

HW 2

Osama Refaat (SE)'

1) First test

$${}^{12}C_4 = \frac{12!}{4!8!} = 495$$

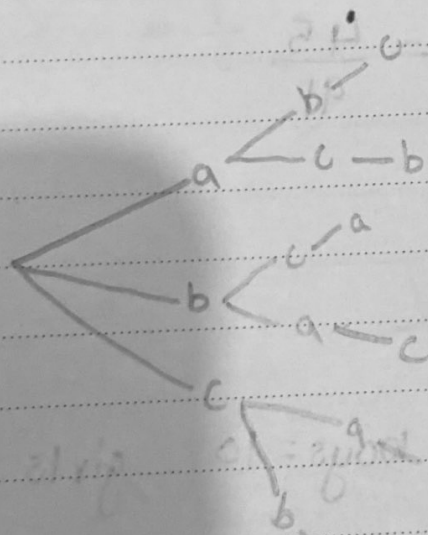
second test

$${}^8C_4 = 70$$

third = 1

so there are $1 \times 70 \times 495$ (34650) ways.

2)



3) 12 items total

$$P(D) = \frac{4}{12}$$

$$i) P(A) = \frac{4}{12} \times \frac{3}{11} = \frac{1}{11}$$

$$P(B) = \frac{8}{12} \times \frac{7}{11} = \frac{14}{33}$$

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$$\text{ii) } \left(\frac{8}{12} \times \frac{4}{11} \right) + \left(\frac{4}{12} \times \frac{8}{11} \right) + \frac{4}{12} \times P(A)$$

$$= \frac{19}{33}$$

4) 15 items Defective = 5

$$\text{i) } \frac{10}{15} \times \frac{9}{14} \times \frac{8}{13} = \frac{24}{91}$$

$$\text{ii) } \left(\frac{10}{15} \times \frac{9}{14} \times \frac{5}{13} \right) \times 3 = \frac{45}{91}$$

$$\text{iii) } 1 - \frac{24}{91} = \frac{67}{91}$$

5) Total students = 30 boys = 10 girls = 20

boys from mansoura = 5 girls from mansoura = 10

	boys	girls
from mans	5	10
not	5	10
Total	10	20

= 30

$$\text{Answer} = \frac{10}{30} + \frac{15}{30} - \frac{5}{30}$$

$$= \frac{2}{3}$$

$$6) P(A) = \frac{3}{8}$$

$$P(B) = \frac{1}{2}$$

$$P(A \cap B) = \frac{1}{2}$$

$$i) P(A^c) = 1 - \frac{3}{8} = \frac{5}{8}$$

$$ii) P(B^c) = 1 - \frac{1}{2} = \frac{1}{2}$$

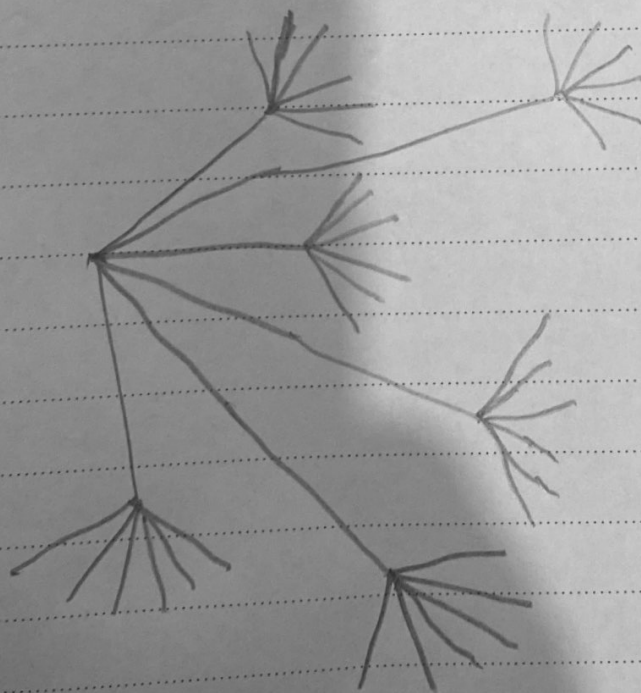
$$iii) P(A^c \cap B^c) = P(A \cup B)^c \Rightarrow 1 - \left(\frac{3}{8} + \frac{1}{2} - \frac{1}{2} \right) = \frac{5}{8}$$

$$iv) P(A^c \cup B^c) = P(A \cap B)^c \Rightarrow 1 - \frac{1}{2} = \frac{1}{2}$$

$$v) P(A \cap B^c) = \frac{1}{8}$$

$$vi) P(A \cap B \cap A^c) = 0$$

7)



$$= 1 - \frac{125}{216} = \frac{91}{216}$$

$$8) \sum P(x) = k^2 - 8$$

$$1 = k^2 - 8$$

$$k^2 = 9$$

$$k = 3$$

$$9) P(A) = 0.35 \quad P(B) = 0.45$$

$$P(A^c \cap B^c) = P(A \cup B)^c = 1 - (0.35 + 0.45) = \frac{1}{5}$$