

Question 1:

```
function ComputeExpression(str)
  init(DigitStack), init(OprtStack)
  ValidDigit = ('0', '1', '2', '3', '4', '5', '6', '7', '8', '9')
  ValidOperator = ('(', ')', '+', '-', '/', '*')
  LastCharDigit<-False
  for i<-0 to length(str)-1 do
    if (str[i] in ValidDigit) and !LastCharDigit then
      push(DigitStack, str[i])
      LastCharDigit<-True
    elseif str[i] in ValidOperator then
      push(OprtStack, str[i])
      LastCharDigit<-False
    else then
      return NotWellFormed
  if str[i] == ')' then
    pop(OprtStack)
    if len(DigitStack) < 2 or len(OprtStack) < 2 then
      return NotWellFormed
    A<-pop(DigitStack), O<-pop(OprtStack), B<-pop(DigitStack)
    if O not equal to '(' or ')' then
      total <- apply A with the operator O by B
      push(DigitStack, total)
    else then
      return NotWellFormed
    if pop(OprtStack) not equal to '(' then
      return NotWellFormed
  if len(DigitStack) == 1 and len(OprtStack) == 0 then
    return pop(DigitStack)
  else then
    return NotWellFormed
```

Question 3b

The algorithm used in 3a is a variation of a topological sort. First the data is organised into tree data structures, which have integer values for tree number/index and amount of incoming edges, and a deque for the indices of the trees children.

The program takes in the first line which gives the total amount of edges(m) as well as vertices(n), this information is used to create an array of tree pointers with length n . The array is then populated with empty trees and the program begins to read the edges. The parent of each edge has the child's index/tree number pushed onto the deque of outgoing edges, while the child's incoming counter is incremented by 1. This leaves total space occupied by the program at $O(n+m)$ complexity given n trees with a total of m items in deques as well as the time taken being m .

After the program has all of the edges processed, the `max_path_len()` function is called on the array of trees to determine if there is an unbroken path down the hill. Here is the pseudo code for the function:

```

Bool max_path_len(array)
  Current_vertex = array[0]
  For i=1 to len(array)// including
    If current_vertex.outgoing is empty
      break
    found<-false
    for child in current_vertex.outgoing
      child.incoming -= 1
      if !child.incoming
        found<-true
        current_vertex<- child
    if !found
      return false
  if I == len(array)
    return true
  return false

```

The algorithm starts at Tree 0 and identifies the next ordered tree by the amount of incoming edges. This is because if a node has only one incoming edge in a directed acyclic graph it either is the next node in the complete path or the path is impossible to complete. To do this the algorithm iterates n times, and at each vertex it must check each outgoing edge (m - rest of edges). While the algorithm has an embedded loop the time complexity is not quadratic; since the algorithm only looks at each edge once as all outgoing vertices are unique, the worst case is $n+m$ time meaning the algorithm runs in $O(n+m)$ time.

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