



# Programación. Python

## Numpy

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# numpy. Conceptos básicos

```
► import numpy as np

a = np.array([[1., 2., 3.],
              [4., 5., 6.]
              ])

print("a = ", a)

print(a.ndim, a.shape, a.dtype)
```

```
a = [[ 1.  2.  3.]
      [ 4.  5.  6.]]
2 (2, 3) float64
```

```
► b = np.array([[1, 2], [3, 4]], dtype=complex)
print(b, b.dtype)
```

```
[[ 1.+0.j  2.+0.j]
 [ 3.+0.j  4.+0.j]] complex128
```

# Arrays a partir de rangos

```
► a = np.arange(12)
print("a = ", a)
b = a.reshape(3, 4)
print("b = ", b)
print(type(a), type(b))
```

```
print("núm. de dimensiones (ejes) de a: ", a.ndim)
print("núm. de dimensiones (ejes) de b: ", b.ndim)
```

```
print("dimensiones de a: ", a.shape)
print("dimensiones de b: ", b.shape)
```

```
print("Tipo de los elementos de a: ", a.dtype.name)
print("Tipo de los elementos de b: ", b.dtype.name)
```

```
print("Número total de elementos de a: ", a.size)
print("Número total de elementos de b: ", b.size)
```

```
print(np.arange(10000))
```

```
a = [ 0  1  2  3  4  5  6  7  8  9 10 11]
b = [[ 0  1  2  3]
     [ 4  5  6  7]
     [ 8  9 10 11]]
```

```
<class 'numpy.ndarray'> <class 'numpy.ndarray'>
```

```
núm. de dimensiones (ejes) de a: 1
```

```
núm. de dimensiones (ejes) de b: 2
```

```
dimensiones de a: (12,)
```

```
dimensiones de b: (3, 4)
```

```
Tipo de los elementos de a: int32
```

```
Tipo de los elementos de b: int32
```

```
Número total de elementos de a: 12
```

```
Número total de elementos de b: 12
```

```
[ 0  1  2 ..., 9997 9998 9999]
```

# Arrays definidos genéricamente (1 de 3)

```
▶ # Todo ceros:
b = np.zeros((3, 4))
print("b = ", b)

# Todo unos:
c = np.ones((2, 3, 4), dtype=np.int16)
print("c = ", c)

# Array vacío:
d = np.empty( (2,3) )
print("d = ", d)

# Con elementos elegidos aleatoriamente:
e = np.random.random((2,3))
```

```
b = [[ 0.  0.  0.  0.]
      [ 0.  0.  0.  0.]
      [ 0.  0.  0.  0.]
```

```
c = [[[1 1 1 1]
      [1 1 1 1]
      [1 1 1 1]]
```

```
[[1 1 1 1]
 [1 1 1 1]
 [1 1 1 1]]]
```

```
d = [[ 0.  0.  0.]
      [ 0.  0.  0.]
```

```
In [4]: e
```

```
Out[4]:
```

```
array([[0.37103017, 0.9473136 , 0.26915378],
       [0.88303356, 0.44680566, 0.01090937]])
```

# Arrays definidos genéricamente

## (2 de 3)

```
# Secuencias de valores:  
f = np.arange( 10, 50, 5)  
print("f = ", f)  
  
# Secuencias, interpolando linealmente  
g = np.linspace( 0, 2, 25)  
print("g = ", g)  
  
from numpy import pi  
h = np.linspace(0, 2*pi, 50)  
print(h)
```

```
f = [10 15 20 25 30 35 40 45]  
g = [ 0.          0.08333333  0.16666667  0.25          0.33333333  0.41666667  
 0.5          0.58333333  0.66666667  0.75          0.83333333  0.91666667  
 1.          1.08333333  1.16666667  1.25          1.33333333  1.41666667  
 1.5          1.58333333  1.66666667  1.75          1.83333333  1.91666667  
 2.          ]  
[ 0.          0.12822827  0.25645654  0.38468481  0.51291309  0.64114136  
 0.76936963  0.8975979   1.02582617  1.15405444  1.28228272  1.41051099  
 1.53873926  1.66696753  1.7951958   1.92342407  2.05165235  2.17988062  
 2.30810889  2.43633716  2.56456543  2.6927937   2.82102197  2.94925025  
 3.07747852  3.20570679  3.33393506  3.46216333  3.5903916   3.71861988  
 3.84684815  3.97507642  4.10330469  4.23153296  4.35976123  4.48798951  
 4.61621778  4.74444605  4.87267432  5.00090259  5.12913086  5.25735913  
 5.38558741  5.51381568  5.64204395  5.77027222  5.89850049  6.02672876  
 6.15495704  6.28318531]
```

# Arrays definidos genéricamente (3 de 3)

```
np.sin(h)      # se aplica la función seno a todos los puntos
```

```
array([ 0.00000000e+00,  1.27877162e-01,  2.53654584e-01,
        3.75267005e-01,  4.90717552e-01,  5.98110530e-01,
        6.95682551e-01,  7.81831482e-01,  8.55142763e-01,
        9.14412623e-01,  9.58667853e-01,  9.87181783e-01,
        9.99486216e-01,  9.95379113e-01,  9.74927912e-01,
        9.38468422e-01,  8.86599306e-01,  8.20172255e-01,
        7.40277997e-01,  6.48228395e-01,  5.45534901e-01,
        4.33883739e-01,  3.15108218e-01,  1.91158629e-01,
        6.40702200e-02, -6.40702200e-02, -1.91158629e-01,
       -3.15108218e-01, -4.33883739e-01, -5.45534901e-01,
       -6.48228395e-01, -7.40277997e-01, -8.20172255e-01,
       -8.86599306e-01, -9.38468422e-01, -9.74927912e-01,
       -9.95379113e-01, -9.99486216e-01, -9.87181783e-01,
       -9.58667853e-01, -9.14412623e-01, -8.55142763e-01,
       -7.81831482e-01, -6.95682551e-01, -5.98110530e-01,
       -4.90717552e-01, -3.75267005e-01, -2.53654584e-01,
       -1.27877162e-01, -2.44929360e-16])
```

# Operaciones aritméticas

```
a = np.array([[1, 2, 3], [4, 5, 6]])
print(a)
print(a+1)
print(a**2)
print(np.sin(a))
print(a<4)

b = np.array([[2, 2, 2], [3, 3, 3]])
print(a+b)
print(a-b)
print(a*b) # OJO: elemento a elemento
```

```
a = np.array([[1, 2, 3], [4, 5, 6]])
print(a)

print(a.sum(), a.prod(), a.min(), a.max())
print(a.sum(axis=0), a.sum(axis=1))
print(a.cumsum(axis=1)) #sumas acumuladas por filas
```

```
[[1 2 3]
 [4 5 6]]
[[2 3 4]
 [5 6 7]]
[[ 1  4  9]
 [16 25 36]]
[[ 0.84147098  0.90929743  0.14112001]
 [-0.7568025  -0.95892427 -0.2794155 ]]
[[ True  True  True]
 [False False False]]
[[3 4 5]
 [7 8 9]]
[[-1  0  1]
 [ 1  2  3]]
[[ 2  4  6]
 [12 15 18]]
```

```
[[1 2 3]
 [4 5 6]]
21 720 1 6
[5 7 9] [ 6 15]
[[ 1  3  6]
 [ 4  9 15]]
```

# Ops. vectores y matrices

*# Operaciones matemáticas con vectores:*

```
u = [1, 2, 3]
v = [4, 5, 6]
```

*# Producto interior o escalar:*

```
print("u . v = ", np.inner(u, v))
```

*# Producto vectorial o producto cruzado:*

```
print("u x v = ", np.cross(u, v))
```

*# Producto combinado (cada  $u_i$  \* cada  $v_j$ ):*

```
print("u xx v = ", np.outer(u, v))
```

```
u . v = 32
u x v = [-3  6 -3]
u xx v = [[ 4  5  6]
          [ 8 10 12]
          [12 15 18]]
```

```
a = np.array([[1, 2, 3], [4, 5, 6]])
b = np.array([[10, 20], [30, 40], [50, 60]])
print(a)
print(b)
```

*# Producto de matrices:*

```
print(a@b)
print(a.dot(b))
```

*# Producto "escalar" de matrices:*

```
a = np.array([[1, 2], [3, 4]])
b = np.array([[5, 6], [7, 8]])
print(np.vdot(a, b))    # 1*5 + 2*6 + 3*7 + 4*8
```

```
[[1 2 3]
 [4 5 6]]
[[10 20]
 [30 40]
 [50 60]]
[[220 280]
 [490 640]]
[[220 280]
 [490 640]]
70
```



# Funciones con matrices

```
a = np.array([[1.0, 2.0], [3.0, 4.0]])
print(a)

# Traspuesta de una matriz:
print(a.transpose())

# Inversa de una matriz:
print(np.linalg.inv(a))

# Matriz unidad:
u = np.eye(2)
print(u)

j = np.array([[0.0, -1.0], [1.0, 0.0]])

print(j @ j)

print(np.trace(u))
2.0
```

```
[[ 1.  2.]
 [ 3.  4.]]
[[ 1.  3.]
 [ 2.  4.]]
[[-2.  1.]
 [ 1.5 -0.5]]
[[ 1.  0.]
 [ 0.  1.]]
[[-1.  0.]
 [ 0. -1.]]
2.0
```

# Álgebra lineal básica

```
# Resolución de ecuaciones lineales:

a = np.array([[1.0, 2.0], [3.0, 4.0]])
print(a)
y = np.array([[5.], [7.]])
print(y)

print(np.linalg.solve(a, y))

# Vectores y valores propios:

print(np.linalg.eig(j))
```

```
[[ 1.  2.]
 [ 3.  4.]]
[[ 5.]
 [ 7.]]
[[-3.]
 [ 4.]]
(array([ 0.+1.j,  0.-1.j]), array([[ 0.70710678+0.j,  0.70710678-0.j],
 [ 0.00000000-0.70710678j,  0.00000000+0.70710678j]]))
```

# Iteración con arrays

```
a = np.array([[1, 2, 3], [4, 5, 6]])
print(a)
print("líneas:")
for linea in a:
    print(" -> ", linea)
print("elementos:")
for elemento in a.flat:
    print(" -> ", elemento)
```

```
[[1 2 3]
 [4 5 6]]
líneas:
-> [1 2 3]
-> [4 5 6]
elementos:
-> 1
-> 2
-> 3
-> 4
-> 5
-> 6
```

# Estadística básica

*# Media:*

```
a = np.array([[1, 2], [3, 4]])
```

```
print(a)
print("Media de una matriz:", np.mean(a))
print("... por columnas: ", np.mean(a, axis=0))
print("... por filas: ", np.mean(a, axis=1))
print("... mdia ponderada: ", np.average([1, 2, 3, 4], weights=[0.1, 0.3, 5.2, 1.3]))
```

*# Mediana:*

```
print("Mediana de un vector: ", np.median(np.array([4, 2, 5, 3, 7, 6, 1, 9, 8, 2, 3, 4, 6, 1], float)))
```

*# Varianza:*

```
print("Varianza de una matriz: ", np.var(a))
```

*# Desviación típica*

```
print("Desviación típica: ", np.std(a))
```

*# Matriz de covarianzas:*

```
x = [-2.1, -1, 4.3]
```

```
y = [3, 1.1, 0.12]
```

```
print("Covarianza de x", np.cov(x))
```

```
print("Covarianza de x e y: ", np.cov(x, y))
```

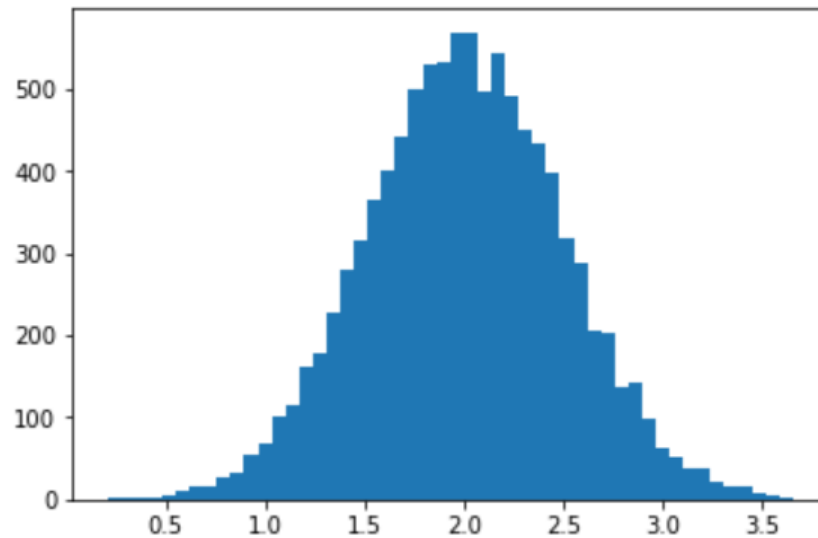
```
xy = np.stack((x, y), axis=0) # Combinamos ambos vectores
```

```
print(np.cov(xy))
```

```
[[1 2]
 [3 4]]
Media de una matriz: 2.5
... por columnas: [ 2.  3.]
... por filas: [ 1.5  3.5]
... mdia ponderada: 3.11594202899
Mediana de un vector: 4.0
Varianza de una matriz: 1.25
Desviación típica: 1.11803398875
Covarianza de x 11.709999999999999
Covarianza de x e y: [[ 11.71      -4.286      ]
 [ -4.286      2.14413333]]
[[ 11.71      -4.286      ]
 [ -4.286      2.14413333]]
```

# Histogramas

```
import numpy as np
import matplotlib.pyplot as plt
v = np.random.normal(2, 0.5, 10000)
plt.hist(v, bins=50)      # matplotlib
plt.show()
```



```
(n, bins) = np.histogram(v, bins=50, density=True)
plt.plot(.5*(bins[1:]+bins[:-1]), n)
plt.show()
```

