# ADS 503 - Team 7

## Summer Purschke, Jacqueline Urenda, Oscar Gil

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```
# R Libraries
library(caret)
library(AppliedPredictiveModeling)
library(Hmisc)
library(dplyr)
library(tidyverse)
library(ggplot2)
library(corrplot)
library(MASS)
library(ISLR)
library(rpart)
library(partykit)
library(randomForestSRC)
library(earth)
library(MARSS)
library(e1071)
library(summarytools)
library(grid)
```

Load the Red Wine Quality data set from GitHub - data set copied from Kaggle and imported into GitHub.

```
wine <- read.csv(
  url("https://raw.githubusercontent.com/OscarG-DataSci/ADS503/main/winequality-red.csv")
      , header = TRUE)</pre>
```

# **Data Summary**

#### **Data Frame Summary**

wine Dimensions:  $1599 \times 12$ 

Duplicates: 240

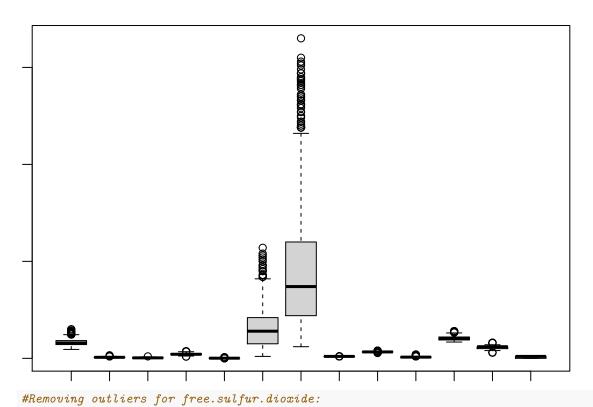
No	Variable	Stats / Values	Freqs (% of Valid)	Graph	Missing
1	fixed.acidity [numeric]	Mean (sd): $8.3 (1.7)$ min $<$ med $<$ max: 4.6 < 7.9 < 15.9 IQR (CV): 2.1 (0.2)	96 distinct values		0 (0.0%)
2	volatile.acidity [numeric]	Mean (sd): $0.5 (0.2)$ min < med < max: 0.1 < 0.5 < 1.6 IQR (CV): $0.2 (0.3)$	143 distinct values		0 (0.0%)
3	citric.acid [numeric]	Mean (sd) : $0.3 (0.2)$ min < med < max: 0 < 0.3 < 1 IQR (CV) : $0.3 (0.7)$	80 distinct values		0 (0.0%)
4	residual.sugar [numeric]	Mean (sd): 2.5 (1.4) min < med < max: 0.9 < 2.2 < 15.5 IQR (CV): 0.7 (0.6)	91 distinct values		0 (0.0%)
5	chlorides [numeric]	Mean (sd): $0.1$ (0) min < med < max: 0 < 0.1 < 0.6 IQR (CV): $0$ (0.5)	153 distinct values	<u></u>	0 (0.0%)
6	free.sulfur.dioxide [numeric]	Mean (sd): 15.9 (10.5) min < med < max: 1 < 14 < 72 IQR (CV): 14 (0.7)	60 distinct values		0 (0.0%)

No	Variable	Stats / Values	Freqs (% of Valid)	Graph	Missing
7	total.sulfur.dioxide [numeric]	Mean (sd): 46.5 (32.9) min < med < max: 6 < 38 < 289 IQR (CV): 40 (0.7)	144 distinct values		0 (0.0%)
8	density [numeric]	Mean (sd): 1 (0) min < med < max: 1 < 1 < 1 IQR (CV): 0 (0)	436 distinct values		0 (0.0%)
9	pH [numeric]	Mean (sd): 3.3 (0.2) min < med < max: 2.7 < 3.3 < 4 IQR (CV): 0.2 (0)	89 distinct values		0 (0.0%)
10	sulphates [numeric]	Mean (sd): $0.7 (0.2)$ min < med < max: 0.3 < 0.6 < 2 IQR (CV): $0.2 (0.3)$	96 distinct values		0 (0.0%)
11	alcohol [numeric]	Mean (sd): 10.4 (1.1) min < med < max: 8.4 < 10.2 < 14.9 IQR (CV): 1.6 (0.1)	65 distinct values		0 (0.0%)

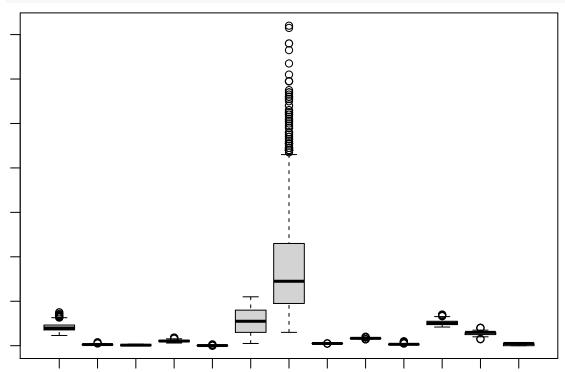
No	Variable	Stats / Values	Freqs (% of Valid)	Graph	Missing
12	quality [integer]	Mean (sd): $5.6$ (0.8) min < med < max: 3 < 6 < 8 IQR (CV): $1$ (0.1)	3: 10 ( 0.6%) 4: 53 ( 3.3%) 5: 681 (42.6%) 6: 638 (39.9%) 7: 199 (12.4%) 8: 18 ( 1.1%)	'	0 (0.0%)

#### **Pre-processing**

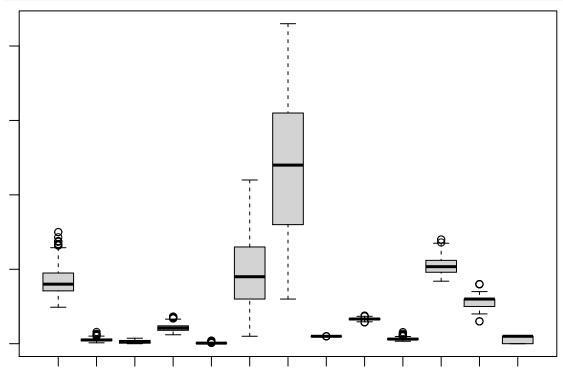
```
par(mar=c(1,1,1,1)) # to fix boxplot knit processing issues
# Create new variable, for quality values, split by half (0, 1)
wine$quality_target <- ifelse( wine$quality <= 5, 0, 1)</pre>
# Mean of new variable is at 0.5347 (close enough to 50% to maintain balance)
summary(wine$quality_target)
      Min. 1st Qu. Median
                              Mean 3rd Qu.
## 0.0000 0.0000 1.0000 0.5347 1.0000 1.0000
# Check for missing values in data set
wine %>% na.omit() %>% count() # there are no missing values
##
## 1 1599
# Removing outliers for residual sugar:
Q <- quantile(wine$residual.sugar, probs=c(.25, .75), na.rm = FALSE)
iqr_rs <- IQR(wine$residual.sugar)</pre>
up_rs <- Q[2]+1.5*iqr_rs # Upper Range
low_rs <- Q[1]-1.5*iqr_rs # Lower Range</pre>
eliminated_rs <- subset(wine, wine$residual.sugar > (Q[1] - 1.5*iqr_rs) & wine$residual.sugar < (Q[2]+1
boxplot(eliminated_rs)
```



```
Q2 <- quantile(wine$free.sulfur.dioxide, probs=c(.25, .75), na.rm = FALSE)
iqr_fs <- IQR(eliminated_rs$free.sulfur.dioxide)
up_fs <- Q2[2]+1.5*iqr_fs # Upper Range
low_fs <- Q2[1]-1.5*iqr_fs # Lower Range
eliminated_fs <- subset(eliminated_rs, eliminated_rs$free.sulfur.dioxide > (Q[1] - 1.5*iqr_fs) & elimin boxplot(eliminated_fs)
```



```
#Removing outliers for total.sulfur.dioxide:
Q3 <- quantile(wine$total.sulfur.dioxide, probs=c(.25, .75), na.rm = FALSE)
iqr_ts <- IQR(eliminated_fs$total.sulfur.dioxide)
up_ts <- Q3[2]+1.5*iqr_ts # Upper Range
low_ts <- Q3[1]-1.5*iqr_ts # Lower Range
eliminated_ts <- subset(eliminated_fs, eliminated_fs$total.sulfur.dioxide > (Q[1] - 1.5*iqr_ts) & eliminated_ts)
```

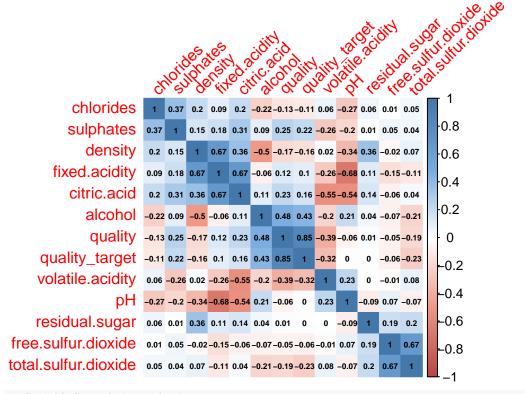


```
#Removing outliers for fixed.acidity:
Q4 <- quantile(wine$fixed.acidity, probs=c(.25, .75), na.rm = FALSE)
iqr_fa <- IQR(eliminated_ts$fixed.acidity)
up_fa <- Q[2]+1.5*iqr_fa # Upper Range
low_fa <- Q[1]-1.5*iqr_fa # Lower Range
eliminated_fa <- subset(eliminated_ts, eliminated_ts$fixed.acidity > (Q[1] - 1.5*iqr_fa) & eliminated_t
boxplot(eliminated_fa)
```

```
new_wine_data <- eliminated_fa

# Removing outliers reduced dimension of data set from 1599 observations to 48

# team opted not to use new_wine_data and keep outlier data
dim(new_wine_data)
```



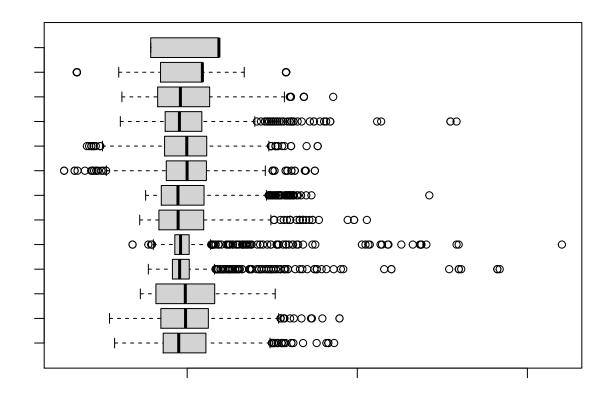
```
# Cutoff Correlation features
cutoffCorr <- findCorrelation(cor, cutoff = .8)
cutoffCorrFeatures <- wine[, -cutoffCorr]

# Train and Test split
wine_split <- createDataPartition(wine$quality, p = .8, list = FALSE)
wine_train <- wine[ wine_split,]
wine_test <- wine[-wine_split,]

# Transform Train Data
train_trans <- preProcess(wine_train, method = c("center", "scale"))
train_transformed <- predict(train_trans, wine_train)

# Transform Test Data
test_trans <- preProcess(wine_test, method = c("center", "scale"))
test_transformed <- predict(test_trans, wine_test)

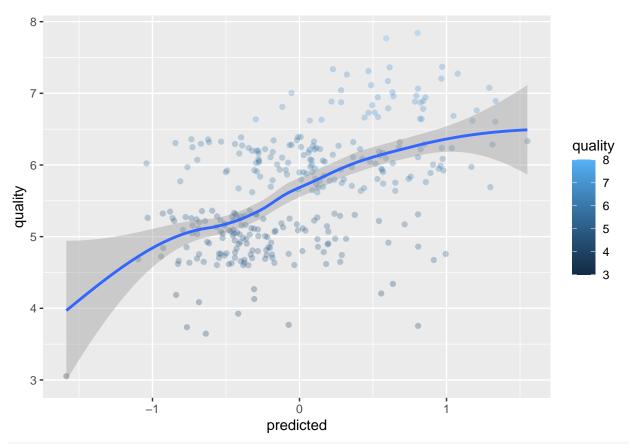
# Boxplot of transformed train data
boxplot(train_transformed, horizontal = TRUE, las = 2, cex.axis = .65, cex.lab = 7)</pre>
```



## Logistic Regression Model

```
# Cutoff Correlation string to copy + paste into feature area of model
subset(cutoffCorrFeatures, select = -c(quality_target)) %>%
      colnames() %>%
     paste0(collapse = " + ")
## [1] "fixed.acidity + volatile.acidity + citric.acid + residual.sugar + chlorides + free.sulfur.dioxi
set.seed(4)
# Model using "quality_target" as target variable
lmodel1 <- lm(quality_target~ volatile.acidity + sulphates + alcohol, data = train_transformed)</pre>
summary(lmodel1)
##
## Call:
## lm(formula = quality_target ~ volatile.acidity + sulphates +
       alcohol, data = train_transformed)
##
##
## Residuals:
                  1Q
                      Median
## -3.00967 -0.71610 -0.03202 0.75503 2.07175
## Coefficients:
##
                      Estimate Std. Error t value Pr(>|t|)
                                           0.000
## (Intercept)
                   -3.737e-15 2.405e-02
## volatile.acidity -2.094e-01 2.538e-02 -8.249 3.95e-16 ***
                     1.381e-01 2.502e-02
                                           5.521 4.07e-08 ***
## sulphates
```

```
## alcohol
                    3.706e-01 2.467e-02 15.020 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.8608 on 1277 degrees of freedom
## Multiple R-squared: 0.2608, Adjusted R-squared: 0.2591
## F-statistic: 150.2 on 3 and 1277 DF, p-value: < 2.2e-16
# Model using "quality" as target variable
lmodel2 <- lm(quality~ volatile.acidity + sulphates + alcohol, data = train_transformed)</pre>
summary(lmodel2)
##
## Call:
## lm(formula = quality ~ volatile.acidity + sulphates + alcohol,
      data = train_transformed)
## Residuals:
      Min
               1Q Median
                               ЗQ
                                      Max
## -3.3627 -0.4659 -0.0807 0.5825 2.6769
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   -5.684e-16 2.273e-02
                                          0.000
## volatile.acidity -2.563e-01 2.399e-02 -10.683 < 2e-16 ***
## sulphates
                    1.592e-01 2.364e-02
                                          6.733 2.5e-11 ***
## alcohol
                    4.087e-01 2.332e-02 17.527 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.8135 on 1277 degrees of freedom
## Multiple R-squared: 0.3397, Adjusted R-squared: 0.3382
## F-statistic:
                219 on 3 and 1277 DF, p-value: < 2.2e-16
# Add predicted values to new data frame
wine test %>%
 mutate(predicted = predict(lmodel2, newdata = test_transformed)) -> df
# Summary of predicted interval
predict(lmodel2, newdata = test_transformed, interval = "prediction") %>%
 summary()
##
        fit
                           lwr
                                              upr
## Min. :-1.58572
                             :-3.20536
                                                :0.03391
                     Min.
                                         Min.
                                         1st Qu.:1.18282
## 1st Qu.:-0.41602
                     1st Qu.:-2.01530
## Median :-0.07018
                     Median :-1.66892
                                         Median :1.52813
## Mean
         : 0.00000
                      Mean
                            :-1.59850
                                         Mean
                                               :1.59850
## 3rd Qu.: 0.41586
                      3rd Qu.:-1.18207
                                         3rd Qu.:2.01379
## Max.
          : 1.55001
                             :-0.05255
                                         Max.
                                                :3.15257
                     {	t Max.}
# Scatter plot of predicted
ggplot(df, aes(x = predicted, y = quality, colour = quality))+
geom_point(alpha = 0.3, position = position_jitter()) + stat_smooth()
```



# The scatter plot supports the summary of the predicted interval, in the ranges of the fit, # lower, and upper ranges. The R-squared value of 0.3283 of the model, indicates that this # information can be predicted 33% of the time, with the data available, for the variance # of the information.

#### **CART**

```
set.seed(4)
# Subset both train and test sets, to exclude "quality_target"
# Using non-transformed versions of train and test, to get actual values in the nodes
subset(wine_train, select = -c(quality_target)) -> rf_wine_train
subset(wine_test, select = -c(quality_target)) -> rf_wine_test

rPartTree <- rpart(quality ~ ., data = rf_wine_train)

rpartTree2 <- as.party(rPartTree)

# R-Squared plot
par(mfrow=c(1,2))
rsq.rpart(rPartTree)

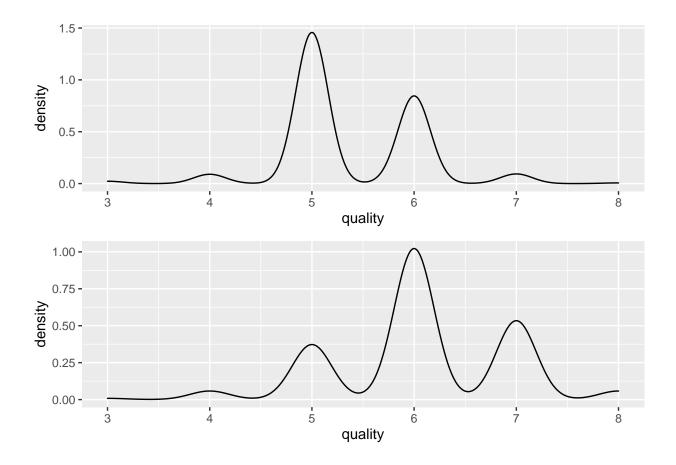
##
## Regression tree:
## rpart(formula = quality ~ ., data = rf_wine_train)
##</pre>
```

```
## Variables actually used in tree construction:
## [1] alcohol
                         sulphates
                                            volatile.acidity
##
## Root node error: 846.48/1281 = 0.6608
##
## n= 1281
##
##
           CP nsplit rel error xerror
## 1 0.177055
                        1.00000 1.00133 0.043043
## 2 0.061856
                    1
                        0.82294 0.86268 0.041009
## 3 0.033949
                    2
                        0.76109 0.80492 0.036499
## 4 0.033148
                    3
                        0.72714 0.78692 0.035181
## 5 0.022754
                    4
                        0.69399 0.76507 0.034959
## 6 0.021017
                    5
                        0.67124 0.74352 0.034234
## 7 0.014882
                    6
                        0.65022 0.72416 0.033199
## 8 0.010000
                        0.63534 0.69828 0.032057
                      Apparent
                      X Relative
      0.8
                                                      1.0
                                                X Relative Error
R-square
      ဖ
                                                      6.0
      ö
                                                      0.8
      0.4
                                                      0.7
      0.2
                                                      9.0
      0.0
            0
                1
                    2
                        3
                            4
                                5
                                                                    2
                                                                        3
                                                                                5
                                    6
                                       7
                                                            0
                                                                            4
                                                                                    6
                                                                                       7
                 Number of Splits
                                                                 Number of Splits
# Results
rpartTree2
##
## Model formula:
  quality ~ fixed.acidity + volatile.acidity + citric.acid + residual.sugar +
##
       chlorides + free.sulfur.dioxide + total.sulfur.dioxide +
##
       density + pH + sulphates + alcohol
##
## Fitted party:
##
  [1] root
##
       [2] alcohol < 10.525
##
            [3] sulphates < 0.575: 5.135 (n = 318, err = 111.2)
##
            [4] sulphates >= 0.575
                [5] volatile.acidity \geq 0.335: 5.449 (n = 412, err = 161.9)
## |
```

[6] volatile.acidity < 0.335: 6.055 (n = 55, err = 30.8)

```
[7] alcohol >= 10.525
## |
## |
           [8] sulphates < 0.585
               [9] volatile.acidity >= 0.385
                   [10] volatile.acidity >= 1: 4.000 (n = 7, err = 4.0)
## |
##
                   [11] volatile.acidity < 1: 5.393  (n = 89, err = 47.2)
               [12] volatile.acidity < 0.385: 6.188 (n = 32, err = 10.9)
## |
           [13] sulphates >= 0.585
##
               [14] alcohol < 11.55: 6.032 (n = 222, err = 106.8)
##
##
               [15] alcohol \geq 11.55: 6.603 (n = 146, err = 65.0)
##
## Number of inner nodes:
## Number of terminal nodes: 8
plot(rpartTree2, gp = gpar(fontsize=4))
# Root Node Left vs Right, Quality Density Comparisons
grid.newpage()
filter(wine_train, alcohol < 10.525) %>%
  dplyr::select(quality, alcohol) %>%
  ggplot(aes(x = quality)) + geom_density() -> RootNodeLeft
filter(wine_train, alcohol >= 10.525) %>%
  dplyr::select(quality, alcohol) %>%
  ggplot(aes(x = quality)) + geom_density() -> RootNodeRight
```

grid.draw(rbind(ggplotGrob(RootNodeLeft), ggplotGrob(RootNodeRight), size = "last"))



## Random Forest

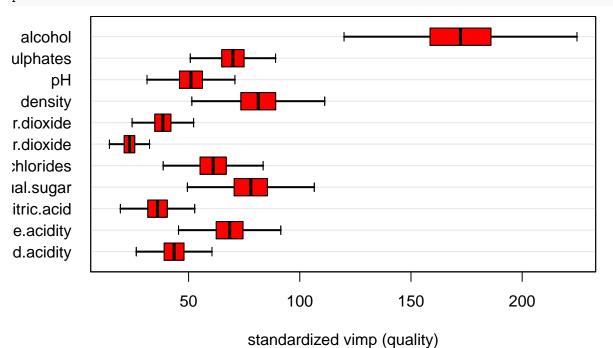
```
set.seed(4)
rf <- rfsrc(quality ~ ., data = rf_wine_train)</pre>
print(rf)
                             Sample size: 1281
##
##
                         Number of trees: 500
##
              Forest terminal node size: 5
          Average no. of terminal nodes: 154.44
##
  No. of variables tried at each split: 4
##
                 Total no. of variables: 11
##
##
          Resampling used to grow trees: swor
##
       Resample size used to grow trees: 810
##
                                Analysis: RF-R
##
                                  Family: regr
##
                          Splitting rule: mse
                         (OOB) R squared: 0.47483782
##
##
      (OOB) Requested performance error: 0.34729603
# Variable Importance
vi <- subsample(rf, verbose = FALSE)</pre>
```

#### extract.subsample(vi)\$var.jk.sel.Z

```
pvalue signif
                            lower
                                       mean
                                                upper
                                             56.44027 2.268062e-11
                                                                      TRUE
## fixed.acidity
                         30.55005
                                   43.49516
## volatile.acidity
                                                                      TRUE
                         50.98391
                                   68.47067
                                             85.95743 8.311031e-15
## citric.acid
                         23.32641
                                   36.03789
                                             48.74937 1.375194e-08
                                                                      TRUE
## residual.sugar
                         56.28516
                                   77.99340
                                             99.70164 9.491215e-13
                                                                      TRUE
                                                                      TRUE
## chlorides
                         43.94843 61.04596
                                             78.14348 1.298541e-12
## free.sulfur.dioxide
                                                                      TRUE
                         16.55683 23.41198
                                             30.26714 1.087685e-11
## total.sulfur.dioxide
                         27.90961 38.42750
                                             48.94539 4.010368e-13
                                                                      TRUE
## density
                         58.60194 81.33127 104.06059 1.164247e-12
                                                                      TRUE.
## pH
                         36.03962 51.07339
                                            66.10716 1.383412e-11
                                                                      TRUE
## sulphates
                         55.34834 69.93480 84.52126 2.805752e-21
                                                                      TRUE
## alcohol
                        132.42797 172.27663 212.12529 1.191053e-17
                                                                      TRUE
```

# # Variable Importance Plot

plot(vi)



#### # Predict

```
##
     Sample size of test (predict) data: 318
##
                   Number of grow trees: 500
##
     Average no. of grow terminal nodes: 154.44
##
            Total no. of grow variables: 11
##
          Resampling used to grow trees: swor
##
       Resample size used to grow trees: 810
##
                                Analysis: RF-R
##
                                  Family: regr
##
                               R squared: 0.4738014
##
            Requested performance error: 0.32482477
```

### Partial Least Squares

summary(mars\_wine)

```
tctrl <- trainControl(method = "repeatedcv", repeats = 5, number =10)
set.seed(4)
pls_wine <- train(quality~ volatile.acidity + chlorides + total.sulfur.dioxide +
               sulphates + alcohol, data = train_transformed,
                  method = "pls",
                  preProc = c("center", "scale", "BoxCox"),
                  tunelength =20,
                  trControl = tctrl)
pls_wine
## Partial Least Squares
## 1281 samples
##
      5 predictor
##
## Pre-processing: centered (5), scaled (5)
## Resampling: Cross-Validated (10 fold, repeated 5 times)
## Summary of sample sizes: 1153, 1153, 1154, 1153, 1152, ...
## Resampling results across tuning parameters:
##
##
    ncomp RMSE
                       Rsquared
                                  MAE
           0.8087530 0.3502403 0.6295864
##
     1
##
           0.8076009 0.3523703 0.6280769
           0.8078026 0.3520609 0.6279273
##
##
## RMSE was used to select the optimal model using the smallest value.
## The final value used for the model was ncomp = 2.
Mars Tuning
mars_wine <- earth(quality~ volatile.acidity + chlorides + total.sulfur.dioxide +
               sulphates + alcohol, data =train_transformed)
mars_wine
## Selected 14 of 16 terms, and 5 of 5 predictors
## Termination condition: Reached nk 21
## Importance: alcohol, sulphates, volatile.acidity, chlorides, ...
## Number of terms at each degree of interaction: 1 13 (additive model)
## GCV 0.6237366
                   RSS 765.6798
                                    GRSq 0.3767503
                                                      RSq 0.4018126
```

```
## Call: earth(formula=quality~volatile.acidity+chlorides+total.sulfur.di...),
##
               data=train_transformed)
##
##
                                      coefficients
## (Intercept)
                                         45.995356
## h(-1.22088-volatile.acidity)
                                         -0.646512
```

```
## h(volatile.acidity- -1.22088)
                                         -0.870343
## h(volatile.acidity- -0.77398)
                                          0.695562
## h(1.34361-chlorides)
                                          0.148853
## h(total.sulfur.dioxide- -1.09835)
                                        -34.386053
## h(total.sulfur.dioxide- -1.06769)
                                         24.754346
## h(total.sulfur.dioxide- -0.914415)
                                         -2.095996
## h(2.70295-total.sulfur.dioxide)
                                        -11.632045
## h(total.sulfur.dioxide-2.70295)
                                         11.949287
## h(0.491101-sulphates)
                                         -0.455812
## h(alcohol-0.565375)
                                          0.264400
## h(2.8584-alcohol)
                                         -0.258158
## h(alcohol-2.8584)
                                         -1.472078
## Selected 14 of 16 terms, and 5 of 5 predictors
## Termination condition: Reached nk 21
## Importance: alcohol, sulphates, volatile.acidity, chlorides, ...
## Number of terms at each degree of interaction: 1 13 (additive model)
## GCV 0.6237366
                    RSS 765.6798
                                    GRSq 0.3767503
                                                      RSq 0.4018126
preProc_Arguments = c("center", "scale")
marsGrid_wine = expand.grid(.degree=1:2, .nprune=2:38)
set.seed(4)
marsModel_wine = train(quality~ volatile.acidity + chlorides + total.sulfur.dioxide +
                       sulphates + alcohol, data = train transformed,
                       method="earth",
                       preProc=preProc_Arguments,
                       tuneGrid=marsGrid_wine)
marsModel_wine
## Multivariate Adaptive Regression Spline
##
## 1281 samples
##
      5 predictor
##
## Pre-processing: centered (5), scaled (5)
## Resampling: Bootstrapped (25 reps)
## Summary of sample sizes: 1281, 1281, 1281, 1281, 1281, 1281, ...
  Resampling results across tuning parameters:
##
##
##
            nprune RMSE
     degree
                                Rsquared
                                           MAE
##
             2
                     0.8850014 0.2312022
                                          0.7053687
##
              3
                     0.8377666 0.3099770 0.6500428
     1
##
     1
             4
                     0.8122972 0.3507056
                                          0.6324137
##
     1
             5
                     0.8114462 0.3525609 0.6303420
##
     1
             6
                     0.8136694 0.3495223 0.6310561
             7
##
     1
                     0.8156143 0.3463378 0.6319505
##
     1
             8
                     0.8167655 0.3447020 0.6332684
##
     1
             9
                     10
##
     1
                     0.8168680 0.3457867
                                           0.6312923
##
     1
            11
                     0.8174787 0.3455033
                                           0.6318670
##
            12
     1
                     0.8194375 0.3431718
                                          0.6319792
##
     1
            13
                     0.8189981 0.3435539
                                          0.6315615
```

##	1	14	0.8199610	0.3423760	0.6319039
##	1	15	0.8199553	0.3423410	0.6320242
##	1	16	0.8199553	0.3423410	0.6320242
##	1	17	0.8199553	0.3423410	0.6320242
##	1	18	0.8199553	0.3423410	0.6320242
##	1	19	0.8199553	0.3423410	0.6320242
##	1	20	0.8199553	0.3423410	0.6320242
##	1	21	0.8199553	0.3423410	0.6320242
##	1	22	0.8199553	0.3423410	0.6320242
##	1	23	0.8199553	0.3423410	0.6320242
##	1	24	0.8199553	0.3423410	0.6320242
##	1	25	0.8199553	0.3423410	0.6320242
##	1	26	0.8199553	0.3423410	0.6320242
##	1	27	0.8199553	0.3423410	0.6320242
##	1	28	0.8199553	0.3423410	0.6320242
##	1	29	0.8199553	0.3423410	0.6320242
##	1	30	0.8199553	0.3423410	0.6320242
##	1	31	0.8199553	0.3423410	0.6320242
##	1	32	0.8199553	0.3423410	0.6320242
##	1	33	0.8199553	0.3423410	0.6320242
##	1	34	0.8199553	0.3423410	0.6320242
##	1	35	0.8199553	0.3423410	0.6320242
##	1	36	0.8199553	0.3423410	0.6320242
##	1	37	0.8199553	0.3423410	0.6320242
##	1	38	0.8199553	0.3423410	0.6320242
##	2	2	0.8825968	0.2353626	0.7012423
##	2	3	0.8363814	0.3126894	0.7012423
##	2	4	0.8127832	0.3120094	0.6325345
##	2	5	0.8127832	0.3532361	0.6290777
##	2	6	0.8109811	0.3553752	0.6276453
##	2	7	0.8132258	0.3533752	0.6276455
##	2	8	0.8152948	0.3520718	0.6286829
	2	9	0.8173011	0.3481685	0.6294273
##	2	10	0.8225046	0.3415505	0.6328101
##					
##	2	11	0.8238200	0.3399769	0.6341545
##	2	12	0.8242273	0.3399923	0.6347160
##	2	13	0.8268848		0.6353942 0.6356580
##		14	0.8274111	0.3359898	
##	2	15	0.8282707	0.3351960	0.6362737
##	2	16	0.8287824	0.3346814	0.6368447 0.6370059
##	2	17	0.8290523	0.3343626	
##	2	18	0.8293898	0.3339941	0.6370909
##	2	19	0.8297997	0.3334811	0.6372150
##	2	20	0.8297997	0.3334811	0.6372150
##	2	21	0.8297997	0.3334811	0.6372150
##	2	22	0.8297997	0.3334811	0.6372150
##	2	23	0.8297997	0.3334811	0.6372150
##	2	24	0.8297997	0.3334811	0.6372150
##	2	25	0.8297997	0.3334811	0.6372150
##	2	26	0.8297997	0.3334811	0.6372150
##	2	27	0.8297997	0.3334811	0.6372150
##	2	28	0.8297997	0.3334811	0.6372150
##	2	29	0.8297997	0.3334811	0.6372150
##	2	30	0.8297997	0.3334811	0.6372150

```
##
     2
                     0.8297997 0.3334811 0.6372150
##
     2
            32
                    0.8297997 0.3334811 0.6372150
##
     2
            33
                    0.8297997 0.3334811 0.6372150
     2
                    0.8297997 0.3334811 0.6372150
##
            34
##
     2
            35
                     0.8297997 0.3334811
                                          0.6372150
##
    2
            36
                    0.8297997 0.3334811
                                         0.6372150
##
     2
            37
                     0.8297997 0.3334811
                                          0.6372150
##
                    0.8297997 0.3334811
            38
                                          0.6372150
##
## RMSE was used to select the optimal model using the smallest value.
## The final values used for the model were nprune = 6 and degree = 2.
```

## **KNN** Neighbors

```
set.seed(4)
knn_wine <- train(quality~ volatile.acidity + chlorides + total.sulfur.dioxide +
              sulphates + alcohol, data =train_transformed,
              method = "knn",
              preProc = c("center", "scale"),
              tuneGrid = data.frame(.k = 1:50),
              trControl = trainControl(method = "cv"))
knn_wine
## k-Nearest Neighbors
##
## 1281 samples
     5 predictor
##
##
## Pre-processing: centered (5), scaled (5)
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 1153, 1153, 1154, 1153, 1152, ...
## Resampling results across tuning parameters:
##
##
    k
        RMSE
                   Rsquared
                              MAE
##
       0.9427691
                   0.3097511
                              0.5501662
##
     2 0.8629831 0.3328498 0.5969983
##
     3 0.8368764 0.3405317 0.6030573
     4 0.8279773
##
                   0.3431394
                             0.6124601
##
     5 0.8221784 0.3450349
                              0.6199145
##
     6 0.8160131 0.3486007 0.6194493
##
     7 0.8095582 0.3567541 0.6199686
##
     8 0.8036826 0.3628989 0.6199448
##
     9 0.8021998 0.3639614 0.6214743
##
    10 0.8031749 0.3613022 0.6234298
##
    11 0.7984903 0.3675699 0.6202376
##
    12 0.7981756 0.3682820
                              0.6217025
##
    13 0.7960425 0.3708261 0.6220512
##
    14 0.7999649 0.3652795 0.6254455
##
    15 0.7988554 0.3663144 0.6247548
##
    16 0.7988248 0.3663441 0.6247859
```

```
##
    17 0.8004743 0.3639946 0.6249979
##
    18 0.7991022 0.3659568 0.6231131
##
    19 0.8003750 0.3639124 0.6252625
##
    20 0.8012480 0.3627424 0.6268121
##
       0.7990107 0.3662109 0.6258791
##
    22 0.7995840 0.3654909 0.6262162
##
    23 0.8009324 0.3641209 0.6285904
##
    24 0.8008281 0.3643124 0.6300182
##
    25 0.7985497 0.3681201 0.6281662
##
    26 0.7983149 0.3682929 0.6288287
##
    27 0.7972389 0.3702646 0.6280531
##
    28 0.7958480 0.3720008 0.6272963
##
    29 0.7954800 0.3721615 0.6265835
##
    30 0.7954088 0.3724957 0.6265261
##
    31 0.7959198 0.3716672 0.6274353
##
    32 0.7954233 0.3726451 0.6276219
##
    33 0.7937028 0.3754105 0.6269257
##
    34 0.7948998 0.3732350 0.6273414
##
    35 0.7953070 0.3725203 0.6274869
##
    36 0.7952432 0.3728494 0.6280948
##
    37 0.7956865 0.3720231 0.6277415
##
    38 0.7951890 0.3730701 0.6274628
##
    39 0.7945010 0.3741482 0.6271546
##
    40 0.7948020 0.3739603 0.6268306
##
    41 0.7945344 0.3746530 0.6268870
##
    42 0.7943813 0.3750086 0.6265858
##
    43 0.7944566 0.3751135 0.6267804
    44 0.7945235 0.3749604 0.6272007
##
##
    45 0.7938029 0.3763423 0.6263954
##
    46 0.7937111 0.3765468 0.6259715
    47 0.7945843 0.3750564
##
                             0.6266835
##
    48 0.7944131 0.3753720
                             0.6266935
##
    49 0.7934151 0.3770704 0.6262354
##
    50 0.7937482 0.3764827 0.6262795
## RMSE was used to select the optimal model using the smallest value.
## The final value used for the model was k = 49.
```

#### SVM

```
## Support Vector Machines with Radial Basis Function Kernel
##
## 1281 samples
##
    11 predictor
## Pre-processing: centered (11), scaled (11)
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 1153, 1153, 1153, 1154, 1153, 1152, ...
## Resampling results across tuning parameters:
##
##
    С
          RMSE
                     Rsquared
                                MAE
##
    0.25 0.7924102 0.3776305 0.5919455
##
    0.50 0.7820502 0.3919129 0.5818012
##
    1.00 0.7784482 0.3977921 0.5757303
##
    2.00 0.7764093 0.4021745 0.5719077
    4.00 0.7774002 0.4057215 0.5687248
##
##
## Tuning parameter 'sigma' was held constant at a value of 0.0959568
## RMSE was used to select the optimal model using the smallest value.
## The final values used for the model were sigma = 0.0959568 and C = 2.
```