# Lab 3: Spread of memes on a network

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## 1 Simple meme spread model

The following model was made from these rules and states:

- Resting: With probability p a resting person will discover a new meme by themselves and become a sharer.
- Sharer: With probability q a sharer will pick one person completely at random from the population. If that person is resting then they will now become a sharer. However, if the person they pick is bored, then the sharer will lose interest and become bored too
- Bored: With probability r a bored person will pick one person completely at random from the population. If that person is resting then the bored person will now become resting, otherwise they will continue to be bored. The simulation was done with N=1000 People where there was 1 sharer and one bored initially. While in another example there was 100 sharers and 100 bored initially.

### 1.1 Examples of two different behaviours

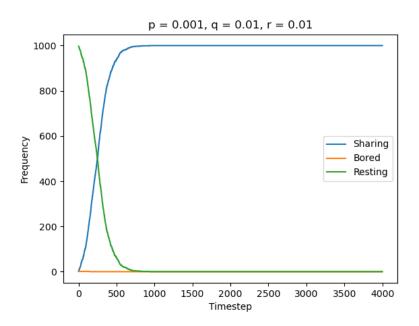


Figure 1: Result of the model with one bored and one spreading initially.

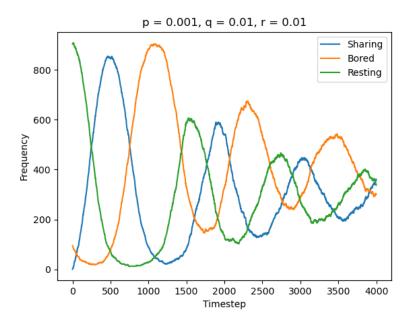


Figure 2: Result of the model with 100 bored and one spreading initially.

Figure 1 shows that the number of bored and number of resting dies out. The reason why bored dies out is likely due to the fact that there are 998 resting initially, so it's most likely that a bored will find someone resting and therefore die out because they also become resting. While the sharer will also likely only find people resting. Which means that the sharer won't likely

be able to find a bored person and become bored. But when setting 100 sharers and 100 bored initially, the three states oscillates as seen in 2. This is because sharers manages to find bored, which makes them bored, but when bored nodes finds nodes that are resting they turn into resting which in turn makes it possible to return to a sharer with probability p. It's also shown in figure 2 that the number of sharers decreases as the number of bored increases, while the number of bored decreases when the number of resting increases. Which is expected considering the rules mentioned above.

#### 1.2 Phase transitions

To generate the heat maps the model was simulated 20 times while varying the parameter p between [0,0.001], while the other parameters are fixed as such q=0.01 r=0.01. Each simulation was done for 2000 time steps. Note that there has been a typo on the y-axes in figures 3 and 4 where it says Q, it should be p. The heat map was also generated for two initial conditions. One configuration where the number of sharers and bored was set to one initially. And another where they're both set to 100.

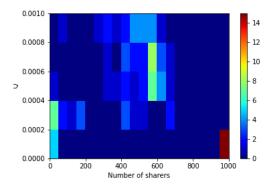


Figure 3: heatmap when varying p with initial conditions set as 100 sharers and 100 bored

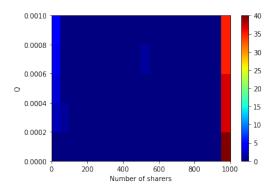


Figure 4: heatmap when varying p with initial conditions set as one sharer and one bored

In figure 4 the same behaviour observed in 1 since most runs gives between 950 and 1000 sharers, while some runs has zero sharers. This is again likely due to the fact that it's unlikely that a sharer finds a bored person. While the other initial condition shows that, when p is at it's

largest the number of sharers decreases because it's also likely that a sharer find a bored person since there are more bored people initially than in 4. This means that the number of sharers can increase with low competition from the bored nodes as seen in figure 3.

### 2 Meme model on real- and lattice network

The meme model was applied to a real and lattice network, but each node can only spread its state to its neighbours. A typical result looked like the following:

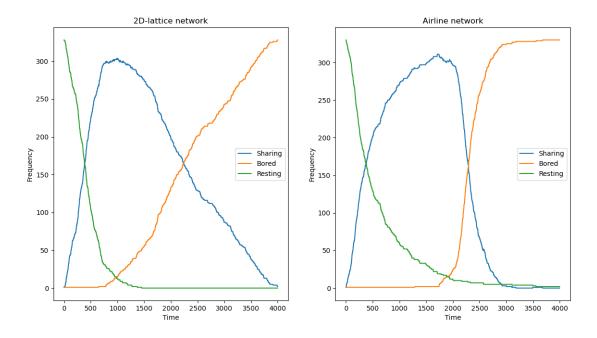


Figure 5: Result of the meme model on a 2D lattice - and real network with parameters r, q = 0.01 and p = 0.001.

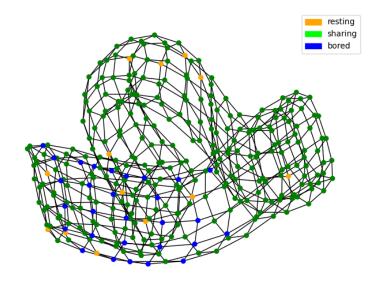


Figure 6: Image of the lattice network after 1000 steps.

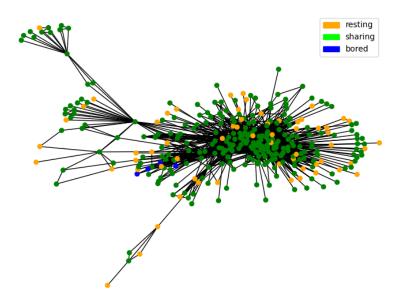


Figure 7: Image of the airlines network after 1000 steps

As seen in 5, both simulations seems to show similar characteristics. The number of sharers shows a significant increase, and reaches its maxima as the number of bored exceedes the number of resting. This means that theres a higher likelyhood that the sharing people finds bored people than resting, which makes the population of bored people increase. Thereafter, the dynamic of number of sharers was examined for different values of p.

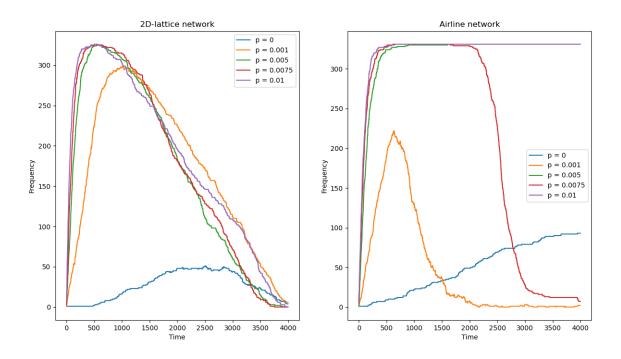


Figure 8: Number of sharers for different values of the p parameters.

As seen in 8, the increase of the p parameter seems to shift the curve to the left and or lowering it. In both networks a lower p seems to speed up the increasing trend of sharers. The airlines network maximum of sharers seem to exist over longer periods of times than the lattice network. This is most likely due to the structural differences in the networks. As seen in figure 6-7, the used networks differs significantly in the number neighbours per node.

The airlines network has a few nodes that are heavily connected, and the majority only has a few neighbours, whereas in the lattice network each node has four neighbours. This leads to the fact that a sharer "hitting" a bored node is generally harder in the airlines network compared to the lattice network. The cause for this is the fact that the nodes with more connections has a lower chance to find individual bored nodes in its neighbouring reach. As the model is built on an random choice of neighbours the same neighbour can be chosen over and over. The probability is therefore lower since a highly connected node has many neighbours. So when the number of sharers is high, then the system has to generally wait longer in order to find a bored node and transition into a bored spread. Though if an highly connected node becomes a "bored-spreading" state, then the shift from sharing to bored happens fast in the network since there are many neighbours to spread to.

# Appendix

```
1 from networkx.algorithms import community
```

<sup>2</sup> import networkx as nx

<sup>3</sup> import numpy as np

<sup>4</sup> import matplotlib.pyplot as plt

```
5 import seaborn as sns
6
7
8 state_dict = {'resting': 0, 'sharing': 1, 'bored': 2}
10 def generate_mesh(N):
11
     mesh = [state_dict['resting'] for i in range(N)]
13
     mesh[0] = state_dict['bored']
     mesh[1] = state_dict['sharing']
     # mesh[1:100] = [state_dict['bored'] for i in range(100)]
16
     # mesh[100] = state_dict['sharing']
17
18
     return mesh
19
20
21 \#e.g. p = 0.001, q = 0.01, r = 0.01)
22 def resting_or_sharing(p):
     return int(np.random.choice([state_dict['resting'], state_dict['sharing']], /
         size = 1, p = [1 - p, p]))
24
25 def sharer_or_bored(q, mesh, ind, N):
26
27
     choice = np.random.choice([0, 1], size = 1, p = [1 - q, q])
28
     if choice:
29
30
        while True:
31
            rand_person = int(np.random.randint(0, N, 1))
32
            if ind!=rand_person:
33
               break
        if mesh[rand_person] == state_dict['resting']:
36
            mesh[rand_person] = state_dict['sharing']
37
38
        elif mesh[rand_person] == state_dict['bored']:
39
           mesh[ind] = state_dict['bored']
40
41
43 def bored_or_resting(r, mesh, ind, N):
     choice = int(np.random.choice([0, 1], size = 1, p = [1 - r, r]))
44
46
     if choice:
        while True:
47
           rand_person = int(np.random.randint(0, N, 1))
48
            if ind!=rand_person:
49
              break
50
        if mesh[rand_person] == state_dict['resting']:
51
           mesh[ind] = state_dict['resting']
52
55 def get_stats(mesh, N):
57
     mesh_temp = np.array(mesh)
58
     nr_sharing = len(mesh_temp[mesh_temp == state_dict['sharing']])
59
     nr_bored = len(mesh_temp[mesh_temp == state_dict['bored']])
60
     return [nr_sharing, nr_bored, N - nr_sharing - nr_bored]
61
62
63
```

```
64 def run_sim(N , num_steps, p, q, r):
65
      mesh = generate_mesh(N)
66
67
68
      stats = []
69
70
71
      for step in range(num_steps):
         #print(mesh)
73
         for ind, person in enumerate (mesh):
74
75
             if person == state_dict['resting']:
76
77
                mesh[ind] = resting_or_sharing(p)
78
79
             elif person == state_dict['sharing']:
80
81
                sharer_or_bored(q,mesh, ind, N)
82
83
            else:
85
86
                bored_or_resting(r,mesh,ind, N)
87
         stats.append(get_stats(mesh, N))
88
89
      return stats
90
91
92
93
94 if __name__ == '__main__':
96
      p = 0.001
97
      q = 0.01
98
99
      r = 0.01
100
      N_persons = 1000
101
      num\_steps = 4000
102
103
     n_{sharers} = np.linspace(0, 1000, 50)
104
105
      # tot_result_list = []
106
      # iter = 0
107
      # totiter = len(q_list) * 50
108
109
      # for j, q in enumerate(q_list):
110
111
112
      # for i in range(50):
      # stats = run_sim(N_persons , num_steps, p, q, r)
113
      # tot_result_list.append([stats[-1][0], q])
114
      # iter += 1
      # print(f"{100 *round(iter / totiter, 3)}% done")
116
117
118
119
      # tot_result_list = np.array(tot_result_list)
120
121
      # plt.figure()
122
123
      # plt.hist2d(tot_result_list[:,0], tot_result_list[:,1], bins=20, /
```

```
cmap=plt.cm.jet)
      # plt.colorbar()
124
      # plt.xlabel('Number of sharers')
125
      # plt.ylabel('Q')
126
      # plt.show()
127
128
      stats = run_sim(N_persons , num_steps, p, q, r)
129
130
      stats = np.array(stats)
131
132
      ticks = list(range(num_steps))
133
      plt.plot(ticks, stats[:,0], label = 'Sharing')
134
      plt.plot(ticks, stats[:,1], label = 'Bored')
135
      plt.plot(ticks, stats[:,2], label = 'Resting')
136
      plt.xlabel('Timestep')
137
      plt.ylabel('Frequency')
138
      plt.title(f'p_=_{\{p\}},_q_=_{\{q\}},_r_=_{\{r\}}')
139
140
      plt.legend()
      plt.show()
141
```

Listing 1: The code for the simple meme spread model

```
1 import numpy as np
2 import matplotlib.pyplot as plt
3 import matplotlib.patches as mpatches
4 import networkx as nx
5 from celluloid import Camera
6 import random
7 import os
9 MAIN_DIR = os.path.split(os.path.abspath(__file__))[0]
10 fig_dir = os.path.abspath(os.path.join(MAIN_DIR,'..', 'figs'))
11 data_dir = os.path.abspath(os.path.join(MAIN_DIR,'...', 'data'))
13 state_dict = {'resting': 0, 'sharing': 1, 'bored': 2}
14 colour_list = ['orange', 'green', 'blue']
15 color_dict = {'resting': np.array([255, 165, 0]), 'sharing': np.array([0, 255, /
      0]), 'bored': np.array([0, 0, 255])}
16 legend = [mpatches.Patch(color = color_dict[state] / 255, label = f"{state}") for /
      state in color_dict]
17
18
19 def generate_real_network():
20
21
     df = open(os.path.join(data_dir, 'airlines.txt'), 'r')
     num\_vertices = 0
     for line in df:
25
        line_list = line.strip().split()
        if line_list[0] == '*Vertices':
26
           num_vertices = int(line_list[1])
27
           break
28
29
30
     G = nx.empty_graph(num_vertices)
31
     reading_edges = False
32
     for line in df:
        line_list = line.strip().split()
        if not reading_edges:
           if line_list[0] != "*Edges":
35
               continue
           else:
37
```

```
38
               reading_edges = True
39
               continue
        else:
40
            G.add_edge(int(line_list[0]), int(line_list[1]))
41
42
     node_list = list(G.nodes)
43
44
     for node in node_list:
45
46
        if len(list(G.neighbors(node))) == 0:
47
            G.remove_node(node)
48
     node_list = list(G.nodes)
49
50
     print(f"Number_of_nodes:_{len(node_list)}")
51
     number_nodes = len(node_list)
52
53
     indicies = [i for i in range(number_nodes)]
54
55
     ind1 = indicies[random.randint(0, number_nodes - 1)]
56
57
     indicies.pop(indicies.index(ind1))
58
59
60
     ind2 = indicies[random.randint(0, number_nodes - 2)]
61
     attr_dict = { node : {"state" : 0} for node in node_list}
62
     attr_dict[node_list[ind1]]["state"] = 1
63
     attr_dict[node_list[ind2]]["state"] = 2
64
65
     nx.set_node_attributes(G, values=attr_dict)
66
67
68
     return G
70 def generate_lattice_network(N):
71
     indicies = [i for i in range(N)]
72
73
     ind1 = indicies[random.randint(0, N - 1)]
74
75
     indicies.pop(indicies.index(ind1))
76
77
     ind2 = indicies[random.randint(0, N - 2)]
78
79
80
     G = nx.grid_2d_graph(int(N / 10), 10, periodic = True)
81
82
     node_list = list(G.nodes)
83
84
     attr_dict = { node : {"state" : 0} for node in node_list}
85
     attr_dict[node_list[ind1]]["state"] = 1
86
     attr_dict[node_list[ind2]]["state"] = 2
87
88
     nx.set_node_attributes(G, values=attr_dict)
91
     return G
92
93
94
95
96
97 \# e.g. p = 0.001, q = 0.01, r = 0.01)
```

```
98 def resting_or_sharing(p, G, node):
      new_state = int(np.random.choice([state_dict['resting'], /
          state\_dict['sharing']], size = 1, p = [1 - p, p]))
      G.nodes[node]["state"] = new_state
100
101
102 def sharer_or_bored(G, old_state, q, node):
103
104
      choice = np.random.choice([0, 1], size = 1, p = [1 - q, q])
105
106
      if choice:
107
108
         neighbor = list(G.neighbors(node))
109
         num_neigh = len(neighbor)
110
         if num_neigh > 1:
111
            ind = random.randint(0, num_neigh - 1)
112
         else:
113
            ind = 0
114
115
         rand_person = neighbor[ind]
116
117
118
         if old_state.nodes[rand_person]["state"] == state_dict['resting']:
119
            G.nodes[rand_person]['state'] = state_dict['sharing']
120
         elif old_state.nodes[rand_person]["state"] == state_dict['bored']:
121
            G.nodes[node]['state'] = state_dict['bored']
122
123
124
125 def bored_or_resting(G, r, old_state , node):
      choice = int(np.random.choice([0, 1], size = 1, p = [1 - r, r]))
126
127
128
      if choice:
129
         neighbor = list(G.neighbors(node))
130
         ind = random.randint(0, len(neighbor) - 1)
131
         rand_person = neighbor[ind]
132
         if old_state.nodes[rand_person]["state"] == state_dict['resting']:
133
            G.nodes[rand_person]['state'] = state_dict['resting']
134
135
136
137 def get_stats(G):
139
      nodes = G.nodes
140
      nr_sharing = 0
141
      nr\_bored = 0
142
      nr_resting = 0
143
144
      for node in nodes:
145
146
         if nodes[node]["state"] == state_dict['sharing']:
147
            nr\_sharing += 1
         elif nodes[node]["state"] == state_dict['bored']:
150
151
            nr\_bored += 1
152
153
         else:
154
            nr_resting += 1
155
156
```

```
157
      return [nr_sharing, nr_bored, nr_resting]
158
159
160
161 def plot_mesh(G, camera, tick):
      node_colours = []
162
      for i in G.nodes():
163
164
         node_colours.append(colour_list[G.nodes[i]['state']])
      nx.draw(G, with_labels=False, node_color = node_colours, node_size=30, /
          edge_color='black', linewidths=1, font_size=15)
      plt.legend(handles = legend)
166
      plt.title(f"T_=_{tick}")
167
      camera.snap()
168
169
170 def run_sim(N , num_steps, p, q, r, record = False, assignment = 1):
171
172
173
      if assignment == 1:
174
         G = generate_lattice_network(N)
175
176
      else:
177
         G = generate_real_network()
178
179
      if record:
180
         fig = plt.figure()
181
         camera = Camera(fig)
182
         plot_mesh(G, camera, 0)
183
184
      else:
         camera = None
185
186
187
      stats = []
188
      for step in range(num_steps):
189
         #print(mesh)
190
191
         node_list = G.nodes
192
         old_state = G.copy()
193
194
195
         for node in node_list:
196
197
             if old_state.nodes[node]["state"] == state_dict['resting']:
198
199
                resting_or_sharing(p, G, node)
200
201
             elif old_state.nodes[node]["state"] == state_dict['sharing']:
202
203
204
                sharer_or_bored(G, old_state, q, node)
205
             else:
206
207
208
                bored_or_resting(G, r, old_state, node)
209
         stats.append(get_stats(G))
210
         if record and step % 10 == 0:
211
             plot_mesh(G, camera, step)
212
213
214
215
      return stats, G, camera
```

```
216
217
218
219
220 if __name__ == '__main__':
221
222
223
      p_{list} = [0.001]
224
      q = 0.01
225
      r = 0.01
226
      N_persons = 332
227
      num\_steps = 1000
228
      record = False
229
      assignment = 2
230
231
      sharer_lat = []
232
233
      sharer_net = []
      for p in p_list:
234
         stats1, G1, camera = run_sim(N_persons , num_steps, p, q, r, record=record, /
235
             assignment = 1)
236
         stats1 = np.array(stats1)
237
         stats2, G2, camera = run_sim(N_persons , num_steps, p, q, r, record=record, /
             assignment = 2)
         stats2 = np.array(stats2)
238
         sharer_lat.append(stats1[:,0])
239
         sharer_net.append(stats2[:,0])
240
241
      if record:
242
         animation = camera.animate()
243
         animation.save(os.path.join(fig_dir, 'sim.gif'))
244
246
      node_colours1 = []
      node_colours2 = []
247
248
      for i in G1.nodes():
249
         node_colours1.append(colour_list[G1.nodes[i]['state']])
250
251
      for i in G2.nodes():
252
         node_colours2.append(colour_list[G2.nodes[i]['state']])
253
254
255
256
      plt.figure()
      nx.draw(G1, with_labels=False, node_color = node_colours1, node_size=30, /
257
          edge_color='black', linewidths=1, font_size=15)
      plt.legend(handles = legend)
258
      plt.show()
259
260
      plt.figure()
261
      nx.draw(G2, with_labels=False, node_color = node_colours2, node_size=30, /
262
          edge_color='black', linewidths=1, font_size=15)
      plt.legend(handles = legend)
263
      plt.show()
264
265
266
      time = list(range(num_steps))
267
      fig, (ax1, ax2) = plt.subplots(1,2)
268
269
270
      # for i, p in enumerate(p_list):
271
```

```
272
      # ax1.plot(time, sharer_lat[i], label = f"p = {p}")
273
      # ax2.plot(time, sharer_net[i], label = f"p = {p}")
274
      # ax1.set_xlabel("Time")
275
      # ax1.set_ylabel("Frequency")
276
      # ax1.set_title("2D-lattice network")
277
      # ax1.legend()
278
279
      # ax2.set_xlabel("Time")
280
      # ax2.set_ylabel("Frequency")
      # ax2.set_title("Airline network")
      # ax2.legend()
283
      # plt.show()
284
      # ax1.plot(list(range(num_steps)), stats1[:,0], label = 'Sharing')
285
      # ax1.plot(list(range(num_steps)), stats1[:,1], label = 'Bored')
286
      # ax1.plot(list(range(num_steps)), stats1[:,2], label = 'Resting')
287
     # ax1.set_xlabel("Time")
288
289
     # ax1.set_ylabel("Frequency")
     # ax1.set_title("2D-lattice network")
290
      # ax1.legend()
      # ax2.plot(list(range(num_steps)), stats2[:,0], label = 'Sharing')
293
      # ax2.plot(list(range(num_steps)), stats2[:,1], label = 'Bored')
294
      # ax2.plot(list(range(num_steps)), stats2[:,2], label = 'Resting')
295
      # ax2.set_xlabel("Time")
      # ax2.set_ylabel("Frequency")
296
      # ax2.set_title("Airline network")
297
      # ax2.legend()
298
      # plt.show()
299
300
301
      \# n_sharers = np.linspace(0, 1000, 50)
302
304
      # tot_result_list = []
      # iter = 0
305
      \# num_iter = 20
306
      # totiter = len(p_list) * num_iter
307
308
      # for j, p in enumerate(p_list):
309
310
      # for i in range(num_iter):
311
      # stats = run_sim(N_persons , num_steps, p, q, r)
      # tot_result_list.append([stats[-1][0], q])
314
      # iter += 1
      # print(f"{100 *round(iter / totiter, 3)}% done")
315
```

Listing 2: The code for the 2D lattice