## ADS 503 - Team 7

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## 06/12/2022

```
# R Libraries
library(caret)
library(AppliedPredictiveModeling)
library(Hmisc)
library(dplyr)
library(tidyverse)
library(ggplot2)
library(corrplot)
library(MASS)
library(ISLR)
library(rpart)
library(partykit)
library(randomForestSRC)
library(earth)
library(MARSS)
library(e1071)
library(summarytools)
library(grid)
```

Load the Red Wine Quality data set from GitHub - data set copied from Kaggle and imported into GitHub.

```
wine <- read.csv(
  url("https://raw.githubusercontent.com/OscarG-DataSci/ADS503/main/winequality-red.csv")
      , header = TRUE)</pre>
```

## **Data Summary**

#### **Data Frame Summary**

wine Dimensions:  $1599 \times 12$ 

Duplicates: 240

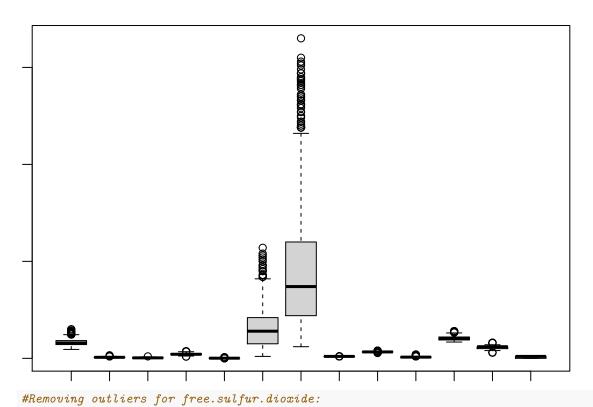
No	Variable	Stats / Values	Freqs (% of Valid)	Graph	Missing
1	fixed.acidity [numeric]	Mean (sd): $8.3 (1.7)$ min $<$ med $<$ max: 4.6 < 7.9 < 15.9 IQR (CV): 2.1 (0.2)	96 distinct values		0 (0.0%)
2	volatile.acidity [numeric]	Mean (sd): $0.5 (0.2)$ min < med < max: 0.1 < 0.5 < 1.6 IQR (CV): $0.2 (0.3)$	143 distinct values		0 (0.0%)
3	citric.acid [numeric]	Mean (sd) : $0.3 (0.2)$ min < med < max: 0 < 0.3 < 1 IQR (CV) : $0.3 (0.7)$	80 distinct values		0 (0.0%)
4	residual.sugar [numeric]	Mean (sd): 2.5 (1.4) min < med < max: 0.9 < 2.2 < 15.5 IQR (CV): 0.7 (0.6)	91 distinct values		0 (0.0%)
5	chlorides [numeric]	Mean (sd): $0.1$ (0) min < med < max: 0 < 0.1 < 0.6 IQR (CV): $0$ (0.5)	153 distinct values	<u></u>	0 (0.0%)
6	free.sulfur.dioxide [numeric]	Mean (sd): 15.9 (10.5) min < med < max: 1 < 14 < 72 IQR (CV): 14 (0.7)	60 distinct values		0 (0.0%)

No	Variable	Stats / Values	Freqs (% of Valid)	Graph	Missing
7	total.sulfur.dioxide [numeric]	Mean (sd): 46.5 (32.9) min < med < max: 6 < 38 < 289 IQR (CV): 40 (0.7)	144 distinct values		0 (0.0%)
8	density [numeric]	Mean (sd): 1 (0) min < med < max: 1 < 1 < 1 IQR (CV): 0 (0)	436 distinct values		0 (0.0%)
9	pH [numeric]	Mean (sd): 3.3 (0.2) min < med < max: 2.7 < 3.3 < 4 IQR (CV): 0.2 (0)	89 distinct values		0 (0.0%)
10	sulphates [numeric]	Mean (sd): $0.7 (0.2)$ min < med < max: 0.3 < 0.6 < 2 IQR (CV): $0.2 (0.3)$	96 distinct values		0 (0.0%)
11	alcohol [numeric]	Mean (sd): 10.4 (1.1) min < med < max: 8.4 < 10.2 < 14.9 IQR (CV): 1.6 (0.1)	65 distinct values		0 (0.0%)

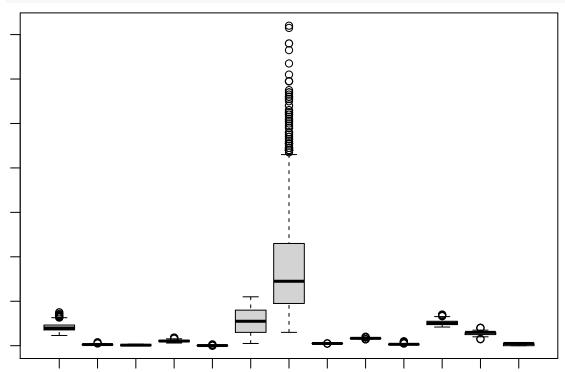
No	Variable	Stats / Values	Freqs (% of Valid)	Graph	Missing
12	quality [integer]	Mean (sd): $5.6$ (0.8) min < med < max: 3 < 6 < 8 IQR (CV): $1$ (0.1)	3: 10 ( 0.6%) 4: 53 ( 3.3%) 5: 681 (42.6%) 6: 638 (39.9%) 7: 199 (12.4%) 8: 18 ( 1.1%)	'	0 (0.0%)

### **Pre-processing**

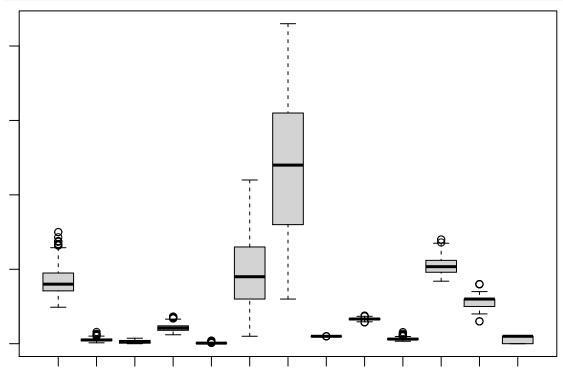
```
par(mar=c(1,1,1,1)) # to fix boxplot knit processing issues
# Create new variable, for quality values, split by half (0, 1)
wine$quality_target <- ifelse( wine$quality <= 5, 0, 1)</pre>
# Mean of new variable is at 0.5347 (close enough to 50% to maintain balance)
summary(wine$quality_target)
      Min. 1st Qu. Median
                              Mean 3rd Qu.
## 0.0000 0.0000 1.0000 0.5347 1.0000 1.0000
# Check for missing values in data set
wine %>% na.omit() %>% count() # there are no missing values
##
## 1 1599
# Removing outliers for residual sugar:
Q <- quantile(wine$residual.sugar, probs=c(.25, .75), na.rm = FALSE)
iqr_rs <- IQR(wine$residual.sugar)</pre>
up_rs <- Q[2]+1.5*iqr_rs # Upper Range
low_rs <- Q[1]-1.5*iqr_rs # Lower Range</pre>
eliminated_rs <- subset(wine, wine$residual.sugar > (Q[1] - 1.5*iqr_rs) & wine$residual.sugar < (Q[2]+1
boxplot(eliminated_rs)
```



```
Q2 <- quantile(wine$free.sulfur.dioxide, probs=c(.25, .75), na.rm = FALSE)
iqr_fs <- IQR(eliminated_rs$free.sulfur.dioxide)
up_fs <- Q2[2]+1.5*iqr_fs # Upper Range
low_fs <- Q2[1]-1.5*iqr_fs # Lower Range
eliminated_fs <- subset(eliminated_rs, eliminated_rs$free.sulfur.dioxide > (Q[1] - 1.5*iqr_fs) & elimin boxplot(eliminated_fs)
```



```
#Removing outliers for total.sulfur.dioxide:
Q3 <- quantile(wine$total.sulfur.dioxide, probs=c(.25, .75), na.rm = FALSE)
iqr_ts <- IQR(eliminated_fs$total.sulfur.dioxide)
up_ts <- Q3[2]+1.5*iqr_ts # Upper Range
low_ts <- Q3[1]-1.5*iqr_ts # Lower Range
eliminated_ts <- subset(eliminated_fs, eliminated_fs$total.sulfur.dioxide > (Q[1] - 1.5*iqr_ts) & eliminated_ts)
```

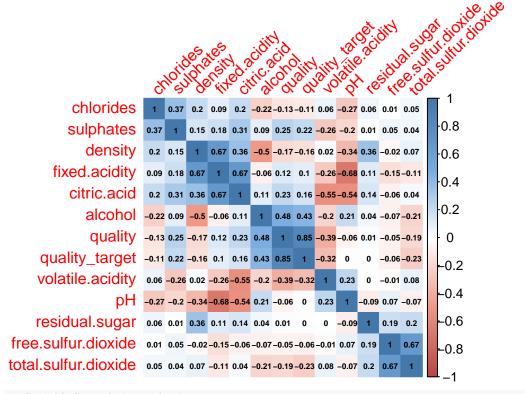


```
#Removing outliers for fixed.acidity:
Q4 <- quantile(wine$fixed.acidity, probs=c(.25, .75), na.rm = FALSE)
iqr_fa <- IQR(eliminated_ts$fixed.acidity)
up_fa <- Q[2]+1.5*iqr_fa # Upper Range
low_fa <- Q[1]-1.5*iqr_fa # Lower Range
eliminated_fa <- subset(eliminated_ts, eliminated_ts$fixed.acidity > (Q[1] - 1.5*iqr_fa) & eliminated_t
boxplot(eliminated_fa)
```

```
new_wine_data <- eliminated_fa

# Removing outliers reduced dimension of data set from 1599 observations to 48

# team opted not to use new_wine_data and keep outlier data
dim(new_wine_data)
```



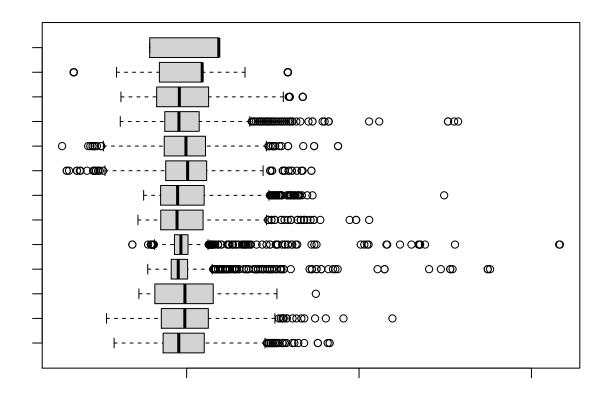
```
# Cutoff Correlation features
cutoffCorr <- findCorrelation(cor, cutoff = .8)
cutoffCorrFeatures <- wine[, -cutoffCorr]

# Train and Test split
wine_split <- createDataPartition(wine$quality, p = .8, list = FALSE)
wine_train <- wine[ wine_split,]
wine_test <- wine[-wine_split,]

# Transform Train Data
train_trans <- preProcess(wine_train, method = c("center", "scale"))
train_transformed <- predict(train_trans, wine_train)

# Transform Test Data
test_trans <- preProcess(wine_test, method = c("center", "scale"))
test_transformed <- predict(test_trans, wine_test)

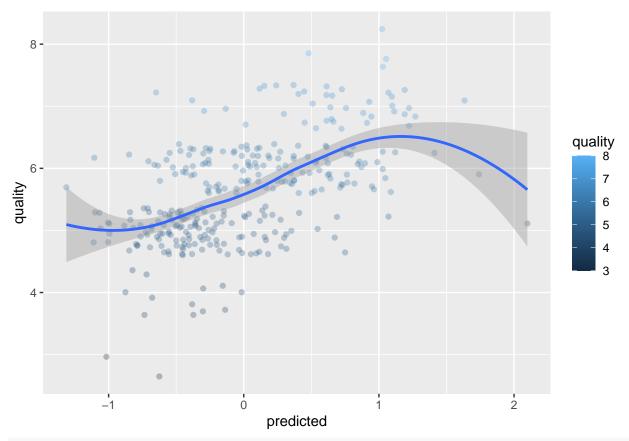
# Boxplot of transformed train data
boxplot(train_transformed, horizontal = TRUE, las = 2, cex.axis = .65, cex.lab = 7)</pre>
```



## Logistic Regression Model

```
# Cutoff Correlation string to copy + paste into feature area of model
subset(cutoffCorrFeatures, select = -c(quality_target)) %>%
      colnames() %>%
     paste0(collapse = " + ")
## [1] "fixed.acidity + volatile.acidity + citric.acid + residual.sugar + chlorides + free.sulfur.dioxi
set.seed(4)
# Model using "quality_target" as target variable
lmodel1 <- lm(quality_target~ volatile.acidity + sulphates + alcohol, data = train_transformed)</pre>
summary(lmodel1)
##
## Call:
## lm(formula = quality_target ~ volatile.acidity + sulphates +
       alcohol, data = train_transformed)
##
##
## Residuals:
                  1Q
                       Median
## -2.01994 -0.70808 -0.02156 0.77597
## Coefficients:
##
                      Estimate Std. Error t value Pr(>|t|)
                                           0.000
## (Intercept)
                    -3.395e-15 2.409e-02
## volatile.acidity -1.937e-01 2.519e-02 -7.691 2.91e-14 ***
                     1.402e-01 2.484e-02
                                           5.646 2.03e-08 ***
## sulphates
```

```
## alcohol
                    3.871e-01 2.457e-02 15.753 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.8622 on 1277 degrees of freedom
## Multiple R-squared: 0.2584, Adjusted R-squared: 0.2567
## F-statistic: 148.3 on 3 and 1277 DF, p-value: < 2.2e-16
# Model using "quality" as target variable
lmodel2 <- lm(quality~ volatile.acidity + sulphates + alcohol, data = train_transformed)</pre>
summary(lmodel2)
##
## Call:
## lm(formula = quality ~ volatile.acidity + sulphates + alcohol,
      data = train_transformed)
## Residuals:
      Min
               1Q Median
                               ЗQ
                                      Max
## -3.3710 -0.4761 -0.0750 0.5986 2.7090
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                    3.314e-16 2.280e-02
                                          0.000
## volatile.acidity -2.709e-01 2.384e-02 -11.362
                                                   <2e-16 ***
                                                    5e-09 ***
## sulphates
                    1.384e-01 2.351e-02
                                          5.888
## alcohol
                    4.150e-01 2.326e-02 17.844
                                                   <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.816 on 1277 degrees of freedom
## Multiple R-squared: 0.3358, Adjusted R-squared: 0.3342
## F-statistic: 215.2 on 3 and 1277 DF, p-value: < 2.2e-16
# Add predicted values to new data frame
wine test %>%
 mutate(predicted = predict(lmodel2, newdata = test_transformed)) -> df
# Summary of predicted interval
predict(lmodel2, newdata = test_transformed, interval = "prediction") %>%
 summary()
##
        fit
                           lwr
                                             upr
## Min. :-1.31279
                             :-2.9185
                     Min.
                                      Min.
                                              :0.293
## 1st Qu.:-0.45010
                     1st Qu.:-2.0521
                                      1st Qu.:1.152
                     Median :-1.6756
## Median :-0.07221
                                       Median :1.531
## Mean
         : 0.00000
                     Mean
                            :-1.6032
                                      Mean
                                              :1.603
## 3rd Qu.: 0.40626
                      3rd Qu.:-1.1957
                                        3rd Qu.:2.008
                                        Max.
                                               :3.711
## Max.
          : 2.09848
                     {\tt Max.}
                             : 0.4861
# Scatter plot of predicted
ggplot(df, aes(x = predicted, y = quality, colour = quality))+
geom_point(alpha = 0.3, position = position_jitter()) + stat_smooth()
```



# The scatter plot supports the summary of the predicted interval, in the ranges of the fit, # lower, and upper ranges. The R-squared value of 0.3283 of the model, indicates that this # information can be predicted 33% of the time, with the data available, for the variance # of the information.

#### CART

```
set.seed(4)
# Subset both train and test sets, to exclude "quality_target"
# Using non-transformed versions of train and test, to get actual values in the nodes
subset(wine_train, select = -c(quality_target)) -> rf_wine_train
subset(wine_test, select = -c(quality_target)) -> rf_wine_test

# Convert target variable to factor to ensure proper interpretation by model
rf_wine_train$quality <- as.factor(rf_wine_train$quality)

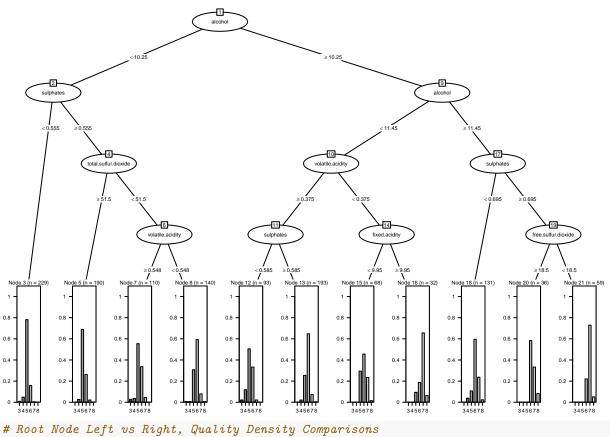
# Begin model...
rPartTree <- rpart(quality ~ ., data = rf_wine_train)

rpartTree2 <- as.party(rPartTree)

# R-Squared plot
par(mfrow=c(1,2))
rsq.rpart(rPartTree)</pre>
```

```
##
## Classification tree:
## rpart(formula = quality ~ ., data = rf_wine_train)
## Variables actually used in tree construction:
                                                    free.sulfur.dioxide
## [1] alcohol
                             fixed.acidity
## [4] sulphates
                             total.sulfur.dioxide volatile.acidity
##
## Root node error: 734/1281 = 0.57299
##
## n= 1281
##
           CP nsplit rel error xerror
##
## 1 0.234332
                    0
                        1.00000 1.00000 0.024120
## 2 0.018165
                    1
                        0.76567 0.78610 0.024261
## 3 0.014305
                    4
                        0.71117 0.76703 0.024202
## 4 0.014078
                    6
                        0.68256 0.76022 0.024178
## 5 0.012262
                        0.64033 0.75341 0.024152
## 6 0.010000
                        0.62807 0.73297 0.024067
                   10
                      Apparent
                      X Relative
      \infty
                                                      1.0
                                                X Relative Error
      9.0
R-square
                                                      တ
                                                      Ö.
      0.4
                                                      0.8
      0.2
                                                      0.7
      0.0
                                                      9.0
            0
                 2
                       4
                            6
                                  8
                                       10
                                                            0
                                                                 2
                                                                       4
                                                                            6
                                                                                  8
                                                                                       10
                 Number of Splits
                                                                 Number of Splits
# Results
rpartTree2
##
## Model formula:
## quality ~ fixed.acidity + volatile.acidity + citric.acid + residual.sugar +
       chlorides + free.sulfur.dioxide + total.sulfur.dioxide +
##
       density + pH + sulphates + alcohol
##
##
## Fitted party:
## [1] root
       [2] alcohol < 10.25
## |
          [3] sulphates < 0.555: 5 (n = 229, err = 21.8%)
```

```
[4] sulphates \geq 0.555
               [5] total.sulfur.dioxide >= 51.5: 5 (n = 190, err = 31.1%)
               [6] total.sulfur.dioxide < 51.5
                   [7] volatile.acidity \geq 0.5475: 5 (n = 110, err = 44.5%)
##
##
                   [8] volatile.acidity < 0.5475: 6 (n = 140, err = 40.7%)
       [9] alcohol >= 10.25
## |
           [10] alcohol < 11.45
## |
               [11] volatile.acidity >= 0.375
## |
##
                   [12] sulphates < 0.585: 5 (n = 93, err = 49.5%)
##
                   [13] sulphates \geq 0.585: 6 (n = 193, err = 35.2%)
               [14] volatile.acidity < 0.375
                   [15] fixed.acidity < 9.95: 6 (n = 68, err = 54.4%)
##
                   [16] fixed.acidity \geq 9.95: 7 (n = 32, err = 34.4%)
##
##
           [17] alcohol >= 11.45
               [18] sulphates < 0.695: 6 (n = 131, err = 40.5%)
##
##
               [19] sulphates >= 0.695
                   [20] free.sulfur.dioxide >= 18.5: 6 (n = 36, err = 41.7%)
##
                    [21] free.sulfur.dioxide < 18.5: 7 (n = 59, err = 27.1%)
##
## Number of inner nodes:
## Number of terminal nodes: 11
plot(rpartTree2, gp = gpar(fontsize=4))
```



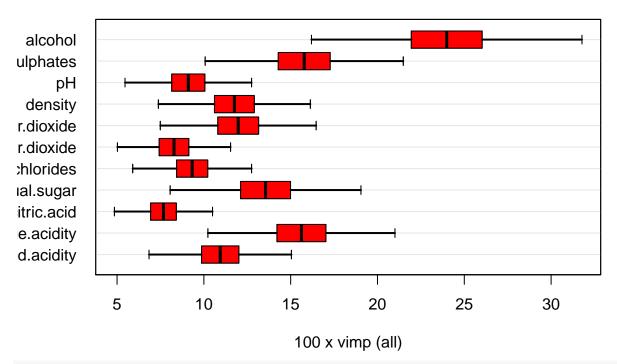
```
# Root Node Left vs Right, Quality Density Comparisons
grid.newpage()
filter(wine_train, alcohol < 10.525) %>%
  dplyr::select(quality, alcohol) %>%
  ggplot(aes(x = quality)) + geom_density() -> RootNodeLeft
```

```
filter(wine_train, alcohol >= 10.525) %>%
  dplyr::select(quality, alcohol) %>%
  ggplot(aes(x = quality)) + geom_density() -> RootNodeRight
grid.draw(rbind(ggplotGrob(RootNodeLeft), ggplotGrob(RootNodeRight), size = "last"))
    1.5 -
    1.0 -
density
    0.5 -
    0.0
                                            5
                                                 quality
   1.00 -
   0.75 -
density
0.50
   0.25 -
   0.00 -
                                            5
                                                             6
                                                 quality
```

## Random Forest

```
set.seed(4)
rf <- rfsrc(quality ~ ., data = rf_wine_train)</pre>
print(rf)
##
                             Sample size: 1281
##
              Frequency of class labels: 8, 41, 547, 511, 160, 14
##
                         Number of trees: 500
##
              Forest terminal node size: 1
          Average no. of terminal nodes: 251.55
##
## No. of variables tried at each split: 4
##
                 Total no. of variables: 11
##
          Resampling used to grow trees: swor
##
       Resample size used to grow trees: 810
```

```
Analysis: RF-C
##
##
                                 Family: class
                         Splitting rule: gini
##
##
                      (OOB) Brier score: 0.06888955
           (OOB) Normalized Brier score: 0.49600479
##
##
                              (OOB) AUC: 0.81308972
##
      (OOB) Requested performance error: 0.28883685, 1, 1, 0.19561243, 0.26027397, 0.43125, 0.85714286
##
## Confusion matrix:
##
##
            predicted
##
     observed 3 4 5
                        6 7 8 class.error
            3 0 1
                    5
                       2 0 0
                                    1.0000
##
##
            4 1 0 25 14 1 0
                                    1.0000
##
            5 1 2 440 100 4 0
                                    0.1956
##
            6 0 1 110 376 24 0
                                    0.2642
##
           7 0 0
                    4 64 91 1
                                    0.4312
                       8 4 2
                                    0.8571
##
            8 0 0
##
         (OOB) Misclassification rate: 0.2903981
##
# Variable Importance
vi <- subsample(rf, verbose = FALSE)</pre>
extract.subsample(vi)$var.jk.sel.Z
                                                            pvalue signif
                            lower
                                       mean
                                                upper
## fixed.acidity
                         7.822284 10.942251 14.062217 3.122965e-12
                                                                     TRUE
## volatile.acidity
                        11.519656 15.619108 19.718560 4.084881e-14
                                                                     TRUE
## citric.acid
                         5.523488 7.673461 9.823434 1.323452e-12
                                                                     TRUE
## residual.sugar
                        9.372322 13.552866 17.733411 1.049014e-10
                                                                     TRUE
## chlorides
                         6.719966 9.324841 11.929716 1.139834e-12
                                                                     TRUE
## free.sulfur.dioxide
                         5.800015 8.279406 10.758796 2.976994e-11
                                                                     TRUE
## total.sulfur.dioxide 8.562416 11.977919 15.393422 3.133360e-12
                                                                     TRUE
## density
                         8.426709 11.756688 15.086667 2.261907e-12
                                                                     TRUE
## pH
                         6.330221 9.103185 11.876148 6.204633e-11
                                                                     TRUE
## sulphates
                       11.438171 15.779618 20.121064 5.250561e-13
                                                                     TRUE
                        18.060354 23.988110 29.915867 1.082823e-15
                                                                     TRUE
## alcohol
# Variable Importance Plot
plot(vi)
```



# # Predict # https://www.rdocumentation.org/packages/randomForestSRC/versions/3.1.0/topics/predict.rfsrc randomForestSRC::predict.rfsrc(rf, rf\_wine\_test)

```
##
     Sample size of test (predict) data: 318
##
                   Number of grow trees: 500
##
     Average no. of grow terminal nodes: 251.55
##
            Total no. of grow variables: 11
##
          Resampling used to grow trees: swor
##
       Resample size used to grow trees: 810
                                Analysis: RF-C
##
##
                                  Family: class
                             Brier score: 0.07125171
##
##
                 Normalized Brier score: 0.51301232
##
                                     AUC: 0.83566831
##
            Requested performance error: 0.31446541, 1, 1, 0.20149254, 0.27559055, 0.51282051, 1
##
##
   Confusion matrix:
##
##
             predicted
##
     observed 3 4
                    5
                        6
                           7 8 class.error
            3 0 0
                    2
                       0
                                    1.0000
##
                           0 0
            4 0 0 11
                                    1.0000
##
                       1
                          0 0
            5 0 0 107 23
                          4 0
                                    0.2015
##
            6 0 0
##
                   24 92 11 0
                                    0.2756
            7 0 0
                    3 15 19 2
##
                                    0.5128
##
            8 0 0
                       3
                          1 0
                                    1.0000
##
              Misclassification error: 0.3144654
##
```

## Partial Least Squares

```
tctrl <- trainControl(method = "repeatedcv", repeats = 5, number =10)
set.seed(4)
pls_wine <- train(quality~ volatile.acidity + chlorides + total.sulfur.dioxide +
               sulphates + alcohol, data = train_transformed,
                  method = "pls",
                  preProc = c("center", "scale", "BoxCox"),
                  tunelength =20,
                  trControl = tctrl)
pls_wine
## Partial Least Squares
## 1281 samples
##
      5 predictor
##
## Pre-processing: centered (5), scaled (5)
## Resampling: Cross-Validated (10 fold, repeated 5 times)
## Summary of sample sizes: 1153, 1153, 1153, 1154, 1153, 1152, ...
## Resampling results across tuning parameters:
##
##
     ncomp RMSE
                       Rsquared
                                  MAE
            0.8092217 0.3487899 0.6321922
##
     1
##
            0.8084946 0.3500058 0.6313616
            0.8085600 0.3499713 0.6312280
##
##
## RMSE was used to select the optimal model using the smallest value.
## The final value used for the model was ncomp = 2.
Mars Tuning
mars_wine <- earth(quality~ volatile.acidity + chlorides + total.sulfur.dioxide +
               sulphates + alcohol, data =train_transformed)
mars_wine
## Selected 15 of 16 terms, and 5 of 5 predictors
## Termination condition: Reached nk 21
## Importance: alcohol, volatile.acidity, sulphates, total.sulfur.dioxide, ...
## Number of terms at each degree of interaction: 1 14 (additive model)
## GCV 0.6320845
                    RSS 773.4543
                                    GRSq 0.3684089
                                                      RSq 0.3957388
summary(mars_wine)
```

```
## Call: earth(formula=quality~volatile.acidity+chlorides+total.sulfur.di...),
## data=train_transformed)
##
##

coefficients
## (Intercept) -2.5033210
## h(2.67395-volatile.acidity) 0.1991889
```

```
## h(volatile.acidity-2.67395)
                                     -0.6668072
## h(chlorides- -0.974217)
                                      3.1754977
## h(-0.0840505-chlorides)
                                      2.9589079
## h(chlorides- -0.0840505)
                                     -3.2562975
## h(total.sulfur.dioxide-1.4629)
                                     -0.3625056
## h(2.54092-total.sulfur.dioxide)
                                      0.0681306
## h(total.sulfur.dioxide-2.54092)
                                      0.7874583
                                      5.1631418
## h(sulphates-0.891645)
## h(0.950322-sulphates)
                                     -0.4029818
## h(sulphates-0.950322)
                                     -5.9799150
## h(sulphates-1.77179)
                                      0.8950301
## h(alcohol-0.730876)
                                      0.2508004
## h(1.86099-alcohol)
                                     -0.2972706
##
## Selected 15 of 16 terms, and 5 of 5 predictors
## Termination condition: Reached nk 21
## Importance: alcohol, volatile.acidity, sulphates, total.sulfur.dioxide, ...
## Number of terms at each degree of interaction: 1 14 (additive model)
## GCV 0.6320845
                    RSS 773.4543
                                    GRSq 0.3684089
                                                      RSq 0.3957388
preProc_Arguments = c("center", "scale")
marsGrid_wine = expand.grid(.degree=1:2, .nprune=2:38)
set.seed(4)
marsModel_wine = train(quality~ volatile.acidity + chlorides + total.sulfur.dioxide +
                       sulphates + alcohol, data =train transformed,
                       method="earth",
                       preProc=preProc_Arguments,
                       tuneGrid=marsGrid_wine)
marsModel_wine
## Multivariate Adaptive Regression Spline
##
## 1281 samples
##
      5 predictor
##
## Pre-processing: centered (5), scaled (5)
## Resampling: Bootstrapped (25 reps)
## Summary of sample sizes: 1281, 1281, 1281, 1281, 1281, 1281, ...
## Resampling results across tuning parameters:
##
##
     degree nprune RMSE
                                Rsquared
##
              2
                     0.8772197 0.2325876 0.6968713
     1
              3
##
     1
                     0.8377194 0.3005966 0.6561111
              4
                     0.8098598 0.3462154 0.6318368
##
     1
##
     1
              5
                     0.8120630 0.3466304 0.6309034
              6
                     0.8192711 0.3390515 0.6325261
##
     1
##
     1
              7
                     0.8256888 0.3340875 0.6344632
##
     1
              8
                     0.8249701 0.3333771 0.6350216
##
             9
                     0.8220832 0.3374982 0.6336243
     1
##
     1
             10
                     0.8233786 0.3352357
                                           0.6334661
##
     1
             11
                     0.8245091 0.3336547
                                           0.6344863
##
     1
                     0.8274942 0.3319896 0.6358688
```

##	1	13	0.8286668	0.3303074	0.6368753
##	1	14	0.8334899	0.3277271	0.6383487
##	1	15	0.8337138	0.3276716	0.6383209
##	1	16	0.8337138	0.3276716	0.6383209
##	1	17	0.8337138	0.3276716	0.6383209
##	1	18	0.8337138	0.3276716	0.6383209
##	1	19	0.8337138	0.3276716	0.6383209
##	1	20	0.8337138	0.3276716	0.6383209
##	1	21	0.8337138	0.3276716	0.6383209
##	1	22	0.8337138	0.3276716	0.6383209
##	1	23	0.8337138	0.3276716	0.6383209
##	1	24	0.8337138	0.3276716	0.6383209
##	1	25	0.8337138	0.3276716	0.6383209
##	1	26	0.8337138	0.3276716	0.6383209
##	1	27	0.8337138	0.3276716	0.6383209
##	1	28	0.8337138	0.3276716	0.6383209
##	1	29	0.8337138	0.3276716	0.6383209
##	1	30	0.8337138	0.3276716	0.6383209
##	1	31	0.8337138	0.3276716	0.6383209
##	1	32	0.8337138	0.3276716	0.6383209
##	1	33	0.8337138	0.3276716	0.6383209
##	1	34	0.8337138	0.3276716	0.6383209
	1		0.8337138	0.3276716	0.6383209
##	1	35 36	0.8337138	0.3276716	0.6383209
##		36			
##	1	37	0.8337138	0.3276716	0.6383209
##	1	38	0.8337138	0.3276716	0.6383209
##	2	2	0.8798762	0.2279516	0.6983886
##	2	3	0.8400993	0.2973075	0.6617128
##	2	4	0.8135537	0.3413551	0.6336905
##	2	5	0.8072307	0.3520153	0.6286168
##	2	6	0.8064809	0.3533716	0.6261324
##	2	7	0.8035546	0.3583334	0.6231224
##	2	8	0.8057935	0.3573503	0.6232250
##	2	9	0.8090957	0.3519144	0.6260984
##	2	10	0.8144111	0.3474315	0.6286740
##	2	11	0.8188760	0.3415895	0.6321054
##	2	12	0.8246988	0.3375539	0.6335220
##	2	13	0.8250409	0.3376475	0.6339500
##	2	14	0.8254534	0.3371904	0.6340676
##	2	15	0.8247307	0.3384005	0.6335939
##	2	16	0.8253053	0.3378067	0.6338244
##	2	17	0.8263724	0.3364452	0.6344826
##	2	18	0.8263724	0.3364452	0.6344826
##	2	19	0.8263724	0.3364452	0.6344826
##	2	20	0.8263724	0.3364452	0.6344826
##	2	21	0.8263724	0.3364452	0.6344826
##	2	22	0.8263724	0.3364452	0.6344826
##	2	23	0.8263724	0.3364452	0.6344826
##	2	24	0.8263724	0.3364452	0.6344826
##	2	25	0.8263724	0.3364452	0.6344826
##	2	26	0.8263724	0.3364452	0.6344826
##	2	27	0.8263724	0.3364452	0.6344826
##	2	28	0.8263724	0.3364452	0.6344826
##	2	29	0.8263724	0.3364452	0.6344826

```
##
     2
             30
                     0.8263724 0.3364452 0.6344826
##
     2
             31
                     0.8263724 0.3364452 0.6344826
##
     2
             32
                     0.8263724 0.3364452 0.6344826
     2
             33
##
                     0.8263724 0.3364452
                                           0.6344826
##
     2
             34
                     0.8263724 0.3364452
                                           0.6344826
##
    2
             35
                     0.8263724 0.3364452 0.6344826
##
     2
             36
                     0.8263724 0.3364452
                                           0.6344826
##
     2
             37
                     0.8263724 0.3364452
                                           0.6344826
##
     2
                     0.8263724 0.3364452 0.6344826
##
## RMSE was used to select the optimal model using the smallest value.
## The final values used for the model were nprune = 7 and degree = 2.
```

#### **KNN Neighbors**

```
set.seed(4)
knn_wine <- train(quality~ volatile.acidity + chlorides + total.sulfur.dioxide +
              sulphates + alcohol, data =train_transformed,
              method = "knn",
              preProc = c("center", "scale"),
              tuneGrid = data.frame(.k = 1:50),
              trControl = trainControl(method = "cv"))
knn_wine
## k-Nearest Neighbors
##
## 1281 samples
##
     5 predictor
##
## Pre-processing: centered (5), scaled (5)
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 1153, 1153, 1153, 1154, 1153, 1152, ...
  Resampling results across tuning parameters:
##
##
    k
        RMSE
                   Rsquared
                              MAE
##
     1
       0.9502984
                   0.2991612
                              0.5486131
##
     2 0.8844451
                   0.3015216 0.6061430
##
     3 0.8625020
                   0.3075591
                              0.6185690
##
     4 0.8344760
                   0.3294039
                              0.6208217
##
     5 0.8178180 0.3484426 0.6151643
##
     6 0.8107219 0.3563340 0.6138202
##
     7 0.8028777 0.3650241 0.6093655
##
     8 0.8010857 0.3660416 0.6128788
##
     9 0.7963709 0.3719588 0.6106432
##
    10 0.7984982 0.3686980 0.6136400
##
    11 0.7959547
                   0.3714267
                              0.6135750
##
    12 0.7927222 0.3761906 0.6112068
##
    13 0.7915539
                   0.3770617
                              0.6120356
    14 0.7924647
##
                   0.3752828 0.6138970
##
    15 0.7918687 0.3769313 0.6134381
```

```
##
    16 0.7944776 0.3722746 0.6161107
    17 0.7964967 0.3692669 0.6175261
##
##
    18 0.7961766 0.3694947 0.6173256
##
    19 0.7966202 0.3682022 0.6182923
##
    20 0.7941559 0.3722440 0.6164731
##
    21 0.7950309 0.3707509 0.6176403
##
    22 0.7947911 0.3710394 0.6178171
##
    23 0.7944354 0.3714830 0.6180363
##
    24 0.7935100 0.3731100 0.6174050
##
    25 0.7939866 0.3720788 0.6185562
##
    26 0.7937022 0.3728013 0.6187629
##
    27 0.7931459 0.3740204 0.6182039
##
    28 0.7930188 0.3742001 0.6177695
##
    29 0.7930460 0.3741266 0.6174238
##
    30 0.7915465 0.3765013 0.6161953
##
    31 0.7913394 0.3767309 0.6167973
##
    32 0.7921529 0.3753747 0.6177052
##
    33 0.7930361 0.3742365 0.6189554
##
    34 0.7939773 0.3725938 0.6194651
##
    35 0.7940947 0.3727952 0.6195313
##
    36 0.7936816 0.3736685 0.6187028
##
    37 0.7946011 0.3722985 0.6197477
##
    38 0.7954886 0.3710285 0.6206054
##
    39 0.7945168 0.3728000 0.6206926
##
    40 0.7952116 0.3717022 0.6220040
##
    41 0.7948058 0.3725069 0.6213238
##
    42 0.7952223 0.3719802 0.6216250
    43 0.7959278 0.3708367 0.6222182
##
##
    44 0.7964459 0.3700022 0.6233678
##
    45 0.7963313 0.3703754 0.6232731
##
    46 0.7959668 0.3710433 0.6240970
##
    47 0.7956386 0.3717463 0.6242420
##
    48 0.7947695 0.3733183 0.6239088
##
    49 0.7944822 0.3740503 0.6236121
##
    50 0.7949465 0.3733624 0.6241523
##
## RMSE was used to select the optimal model using the smallest value.
## The final value used for the model was k = 31.
```

#### SVM

```
## Support Vector Machines with Radial Basis Function Kernel
##
## 1281 samples
##
    11 predictor
## Pre-processing: centered (11), scaled (11)
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 1153, 1153, 1153, 1154, 1153, 1152, ...
## Resampling results across tuning parameters:
##
##
    С
          RMSE
                     Rsquared
                                MAE
##
    0.25 0.7933984 0.3755164 0.5910630
##
    0.50 0.7802254 0.3948300 0.5759678
##
    1.00 0.7742886 0.4041230 0.5688540
##
    2.00 0.7745598 0.4059322 0.5662985
##
    4.00 0.7804442 0.4040349 0.5674192
##
## Tuning parameter 'sigma' was held constant at a value of 0.1039459
## RMSE was used to select the optimal model using the smallest value.
## The final values used for the model were sigma = 0.1039459 and C = 1.
```