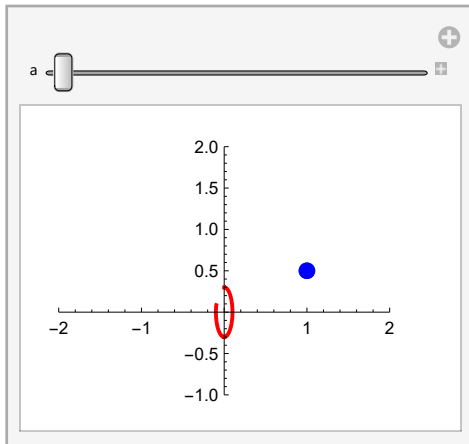
  {t, 0, 5}, PlotStyle -> {{Red, Thick}}, PlotRange -> {{-2, 2}, {-1, 2}}]
```

```
plotl10 = ListPlot[{Paround}, PlotStyle -> {Blue, PointSize[0.05]}]
```



```
plotg10show[a_] := Show[{plotg10[a], plotl10}]
```

```
Manipulate[plotg10show[a], {a, 0, 360 * Degree, 1 * Degree}]
```



(* Problem (11). Using transformations from Problem 10 animate the rotation of a parametric spline based on $\text{data11}=\{1,1\},\{2,3\},\{2,4\},\{7,7\},\{8,6\},\{7,3\},\{7,-1\},\{5,-1\}$ around the point $\text{Paround11}=\{1,1.5\}$. *)

```
{1, 1.5}
```

```
data11 = {{1, 1}, {2, 3}, {2, 4}, {7, 7}, {8, 6}, {7, 3}, {7, -1}, {5, -1}}
```

```
{{1, 1}, {2, 3}, {2, 4}, {7, 7}, {8, 6}, {7, 3}, {7, -1}, {5, -1}}
```

```
{1, 2, 2, 7, 8, 7, 7, 5}
```

```
{1, 3, 4, 7, 6, 3, -1, -1}
```

```
InterpolatingFunction[ Domain: {{1, 8}}  
Output: scalar]
```

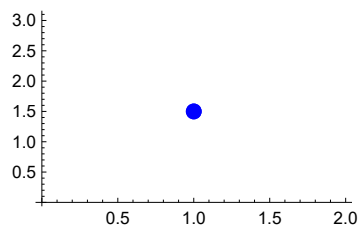
```
InterpolatingFunction[ Domain: {{1, 8}}  
Output: scalar]
```

[REDACTED]

[REDACTED]

[REDACTED]

[REDACTED]



[REDACTED]

[REDACTED]

