# DM887 Assignment2 Q1

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19.03.2024

Implementation of Least-Squares Temporal Differences (LSTD) Deep Q-Learning with Nonlinear Feature Extraction that maps a state to lower-dimensional latent embedding. While the action-value function should be a linear function of the output of the feature extractor.

#### Algorithm 1 Initialization

- 1: Initialize a variational autoencoder  $\mathbf{A}$  as the feature extraction network with initial weights  $w_0$  [ $w_0$  are drawn from Glorot uniform initialization]
- 2: Initialize the learning rate of **A** as  $\alpha = 1 \times 10^{-2}$
- 3: Initialize an Adam optimizer o with a learning rate  $\alpha$  for  ${\bf A}$
- 4: Initialize the minibatch size of DQN as k = 32
- 5: Initialize the total number of training episodes N=500, the number of episodes at each cycle consisting of three phases of training  $N_0=50$ , and the number of episodes at each separate phase of training  $N_1=10$  [It would be a wise choice to separate the warm-up phase, the antoencoder update phase, and the LSTD update phase at each cycle]
- 6: Initialize the number of maximum time step per episode T = 1000
- 7: Initialize the weights  $\theta_0$  for linear approximation function randomly between (0,1) which will be used for LSTD
- 8: Initialize a replay memory buffer  $\mathcal{D}$  with a capacity  $N \times T$
- 9: Initialize a discount factor  $\gamma = 0.9$
- 10: Initialize a small constant  $\lambda = 1 \times 10^{-3}$  to initialize  $A^{-1}$  for LSTD
- 11: Given the number of actions as  $N_a$  and embedding dimension  $N_e$ , initialize a matrix  $\theta$  with shape  $N_a \times N_e$
- 12: Initialize a tensor  $A_a^{-1} = \lambda^{-1}I$  and a tensor  $b_a = 0$  to store the tensors that suffice  $\theta_a = A_a^{-1}b_a$ ,  $\forall a \in A$  at each time step t [A relatively large discount factor encourages long-term planning and faster convergence during training]

[1]

### Algorithm 2 Warm-up phase

```
1: Freeze the weights of f(phi(s)), i.e. \theta
 2: Freeze the weights of \mathbf{A}, i.e. w
 3: for episode e_0 = 1 to N_1 do
        Initialize state s
 4:
        Preprocess s into s_0 to adapt it as input of A [preprocessing of high-dimensional states is necessary
 5:
    w.r.t. autoenconders]
        for each time step t = 1 to T do
 6:
            Encode state s_t using A to get latent embedding \phi(s_t)
 7:
            Select action a_t using \epsilon-greedy policy with \epsilon = 0.2 with an \epsilon decay
 8:
            Execute a_t and obtain reward r_t and new state s_{t+1}
 9:
            if s_{t+1} \notin S then
10:
                break
11:
            end if
12:
            Store the transition of the current t, i.e. (s_t, a_t, r_t, s_{t+1}) in \mathcal{D}
13:
14:
        end for
15: end for
16: e = e + N_1
[1]
```

### Algorithm 3 Autoencoder update phase

```
1: Freeze the weights of f(phi(s)), i.e. \theta
 2: Unfreeze the weights of \mathbf{A}, i.e. w
3: for episode e_0 = 1 to N_1 do
       Repeat the same steps at the warm-up phase
 4:
       for each time step t = 1 to T do
 5:
           Repeat the same steps at the warm-up phase
 6:
   [Start updating the autoencoder using minibatches]
           Sample a minibatch of transitions d from \mathcal{D} with a batch
size k
8:
           Use the s_t of d as input to \mathbf{A}
9:
           First encode, then decode d using A
10:
           Calculate the loss L of s_t by comparing the input and output of A
11:
           Update w with o as per L
12:
       end for
13:
14: end for
15: e = e + N_1
[1]
```

### Algorithm 4 LSTD update phase

```
1: Freeze the weights of f(phi(s)), i.e. \theta
 2: Unfreeze the weights of \mathbf{A}, i.e. w
 3: for episode e_0 = 1 to N_1 do
        Repeat the same steps at the warm-up phase
 4:
        for each time step t = 1 to T do
 5:
            Repeat the same steps at the warm-up phase
 6:
 7: [Start using the online LSTD algorithm to update \theta]
            Calculate \tau = \phi(s_t) - \gamma \phi(s_{t+1})
 8:
            Calculate v = \tau^{T} A^{-1}
 9:
            Update A^{-1} = A^{-1} - \frac{A^{-1}\phi(s)v^T}{1+v\phi(s)}
10:
            Update b = b + r\phi(s)
11:
            Given the action a of the current time step, update \theta_a = A^{-1}b
12:
            Update state s_t = s_{t+1}
13:
        end for
14:
15: end for
16: e = e + N_1
[1]
```

## Algorithm 5 Training procedure

- 1: Run Initialization
- 2: while  $episode \ e \leq N \ \mathbf{do}$
- Run Warm-up phase 3:
- Run Autoencoder update phase 4:
- Reset  $A_a^{-1}$  and  $b_a$  to the default value at the initialization phase,  $\forall a \in A$  at each time step t5:
- 6: Run LSTD update phase
- Run Autoencoder update phase 7:
- Reset  $A_a^{-1}$  and  $b_a$  to the default value at the initialization phase,  $\forall a \in A$  at each time step t Run LSTD update phase 8:
- 9:
- 10: end while

[1]