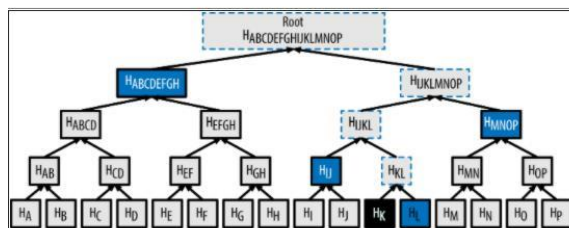


Questions:

How to let any Bitcoin node prove that the Transaction K is included in a block? • •



Please study [How to let any Bitcoin node prove that the Transaction K is included in a block?](#) before answering the following questions.

- Please build up the above Merkle Tree using the following data set, and assuming that the hash function is "msg%7"
 - Transaction A: 31
 - Transaction B: 54
 - Transaction C: 29
 - Transaction D: 7
 - Transaction E: 23
 - Transaction F: 21
 - Transaction G: 27
 - Transaction H: 13
 - Transaction I: 15
 - Transaction J: 11
 - Transaction K: 26
 - Transaction L: 34
 - Transaction M: 89
 - Transaction N: 32
 - Transaction O: 18
 - Transaction P: 17
- If a Bitcoin node would like to prove that Transaction H is part of the block.
 - What information does the system need to provide?
 - What does the bitcoin node need to do?

Ans:

As we know the equation is $\text{Hash} = \text{msg} \% 7$
 $H(AB) = H(A) + H(B)$ "HA + HB" is the concatenation of "HA" and "HB"

We calculate the hash for each one first,

Transaction A: $31 \% 7 = 3$
 Transaction B: $54 \% 7 = 5$
 Transaction C: $29 \% 7 = 1$
 Transaction D: $7 \% 7 = 0$
 Transaction E: $23 \% 7 = 2$
 Transaction F: $21 \% 7 = 0$
 Transaction G: $27 \% 7 = 6$
 Transaction H: $13 \% 7 = 6$
 Transaction I: $15 \% 7 = 1$
 Transaction J: $11 \% 7 = 4$
 Transaction K: $26 \% 7 = 5$
 Transaction L: $34 \% 7 = 6$
 Transaction M: $89 \% 7 = 5$

Transaction N: $32 \% 7 = 4$

Transaction O: $18 \% 7 = 4$

Transaction P: $17 \% 7 = 3$

Then, calculate the combinations,

$H(AB) = 35 \% 7 = 0$

$H(CD) = 10 \% 7 = 3$

$H(EF) = 20 \% 7 = 6$

$H(GH) = 66 \% 7 = 3$

$H(IJ) = 14 \% 7 = 0$

$H(KL) = 56 \% 7 = 0$

$H(MN) = 54 \% 7 = 5$

$H(OP) = 43 \% 7 = 1$

$H(ABCD) = 3 \% 7 = 3$

$H(EFGH) = 63 \% 7 = 0$

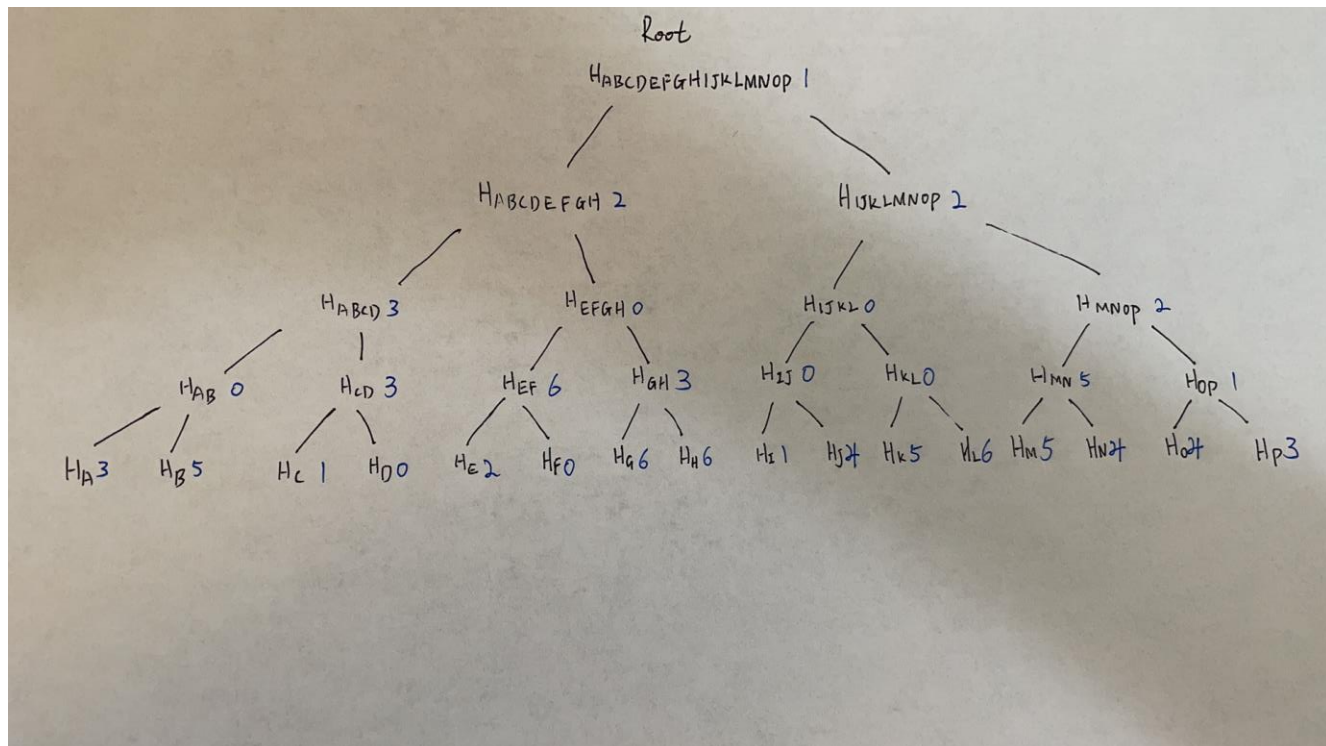
$H(IJKL) = 0 \% 7 = 0$

$H(MNOP) = 51 \% 7 = 2$

$H(ABCDEFGH) = 30 \% 7 = 2$

$H(IJKLMNOP) = 2 \% 7 = 2$

$H(ABCDEFGHIJKLMNOP) = 22 \% 7 = 1$



Step 1: The **system** provides **two sets of information**:

Transaction H :

$H(G) \Rightarrow H(EF) \Rightarrow H(ABCD) \Rightarrow H(IJKLMNOP)$

Step 2: The **Bitcoin node** need to do:

Transaction H :

$H(GH) \Rightarrow H(EFGH) \Rightarrow H(ABCDEFGH) \Rightarrow \text{MERKLE ROOT}$