ADS 503 - Team 7

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06/12/2022

```
# R Libraries
library(caret)
library(AppliedPredictiveModeling)
library(Hmisc)
library(dplyr)
library(tidyverse)
library(ggplot2)
library(corrplot)
library(MASS)
library(ISLR)
library(rpart)
library(partykit)
library(randomForestSRC)
library(earth)
library(MARSS)
library(e1071)
library(summarytools)
library(grid)
```

Load the Red Wine Quality data set from GitHub - data set copied from Kaggle and imported into GitHub.

```
wine <- read.csv(
  url("https://raw.githubusercontent.com/OscarG-DataSci/ADS503/main/winequality-red.csv")
      , header = TRUE)</pre>
```

Data Summary

Data Frame Summary

wine Dimensions: 1599×12

Duplicates: 240

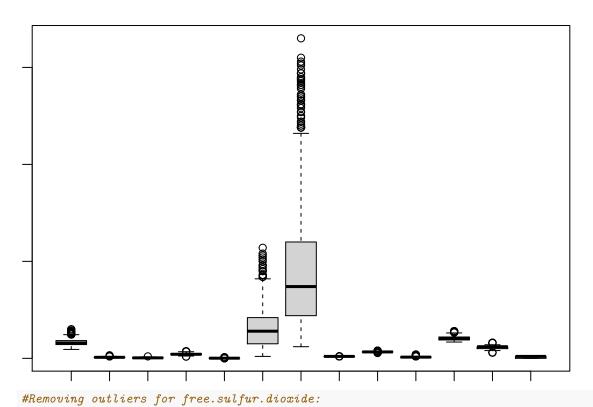
No	Variable	Stats / Values	Freqs (% of Valid)	Graph	Missing
1	fixed.acidity [numeric]	Mean (sd): $8.3 (1.7)$ min $<$ med $<$ max: 4.6 < 7.9 < 15.9 IQR (CV): 2.1 (0.2)	96 distinct values		0 (0.0%)
2	volatile.acidity [numeric]	Mean (sd): $0.5 (0.2)$ min < med < max: 0.1 < 0.5 < 1.6 IQR (CV): $0.2 (0.3)$	143 distinct values		0 (0.0%)
3	citric.acid [numeric]	Mean (sd) : $0.3 (0.2)$ min < med < max: 0 < 0.3 < 1 IQR (CV) : $0.3 (0.7)$	80 distinct values		0 (0.0%)
4	residual.sugar [numeric]	Mean (sd): 2.5 (1.4) min < med < max: 0.9 < 2.2 < 15.5 IQR (CV): 0.7 (0.6)	91 distinct values		0 (0.0%)
5	chlorides [numeric]	Mean (sd): 0.1 (0) min < med < max: 0 < 0.1 < 0.6 IQR (CV): 0 (0.5)	153 distinct values	<u></u>	0 (0.0%)
6	free.sulfur.dioxide [numeric]	Mean (sd): 15.9 (10.5) min < med < max: 1 < 14 < 72 IQR (CV): 14 (0.7)	60 distinct values		0 (0.0%)

No	Variable	Stats / Values	Freqs (% of Valid)	Graph	Missing
7	total.sulfur.dioxide [numeric]	Mean (sd): 46.5 (32.9) min < med < max: 6 < 38 < 289 IQR (CV): 40 (0.7)	144 distinct values		0 (0.0%)
8	density [numeric]	Mean (sd): 1 (0) min < med < max: 1 < 1 < 1 IQR (CV): 0 (0)	436 distinct values		0 (0.0%)
9	pH [numeric]	Mean (sd): 3.3 (0.2) min < med < max: 2.7 < 3.3 < 4 IQR (CV): 0.2 (0)	89 distinct values		0 (0.0%)
10	sulphates [numeric]	Mean (sd): $0.7 (0.2)$ min < med < max: 0.3 < 0.6 < 2 IQR (CV): $0.2 (0.3)$	96 distinct values		0 (0.0%)
11	alcohol [numeric]	Mean (sd): 10.4 (1.1) min < med < max: 8.4 < 10.2 < 14.9 IQR (CV): 1.6 (0.1)	65 distinct values		0 (0.0%)

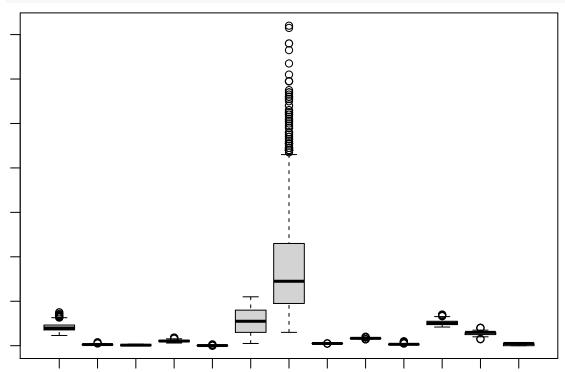
No	Variable	Stats / Values	Freqs (% of Valid)	Graph	Missing
12	quality [integer]	Mean (sd): 5.6 (0.8) min < med < max: 3 < 6 < 8 IQR (CV): 1 (0.1)	3: 10 (0.6%) 4: 53 (3.3%) 5: 681 (42.6%) 6: 638 (39.9%) 7: 199 (12.4%) 8: 18 (1.1%)	'	0 (0.0%)

Pre-processing

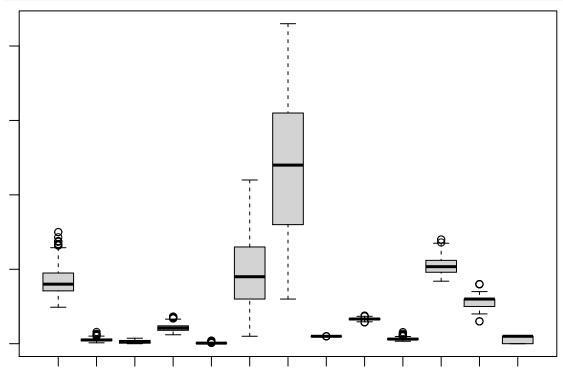
```
par(mar=c(1,1,1,1)) # to fix boxplot knit processing issues
# Create new variable, for quality values, split by half (0, 1)
wine$quality_target <- ifelse( wine$quality <= 5, 0, 1)</pre>
# Mean of new variable is at 0.5347 (close enough to 50% to maintain balance)
summary(wine$quality_target)
      Min. 1st Qu. Median
                              Mean 3rd Qu.
## 0.0000 0.0000 1.0000 0.5347 1.0000 1.0000
# Check for missing values in data set
wine %>% na.omit() %>% count() # there are no missing values
##
## 1 1599
# Removing outliers for residual sugar:
Q <- quantile(wine$residual.sugar, probs=c(.25, .75), na.rm = FALSE)
iqr_rs <- IQR(wine$residual.sugar)</pre>
up_rs <- Q[2]+1.5*iqr_rs # Upper Range
low_rs <- Q[1]-1.5*iqr_rs # Lower Range</pre>
eliminated_rs <- subset(wine, wine$residual.sugar > (Q[1] - 1.5*iqr_rs) & wine$residual.sugar < (Q[2]+1
boxplot(eliminated_rs)
```



```
Q2 <- quantile(wine$free.sulfur.dioxide, probs=c(.25, .75), na.rm = FALSE)
iqr_fs <- IQR(eliminated_rs$free.sulfur.dioxide)
up_fs <- Q2[2]+1.5*iqr_fs # Upper Range
low_fs <- Q2[1]-1.5*iqr_fs # Lower Range
eliminated_fs <- subset(eliminated_rs, eliminated_rs$free.sulfur.dioxide > (Q[1] - 1.5*iqr_fs) & elimin boxplot(eliminated_fs)
```



```
#Removing outliers for total.sulfur.dioxide:
Q3 <- quantile(wine$total.sulfur.dioxide, probs=c(.25, .75), na.rm = FALSE)
iqr_ts <- IQR(eliminated_fs$total.sulfur.dioxide)
up_ts <- Q3[2]+1.5*iqr_ts # Upper Range
low_ts <- Q3[1]-1.5*iqr_ts # Lower Range
eliminated_ts <- subset(eliminated_fs, eliminated_fs$total.sulfur.dioxide > (Q[1] - 1.5*iqr_ts) & eliminated_ts)
```

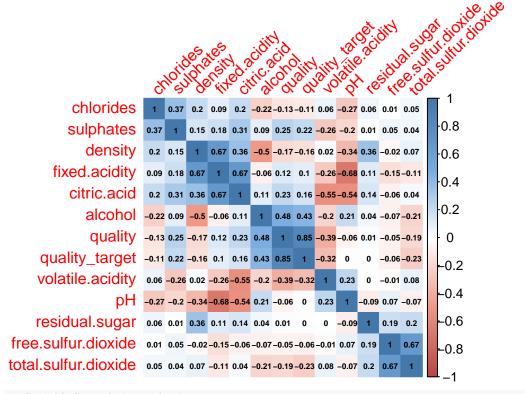


```
#Removing outliers for fixed.acidity:
Q4 <- quantile(wine$fixed.acidity, probs=c(.25, .75), na.rm = FALSE)
iqr_fa <- IQR(eliminated_ts$fixed.acidity)
up_fa <- Q[2]+1.5*iqr_fa # Upper Range
low_fa <- Q[1]-1.5*iqr_fa # Lower Range
eliminated_fa <- subset(eliminated_ts, eliminated_ts$fixed.acidity > (Q[1] - 1.5*iqr_fa) & eliminated_t
boxplot(eliminated_fa)
```

```
new_wine_data <- eliminated_fa

# Removing outliers reduced dimension of data set from 1599 observations to 48

# team opted not to use new_wine_data and keep outlier data
dim(new_wine_data)
```



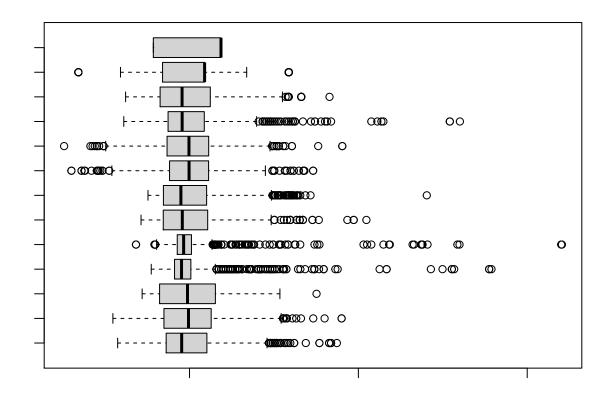
```
# Cutoff Correlation features
cutoffCorr <- findCorrelation(cor, cutoff = .8)
cutoffCorrFeatures <- wine[, -cutoffCorr]

# Train and Test split
wine_split <- createDataPartition(wine$quality, p = .8, list = FALSE)
wine_train <- wine[ wine_split,]
wine_test <- wine[-wine_split,]

# Transform Train Data
train_trans <- preProcess(wine_train, method = c("center", "scale"))
train_transformed <- predict(train_trans, wine_train)

# Transform Test Data
test_trans <- preProcess(wine_test, method = c("center", "scale"))
test_transformed <- predict(test_trans, wine_test)

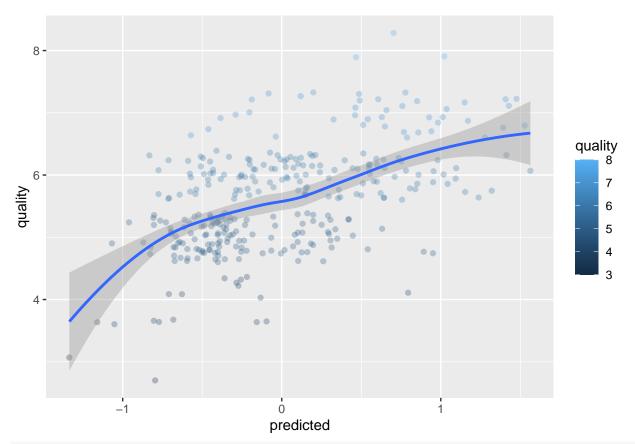
# Boxplot of transformed train data
boxplot(train_transformed, horizontal = TRUE, las = 2, cex.axis = .65, cex.lab = 7)</pre>
```



Logistic Regression Model

```
# Cutoff Correlation string to copy + paste into feature area of model
subset(cutoffCorrFeatures, select = -c(quality_target)) %>%
      colnames() %>%
     paste0(collapse = " + ")
## [1] "fixed.acidity + volatile.acidity + citric.acid + residual.sugar + chlorides + free.sulfur.dioxi
set.seed(4)
# Model using "quality_target" as target variable
lmodel1 <- lm(quality_target~ volatile.acidity + sulphates + alcohol, data = train_transformed)</pre>
summary(lmodel1)
##
## Call:
## lm(formula = quality_target ~ volatile.acidity + sulphates +
       alcohol, data = train_transformed)
##
##
## Residuals:
                  1Q
                       Median
## -3.03401 -0.69442 -0.04274 0.73427
                                        2.06407
## Coefficients:
##
                      Estimate Std. Error t value Pr(>|t|)
                                           0.000
## (Intercept)
                    -4.524e-15 2.396e-02
## volatile.acidity -1.964e-01 2.522e-02 -7.788 1.40e-14 ***
                     1.289e-01 2.479e-02
                                           5.198 2.34e-07 ***
## sulphates
```

```
## alcohol
                    3.955e-01 2.453e-02 16.126 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.8574 on 1277 degrees of freedom
## Multiple R-squared: 0.2666, Adjusted R-squared: 0.2649
## F-statistic: 154.7 on 3 and 1277 DF, p-value: < 2.2e-16
# Model using "quality" as target variable
lmodel2 <- lm(quality~ volatile.acidity + sulphates + alcohol, data = train_transformed)</pre>
summary(lmodel2)
##
## Call:
## lm(formula = quality ~ volatile.acidity + sulphates + alcohol,
      data = train_transformed)
## Residuals:
      Min
               1Q Median
                               ЗQ
                                      Max
## -3.3574 -0.4662 -0.0793 0.5930 2.7763
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                    1.542e-15 2.274e-02
                                          0.000
## volatile.acidity -2.337e-01 2.394e-02 -9.760 < 2e-16 ***
## sulphates
                    1.440e-01 2.353e-02
                                          6.117 1.26e-09 ***
## alcohol
                    4.381e-01 2.328e-02 18.815 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.814 on 1277 degrees of freedom
## Multiple R-squared: 0.339, Adjusted R-squared: 0.3375
## F-statistic: 218.3 on 3 and 1277 DF, p-value: < 2.2e-16
# Add predicted values to new data frame
wine test %>%
 mutate(predicted = predict(lmodel2, newdata = test_transformed)) -> df
# Summary of predicted interval
predict(lmodel2, newdata = test_transformed, interval = "prediction") %>%
 summary()
##
        fit
                          lwr
                                             upr
                    Min. :-2.95538
## Min. :-1.3354
                                      Min.
                                               :0.2847
## 1st Qu.:-0.4413
                    1st Qu.:-2.04038
                                      1st Qu.:1.1578
## Median :-0.1168
                    Median :-1.71700
                                      Median :1.4834
## Mean
         : 0.0000
                     Mean
                           :-1.59933
                                      Mean
                                              :1.5993
## 3rd Qu.: 0.4143
                     3rd Qu.:-1.18453
                                        3rd Qu.:2.0131
                            :-0.04073
## Max.
          : 1.5631
                     {\tt Max.}
                                        Max.
                                               :3.1669
# Scatter plot of predicted
ggplot(df, aes(x = predicted, y = quality, colour = quality))+
geom_point(alpha = 0.3, position = position_jitter()) + stat_smooth()
```



The scatter plot supports the summary of the predicted interval, in the ranges of the fit, # lower, and upper ranges. The R-squared value of 0.3283 of the model, indicates that this # information can be predicted 33% of the time, with the data available, for the variance # of the information.

CART

```
set.seed(4)
# Subset both train and test sets, to exclude "quality_target"
# Using non-transformed versions of train and test, to get actual values in the nodes
subset(wine_train, select = -c(quality_target)) -> rf_wine_train
subset(wine_test, select = -c(quality_target)) -> rf_wine_test

# Convert target variable to factor to ensure proper interpretation by model
rf_wine_train$quality <- as.factor(rf_wine_train$quality)

# Begin model...
rPartTree <- rpart(quality ~ ., data = rf_wine_train)

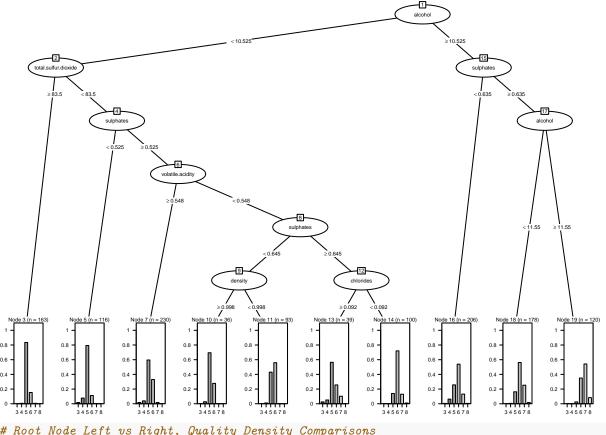
rpartTree2 <- as.party(rPartTree)

# R-Squared plot
par(mfrow=c(1,2))
rsq.rpart(rPartTree)</pre>
```

```
##
## Classification tree:
## rpart(formula = quality ~ ., data = rf_wine_train)
## Variables actually used in tree construction:
## [1] alcohol
                             chlorides
                                                    density
## [4] sulphates
                             total.sulfur.dioxide volatile.acidity
##
## Root node error: 730/1281 = 0.56987
##
## n= 1281
##
           CP nsplit rel error xerror
##
## 1 0.230137
                    0
                        1.00000 1.00000 0.024274
## 2 0.019635
                    1
                        0.76986 0.78493 0.024378
## 3 0.015753
                    4
                        0.71096 0.77945 0.024361
## 4 0.012329
                    6
                        0.67945 0.76027 0.024295
## 5 0.010000
                        0.64247 0.73151 0.024173
                     Apparent
                      X Relative
      0.8
                                                      1.0
                                                X Relative Error
      9.0
R-square
                                                      0
                                                      0
      0.4
                                                      \infty
                                                      o.
      0.2
                                                      0.7
      0.0
                                                      9
            0
                  2
                                    8
                                                            0
                                                                  2
                                                                                    8
                        4
                              6
                                                                        4
                                                                              6
                 Number of Splits
                                                                 Number of Splits
# Results
rpartTree2
##
## Model formula:
## quality ~ fixed.acidity + volatile.acidity + citric.acid + residual.sugar +
       chlorides + free.sulfur.dioxide + total.sulfur.dioxide +
       density + pH + sulphates + alcohol
##
##
## Fitted party:
## [1] root
       [2] alcohol < 10.525
           [3] total.sulfur.dioxide >= 83.5: 5 (n = 163, err = 16.6%)
## |
```

[4] total.sulfur.dioxide < 83.5

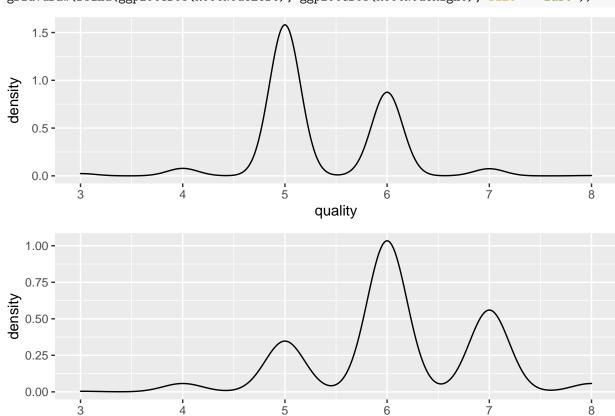
```
[5] sulphates < 0.525: 5 (n = 116, err = 20.7%)
##
               [6] sulphates >= 0.525
                   [7] volatile.acidity \geq 0.5475: 5 (n = 230, err = 40.4%)
                    [8] volatile.acidity < 0.5475
##
##
                        [9] sulphates < 0.645
                            [10] density \geq 0.9977: 5 (n = 36, err = 30.6%)
## |
                            [11] density < 0.9977: 6 (n = 93, err = 44.1%)
##
                        [12] sulphates >= 0.645
##
##
                            [13] chlorides \geq 0.0925: 5 (n = 39, err = 43.6%)
                            [14] chlorides < 0.0925: 6 (n = 100, err = 28.0%)
##
##
       [15] alcohol >= 10.525
           [16] sulphates < 0.635: 6 (n = 206, err = 46.1%)
##
           [17] sulphates >= 0.635
##
               [18] alcohol < 11.55: 6 (n = 178, err = 43.8%)
## I
               [19] alcohol \geq 11.55: 7 (n = 120, err = 45.8%)
##
## Number of inner nodes:
## Number of terminal nodes: 10
plot(rpartTree2, gp = gpar(fontsize=4))
```



```
# Root Node Left vs Right, Quality Density Comparisons
grid.newpage()
filter(wine_train, alcohol < 10.525) %>%
  dplyr::select(quality, alcohol) %>%
  ggplot(aes(x = quality)) + geom_density() -> RootNodeLeft
```

```
filter(wine_train, alcohol >= 10.525) %>%
  dplyr::select(quality, alcohol) %>%
  ggplot(aes(x = quality)) + geom_density() -> RootNodeRight

grid.draw(rbind(ggplotGrob(RootNodeLeft), ggplotGrob(RootNodeRight), size = "last"))
```



Random Forest

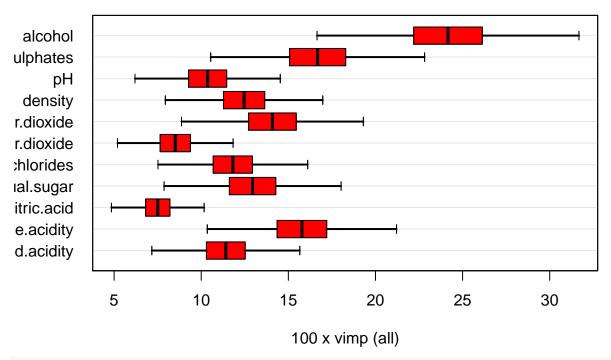
##

```
set.seed(4)
rf <- rfsrc(quality ~ ., data = rf_wine_train)</pre>
print(rf)
##
                             Sample size: 1281
##
              Frequency of class labels: 8, 37, 551, 511, 159, 15
##
                         Number of trees: 500
##
              Forest terminal node size: 1
          Average no. of terminal nodes: 247.234
##
##
  No. of variables tried at each split: 4
##
                 Total no. of variables: 11
##
          Resampling used to grow trees: swor
##
       Resample size used to grow trees: 810
##
                                Analysis: RF-C
```

quality

Family: class

```
Splitting rule: gini
##
                      (OOB) Brier score: 0.0667632
##
           (OOB) Normalized Brier score: 0.48069502
##
##
                              (OOB) AUC: 0.82205375
##
      (00B) Requested performance error: 0.29274005, 1, 1, 0.19419238, 0.28571429, 0.40251572, 0.866666
##
## Confusion matrix:
##
##
             predicted
##
     observed 3 4
                   5
                        6 7 8 class.error
##
            3 0 1
                    5
                        2 0 0
                                    1.0000
            4 0 0 25 12 0 0
                                    1.0000
##
            5 0 1 444 100 6 0
##
                                    0.1942
##
            6 0 0 117 363 31 0
                                    0.2896
##
            7 0 0
                  7 58 93 1
                                    0.4151
##
            8 0 0
                    0
                       4 9 2
                                    0.8667
##
         (OOB) Misclassification rate: 0.2958626
##
# Variable Importance
vi <- subsample(rf, verbose = FALSE)</pre>
extract.subsample(vi)$var.jk.sel.Z
##
                                                            pvalue signif
                                       mean
                                                upper
                                                                     TRUE
## fixed.acidity
                         8.180121 11.410616 14.641111 2.212440e-12
## volatile.acidity
                        11.647117 15.779193 19.911270 3.590176e-14
                                                                     TRUE
                         5.482045 7.506582 9.531118 1.835635e-13
## citric.acid
                                                                     TRUE
## residual.sugar
                         9.081405 12.946072 16.810740 2.591304e-11
                                                                     TRUE
## chlorides
                         8.545886 11.814013 15.082139 6.946629e-13
                                                                     TRUE
## free.sulfur.dioxide 5.987560 8.512102 11.036643 1.941270e-11
                                                                     TRUE
## total.sulfur.dioxide 10.116592 14.086624 18.056657 1.770066e-12
                                                                     TRUE
## density
                         9.022301 12.459023 15.895746 5.999366e-13
                                                                     TRUE
## pH
                         7.195548 10.367728 13.539909 7.478815e-11
                                                                     TRUE
## sulphates
                        12.010919 16.681529 21.352138 1.277993e-12
                                                                     TRUE
                        18.443184 24.163057 29.882931 6.175356e-17
## alcohol
                                                                     TRUE
# Variable Importance Plot
plot(vi)
```



```
# Predict
# https://www.rdocumentation.org/packages/randomForestSRC/versions/3.1.0/topics/predict.rfsrc
randomForestSRC::predict.rfsrc(rf, rf_wine_test)
```

```
##
     Sample size of test (predict) data: 318
##
                   Number of grow trees: 500
##
     Average no. of grow terminal nodes: 247.234
##
            Total no. of grow variables: 11
##
          Resampling used to grow trees: swor
##
       Resample size used to grow trees: 810
                                Analysis: RF-C
##
##
                                  Family: class
                             Brier score: 0.08004649
##
##
                 Normalized Brier score: 0.57633473
##
                                     AUC: 0.80679148
##
            Requested performance error: 0.36163522, 1, 1, 0.23846154, 0.30708661, 0.6, 1
##
##
  Confusion matrix:
##
             predicted
##
##
     observed 3 4 5
                      6
                         7 8 class.error
            3 0 0 2
                      0
                         0 0
                                   1.0000
##
            4 0 0 11
                      4
                                   1.0000
##
                        1 0
            5 0 0 99 31 0 0
                                   0.2385
##
            6 0 0 29 88 10 0
                                   0.3071
##
            7 0 0 4 20 16 0
##
                                   0.6000
##
            8 0 0 0
                      3
                        0 0
                                   1.0000
##
              Misclassification error: 0.3616352
##
```

Partial Least Squares

##

##

(Intercept)

h(volatile.acidity-0.26)

```
tctrl <- trainControl(method = "repeatedcv", repeats = 5, number =10)
set.seed(4)
pls_wine <- train(quality~ volatile.acidity + chlorides + total.sulfur.dioxide +
               sulphates + alcohol, data = wine_train,
                  method = "pls",
                  preProc = c("center", "scale", "BoxCox"),
                  tunelength =20,
                  trControl = tctrl)
pls_wine
## Partial Least Squares
## 1281 samples
##
      5 predictor
##
## Pre-processing: centered (5), scaled (5), Box-Cox transformation (5)
## Resampling: Cross-Validated (10 fold, repeated 5 times)
## Summary of sample sizes: 1153, 1153, 1154, 1153, 1152, ...
## Resampling results across tuning parameters:
##
##
     ncomp RMSE
                       Rsquared
                                  MAE
           0.6410968 0.3647402 0.4947294
##
     1
##
            0.6390156 0.3687722 0.4930808
           0.6388538 0.3691179 0.4921412
##
##
## RMSE was used to select the optimal model using the smallest value.
## The final value used for the model was ncomp = 3.
Mars Tuning
mars_wine <- earth(quality~ volatile.acidity + chlorides + total.sulfur.dioxide +
               sulphates + alcohol, data =wine_train)
mars_wine
## Selected 11 of 16 terms, and 5 of 5 predictors
## Termination condition: Reached nk 21
## Importance: alcohol, sulphates, volatile.acidity, chlorides, ...
## Number of terms at each degree of interaction: 1 10 (additive model)
## GCV 0.3995695
                   RSS 495.2041
                                    GRSq 0.3804081
                                                      RSq 0.3996191
summary(mars_wine)
```

Call: earth(formula=quality~volatile.acidity+chlorides+total.sulfur.di...),

coefficients

6.2560668

-0.7896152

data=wine_train)

```
## h(0.152-chlorides)
                                  2.8759318
## h(144-total.sulfur.dioxide)
                                  0.0020873
## h(0.82-sulphates)
                                 -1.9120561
## h(sulphates-0.82)
                                 -0.4929467
## h(alcohol-11.3)
                                 -3.4323569
## h(alcohol-11.4)
                                  6.5386404
## h(alcohol-11.7)
                                 -6.7169766
## h(alcohol-11.8)
                                  3.5629306
## h(12.4-alcohol)
                                 -0.2402167
##
## Selected 11 of 16 terms, and 5 of 5 predictors
## Termination condition: Reached nk 21
## Importance: alcohol, sulphates, volatile.acidity, chlorides, ...
## Number of terms at each degree of interaction: 1 10 (additive model)
## GCV 0.3995695
                    RSS 495.2041
                                    GRSq 0.3804081
                                                      RSq 0.3996191
preProc_Arguments = c("center", "scale")
marsGrid_wine = expand.grid(.degree=1:2, .nprune=2:38)
set.seed(4)
marsModel_wine = train(quality~ volatile.acidity + chlorides + total.sulfur.dioxide +
                       sulphates + alcohol, data =wine_train,
                       method="earth",
                       preProc=preProc_Arguments,
                       tuneGrid=marsGrid wine)
marsModel wine
## Multivariate Adaptive Regression Spline
##
## 1281 samples
##
      5 predictor
##
## Pre-processing: centered (5), scaled (5)
## Resampling: Bootstrapped (25 reps)
## Summary of sample sizes: 1281, 1281, 1281, 1281, 1281, 1281, ...
## Resampling results across tuning parameters:
##
##
     degree nprune RMSE
                                Rsquared
                                           MAE
##
                     0.6958248 0.2461512 0.5467038
     1
              2
              3
                     0.6648091 0.3129951 0.5082758
##
     1
##
              4
                     0.6486695 0.3467222 0.4987637
     1
##
              5
                     0.6489489 0.3466279 0.4992545
     1
##
              6
                     0.6505245 0.3440970 0.4996087
     1
              7
##
     1
                     0.6501727 0.3449717
                                           0.4995417
##
     1
              8
                     0.6495943 0.3465777 0.4989477
##
     1
             9
                     0.6495414 0.3468115 0.4985270
             10
                     0.6507816 0.3450530 0.4999083
##
     1
##
     1
             11
                     0.6505098 0.3460652 0.4997600
##
     1
             12
                     0.6520164 0.3438562 0.5003093
##
            13
     1
                     0.6539775 0.3411943 0.5015090
##
     1
             14
                     0.6552017 0.3392044
                                           0.5023241
##
             15
     1
                     0.6549327 0.3396373
                                           0.5020724
##
     1
             16
                     0.6549506 0.3396558 0.5021755
```

##	1	17	0.6549506	0.3396558	0.5021755
##	1	18	0.6549506	0.3396558	0.5021755
##	1	19	0.6549506	0.3396558	0.5021755
##	1	20	0.6549506	0.3396558	0.5021755
##	1	21	0.6549506	0.3396558	0.5021755
##	1	22	0.6549506	0.3396558	0.5021755
##	1	23	0.6549506	0.3396558	0.5021755
##	1	24	0.6549506	0.3396558	0.5021755
##	1	25	0.6549506	0.3396558	0.5021755
##	1	26	0.6549506	0.3396558	0.5021755
##	1	27	0.6549506	0.3396558	0.5021755
##	1	28	0.6549506	0.3396558	0.5021755
##	1	29	0.6549506	0.3396558	0.5021755
##	1	30	0.6549506	0.3396558	0.5021755
##	1	31	0.6549506	0.3396558	0.5021755
##	1	32	0.6549506	0.3396558	0.5021755
##	1	33	0.6549506	0.3396558	0.5021755
##	1	34	0.6549506	0.3396558	0.5021755
##	1	35	0.6549506	0.3396558	0.5021755
##	1	36	0.6549506	0.3396558	0.5021755
##	1	37	0.6549506	0.3396558	0.5021755
##	1	38	0.6549506	0.3396558	0.5021755
##	2	2	0.6954928	0.2468476	0.5463763
##	2	3	0.6954926	0.2466476	0.5463763
		4			0.4936360
##	2		0.6454110 0.6422467	0.3522298	
##	2	5		0.3598510	0.4931323
##		6	0.6437021	0.3580451	0.4932673
##	2	7	0.6444236	0.3580010	0.4944992
##	2	8	0.6468150	0.3544162	0.4953825
##	2	9	0.6483401	0.3524432	0.4964011
##	2	10	0.6507646	0.3491618	0.4975523
##	2	11	0.6523252	0.3471198	0.4982322
##	2	12	0.6540995	0.3445165	0.4984894
##	2	13	0.6542404	0.3445736	0.4985894
##	2	14	0.6550265	0.3443170	0.4985331
##	2	15	0.6560467	0.3430849	0.4987826
##	2	16	0.6562863	0.3426595	0.4989498
##	2	17	0.6560625	0.3428740	0.4988956
##	2	18	0.6564013	0.3423725	0.4989296
##	2	19	0.6564013	0.3423725	0.4989296
##	2	20	0.6564013	0.3423725	0.4989296
##	2	21	0.6564013	0.3423725	0.4989296
##	2	22	0.6564013	0.3423725	0.4989296
##	2	23	0.6564013	0.3423725	0.4989296
##	2	24	0.6564013	0.3423725	0.4989296
##	2	25	0.6564013	0.3423725	0.4989296
##	2	26	0.6564013	0.3423725	0.4989296
##	2	27	0.6564013	0.3423725	0.4989296
##	2	28	0.6564013	0.3423725	0.4989296
##	2	29	0.6564013	0.3423725	0.4989296
##	2	30	0.6564013	0.3423725	0.4989296
##	2	31	0.6564013	0.3423725	0.4989296
##	2	32	0.6564013	0.3423725	0.4989296
##	2	33	0.6564013	0.3423725	0.4989296

```
2
##
            34
                    0.6564013 0.3423725 0.4989296
##
    2
            35
                    0.6564013 0.3423725 0.4989296
##
    2
            36
                    0.6564013 0.3423725 0.4989296
##
    2
            37
                    0.6564013 0.3423725 0.4989296
##
            38
                    0.6564013 0.3423725 0.4989296
##
## RMSE was used to select the optimal model using the smallest value.
## The final values used for the model were nprune = 5 and degree = 2.
```

KNN Neighbors

```
set.seed(4)
knn_wine <- train(quality~ volatile.acidity + chlorides + total.sulfur.dioxide +
              sulphates + alcohol, data =wine_train,
              method = "knn",
              preProc = c("center", "scale"),
              tuneGrid = data.frame(.k = 1:50),
              trControl = trainControl(method = "cv"))
knn_wine
## k-Nearest Neighbors
##
## 1281 samples
##
     5 predictor
##
## Pre-processing: centered (5), scaled (5)
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 1153, 1153, 1153, 1154, 1153, 1152, ...
## Resampling results across tuning parameters:
##
##
        RMSE
                   Rsquared
##
     1 0.7417840 0.3247830 0.4177499
##
     2 0.6974146 0.3323450 0.4696999
##
     3 0.6731901 0.3448979 0.4791641
##
     4 0.6665302 0.3467985 0.4836518
##
     5 0.6533331 0.3600591 0.4824286
     6 0.6457641 0.3687854 0.4794655
##
##
     7 0.6430043 0.3710435 0.4799530
##
     8 0.6416843 0.3717036 0.4821467
##
     9 0.6339821 0.3832671 0.4796633
##
    10 0.6354233 0.3804117 0.4819247
    11 0.6338017 0.3827153 0.4821245
##
##
    12 0.6360295 0.3780547 0.4844249
##
    13 0.6366929 0.3757671 0.4856975
##
    14 0.6349456 0.3781415 0.4862533
##
    15 0.6338248 0.3798528 0.4858869
##
    16 0.6351536 0.3769359 0.4873973
##
    17 0.6335827 0.3795098 0.4862066
##
    18 0.6325047 0.3814530 0.4848592
##
    19 0.6325468 0.3809950 0.4861473
```

```
##
    20 0.6307150 0.3843236 0.4845210
##
    21 0.6333513 0.3793499 0.4872637
    22 0.6344618 0.3769321 0.4892463
##
##
    23 0.6341257 0.3778016 0.4894453
##
    24 0.6334651 0.3789900 0.4900132
##
    25 0.6320417 0.3818758 0.4891855
##
    26 0.6325094 0.3809279 0.4899857
##
    27 0.6319274 0.3823033 0.4905126
##
    28 0.6316129 0.3832613 0.4907701
##
    29 0.6310374 0.3848262 0.4909850
##
    30 0.6309881 0.3848130 0.4908735
##
    31 0.6298325 0.3870258 0.4899401
##
    32 0.6298265 0.3871018 0.4907527
##
    33 0.6301718 0.3862833 0.4908459
##
    34 0.6292436 0.3880411 0.4897946
##
    35 0.6292789
                  0.3881321
                             0.4899380
##
    36 0.6291079 0.3885095 0.4893900
##
    37 0.6307087 0.3854649 0.4905386
##
    38 0.6307204 0.3856069 0.4900028
##
    39 0.6301815 0.3866979 0.4898142
##
    40 0.6298177 0.3875118 0.4901264
##
    41 0.6286737 0.3897724 0.4892917
##
    42 0.6280837 0.3911209 0.4889145
    43 0.6275018 0.3922607
                             0.4888636
##
##
    44 0.6277265 0.3918345 0.4891569
##
    45 0.6278012 0.3918612 0.4889342
##
    46 0.6281747 0.3912383 0.4892897
##
    47 0.6278795 0.3918446 0.4896199
##
    48 0.6273854 0.3931893 0.4891903
##
    49 0.6279997 0.3919908 0.4901511
##
    50 0.6286275 0.3907562 0.4906589
##
## RMSE was used to select the optimal model using the smallest value.
## The final value used for the model was k = 48.
```

SVM

```
11 predictor
##
##
## Pre-processing: centered (11), scaled (11)
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 1153, 1153, 1153, 1154, 1153, 1152, ...
## Resampling results across tuning parameters:
##
##
           RMSE
                     Rsquared
##
    0.25  0.6253012  0.3968055  0.4644470
##
    0.50 0.6184829 0.4095823 0.4549595
    1.00 0.6130196 0.4198850 0.4475702
##
     2.00 0.6135949 0.4206505 0.4458400
##
     4.00 0.6207280 0.4117663 0.4492851
##
\#\# Tuning parameter 'sigma' was held constant at a value of 0.08844672
## RMSE was used to select the optimal model using the smallest value.
## The final values used for the model were sigma = 0.08844672 and C = 1.
```