ADS 503 - Team 7

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06/12/2022

```
# R Libraries
library(caret)
library(AppliedPredictiveModeling)
library(Hmisc)
library(dplyr)
library(tidyverse)
library(ggplot2)
library(corrplot)
library(MASS)
library(ISLR)
library(rpart)
library(partykit)
library(randomForestSRC)
library(earth)
library(MARSS)
library(e1071)
library(summarytools)
library(grid)
```

Load the Red Wine Quality data set from GitHub - data set copied from Kaggle and imported into GitHub.

```
wine <- read.csv(
  url("https://raw.githubusercontent.com/OscarG-DataSci/ADS503/main/winequality-red.csv")
      , header = TRUE)</pre>
```

Data Summary

Data Frame Summary

wine Dimensions: 1599×12

Duplicates: 240

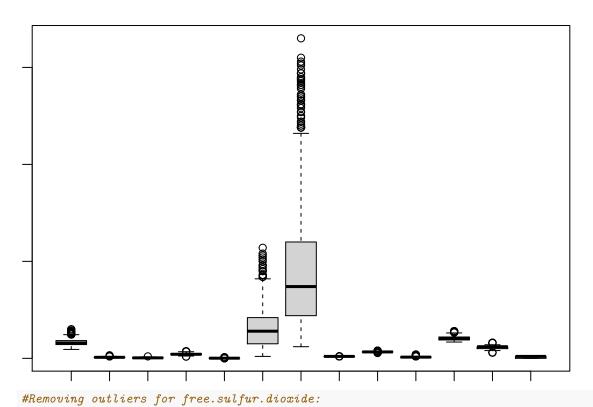
No	Variable	Stats / Values	Freqs (% of Valid)	Graph	Missing
1	fixed.acidity [numeric]	Mean (sd): $8.3 (1.7)$ min $<$ med $<$ max: 4.6 < 7.9 < 15.9 IQR (CV): 2.1 (0.2)	96 distinct values		0 (0.0%)
2	volatile.acidity [numeric]	Mean (sd): $0.5 (0.2)$ min < med < max: 0.1 < 0.5 < 1.6 IQR (CV): $0.2 (0.3)$	143 distinct values		0 (0.0%)
3	citric.acid [numeric]	Mean (sd) : $0.3 (0.2)$ min < med < max: 0 < 0.3 < 1 IQR (CV) : $0.3 (0.7)$	80 distinct values		0 (0.0%)
4	residual.sugar [numeric]	Mean (sd): 2.5 (1.4) min < med < max: 0.9 < 2.2 < 15.5 IQR (CV): 0.7 (0.6)	91 distinct values		0 (0.0%)
5	chlorides [numeric]	Mean (sd): 0.1 (0) min < med < max: 0 < 0.1 < 0.6 IQR (CV): 0 (0.5)	153 distinct values	<u></u>	0 (0.0%)
6	free.sulfur.dioxide [numeric]	Mean (sd): 15.9 (10.5) min < med < max: 1 < 14 < 72 IQR (CV): 14 (0.7)	60 distinct values		0 (0.0%)

No	Variable	Stats / Values	Freqs (% of Valid)	Graph	Missing
7	total.sulfur.dioxide [numeric]	Mean (sd): 46.5 (32.9) min < med < max: 6 < 38 < 289 IQR (CV): 40 (0.7)	144 distinct values		0 (0.0%)
8	density [numeric]	Mean (sd): 1 (0) min < med < max: 1 < 1 < 1 IQR (CV): 0 (0)	436 distinct values		0 (0.0%)
9	pH [numeric]	Mean (sd): 3.3 (0.2) min < med < max: 2.7 < 3.3 < 4 IQR (CV): 0.2 (0)	89 distinct values		0 (0.0%)
10	sulphates [numeric]	Mean (sd): $0.7 (0.2)$ min < med < max: 0.3 < 0.6 < 2 IQR (CV): $0.2 (0.3)$	96 distinct values		0 (0.0%)
11	alcohol [numeric]	Mean (sd): 10.4 (1.1) min < med < max: 8.4 < 10.2 < 14.9 IQR (CV): 1.6 (0.1)	65 distinct values		0 (0.0%)

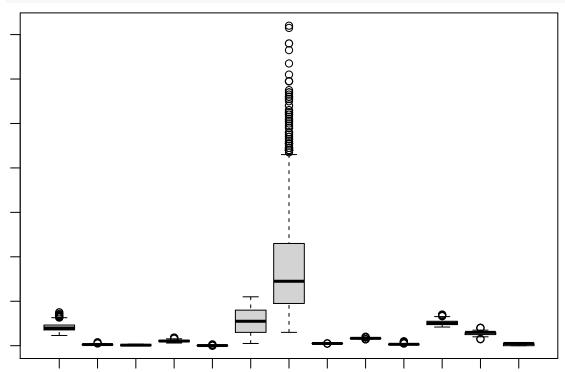
No	Variable	Stats / Values	Freqs (% of Valid)	Graph	Missing
12	quality [integer]	Mean (sd): 5.6 (0.8) min < med < max: 3 < 6 < 8 IQR (CV): 1 (0.1)	3: 10 (0.6%) 4: 53 (3.3%) 5: 681 (42.6%) 6: 638 (39.9%) 7: 199 (12.4%) 8: 18 (1.1%)	'	0 (0.0%)

Pre-processing

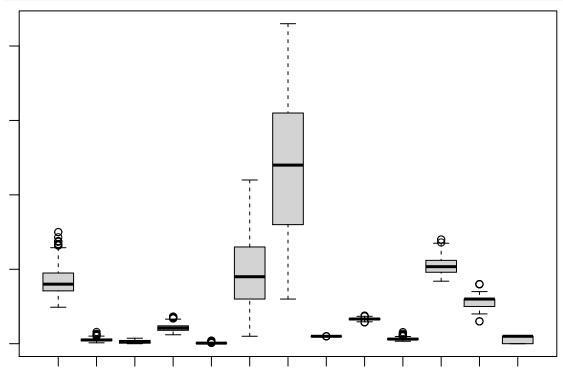
```
par(mar=c(1,1,1,1)) # to fix boxplot knit processing issues
# Create new variable, for quality values, split by half (0, 1)
wine$quality_target <- ifelse( wine$quality <= 5, 0, 1)</pre>
# Mean of new variable is at 0.5347 (close enough to 50% to maintain balance)
summary(wine$quality_target)
      Min. 1st Qu. Median
                              Mean 3rd Qu.
## 0.0000 0.0000 1.0000 0.5347 1.0000 1.0000
# Check for missing values in data set
wine %>% na.omit() %>% count() # there are no missing values
##
## 1 1599
# Removing outliers for residual sugar:
Q <- quantile(wine$residual.sugar, probs=c(.25, .75), na.rm = FALSE)
iqr_rs <- IQR(wine$residual.sugar)</pre>
up_rs <- Q[2]+1.5*iqr_rs # Upper Range
low_rs <- Q[1]-1.5*iqr_rs # Lower Range</pre>
eliminated_rs <- subset(wine, wine$residual.sugar > (Q[1] - 1.5*iqr_rs) & wine$residual.sugar < (Q[2]+1
boxplot(eliminated_rs)
```



```
Q2 <- quantile(wine$free.sulfur.dioxide, probs=c(.25, .75), na.rm = FALSE)
iqr_fs <- IQR(eliminated_rs$free.sulfur.dioxide)
up_fs <- Q2[2]+1.5*iqr_fs # Upper Range
low_fs <- Q2[1]-1.5*iqr_fs # Lower Range
eliminated_fs <- subset(eliminated_rs, eliminated_rs$free.sulfur.dioxide > (Q[1] - 1.5*iqr_fs) & elimin boxplot(eliminated_fs)
```



```
#Removing outliers for total.sulfur.dioxide:
Q3 <- quantile(wine$total.sulfur.dioxide, probs=c(.25, .75), na.rm = FALSE)
iqr_ts <- IQR(eliminated_fs$total.sulfur.dioxide)
up_ts <- Q3[2]+1.5*iqr_ts # Upper Range
low_ts <- Q3[1]-1.5*iqr_ts # Lower Range
eliminated_ts <- subset(eliminated_fs, eliminated_fs$total.sulfur.dioxide > (Q[1] - 1.5*iqr_ts) & eliminated_ts)
```

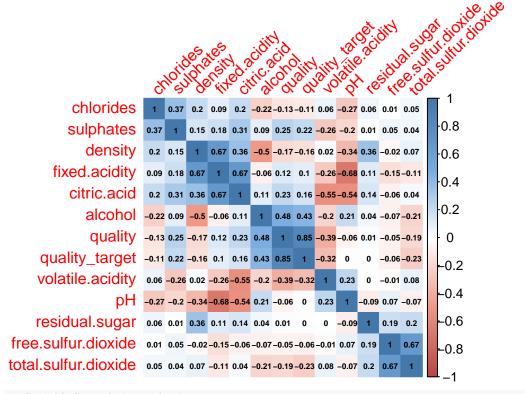


```
#Removing outliers for fixed.acidity:
Q4 <- quantile(wine$fixed.acidity, probs=c(.25, .75), na.rm = FALSE)
iqr_fa <- IQR(eliminated_ts$fixed.acidity)
up_fa <- Q[2]+1.5*iqr_fa # Upper Range
low_fa <- Q[1]-1.5*iqr_fa # Lower Range
eliminated_fa <- subset(eliminated_ts, eliminated_ts$fixed.acidity > (Q[1] - 1.5*iqr_fa) & eliminated_t
boxplot(eliminated_fa)
```

```
new_wine_data <- eliminated_fa

# Removing outliers reduced dimension of data set from 1599 observations to 48

# team opted not to use new_wine_data and keep outlier data
dim(new_wine_data)
```



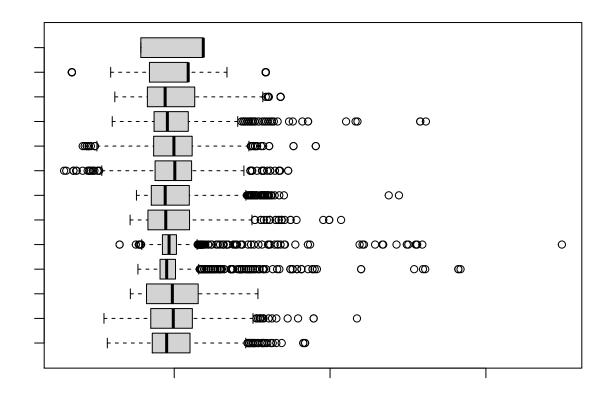
```
# Cutoff Correlation features
cutoffCorr <- findCorrelation(cor, cutoff = .8)
cutoffCorrFeatures <- wine[, -cutoffCorr]

# Train and Test split
wine_split <- createDataPartition(wine$quality, p = .8, list = FALSE)
wine_train <- wine[ wine_split,]
wine_test <- wine[-wine_split,]

# Transform Train Data
train_trans <- preProcess(wine_train, method = c("center", "scale"))
train_transformed <- predict(train_trans, wine_train)

# Transform Test Data
test_trans <- preProcess(wine_test, method = c("center", "scale"))
test_transformed <- predict(test_trans, wine_test)

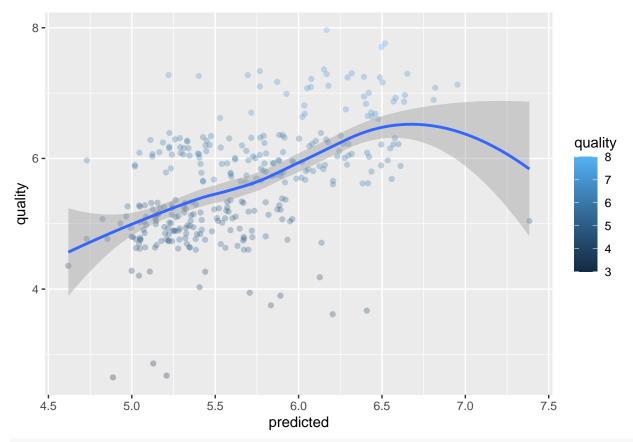
# Boxplot of transformed train data
boxplot(train_transformed, horizontal = TRUE, las = 2, cex.axis = .65, cex.lab = 7)</pre>
```



Logistic Regression Model

```
# Cutoff Correlation string to copy + paste into feature area of model
subset(cutoffCorrFeatures, select = -c(quality_target)) %>%
      colnames() %>%
     paste0(collapse = " + ")
## [1] "fixed.acidity + volatile.acidity + citric.acid + residual.sugar + chlorides + free.sulfur.dioxi
set.seed(4)
# Model using "quality_target" as target variable
lmodel1 <- lm(quality_target~ volatile.acidity + sulphates + alcohol, data = wine_train)</pre>
summary(lmodel1)
##
## Call:
## lm(formula = quality_target ~ volatile.acidity + sulphates +
       alcohol, data = wine_train)
##
##
## Residuals:
                1Q Median
                                ЗQ
                                       Max
## -1.0595 -0.3536 0.0053 0.3861
                                   1.0246
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
                                0.14282 -8.987 < 2e-16 ***
## (Intercept)
                   -1.28359
## volatile.acidity -0.55996
                                0.07064 -7.927 4.87e-15 ***
                                0.07666 6.015 2.35e-09 ***
## sulphates
                     0.46111
```

```
## alcohol
                    0.17393
                               0.01167 14.905 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.4309 on 1277 degrees of freedom
## Multiple R-squared: 0.256, Adjusted R-squared: 0.2543
## F-statistic: 146.5 on 3 and 1277 DF, p-value: < 2.2e-16
# Model using "quality" as target variable
lmodel2 <- lm(quality~ volatile.acidity + sulphates + alcohol, data = wine_train)</pre>
summary(lmodel2)
##
## Call:
## lm(formula = quality ~ volatile.acidity + sulphates + alcohol,
      data = wine_train)
## Residuals:
       Min
                 1Q
                     Median
                                           Max
                                   30
## -2.74152 -0.38150 -0.06589 0.48377 2.17397
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   2.44803
                              0.21704 11.279 < 2e-16 ***
## volatile.acidity -1.13840
                               0.10735 -10.604 < 2e-16 ***
## sulphates
                    0.80327
                               0.11650
                                        6.895 8.46e-12 ***
## alcohol
                    0.31349
                               0.01773 17.678 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.6548 on 1277 degrees of freedom
## Multiple R-squared: 0.3382, Adjusted R-squared: 0.3366
## F-statistic: 217.5 on 3 and 1277 DF, p-value: < 2.2e-16
# Add predicted values to new data frame
wine test %>%
 mutate(predicted = predict(lmodel2, newdata = wine_test)) -> df
# Summary of predicted interval
predict(lmodel2, newdata = wine_test, interval = "prediction") %>%
 summary()
##
        fit
                        lwr
                                        upr
## Min. :4.619
                  Min. :3.329
                                   Min.
                                         :5.910
## 1st Qu.:5.261
                   1st Qu.:3.976
                                   1st Qu.:6.548
## Median :5.592
                                   Median :6.878
                  Median :4.307
## Mean
         :5.660
                  Mean :4.373
                                   Mean
                                         :6.946
## 3rd Qu.:5.999
                   3rd Qu.:4.713
                                   3rd Qu.:7.284
## Max.
          :7.384
                  {\tt Max.}
                          :6.090
                                   Max.
                                          :8.678
# Scatter plot of predicted
ggplot(df, aes(x = predicted, y = quality, colour = quality))+
geom_point(alpha = 0.3, position = position_jitter()) + stat_smooth()
```



The scatter plot supports the summary of the predicted interval, in the ranges of the fit, # lower, and upper ranges. The R-squared value of 0.3283 of the model, indicates that this # information can be predicted 33% of the time, with the data available, for the variance # of the information.

CART

```
set.seed(4)
# Subset both train and test sets, to exclude "quality_target"
# Using non-transformed versions of train and test, to get actual values in the nodes
subset(wine_train, select = -c(quality_target)) -> rf_wine_train
subset(wine_test, select = -c(quality_target)) -> rf_wine_test

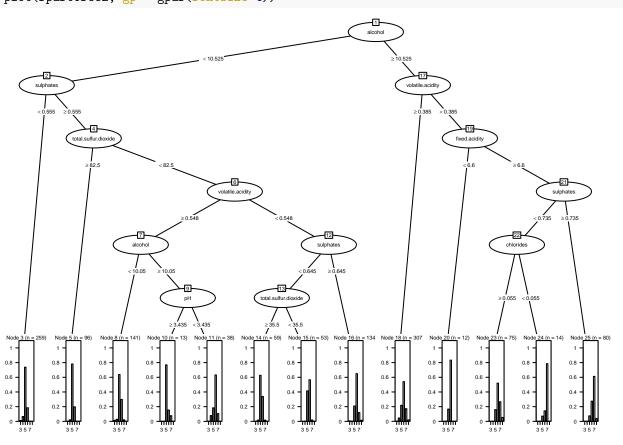
# Convert target variable to factor to ensure proper interpretation by model
rf_wine_train$quality <- as.factor(rf_wine_train$quality)

# Begin model...
rPartTree <- rpart(quality ~ ., data = rf_wine_train)
rpartTree2 <- as.party(rPartTree)

# R-Squared plot
par(mfrow=c(1,2))
rsq.rpart(rPartTree)</pre>
```

```
##
## Classification tree:
## rpart(formula = quality ~ ., data = rf_wine_train)
## Variables actually used in tree construction:
## [1] alcohol
                             chlorides
                                                    fixed.acidity
## [4] pH
                             sulphates
                                                    total.sulfur.dioxide
## [7] volatile.acidity
##
## Root node error: 733/1281 = 0.57221
## n= 1281
##
##
           CP nsplit rel error xerror
## 1 0.206003
                        1.00000 1.00000 0.024158
## 2 0.022738
                    1
                        0.79400 0.80355 0.024335
## 3 0.012278
                    4
                        0.72578 0.80082 0.024329
## 4 0.010914
                        0.65211 0.76535 0.024225
                   10
## 5 0.010000
                        0.63029 0.76262 0.024216
                   12
                      Apparent
                      X Relative
      \infty
                                                      1.0
                                                X Relative Error
      9.0
R-square
                                                      တ
      0.4
                                                      0.8
      0.2
      0.0
            0
                 2
                     4
                          6
                              8
                                  10
                                                                 2
                                                                     4
                                                                              8
                                                                                  10
                                                            0
                                                                          6
                 Number of Splits
                                                                 Number of Splits
# Results
rpartTree2
##
## Model formula:
## quality ~ fixed.acidity + volatile.acidity + citric.acid + residual.sugar +
       chlorides + free.sulfur.dioxide + total.sulfur.dioxide +
##
       density + pH + sulphates + alcohol
##
##
## Fitted party:
## [1] root
## |
       [2] alcohol < 10.525
          [3] sulphates < 0.555: 5 (n = 259, err = 26.3%)
```

```
[4] sulphates >= 0.555
                [5] total.sulfur.dioxide >= 82.5: 5 (n = 96, err = 21.9%)
                [6] total.sulfur.dioxide < 82.5
                    [7] volatile.acidity >= 0.5475
## |
## |
                        [8] alcohol < 10.05: 5 (n = 141, err = 36.2%)
                        [9] alcohol >= 10.05
## |
                            [10] pH \geq= 3.435: 5 (n = 13, err = 23.1%)
## |
                            [11] pH < 3.435: 6 (n = 38, err = 36.8%)
##
                        ##
                    [12] volatile.acidity < 0.5475
##
                        [13] sulphates < 0.645
                            [14] total.sulfur.dioxide \geq= 35.5: 5 (n = 59, err = 37.3%)
                            [15] total.sulfur.dioxide < 35.5: 6 (n = 53, err = 43.4%)
##
                        [16] sulphates >= 0.645: 6 (n = 134, err = 35.1%)
##
## |
       [17] alcohol >= 10.525
## |
            [18] volatile.acidity \geq 0.385: 6 (n = 307, err = 45.9%)
## |
            [19] volatile.acidity < 0.385
                [20] fixed.acidity < 6.6: 6 (n = 12, err = 16.7\%)
## |
                [21] fixed.acidity >= 6.6
                    [22] sulphates < 0.735
##
##
                        [23] chlorides \geq 0.0555: 6 (n = 75, err = 48.0%)
                        [24] chlorides < 0.0555: 7 (n = 14, err = 21.4%)
## |
## |
                    [25] sulphates \geq= 0.735: 7 (n = 80, err = 38.8%)
##
## Number of inner nodes:
                              12
## Number of terminal nodes: 13
plot(rpartTree2, gp = gpar(fontsize=4))
```



```
# Root Node Left vs Right, Quality Density Comparisons
grid.newpage()
filter(wine_train, alcohol < 10.525) %>%
  dplyr::select(quality, alcohol) %>%
  ggplot(aes(x = quality)) + geom_density() -> RootNodeLeft
filter(wine_train, alcohol >= 10.525) %>%
  dplyr::select(quality, alcohol) %>%
  ggplot(aes(x = quality)) + geom_density() -> RootNodeRight
grid.draw(rbind(ggplotGrob(RootNodeLeft), ggplotGrob(RootNodeRight), size = "last"))
    1.5 -
    1.0 -
density
    0.5 -
    0.0 -
                                          5
                                                          6
                                               quality
   1.00 -
   0.75 -
density
   0.25 -
   0.00 -
                                          5
                                                          6
                                               quality
```

Random Forest

```
set.seed(4)

rf <- rfsrc(quality ~ ., data = rf_wine_train)

print(rf)

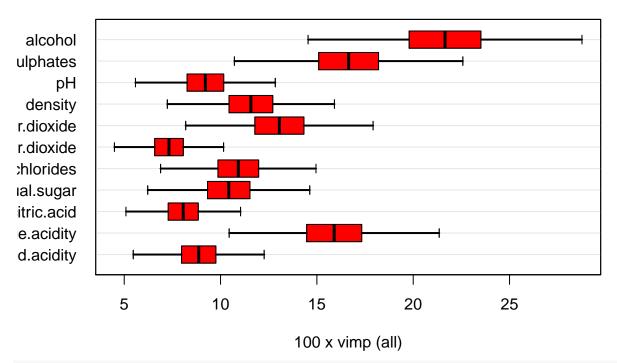
## Sample size: 1281

## Frequency of class labels: 7, 41, 548, 511, 159, 15

## Number of trees: 500

## Forest terminal node size: 1</pre>
```

```
Average no. of terminal nodes: 253.422
## No. of variables tried at each split: 4
                 Total no. of variables: 11
##
##
          Resampling used to grow trees: swor
##
       Resample size used to grow trees: 810
##
                               Analysis: RF-C
##
                                 Family: class
##
                         Splitting rule: gini
##
                      (OOB) Brier score: 0.06943054
##
           (OOB) Normalized Brier score: 0.49989991
##
                              (OOB) AUC: 0.8082197
      (00B) Requested performance error: 0.30444965, 1, 1, 0.20072993, 0.2778865, 0.48427673, 0.8666666
##
##
##
  Confusion matrix:
##
##
             predicted
##
     observed 3 4
                    5
                        6 7 8 class.error
            3 0 0
##
                        3 0 0
                                    1.0000
##
            4 0 0 31 10 0 0
                                    1.0000
##
            5 0 0 440 104 4 0
                                    0.1971
##
            6 0 2 104 367 38 0
                                    0.2818
##
            7 0 0
                    9
                      67 83 0
                                    0.4780
            8 0 0
                       7 6 2
                                    0.8667
##
                    0
##
##
         (OOB) Misclassification rate: 0.303669
# Variable Importance
vi <- subsample(rf, verbose = FALSE)</pre>
extract.subsample(vi)$var.jk.sel.Z
##
                                                             pvalue signif
                            lower
                                       mean
                                                 upper
## fixed.acidity
                         6.281015 8.866242 11.451469 8.971488e-12
                                                                      TRUE
                                                                      TRUE
## volatile.acidity
                        11.750633 15.898089 20.045546 2.890216e-14
## citric.acid
                         5.801079 8.064119 10.327159 1.433068e-12
                                                                      TRUE
## residual.sugar
                         7.224972 10.424628 13.624285 8.533405e-11
                                                                      TRUE
## chlorides
                         7.852130 10.920594 13.989059 1.524279e-12
                                                                      TRUE
                         5.168766 7.324416 9.480067 1.373645e-11
## free.sulfur.dioxide
                                                                      TRUE
## total.sulfur.dioxide 9.353308 13.053928 16.754548 2.359727e-12
                                                                      TRUE
## density
                         8.273913 11.573673 14.873433 3.111819e-12
                                                                      TRUE
## pH
                         6.451411 9.212314 11.973218 3.079709e-11
                                                                      TRUE
## sulphates
                        12.135730 16.647134 21.158537 2.374570e-13
                                                                      TRUE
                        16.242647 21.651380 27.060113 2.150723e-15
                                                                      TRUE
## alcohol
# Variable Importance Plot
plot(vi)
```



Predict # https://www.rdocumentation.org/packages/randomForestSRC/versions/3.1.0/topics/predict.rfsrc randomForestSRC::predict.rfsrc(rf, rf_wine_test)

```
##
     Sample size of test (predict) data: 318
##
                   Number of grow trees: 500
##
     Average no. of grow terminal nodes: 253.422
##
            Total no. of grow variables: 11
##
          Resampling used to grow trees: swor
##
       Resample size used to grow trees: 810
                                Analysis: RF-C
##
##
                                  Family: class
                             Brier score: 0.07068781
##
##
                 Normalized Brier score: 0.50895221
##
                                      AUC: 0.814764
##
            Requested performance error: 0.29874214, 1, 1, 0.17293233, 0.25984252, 0.525, 1
##
##
   Confusion matrix:
##
##
             predicted
##
     observed 3 4
                     5
                        6
                           7 8 class.error
            3 0 0
                     3
                        0
                                    1.0000
##
                           0 0
            4 1 0
                    7
                       4
                                    1,0000
##
                           0 0
            5 0 1 111 20
                          1 0
                                    0.1654
##
            6 0 0
                   27 94
                                    0.2598
##
                           6 0
            7 0 0
##
                     4 16 19 1
                                    0.5250
##
                        2
                          1 0
                                    1.0000
##
              Misclassification error: 0.2955975
##
```

Partial Least Squares

summary(mars_wine)

```
tctrl <- trainControl(method = "repeatedcv", repeats = 5, number =10)
set.seed(4)
pls_wine <- train(quality~ volatile.acidity + chlorides + total.sulfur.dioxide +
               sulphates + alcohol, data = wine_train,
                  method = "pls",
                  preProc = c("center", "scale", "BoxCox"),
                  tunelength =20,
                  trControl = tctrl)
pls_wine
## Partial Least Squares
## 1281 samples
##
      5 predictor
##
## Pre-processing: centered (5), scaled (5), Box-Cox transformation (5)
## Resampling: Cross-Validated (10 fold, repeated 5 times)
## Summary of sample sizes: 1153, 1153, 1154, 1153, 1152, ...
## Resampling results across tuning parameters:
##
##
     ncomp RMSE
                       Rsquared
                                  MAE
           0.6478811 0.3522576 0.5069455
##
     1
##
           0.6470840 0.3536482 0.5065996
           0.6470244 0.3538341 0.5060809
##
##
## RMSE was used to select the optimal model using the smallest value.
## The final value used for the model was ncomp = 3.
Mars Tuning
mars_wine <- earth(quality~ volatile.acidity + chlorides + total.sulfur.dioxide +
               sulphates + alcohol, data =wine_train)
mars_wine
## Selected 15 of 16 terms, and 5 of 5 predictors
## Termination condition: Reached nk 21
## Importance: alcohol, sulphates, volatile.acidity, total.sulfur.dioxide, ...
## Number of terms at each degree of interaction: 1 14 (additive model)
## GCV 0.4100085
                   RSS 501.7096
                                    GRSq 0.3661884
                                                      RSq 0.3936143
```

```
## Call: earth(formula=quality~volatile.acidity+chlorides+total.sulfur.di...),
## data=wine_train)
##
## coefficients
## (Intercept) 29.475710
## h(1.01-volatile.acidity) 0.852686
```

```
## h(volatile.acidity-1.01)
                                 -1.821456
## h(chlorides-0.042)
                                 67.980049
## h(chlorides-0.061)
                                -17.972067
## h(0.152-chlorides)
                                 52.272594
## h(chlorides-0.152)
                                -50.371827
## h(total.sulfur.dioxide-9)
                                 -0.243157
## h(total.sulfur.dioxide-94)
                                 -0.008360
## h(131-total.sulfur.dioxide)
                                 -0.241856
## h(total.sulfur.dioxide-131)
                                  0.260480
## h(0.76-sulphates)
                                 -2.185146
## h(alcohol-11.1)
                                  0.300588
## h(12.3-alcohol)
                                 -0.218249
## h(alcohol-12.3)
                                 -0.389894
##
## Selected 15 of 16 terms, and 5 of 5 predictors
## Termination condition: Reached nk 21
## Importance: alcohol, sulphates, volatile.acidity, total.sulfur.dioxide, ...
## Number of terms at each degree of interaction: 1 14 (additive model)
## GCV 0.4100085
                   RSS 501.7096
                                   GRSq 0.3661884
                                                     RSq 0.3936143
preProc_Arguments = c("center", "scale")
marsGrid_wine = expand.grid(.degree=1:2, .nprune=2:38)
set.seed(4)
marsModel_wine = train(quality~ volatile.acidity + chlorides + total.sulfur.dioxide +
                      sulphates + alcohol, data =wine train,
                      method="earth",
                      preProc=preProc_Arguments,
                      tuneGrid=marsGrid_wine)
marsModel_wine
## Multivariate Adaptive Regression Spline
##
## 1281 samples
##
     5 predictor
##
## Pre-processing: centered (5), scaled (5)
## Resampling: Bootstrapped (25 reps)
## Summary of sample sizes: 1281, 1281, 1281, 1281, 1281, 1281, ...
## Resampling results across tuning parameters:
##
##
    degree nprune RMSE
                               Rsquared
##
             2
                    0.7122760 0.2171101 0.5701033
    1
             3
##
    1
                    0.6752567 0.2973558 0.5289540
             4
##
    1
                    0.6535081 0.3409243 0.5129189
##
    1
             5
                    0.6570769 0.3338440 0.5144791
             6
                    0.6591071 0.3305375 0.5166057
##
    1
##
    1
             7
                    ##
    1
             8
                    0.6590069 0.3318615 0.5170450
##
             9
                    1
##
    1
            10
                    0.6597737 0.3311809
                                          0.5163084
##
            11
    1
                    0.6598222 0.3315357
                                          0.5158173
##
    1
            12
                    0.6595859 0.3323695 0.5157959
```

##	1	13	0.6600013	0.3318148	0.5159406
##	1	14	0.6603922	0.3312989	0.5160279
##	1	15	0.6605024	0.3310738	0.5160779
##	1	16	0.6605024	0.3310738	0.5160779
##	1	17	0.6605024	0.3310738	0.5160779
##	1	18	0.6605024	0.3310738	0.5160779
##	1	19	0.6605024	0.3310738	0.5160779
##	1	20	0.6605024	0.3310738	0.5160779
##	1	21	0.6605024	0.3310738	0.5160779
##	1	22	0.6605024	0.3310738	0.5160779
##	1	23	0.6605024	0.3310738	0.5160779
##	1	24	0.6605024	0.3310738	0.5160779
##	1	25	0.6605024	0.3310738	0.5160779
##	1	26	0.6605024	0.3310738	0.5160779
##	1	27	0.6605024	0.3310738	0.5160779
##	1	28	0.6605024	0.3310738	0.5160779
##	1	29	0.6605024	0.3310738	0.5160779
##	1	30	0.6605024	0.3310738	0.5160779
##	1	31	0.6605024	0.3310738	0.5160779
##	1	32	0.6605024	0.3310738	0.5160779
##	1	33	0.6605024	0.3310738	0.5160779
##	1	34	0.6605024	0.3310738	0.5160779
##	1	35	0.6605024	0.3310738	0.5160779
##	1	36	0.6605024	0.3310738	0.5160779
##	1	37	0.6605024	0.3310738	0.5160779
##	1	38	0.6605024	0.3310738	0.5160779
##	2	2	0.7131117	0.2154654	0.5711957
##	2	3	0.6761504	0.2945847	0.5340899
##	2	4	0.6564135	0.3354539	0.5150608
##	2	5	0.6508974	0.3467644	0.5109214
##	2	6	0.6470358	0.3544765	0.5080996
##	2	7	0.6519450	0.3472954	0.5100834
##	2	8	0.6548159	0.3436376	0.5116912
##	2	9	0.6711602	0.3311970	0.5140466
##	2	10	0.6705270	0.3311357	0.5144146
##	2	11	0.6731133	0.3267571	0.5163083
##	2	12	0.6719547	0.3290581	0.5149547
##	2	13	0.6729162	0.3278180	0.5156340
##	2	14	0.6731796	0.3274458	0.5154864
##	2	15	0.6737603	0.3269853	0.5157601
##	2	16	0.6737658	0.3273973	0.5157295
##	2	17	0.6738441	0.3273854	0.5157636
##	2	18	0.6740397	0.3271363	0.5158683
##	2	19	0.6740397	0.3271363	0.5158683
##	2	20	0.6740397	0.3271363	0.5158683
##	2	21	0.6740397	0.3271363	0.5158683
##	2	22	0.6740397	0.3271363	0.5158683
##	2	23	0.6740397	0.3271363	0.5158683
##	2	24	0.6740397	0.3271363	0.5158683
##	2	25	0.6740397	0.3271363	0.5158683
##	2	26	0.6740397	0.3271363	0.5158683
##	2	27	0.6740397	0.3271363	0.5158683
##	2	28	0.6740397	0.3271363	0.5158683
##	2	29	0.6740397	0.3271363	0.5158683

```
##
     2
             30
                     0.6740397 0.3271363 0.5158683
##
     2
             31
                     0.6740397 0.3271363 0.5158683
##
     2
             32
                     0.6740397 0.3271363 0.5158683
     2
             33
                     0.6740397 0.3271363
##
                                          0.5158683
##
     2
             34
                     0.6740397 0.3271363
                                           0.5158683
##
     2
             35
                     0.6740397 0.3271363 0.5158683
##
     2
             36
                     0.6740397 0.3271363
                                           0.5158683
     2
                     0.6740397 0.3271363
##
             37
                                           0.5158683
##
     2
                     0.6740397 0.3271363 0.5158683
##
## RMSE was used to select the optimal model using the smallest value.
## The final values used for the model were nprune = 6 and degree = 2.
```

KNN Neighbors

```
set.seed(4)
knn_wine <- train(quality~ volatile.acidity + chlorides + total.sulfur.dioxide +
               sulphates + alcohol, data =wine_train,
              method = "knn",
              preProc = c("center", "scale"),
               tuneGrid = data.frame(.k = 1:50),
               trControl = trainControl(method = "cv"))
knn_wine
## k-Nearest Neighbors
##
## 1281 samples
##
      5 predictor
##
## Pre-processing: centered (5), scaled (5)
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 1153, 1153, 1153, 1154, 1153, 1152, ...
  Resampling results across tuning parameters:
##
##
     k
        RMSE
                   Rsquared
                              MAE
##
      1
        0.7504817
                   0.3041580
                              0.4223146
##
      2 0.6983824
                   0.3237618 0.4784021
##
      3 0.6717419
                   0.3442214
                              0.4839236
##
      4 0.6702850
                   0.3371634
                              0.4963434
##
      5 0.6627934 0.3448450 0.4970748
##
      6 0.6600855 0.3448719
                              0.4996920
##
     7 0.6540051 0.3521529
                              0.4974915
##
     8 0.6519397 0.3536865 0.4984599
##
     9 0.6483577 0.3578728 0.4971793
##
     10 0.6458723 0.3620134
                              0.4964883
##
     11 0.6435687
                   0.3655187
                              0.4969729
##
     12 0.6429914 0.3656200 0.4982548
##
     13 0.6397289
                   0.3711190
                              0.4955805
##
     14 0.6411480 0.3678476 0.4973248
##
     15 0.6393988 0.3708496 0.4964588
```

```
##
    16 0.6378593 0.3734042 0.4951719
##
    17 0.6369138 0.3749404 0.4959561
##
    18 0.6362271 0.3765123 0.4952884
##
    19 0.6370582 0.3749337 0.4962376
##
    20 0.6372569 0.3747771 0.4971556
##
    21 0.6382742 0.3731375 0.4986083
##
    22 0.6380964 0.3734679 0.4979368
##
    23 0.6377412 0.3742550 0.4977067
##
    24 0.6387696 0.3722746 0.4985198
##
    25 0.6368451 0.3757202 0.4976829
##
    26 0.6364275 0.3762866 0.4984160
    27 0.6346862 0.3795795 0.4973558
##
##
    28 0.6347058 0.3795358 0.4974800
##
    29 0.6360878 0.3770104 0.4993224
##
    30 0.6357780 0.3778721 0.4999014
##
    31 0.6367139 0.3762620 0.5005842
##
    32 0.6369187 0.3757665 0.5002004
##
    33 0.6371917 0.3752852 0.5006800
##
    34 0.6377712 0.3740873 0.5007256
    35 0.6379469 0.3737611 0.5014462
##
##
    36 0.6378240 0.3742385 0.5015524
##
    37 0.6374811 0.3749206 0.5011665
##
    38 0.6375055 0.3749360 0.5014616
##
    39 0.6371916 0.3757942 0.5006347
##
    40 0.6368473 0.3765730 0.5004336
##
    41 0.6365946 0.3770658 0.5003279
##
    42 0.6365554 0.3772882 0.5006586
    43 0.6367931 0.3768451 0.5006802
##
##
    44 0.6380737 0.3744045 0.5014973
##
    45 0.6381101 0.3745029 0.5011388
##
    46 0.6379189 0.3750057 0.5009169
##
    47 0.6379198 0.3751492 0.5009907
##
    48 0.6375034 0.3761452 0.5005620
##
    49 0.6374270 0.3763801 0.5003075
    50 0.6377491 0.3759204 0.5014729
##
##
## RMSE was used to select the optimal model using the smallest value.
## The final value used for the model was k = 27.
```

SVM

```
## Support Vector Machines with Radial Basis Function Kernel
##
## 1281 samples
##
    11 predictor
## Pre-processing: centered (11), scaled (11)
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 1153, 1153, 1153, 1154, 1153, 1152, ...
## Resampling results across tuning parameters:
##
##
     С
           RMSE
                     Rsquared
                                MAE
##
     0.25  0.6424186  0.3663702  0.4834089
##
    0.50 0.6360205 0.3784258 0.4756782
##
     1.00 0.6303977 0.3892811 0.4703437
##
     2.00 0.6281033 0.3952003 0.4644550
     4.00 0.6342263 0.3896250 0.4665780
##
##
## Tuning parameter 'sigma' was held constant at a value of 0.09155044
## RMSE was used to select the optimal model using the smallest value.
## The final values used for the model were sigma = 0.09155044 and C = 2.
```