MAE 8 - Winter 2015 Homework 8

Instructions: Follow the homework solution template. Put all answers in a MATLAB script named hw8.m. For this homework, you will need to submit multiple files. Create a zip archive named hw8.zip. The zip archive should include the following files: hw8.m, read_input.m, read_number.m, digitsum.m, getGCD.m, number.txt and task1.txt. Submit hw8.zip through TED before 9 PM on 03/6/2015. Use double precision unless otherwise stated.

Problem 1: Download the file task1.txt from TED. This text file contains the initial position, velocity and direction for the 4 trajectories in task 1. In this exercise, you will write a function to read these parameters into MATLAB. The function should have the following declaration: function [Xo, Yo, Zo, Umag, theta, phi, C] = read_input(inputfile, traj_num) where inputfile is a string denoting the name of the file to be read and traj_num is an integer indicating the trajectory number. The outputs are the initial position (Xo, Yo, Zo), magnitude of initial velocity (Umag), direction (theta, phi) and coefficient of friction (C). The function should have a description. In cases when the input traj_num is not available in the file, the function should set all outputs to NaN and display an error warning to screen.

- (a) Set p1a=evalc('help read_input');
- (b) Read in the file **task1.txt** and get the parameters for trajectory 1. Put the parameters into **p1b**.
- (c) Read in the file **task1.txt** and get the parameters for trajectory 2. Put the parameters into **p1c**.
- (d) Read in the file **task1.txt** and get the parameters for trajectory 3. Put the parameters into **p1d**.
- (e) Read in the file **task1.txt** and get the parameters for trajectory 4. Put the parameters into **p1e**.
- (f) Read in the file **task1.txt** and get the parameters for trajectory 5. Put the parameters into **p1f**.

All answers in parts (b-f) should be a 7-element vector listing the parameters in the same order as the outputs in the function **read_input**.

Problem 2: Temperature can be converted from Celsius (°C) and Fahrenheit (°F) to Kelvin (K) by using the following relation:

$$T(K) = T(^{\circ}C) + 273.15,$$

 $T(K) = 5/9 * (T(^{\circ}F) + 459.67).$

(a) Create a 2-element cell array of anonymous functions to define the conversions above. The anonymous function should have a function handle named K. The first anonymous function should have the input argument C and an expression to convert temperature from

C to K. The second anonymous function has the input argument F and an expression to covert temperature from F to K. Set $\mathbf{p2a} = \mathbf{K}$.

- (b) Convert 20° C to Kelvin and put the answer in **p2b**.
- (c) Convert 90° F to Kelvin and put the answer in **p2c**.

The ideal gas law is given by: $\mathbf{P} \mathbf{V} = \mathbf{n} \mathbf{R} \mathbf{T}$ where \mathbf{P} is pressure in atm, \mathbf{V} is volume in liter, \mathbf{n} is number of moles, \mathbf{R} is ideal gas constant and \mathbf{T} is temperature in Kelvin. For the following exercise, set \mathbf{R} to be 0.08206 L atm $mol^{-1} K^{-1}$.

- (d) Create an anonymous function to relate pressure \mathbf{P} to other variables in the ideal gas law. The function should have a function handle named \mathbf{P} and 3 input arguments (\mathbf{n} , \mathbf{T} , \mathbf{V}). Set $\mathbf{p2d} = \mathbf{P}$.
- (e) An 0.12 mol of solid CO_2 is put in an empty sealed 4.0 L container at a temperature of 27°C. When all the solid CO_2 becomes gas, what will be the pressure in the container? Set the answer to $\mathbf{p2e}$.
- (f) An 0.12 mol of solid CO_2 is put in an empty sealed 4.0 L container at a temperature of 90°F. When all the solid CO_2 becomes gas, what will be the pressure in the container? Set the answer to $\mathbf{p2f}$.
- (g) Create a figure to show how the pressure changes with temperature in the container with CO_2 . Use $n = 0.12 \, mol$ and V = 4.0 L. The x-axis will show the temperature ranging from $25^{\circ}C$ to $35^{\circ}C$ with an increment of $0.1^{\circ}C$ while the y-axis shows the corresponding pressure. Label the axes including units, and give the figure a title. Set $\mathbf{p2g} = \mathbf{'See}$ figure 1'.

Problem 3: Download the file **number.txt** from TED. The file contains a combination of text and numbers. In this exercise, you will use low-level input functions to read this file into MATLAB. Write a function **get_number** to read in the file. The function should have the following declaration: **function number** = **get_number(numberfile)** where the input **numberfile** is a string denoting the name of the file and the output **number** is a vector containing the numbers on each line in the file. The function should have a description.

- (a) Set p3a = evalc('help get_number').
- (b) Set **p3b** = **get_number('number.txt')** to read in the file and obtain the numbers on each line in the file.

Now write a recursive function **digitsum** to calculate the sum of all digits of a given number. For example, digitsum(312) = 6. The function should have the following declaration: **function dsum** = **digitsum(n)** where input n is a positive integer and output **dsum** is the sum of all digits in the number n. The function should have a description. When the input is not a positive integer, set the output to be a warning message and use **return** to exit the function.

- (c) Set p3c = evalc('help digitsum').
- (d) Find the digit sum of the first number in the file **number.txt** and set the answer to **p3d**.

- (e) Find the digit sum of the second number in the file and set the answer to **p3e**.
- (f) Find the digit sum of the third number in the file and set the answer to **p3f**.
- (g) Find the digit sum of the fourth number in the file and set the answer to **p3g**.

Now write a recursive function getGCD to calculate the greatest common denominator of two given numbers. For example, getGCD(12, 9) = 3. The function should have the following declaration: function gcd = getGCD(n1, n2) where inputs n1 and n2 are positive integers and output gcd is the greatest common denominator of n1 and n2. The function should have a description. When the inputs are not positive integers, set the output to be a warning message and use **return** to exit the function.

(h) Set p3h = evalc('help getGCD').

- (i) Find the greatest common denominator for the first and the last number in the file **number.txt** and set the answer to **p3i**.
- (j) Find the greatest common denominator for the second and the last number in the file and set the answer to **p3j**.
- (k) Find the greatest common denominator for the last number in the file and 525. Set the answer to **p3k**.
- (l) Find the greatest common denominator for the last number in the file and 345525. Set the answer to **p3l**.