


Algorithmics	Student information	Date	Number of session
	UO: UO294515	24/02/2025	6
	Surname: Lopez Garcia	 Escuela de Ingeniería Informática Universidad de Oviedo	
	Name: Oscar		



Activity 1. [Direct exchange or Bubble algorithm]

n	T ordered	T reverse	T random
10000	333	1524	1079
2*10000	1254	5976	4265
2^2*10000	4908	23844	16829
2^3*10000	19757	OoT	67368
2^4*10000	OoT	OoT	OoT

All three, ordered, reverse and random have a quadratic complexity $O(n^2)$, the times make sense as reverse has to make more changes in the vector than random, and ordered has no changes to do.

Activity 2. [Selection algorithm]

n	T ordered	T reverse	T random
10000	313	296	320
2*10000	1260	1176	1266
2^2*10000	5045	4507	5022
2^3*10000	19450	18041	20069
2^4*10000	OoT	OoT	OoT

All three, ordered, reverse and random have a quadratic complexity $O(n^2)$. It makes sense as for this method it is not better if the vector is ordered or if it is not.

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Activity 3. [Insertion algorithm]

n	T ordered	T reverse	T random
10000	LoR	299	154
2*10000	LoR	1158	584
2^2*10000	LoR	4683	2344
2^3*10000	LoR	18816	9277
2^4*10000	LoR	74765	37072
2^5*10000	LoR	OoT	OoT
2^6*10000	LoR	OoT	OoT
2^7*10000	LoR	OoT	OoT
2^8*10000	LoR	OoT	OoT
2^9*10000	91	OoT	OoT
2^10*10000	179	OoT	OoT
2^11*10000	359	OoT	OoT
2^12*10000	728	OoT	OoT
2^13*10000	1452	OoT	OoT

Yes, as the complexity is linear $O(n)$ for the ordered vectors as it does not have to enter the while loop, and it is quadratic $O(n^2)$ for the reverse and random vectors, as it enters the while loop that iterates n times.

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Activity 4. [Quicksort algorithm]

n	T ordered	T reverse	T random
25000	LoR	LoR	93
2*25000	63	72	192
2^2*25000	123	140	403
2^3*25000	257	289	869
2^4*25000	530	599	1873
2^5*25000	1098	1249	4229
2^6*25000	2263	2523	10312

It matches the expected as for all cases the complexity is between $n \log n$ and n^2 which are the best and worse cases of this algorithm.

Bubble: $O(n^2)$ for random

$n_1 = 10000 \rightarrow t_1 = 1079 \text{ ms}$, $n_2 = 16 \cdot 10^6 \rightarrow t_2 = ?$

$$K = (n_2^2 / n_1^2)$$

$$t_2 = k \cdot t_1 = ((16 \cdot 10^6)^2 / 10000^2) \cdot 1079 \text{ ms} = (16 \cdot 10^{12} / 1 \cdot 10^8) \cdot 1079 \text{ ms} = 16 \cdot 10^4 \cdot 1079 \text{ ms} = 172640000 \text{ ms} \cdot (1 \text{ s} / 1000 \text{ ms}) \cdot (1 \text{ h} / 3600 \text{ s}) \cdot (1 \text{ day} / 24 \text{ h}) = 1,998 \text{ days}$$

Selection: $O(n^2)$ for random

$n_1 = 10000 \rightarrow t_1 = 320 \text{ ms}$, $n_2 = 16 \cdot 10^6 \rightarrow t_2 = ?$

$$K = (n_2^2 / n_1^2)$$

$$t_2 = k \cdot t_1 = ((16 \cdot 10^6)^2 / 10000^2) \cdot 320 \text{ ms} = (16 \cdot 10^{12} / 1 \cdot 10^8) \cdot 320 \text{ ms} = 16 \cdot 10^4 \cdot 320 \text{ ms} = 51200000 \text{ ms} \cdot (1 \text{ s} / 1000 \text{ ms}) \cdot (1 \text{ h} / 3600 \text{ s}) \cdot (1 \text{ day} / 24 \text{ h}) = 0,593 \text{ days}$$

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Selection: $O(n^2)$ for random

$n_1 = 10000 \rightarrow t_1 = 154 \text{ ms}$, $n_2 = 16 \cdot 10^6 \rightarrow t_2 = ?$

$K = (n_2^2 / n_1^2)$

$t_2 = k \cdot t_1 = ((16 \cdot 10^6)^2 / 10000^2) \cdot 154 \text{ ms} = (16 \cdot 10^{12} / 1 \cdot 10^8) \cdot 154 \text{ ms} = 16 \cdot 10^4 \cdot 154 \text{ ms} = 24640000 \text{ ms} \cdot (1 \text{ s} / 1000 \text{ ms}) \cdot (1 \text{ h} / 3600 \text{ s}) \cdot (1 \text{ day} / 24 \text{ h}) = 0,285 \text{ days}$

Activity 5. [Quicksort+Insertion algorithm]

N = $16 \cdot 10^6$	T random
Quicksort	2766
Quicksort+Insertion (k=5)	2544
Quicksort+Insertion (k=10)	2425
Quicksort+Insertion (k=20)	2377
Quicksort+Insertion (k=30)	2353
Quicksort+Insertion (k=50)	2294
Quicksort+Insertion (k=100)	2133
Quicksort+Insertion (k=200)	1810
Quicksort+Insertion (k=500)	2394
Quicksort+Insertion (k=1000)	4034

We can conclude that this algorithm improves the performance of the quicksort algorithm if we choose a good k , if k is too small, the algorithm does not change too much, and if it is too big, we can get a worse time than if we didn't implement the insertion, as we will be doing too many sortings with the insertion.

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