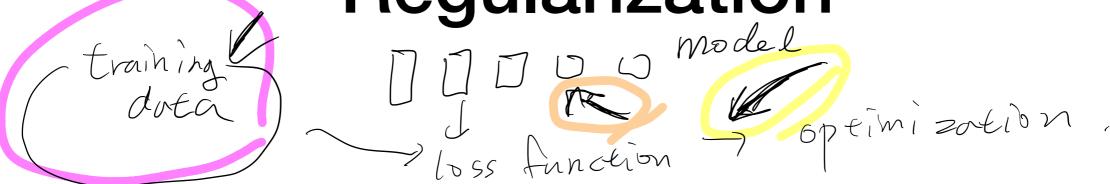
Regularization

Seyoung Yun

- http://cs231n.stanford.edu/slides/2017/ cs231n_2017_lecture7.pdf
- N. Srivstava et al, "Dropout: A Simple Way to Prevent Neural Networks from Overfitting" http://jmlr.org/papers/volume15/srivastava14a/srivastava14a.pdf
- Sergey Ioffe and Christian Szegedy"Batch Normalization: Accelerating Deep Network Training by Reducing Internal Covariate Shift" https://arxiv.org/abs/1502.03167
- C. Zhang et al "Understanding deep learning requires rethinking generalization" https://arxiv.org/abs/
 1611.03530





- "A regularizer is anything that hurts the training process"
 - C. Zhung at ICLR2017 (https://www.youtube.com/watch?v=kCj51pTQPKI)
 - data augmentation
 - weight decay with an additional cost
 - dropout by adding random noise

Linear Regression

RSS: cost of linear regression

$$\mathcal{L}(w,b) = \sum_{i=1}^{m} (\underline{y}^{(i)} - \underline{w}^{\mathsf{T}} x^{(i)} - \underline{b})^{2}$$

regularizer

$$\mathcal{L}(w,b) = \frac{1}{m} \sum_{i=1}^{m} (y^{(i)} - w^{\top} x^{(i)} - b)^2 + \frac{\lambda}{2m} \|w\|_2^2$$

or

$$\mathcal{L}(w,b) = \frac{1}{m} \sum_{i=1}^{m} (y^{(i)} - w^{\top} x^{(i)} - b)^2 + \frac{\lambda}{2m} \|w\|_1$$

Weight Decay

$$J(w^{a}), b^{a} = --, w^{a} = 0$$

$$= \frac{1}{m} \sum_{i=1}^{m} \left(\frac{x^{a}}{x^{i}}, x^{(i)} \right) + \frac{1}{2m} \sum_{i=1}^{n} \|w^{c}\|_{F}^{2}$$

$$\|w^{c}\|_{F}^{2} = \sum_{i=1}^{m} \frac{y^{a}}{y^{a}} \left(\frac{x^{a}}{x^{i}} \right)^{2}$$

$$= \sqrt{2m} J = \frac{1}{m} \sum_{i=1}^{m} \sqrt{2m} \left(\frac{x^{a}}{x^{i}} \right)^{2} + \frac{1}{m} \cdot w^{c}$$

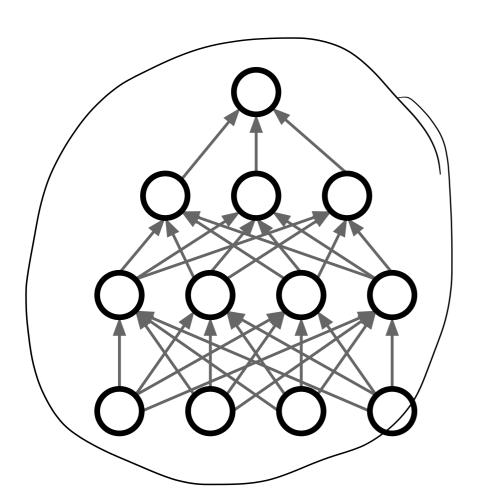
$$= \sqrt{2m} \int_{a}^{m} \frac{y^{a}}{y^{a}} \left(\frac{x^{a}}{x^{i}} \right)^{2} + \frac{1}{m} \cdot w^{c}$$

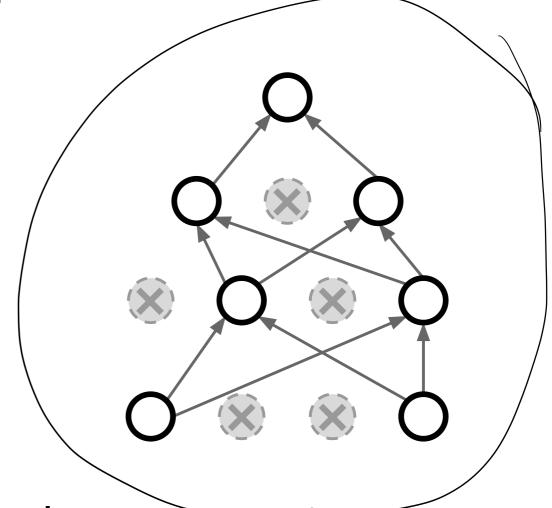
$$= \sqrt{2m} \int_{a}^{m} \frac{y^{a}}{y^{a}} \left(\frac{x^{a}}{x^{i}} \right)^{2}$$

$$= (1 - \frac{x^{2}}{m}) w^{c} \left(\frac{x^{a}}{x^{i}} \right) - \frac{x^{a}}{m} \frac{y^{a}}{x^{a}} \left(\frac{x^{a}}{x^{i}} \right)^{2}$$

Back prop

Dropout

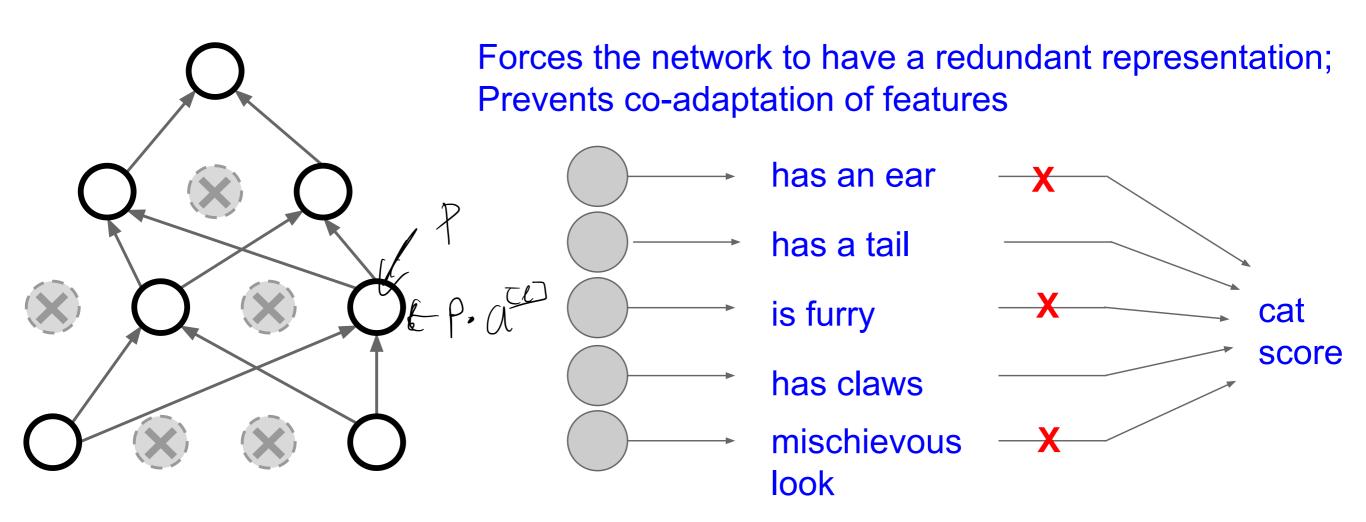




• In each forward pass, randomly erase neurons

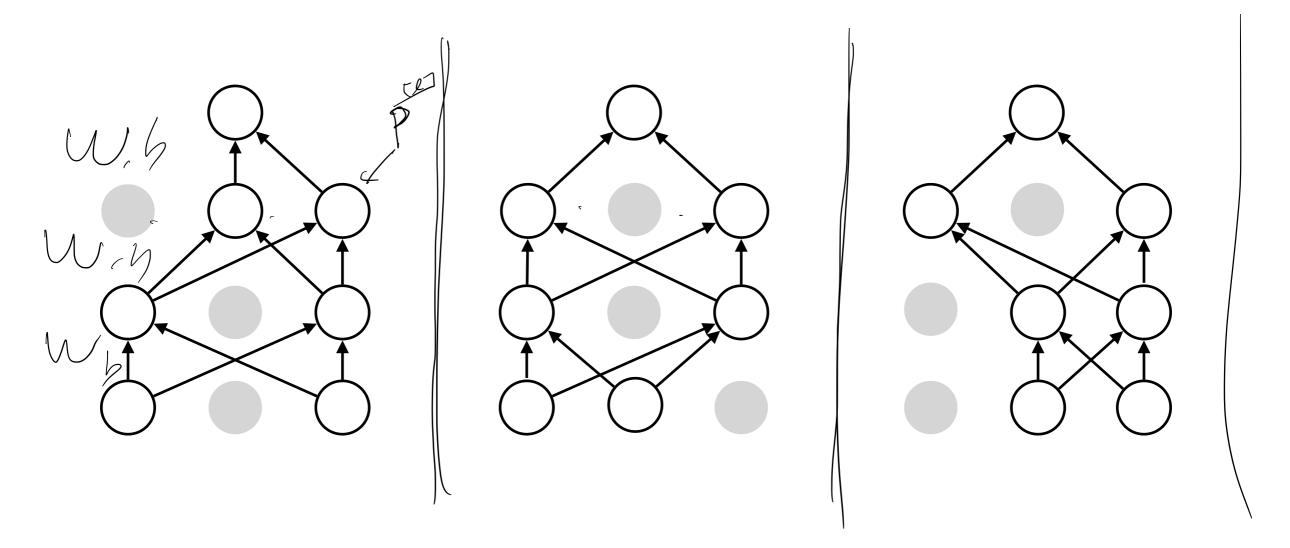
Dropout

Why can this be good?



Training

Ensemble of models

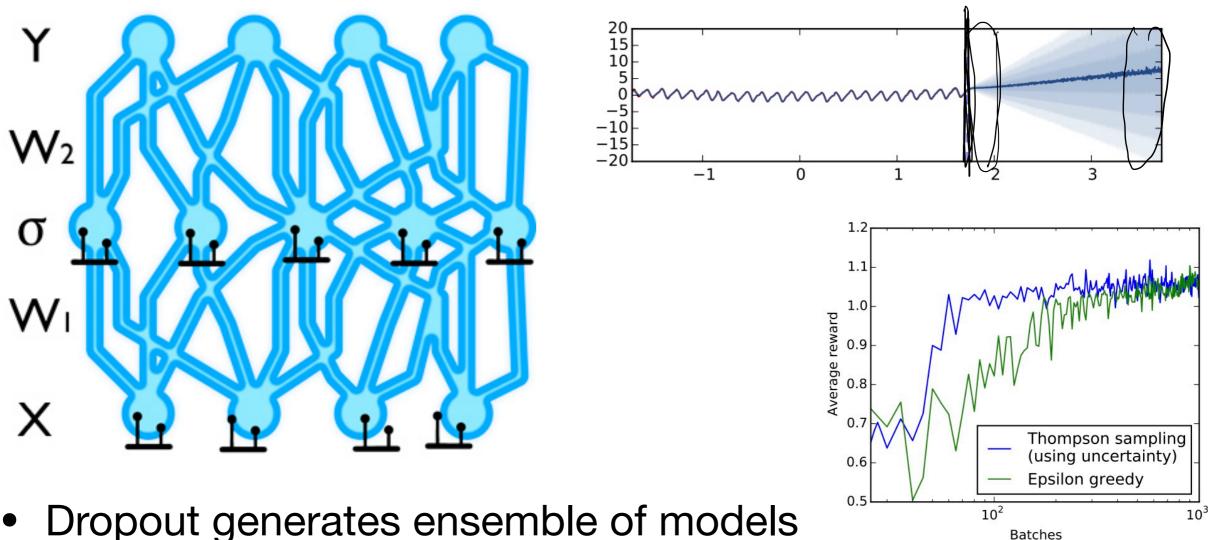


- Dropout is training a large ensemble of models (that share parameters).
- Each binary mask is one model

Dropout: Test time

- No dropout at test time
- scaling by dropout probability

Dropout: uncertainty

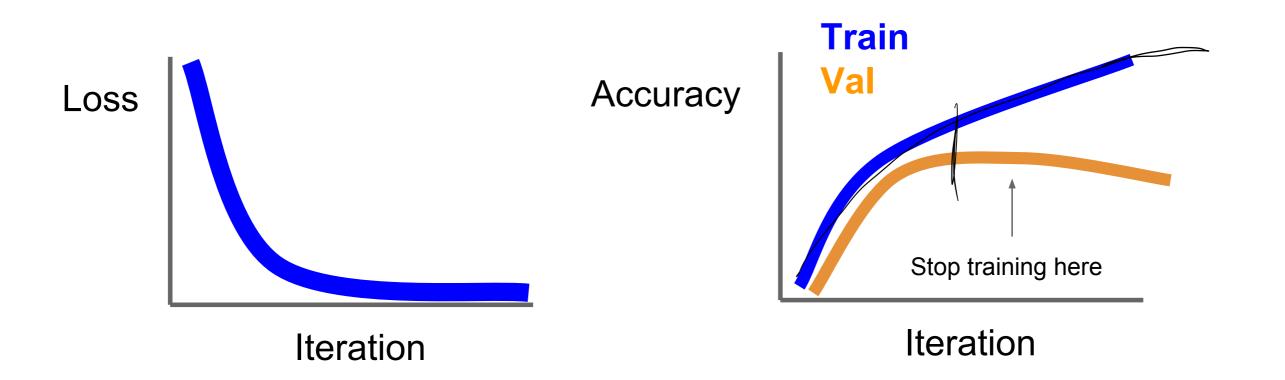


- From the ensemble, estimate mean and variance of the output
- Y. Gal and Z. Ghahrami, "Dropout as a Bayesian Approximation: Representing Model Uncertainty in Deep Learning," https://arxiv.org/abs/1506.02142

SGD and Early stopping

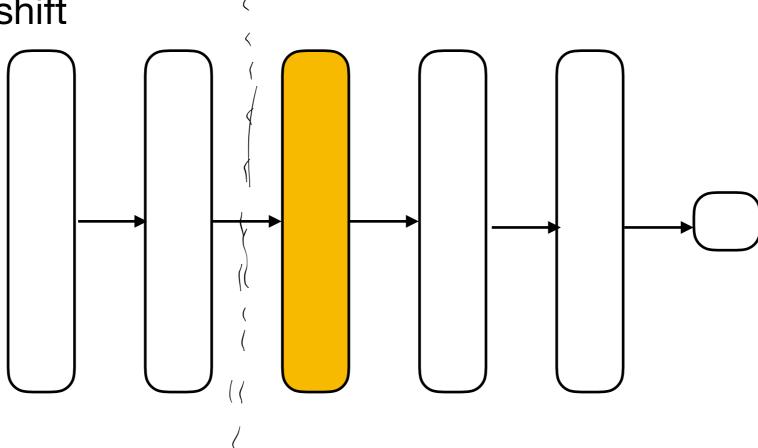
- SGD adds noises to the network -> a regularizer
- Early stopping

the network -> a regularizer
$$\int_{\hat{I}=1}^{N} \left(\int_{\hat{I}} \left(\int_{\hat$$



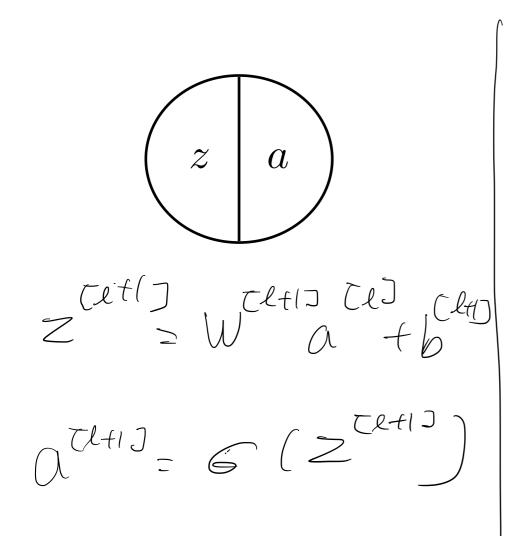
Batch Normalization

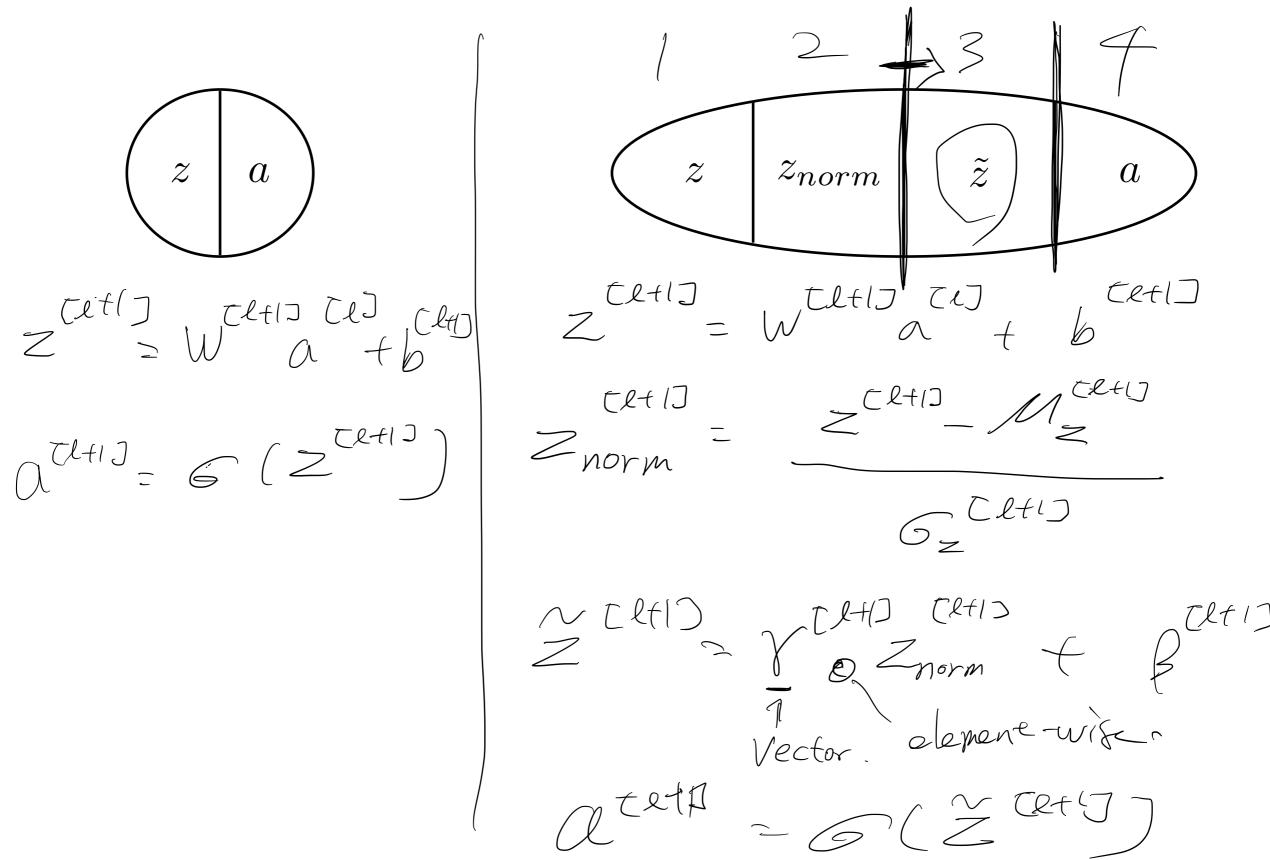
Covariate shift



• "The change in the distributions of layers' inputs presents a problem because the layers need to continuously adapt to the new distribution. When the input distribution to a learning system changes, it is said to experience covariate shift"

Batch Normalization





Training with Batch Norm.

- Original: $\{w^{[1]}, b^{[1]}, \dots, w^{[L]}, b^{[L]}\}$
- With Batch Norm.: $\{w^{[1]}, b^{[1]}, \beta^{[1]}, \gamma^{[1]}, \ldots, w^{[L]}, b^{[L]}, \beta^{[L]}, \gamma^{[L]}\}$

Batch Norm at test time

Batch Norm as regularization

- Each mini-batch is scaled by the mean/variance computed on just that mini-batch.
- This adds some noise to the values $z^{[j]}$ within that minibatch. So similar to dropout, it adds some noise to each hidden layer's activations.
- This has a slight regularization effect.