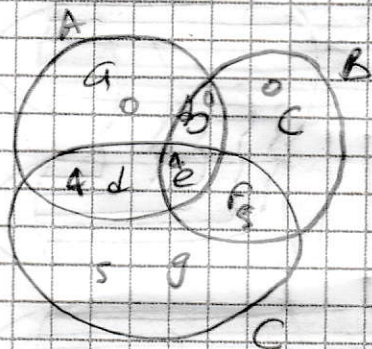


# Parcial Matemáticas Especiales

Oscar Javier Celis  
20172578049

1)



a)  $F = \sum m(0, 1, 2, 5, 7, 9, 10, 14, 15)$

m	a	b	c	d	e	f	g	F
0	0	0	0	0	0	0	0	1
1	0	0	0	0	0	0	1	1
2	0	0	0	0	0	1	0	1
5	0	0	0	0	1	0	1	1
7	0	0	0	0	1	1	1	1
9	0	0	0	1	0	0	1	1
10	0	0	0	1	0	1	0	1
14	0	0	0	1	1	1	0	1
15	0	0	0	1	1	1	1	1

b)

$$F = \overline{a}b\overline{c}d\overline{e}f\overline{g} + \overline{a}b\overline{c}d\overline{e}f\overline{g} + \overline{a}b\overline{c}d\overline{e}f\overline{g} + \overline{a}b\overline{c}d\overline{e}f\overline{g} + \overline{a}b\overline{c}d\overline{e}f\overline{g} + \overline{a}b\overline{c}d\overline{e}f\overline{g} + \overline{a}b\overline{c}d\overline{e}f\overline{g} + \overline{a}b\overline{c}d\overline{e}f\overline{g} + \overline{a}b\overline{c}d\overline{e}f\overline{g}$$

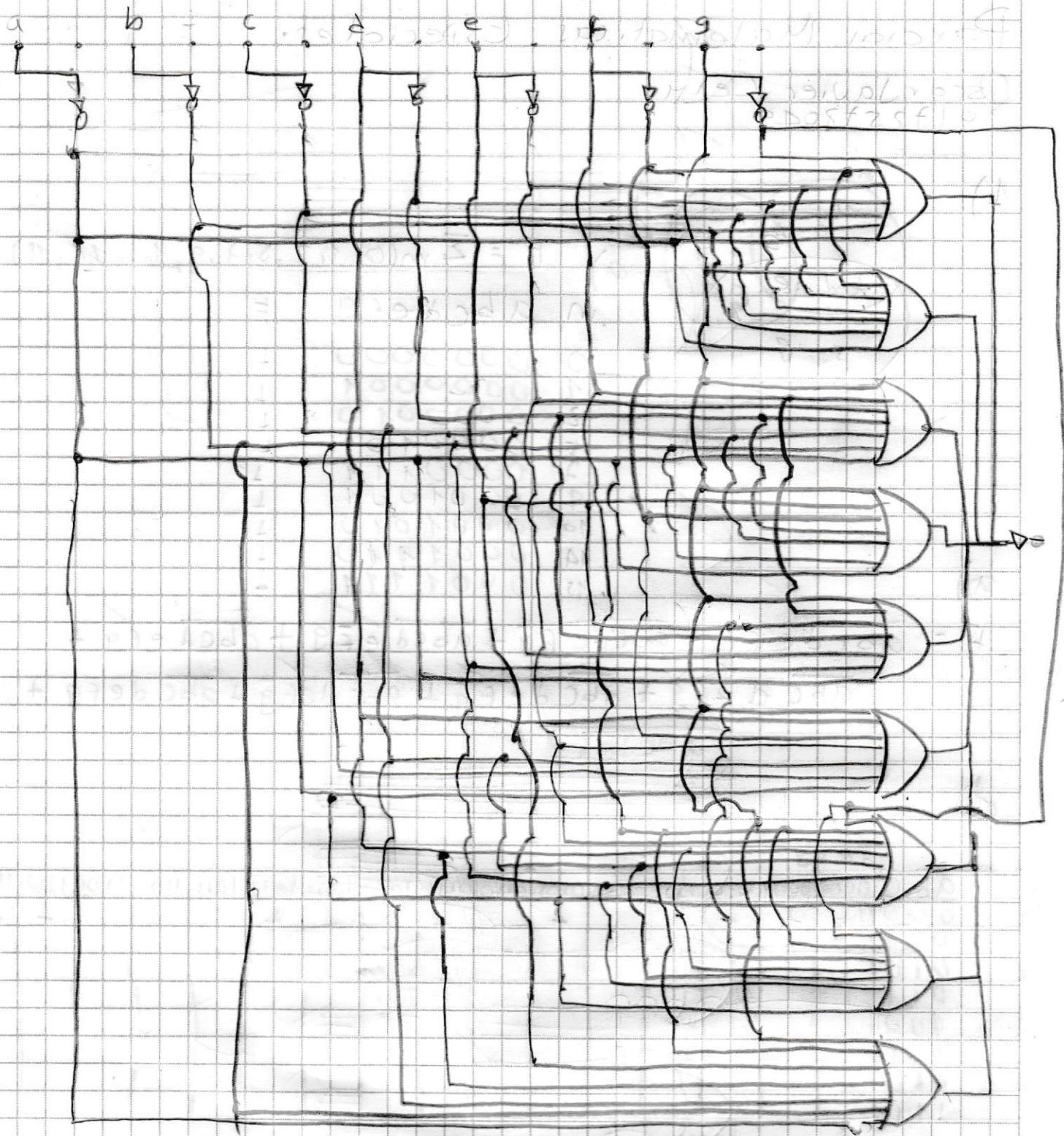
c)

ab C	000	001	010	011	100	101	110	111
000	1	1	1					
001								
010								
011								
100								
101								
110								
111								

$$F = \overline{a}b\overline{c}d\overline{e} + \overline{a}b\overline{c}d\overline{e}f + \overline{a}b\overline{c}d\overline{e}f\overline{g} + \overline{a}b\overline{c}d\overline{e}f\overline{g} + \overline{a}b\overline{c}d\overline{e}f\overline{g}$$

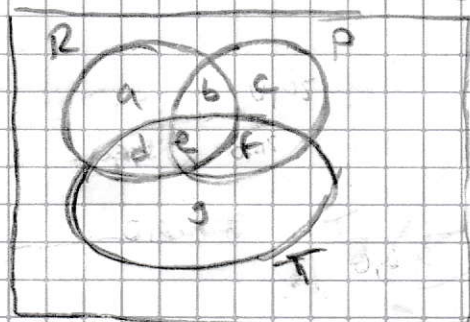


e





2)



$$U = 11000.000$$

$$d = T \cap R = 0,2(0,7U) = 140.000$$

$$f = T \cap P = 0,45(0,7U) = 315.000$$

$$g = 0,7U - T \cap P - T \cap R$$

$$= 7700.000 - 315.000 - 140.000$$

$$T = 245.000$$

a) 140.000 Ven TV

Ninguno de ellos lee  
Periodicos

$$R = 0,4U - R \cap T$$

$$= 400.000 - 140.000$$

$$= 260.000$$

b) 185.000 habitantes

$$P = 0,5U - T \cap P$$

$$= 500.000 - 315.000$$

$$= 185.000$$

3)

$$R_1 = \{(a,a), (b,a), (d,d), (a,b), (b,d), (c,a)\}$$

$$R_2 = \{(a,b), (b,a), (c,d), (c,b), (b,d), (c,c)\}$$

a) Matrices

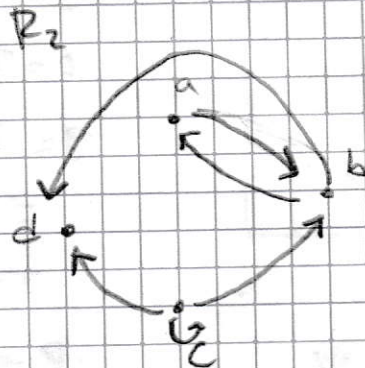
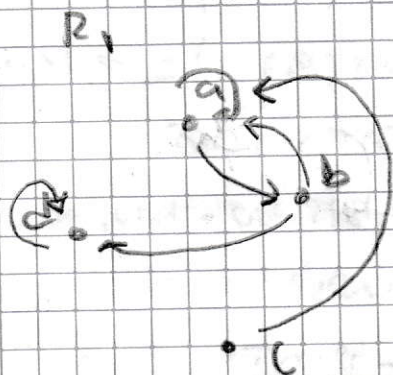
 $M_{R_1}$ 

$$\begin{matrix} & \begin{matrix} a & b & c & d \end{matrix} \\ \begin{matrix} a \\ b \\ c \\ d \end{matrix} & \begin{bmatrix} 1 & 1 & 1 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix} \end{matrix}$$

 $M_{R_2}$ 

$$\begin{matrix} & \begin{matrix} a & b & c & d \end{matrix} \\ \begin{matrix} a \\ b \\ c \\ d \end{matrix} & \begin{bmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 \end{bmatrix} \end{matrix}$$

b) Digrafo



c)  $R_3 = R_1 \oplus R_2$

	a	b	c	d
a	1	1	1	0
b	1	0	1	0
c	0	0	1	0
d	0	1	1	1

$R_4 = R_1 \circ R_2$

	a	b	c	d
a	1	1	1	0
b	1	0	0	0
c	0	0	0	0
d	0	1	0	1

	a	b	c	d
a	1	1	1	0
b	0	1	0	0
c	0	0	0	0
d	1	1	1	0

$R_5 = R_1 \cap R_2$

	a	b	c	d
a	0	1	0	0
b	1	0	0	0
c	0	0	0	0
d	0	1	0	0

d) Ninguna es de orden porque ninguna es reflexiva

Ninguna tiene la diagonal principal con solo 1s



5)

325E<sub>(16)</sub>, 42C3<sub>(16)</sub>

a)

325E<sub>(16)</sub> →

$$\begin{array}{cccccccccccc} & 3 & & 2 & & 5 & & E & & & & \\ \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ 0 & 1 & 1 & 0 & 0 & 1 & 0 & 0 & 1 & 1 & 1 & 0 \\ 0 & 3 & 1 & 1 & 1 & 1 & 3 & 6 & & & & \\ \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ 8192 + 1024 + 512 + 64 + 16 + 9 + 4 + 2 = 12894_{(10)} \end{array}$$

42C3 →

$$\begin{array}{cccccccccccc} & 4 & & 2 & & C & & 3 & & & & \\ \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ 0 & 1 & 0 & 0 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & 0 \\ 0 & 4 & & 1 & & 3 & & 0 & & 3 & & \\ \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ 16384 + 512 + 128 + 64 + 24 + 1 = 17091_{(10)} \end{array}$$

b) mcm

$$\begin{array}{r|l} 12894 & 2 \\ 6447 & 3 \\ 2149 & 7 \\ 307 & 307 \\ \downarrow & \end{array}$$

$$\begin{array}{r|l} 17091 & 3 \\ 5697 & 3 \\ 1899 & 3 \\ 633 & 3 \\ 211 & 211 \\ \downarrow & \end{array}$$

$$\text{mcm} = 220.372354$$

MCD

$$\begin{array}{r|l|l} 12894 & 17091 & 2 \\ 6447 & 17091 & 3 \\ 2149 & 5697 & 3 \\ 2149 & 1899 & 3 \\ 2149 & 633 & 3 \\ 2149 & 211 & 7 \\ 2149 & 211 & 211 \\ 307 & \downarrow & 307 \\ \downarrow & \downarrow & \end{array}$$

$$\text{MCD} = 3$$

c) Mensaje a enviar → 0011

$$\begin{array}{cccccc} 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ P_1 & P_2 & 0 & P_3 & 0 & 1 & 1 \\ \hline 1 & 1 & 0 & 1 & 0 & 1 & 1 \end{array}$$

→ MS) enviado

$$P_1 = D_1 \oplus D_2 \oplus D_4$$

$$P_2 = D_1 \oplus D_3 \oplus D_4$$

$$P_3 = D_2 \oplus D_3 \oplus D_4$$



c) MSJ a enviar  $\rightarrow 0011$   
Error bit 4  $\rightarrow 0010$

1	2	3	4	5	6	7
P <sub>1</sub>	P <sub>2</sub>	D <sub>1</sub>	P <sub>3</sub>	D <sub>2</sub>	P <sub>3</sub>	D <sub>4</sub>

1	1	0	1	0	1	1
---	---	---	---	---	---	---

 $\rightarrow$  MSJ enviado

0	1	0	1	0	1	0
---	---	---	---	---	---	---

 $\rightarrow$  MSJ recibido

X	✓		✓			
---	---	--	---	--	--	--

1	0	0	= D <sub>4</sub>
---	---	---	------------------