Thinking & Coding Algorithms

Kyle Simpson



Recommended Reading

Disclaimer #1

Lab, Not Lecture

Disclaimer #2



JS Using JS



TL;DW

- 1. Ask better clarifying questions
- 2. Balance CPU vs Memory
- 3. Shape data structure(s) to the problem, not the other way
- 4. "premature optimization" vs. "immature optimization"

Quick DSA Primer

Common Data Structures

Array, Stack, Queue

Set, Object, Map

Tree, Graph

Common Algorithms

BubbleSort, QuickSort

Tree Traversal, Path Finding

Binary Search

Common Techniques

Iteration

Recursion

Indexes, References



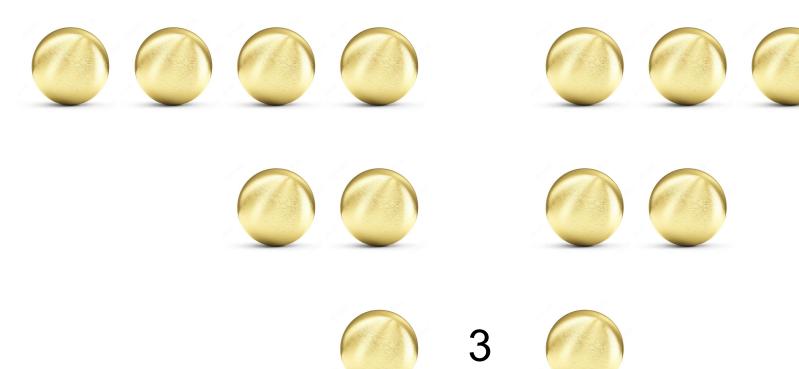


Iteration





Recursion























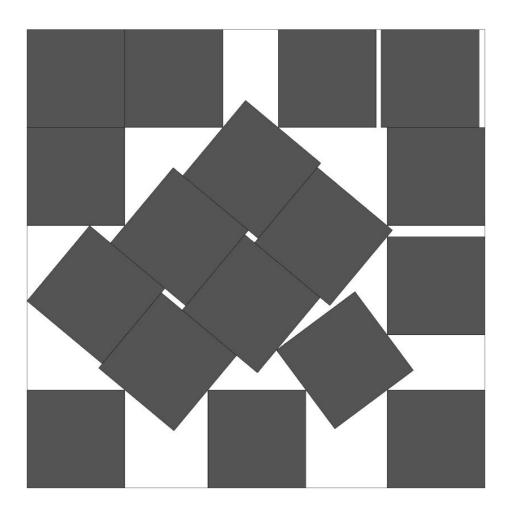


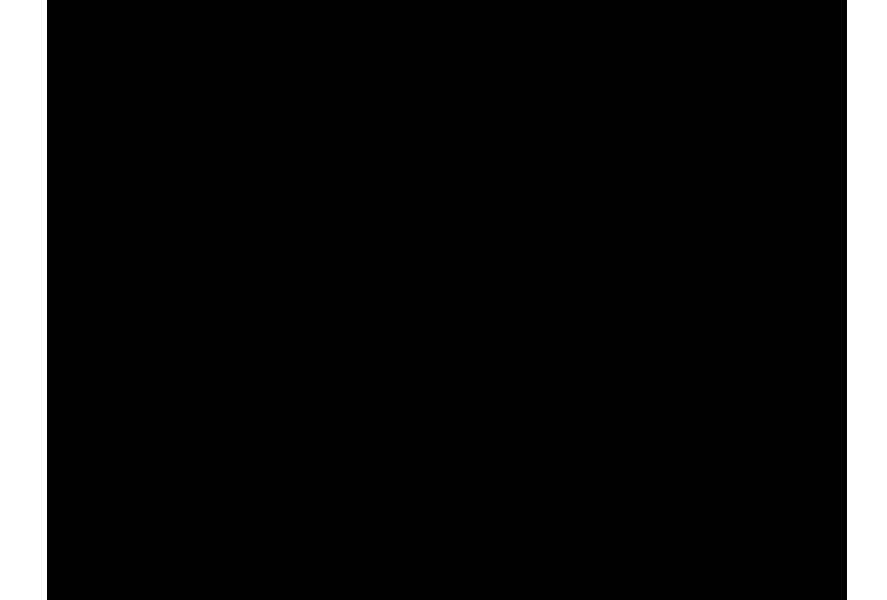


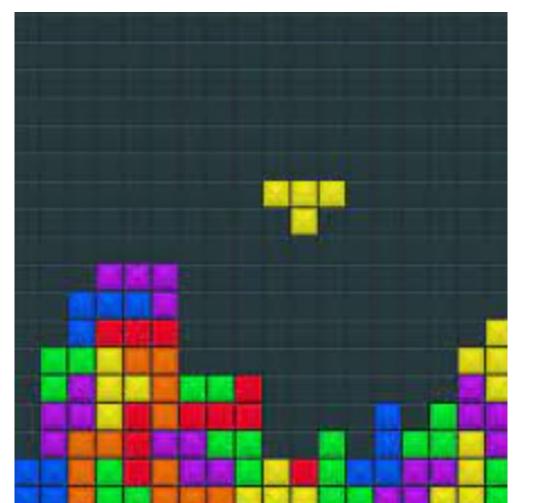
Warm-ups

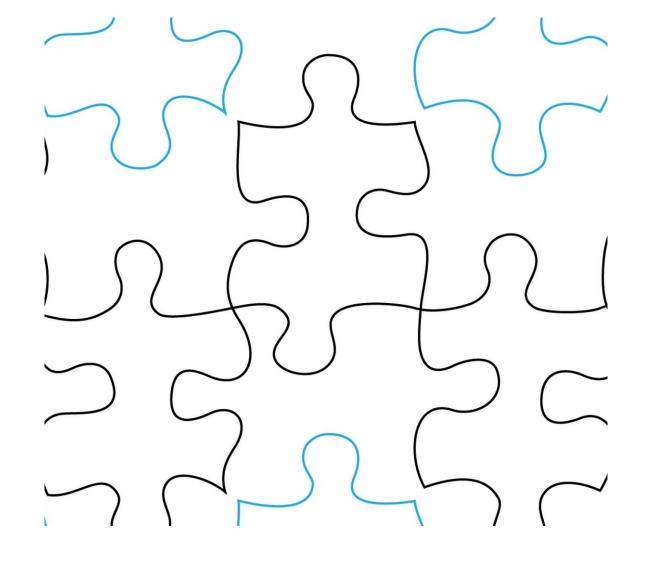
```
    binary-to-decimal.js

       function binaryToDecimalConverter(binaryNumber) {
         var decimal = 0n;
         for (let [idx,digit] of Object.entries(binaryNumber)) {
          let power = binaryNumber.length - idx - 1;
           decimal += BigInt(digit) * (2n ** BigInt(power));
         return decimal;
       binaryToDecimalConverter("111110011101100"); // 31980n
decimal-to-binary.js
       function decimalToBinaryConverter(base10number) {
         var binary = "";
         var next = base10number;
         while (next > 0n) {
         let remainder = next % 2n;
          binary = remainder + binary;
           next = next / 2n;
         return binary;
       decimalToBinaryConverter(31980n); // 111110011101100
```











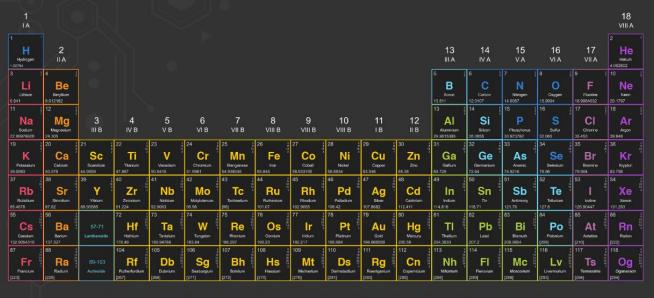
```
3 function findMaxRegionArea(matr) {
       var area = 0;
       var maxArea = 0;
                    !visited.has((rowIdx * ROW_LEN) + colIdx) &&
                       let [ visitedRowIdx, visitedColIdx ] = toVisit.shift();
                           for (let rowDelta of [ -1, 0, 1 ]) {
```



Exercise: Periodic Table Speller



PERIODIC TABLE OF ELEMENTS



57	58	59	60	61	62	63	64	65	66	67	68	69	70	71
La	Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Но	Er	Tm	Yb	Lu
Lanthanum 138.90547	Cerium 140.116	Praseodymium 140,90765	Deodymium 144.242	Promethium [145]	Samarium 150.36	Europium 151.964	Gadolinium 157.25	Terbium 158.9253	Dysprosium 162.5	Helmium 164.93032	Erbium 167.259	Thulium 168.93421	Ytterbium 173.054	Lutetium 174.9668
89	90	91	92	93	94	95 ;	96	97	98	99	100	101	102	103
Ac	Th	Pa	U	Np	Pu	Am	Cm	Bk ⁵	Cf	Es	Fm	Md	No	Lr
Actinium [227]	Thorium 232.03806	Protectinium 231.03588	Uranium 238.02691	Neptunium [237]	Plutorium [244]	Americium [243]	Curium [247]	Berkelium [247]	Californium [251]	Einsteinium [252]	Fermium [257]	Mendelevium [258]	Nobelium [262]	Lawrencium [262]

Word: because spell 20 92 34 Se

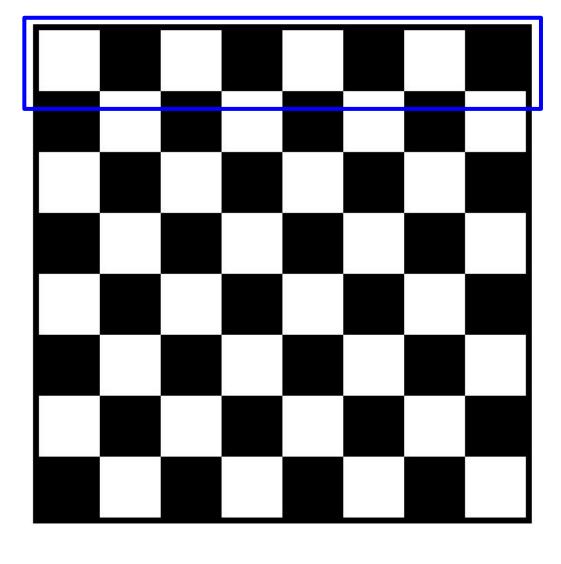
Be Beryllium Calcium

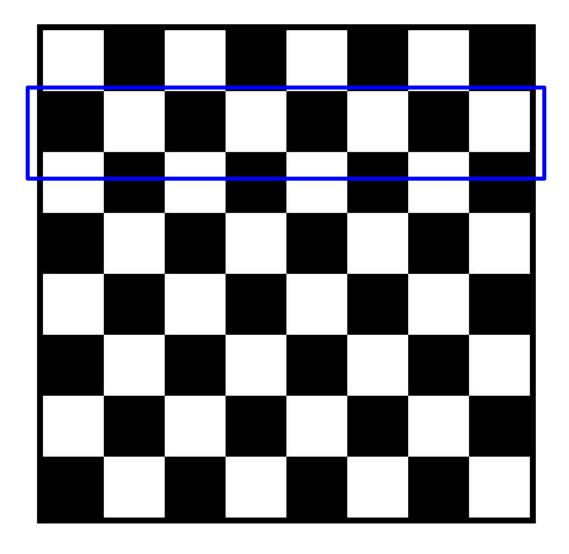
Uranium

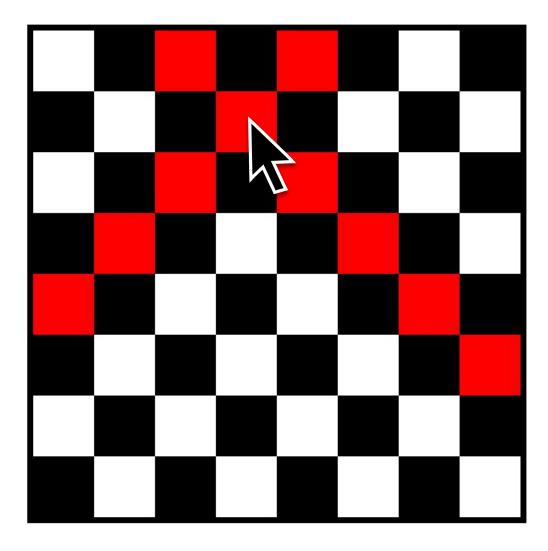
Selenium

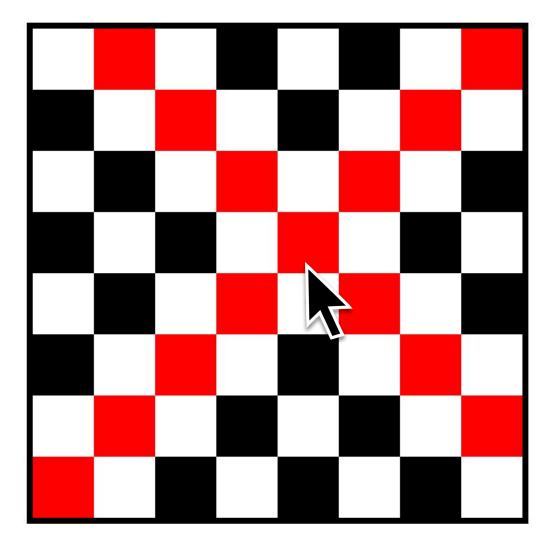
Periodic Table Speller

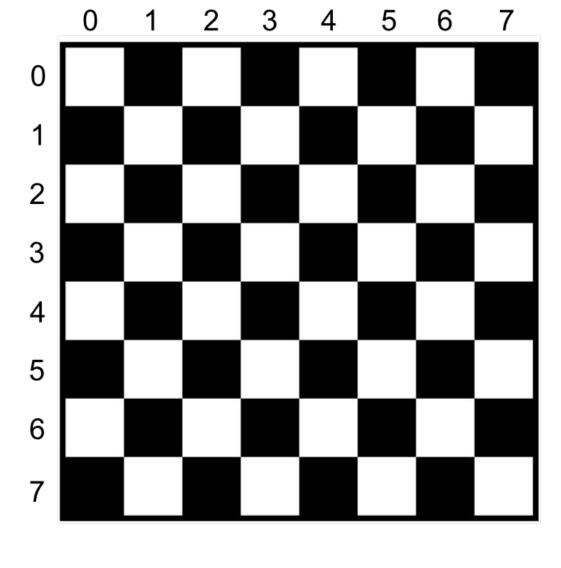
Exercise: Chessboard Diagonals





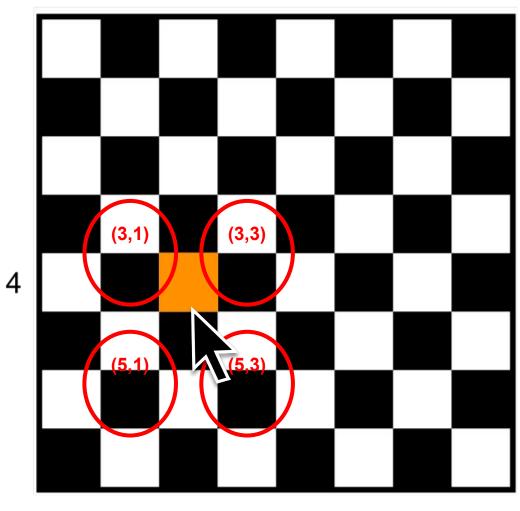


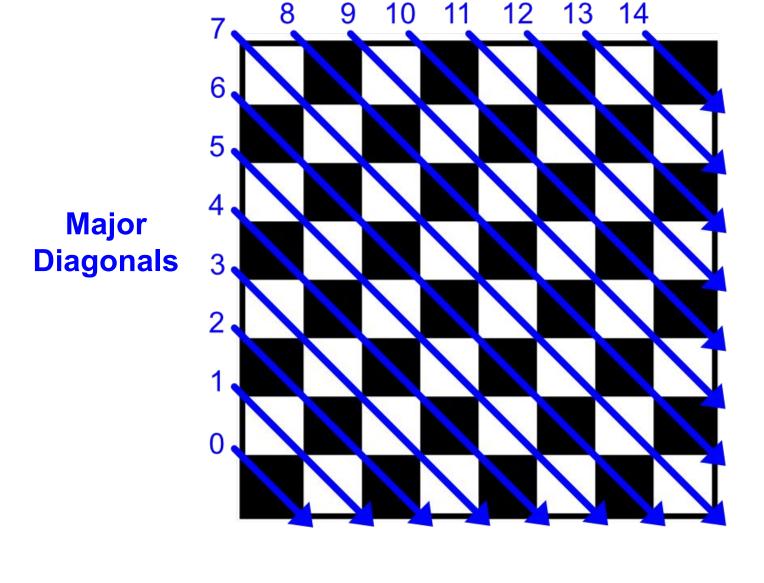


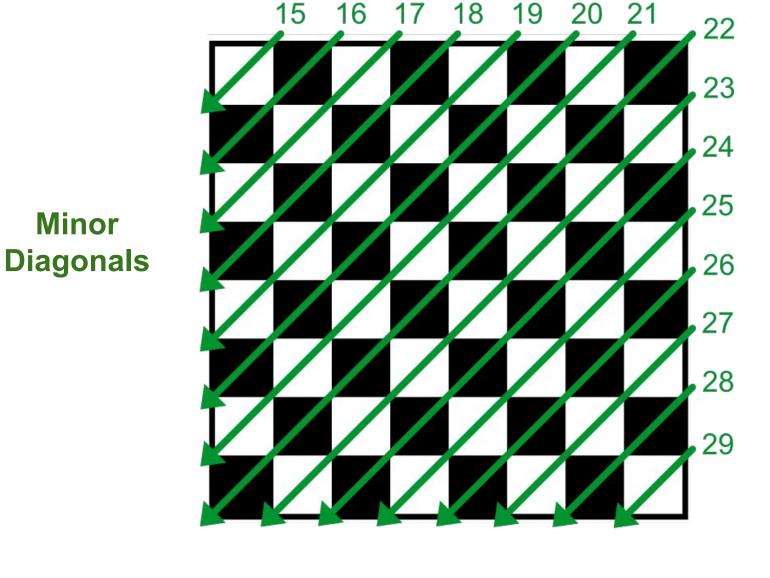




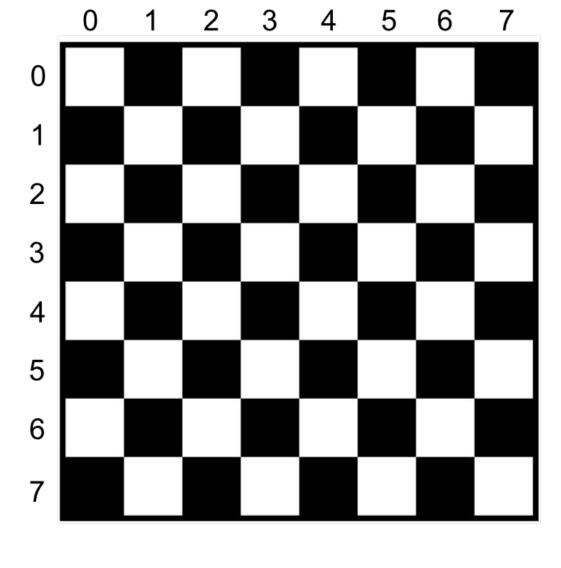
(4,2)





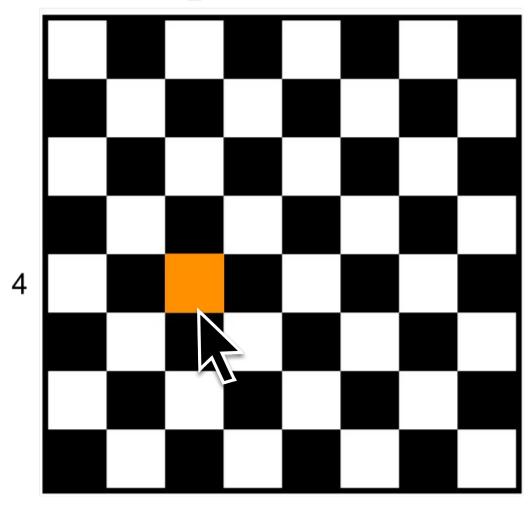


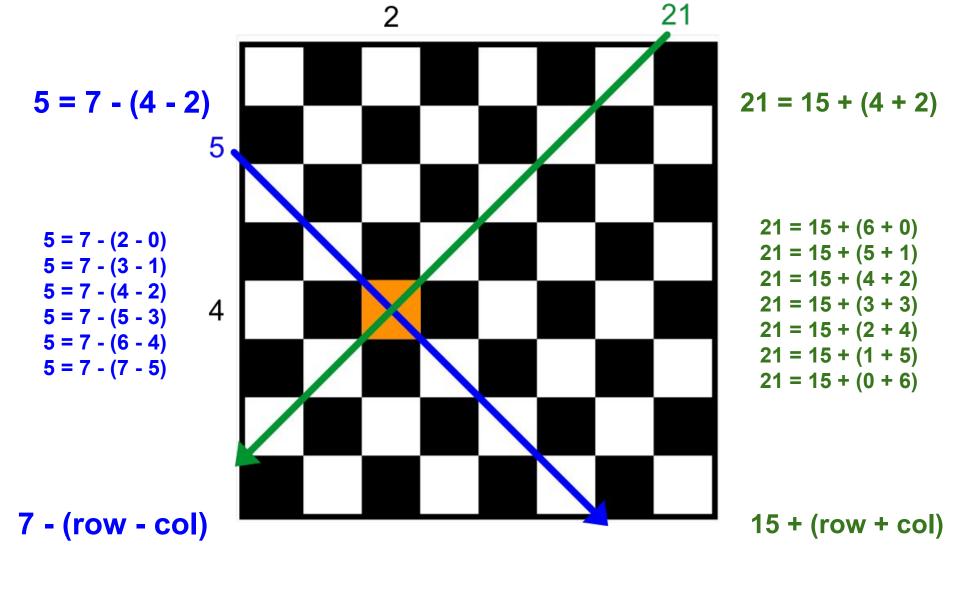
Minor





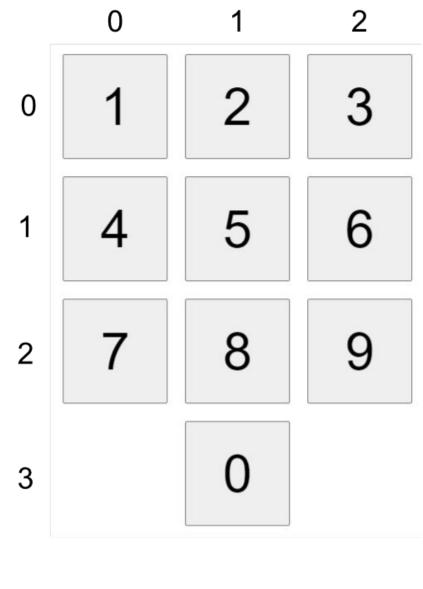
(4,2)

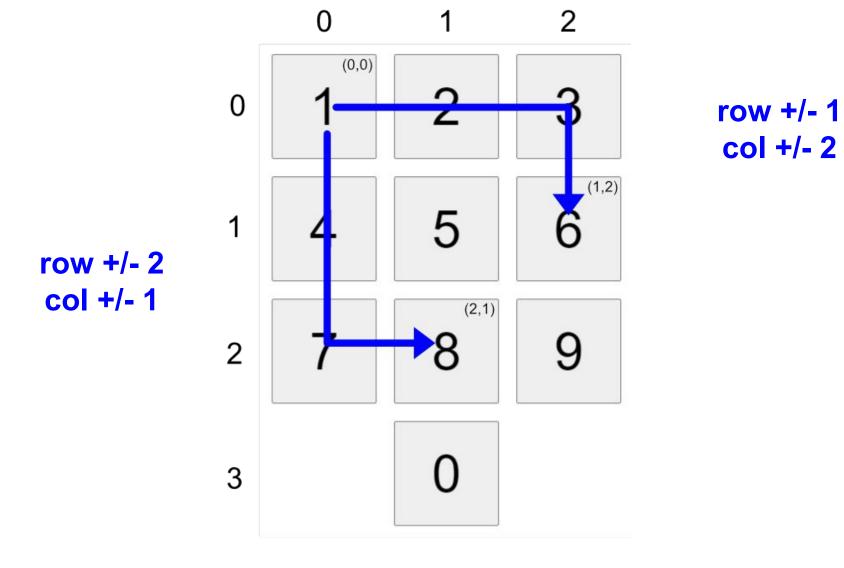


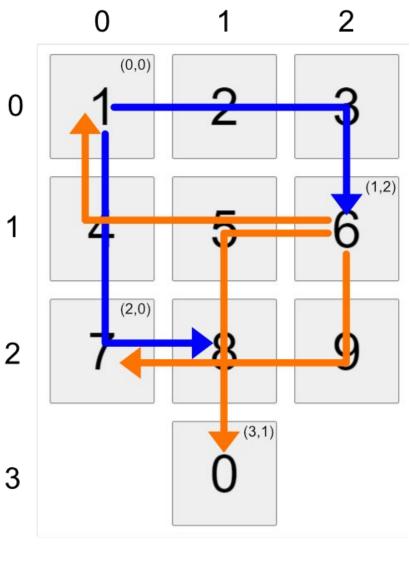


Exercise: Knight's Dialer









countPaths
$$(4,6)$$
 = 168
countPaths $(3,5)$ + 52
countPaths $(9,5)$ + 52
countPaths $(0,5)$ 64

countPaths
$$(3,5) = 52$$

countPaths $(4,4) + 32$
countPaths $(8,4)$

Breadth-First

Depth-First

Traversal



Breadth-First Traversal Iterative+Queue



Depth-First Traversal

O(n): ~2.222ⁿ

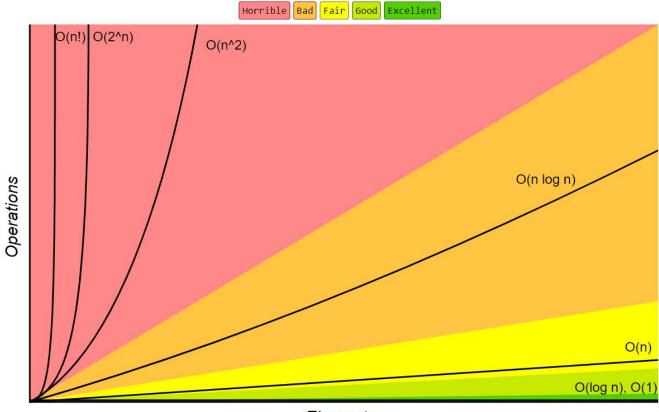
O(6): ~120 ops O(7): ~268 ops O(8): ~595 ops

Exponential

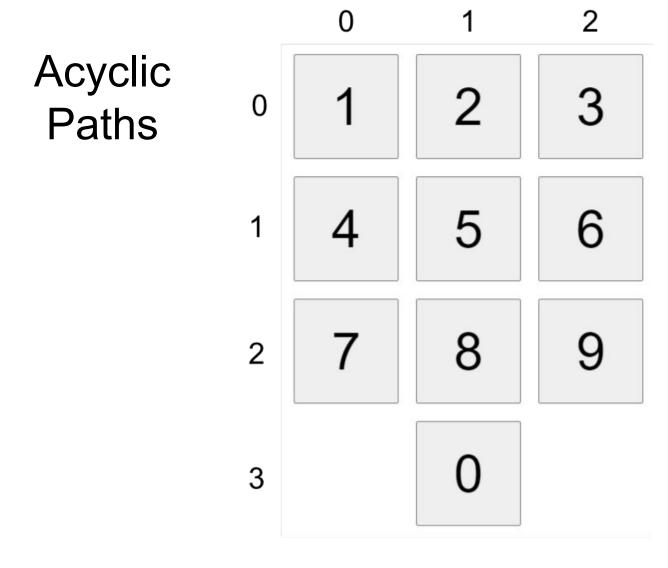
Factorial
Exponential
Polynomic
Linear * Logarithmic
Linear
Logarithmic
Constant



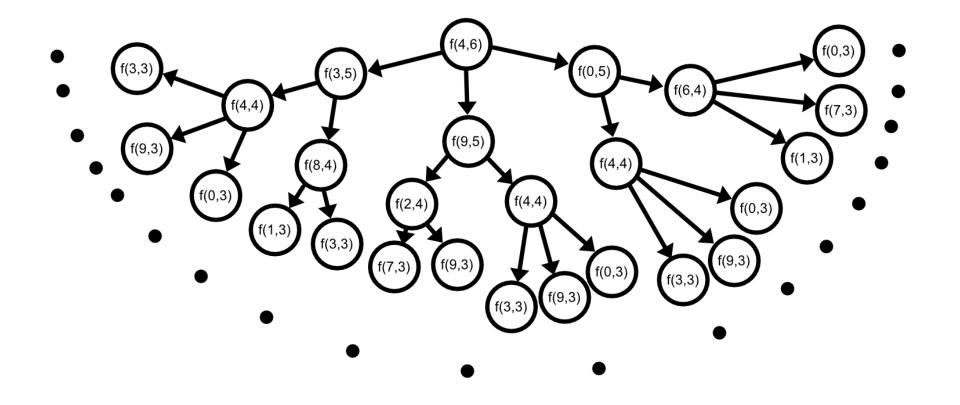
bigocheatsheet.com



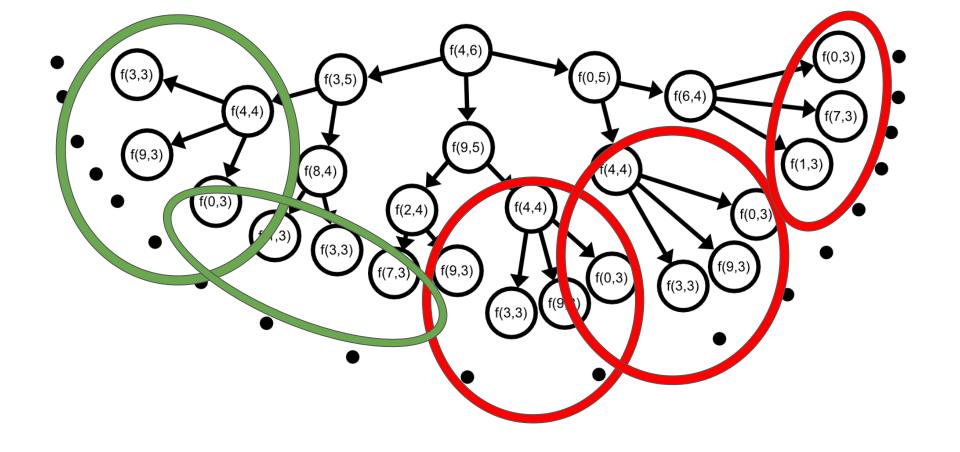
Elements



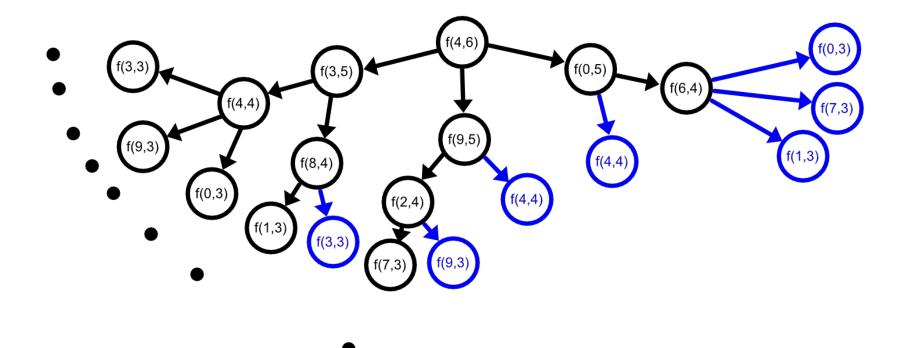
Acyclic Paths $1 \rightarrow 6 \rightarrow 0 \rightarrow 4$ $\rightarrow 3 \rightarrow 8$ 3



(Optimizing) Recursion



Recursion + Memoization

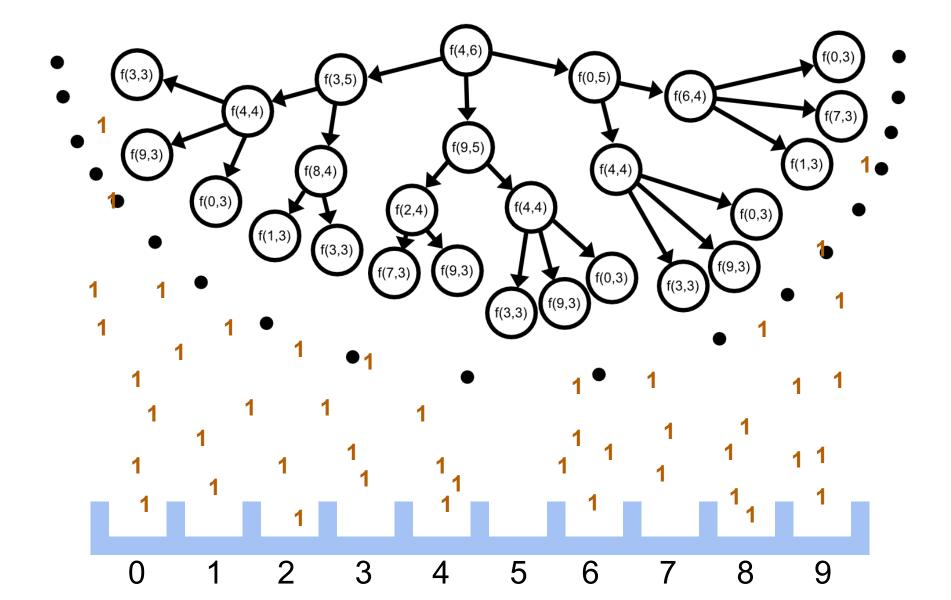


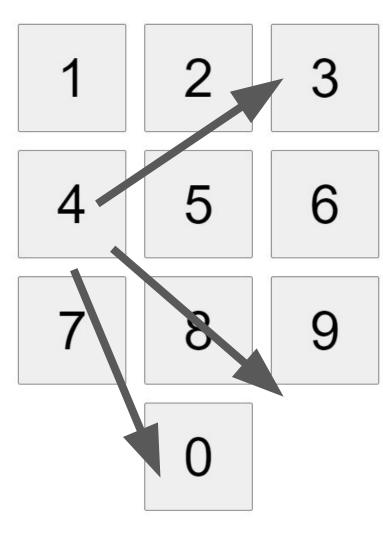
Recursion + Memoization

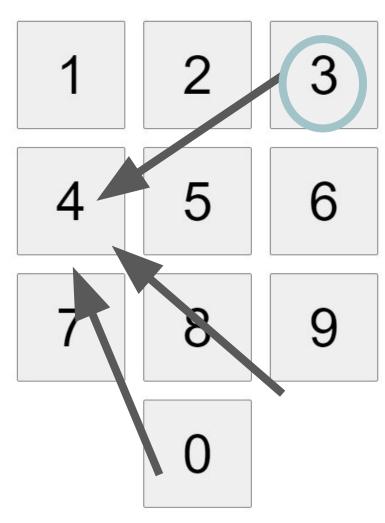
Top-Down Bottom-Up

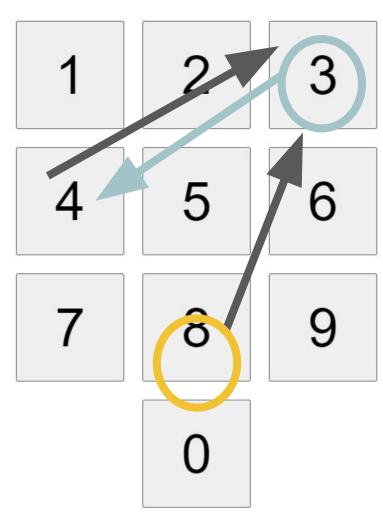
(memoization) (tabulation)

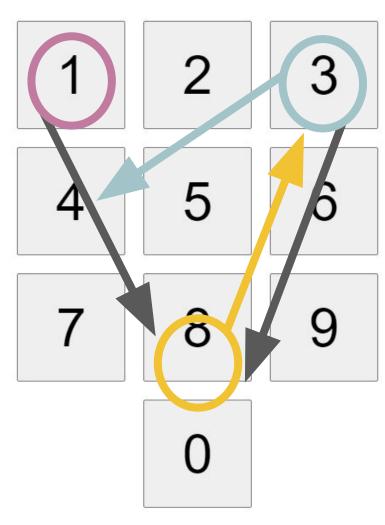
Dynamic Programming



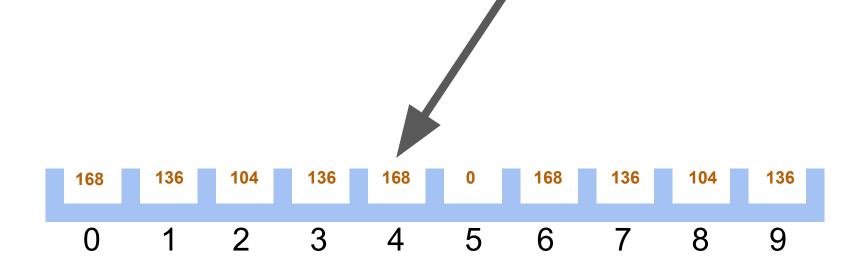




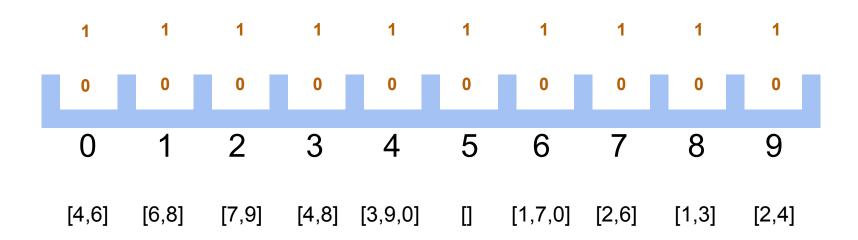




countPaths(4,6)

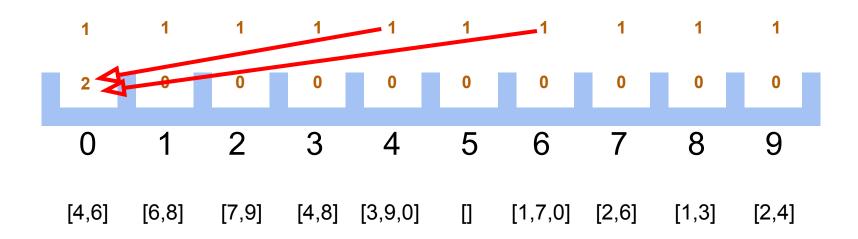


Iteration: 1 hopCount: 6



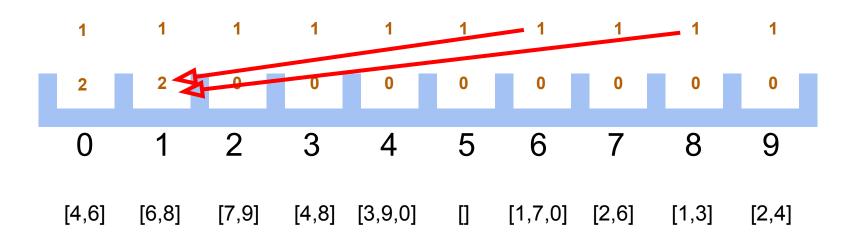


Iteration: 1 hopCount: 6



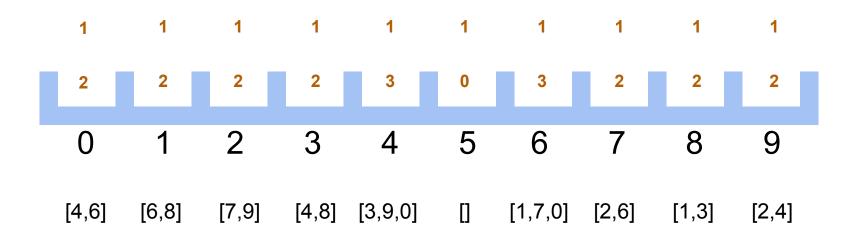


Iteration: 1 hopCount: 6



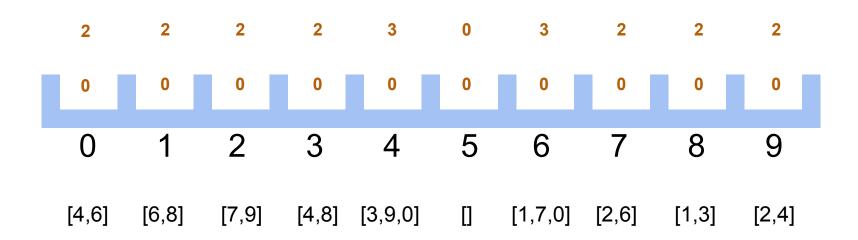


Iteration: 1 hopCount: 6



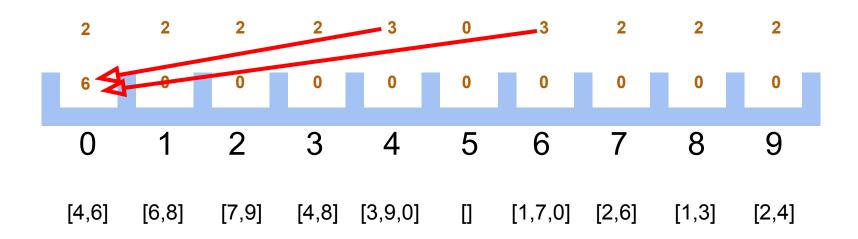


Iteration: 2 hopCount: 5



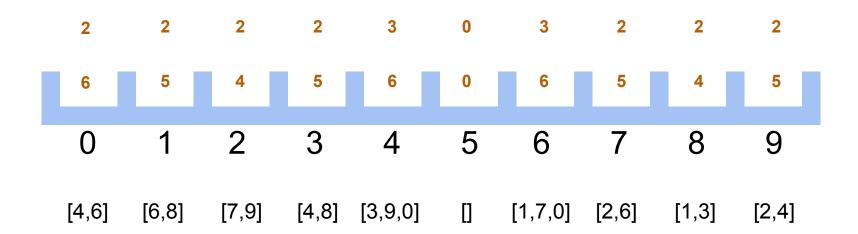


Iteration: 2 hopCount: 5



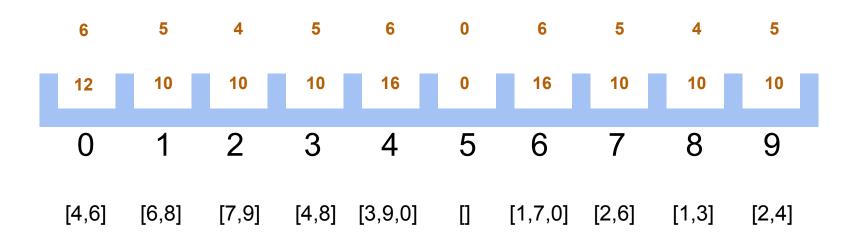


Iteration: 2 hopCount: 5



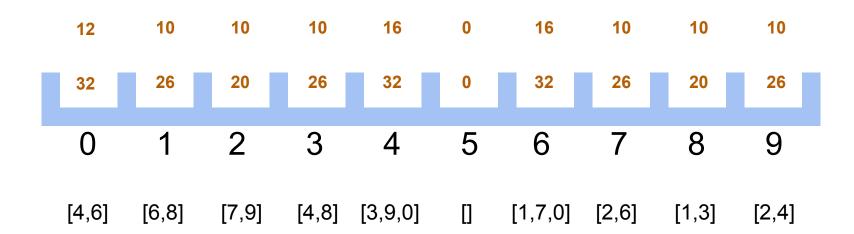


Iteration: 3 hopCount: 4



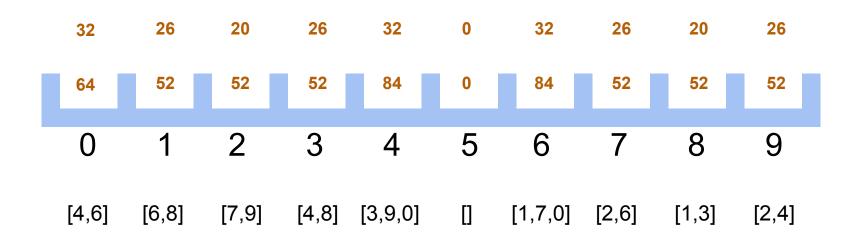


Iteration: 4 hopCount: 3



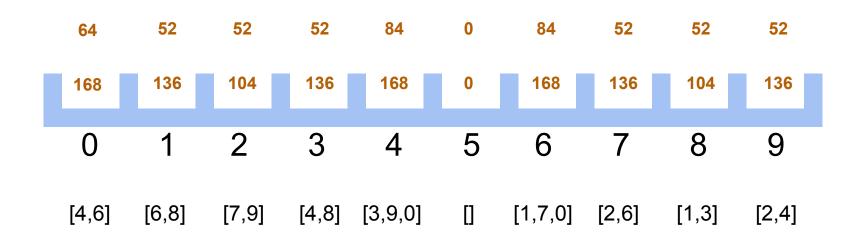


Iteration: 5 hopCount: 2



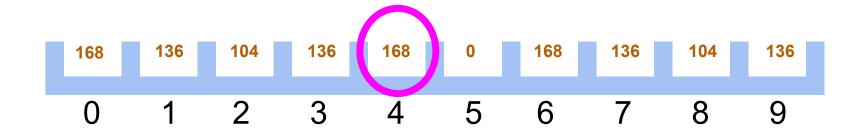


Iteration: 6 hopCount: 1





countPaths(4,6)



$$O(n)$$
: n * 20 => n

O(6): **120 ops**

O(60): **1,200 ops**

O(600): **12,000 ops**

Linear

Exercise: Wordy Unscrambler

Short Dictionary (~2400 words) \vee (entries: 2426) (**0.0** ms)

Letters: PCERA unscramble (28.1 ms)

Input: **PCERA**

ACRE

ARC

ARE

CAP

CAPE

CAR

CARE

EAR

PER

RACE

REAP

Wordscapes



CAN
CAP
CAPE
CAR
CARE
CLAP
EACH
EAR







CAN CAP CAPE CAR CARE CLAP EACH EAR

PCERA

PCERA CPERA EPCRA PECRA... (5! = 120)

PCERA CPERA EPCRA PECRA CEPRA ECPRA RCPEA CRPEA PRCEA RPCEA CPREA PCREA PERCA EPRCA RPECA PRECA ERPCA REPCA RECPA ERCPA CREPA RCEPA FCRPA CERPA AFRPC FARPC RAFPC AREPC FRAPC REAPC PEARC EPARC APERC PAERC EAPRC AEPRC ARPEC RAPEC PAREC APREC RPAEC PRAEC PREAC RPEAC EPRAC PERAC REPAC ERPAC CRPAE RCPAE PCRAE CPRAE RPCAE PRCAE ARCPE RACPE CARPE ACRPE RCAPE CRAPE CPARE PCARE ACPRE CAPRE PACRE APCRE APRCE PARCE RAPCE ARPCE PRACE RPACE FPACR PEACR AFPCR FAPCR PAECR APECR CPEAR PCEAR ECPAR CEPAR PECAR EPCAR EACPR AECPR CEAPR ECAPR ACEPR CAEPR CAPER ACPER PCAER CPAER APCER PACER RACEP ARCEP CRAEP RCAEP ACREP CAREP EARCP AERCP REACP ERACP ARECP RAECP RCEAP CREAP ERCAP RECAP CERAP ECRAP ECARP CEARP AECRP EACRP CAERP ACERP

PCERA CPERA EPCRA PECRA CEPRA ECPRA RCPEA CRPEA PRCEA RPCEA CPREA PCREA PERCA EPRCA RPECA PRECA ERPCA REPCA RECPA ERCPA CREPA RCEPA FCRPA CERPA AFRPC FARPC RAFPC AREPC FRAPC REAPC PEARC EPARC APERC PAERC EAPRC AEPRC ARPEC RAPEC PAREC APREC RPAEC PRAEC PREAC RPEAC EPRAC PERAC REPAC ERPAC CRPAE RCPAE PCRAE CPRAE RPCAE PRCAE ARCPE RACPE CARPE ACRPE RCAPE CRAPE CPARE PCARE ACPRE CAPRE PACRE APCRE APRCE PARCE RAPCE ARPCE PRACE RPACE FPACR PEACR AFPCR FAPCR PAFCR APFCR CPFAR PCFAR ECPAR CEPAR PECAR EPCAR EACPR AECPR CEAPR ECAPR ACEPR CAEPR CAPER ACPER PCAER CPAER APCER PACER RACEP ARCEP CRAEP RCAEP ACREP CAREP EARCP AERCP REACP ERACP ARECP RAECP RCEAP CREAP ERCAP RECAP CERAP ECRAP ECARP CEARP AECRP EACRP CAERP ACERP

CAN

PCERA CPERA EPCRA PECRA CEPRA ECPRA RCPEA CRPEA PRCEA RPCEA CPREA PCREA PERCA EPRCA RPECA PRECA ERPCA REPCA RECPA ERCPA CREPA RCEPA FCRPA CERPA AFRPC FARPC RAFPC AREPC FRAPC REAPC PEARC EPARC APERC PAERC EAPRC AEPRC ARPEC RAPEC PAREC APREC RPAEC PRAEC PREAC RPEAC EPRAC PERAC REPAC ERPAC CRPAE RCPAE PCRAE CPRAE RPCAE PRCAE ARCPE RACPE CARPE ACRPE RCAPE CRAPE CPARE PCARE ACPRE CAPRE PACRE APCRE APRCE PARCE RAPCE ARPCE PRACE RPACE FPACR PEACR AFPCR FAPCR PAECR APECR CPEAR PCEAR ECPAR CEPAR PECAR EPCAR EACPR AECPR CEAPR ECAPR ACEPR CAEPR CAPER ACPER PCAER CPAER APCER PACER RACEP ARCEP CRAEP RCAEP ACREP CAREP EARCP AERCP REACP ERACP ARECP RAECP RCEAP CREAP ERCAP RECAP CERAP ECRAP ECARP CEARP AECRP EACRP CAERP ACERP

CAN CAP

PCERA CPERA EPCRA PECRA CEPRA ECPRA RCPEA CRPEA PRCEA RPCEA CPREA PCREA PERCA EPRCA RPECA PRECA ERPCA REPCA RECPA ERCPA CREPA RCEPA FCRPA CERPA AFRPC FARPC RAFPC AREPC FRAPC REAPC PEARC EPARC APERC PAERC EAPRC AEPRC ARPEC RAPEC PAREC APREC RPAEC PRAEC PREAC RPEAC EPRAC PERAC REPAC ERPAC CRPAE RCPAE PCRAE CPRAE RPCAE PRCAE ARCPE RACPE CARPE ACRPE RCAPE CRAPE CPARE PCARE ACPRE CAPRE PACRE APCRE APRCE PARCE RAPCE ARPCE PRACE RPACE FPACR PEACR AFPCR FAPCR PAFCR APFCR CPFAR PCFAR ECPAR CEPAR PECAR EPCAR EACPR AECPR CEAPR ECAPR ACEPR CAEPR CAPER ACPER PCAER CPAER APCER PACER RACEP ARCEP CRAEP RCAEP ACREP CAREP EARCP AERCP REACP ERACP ARECP RAECP RCEAP CREAP ERCAP RECAP CERAP ECRAP ECARP CEARP AECRP EACRP CAERP ACERP

CAN CAP CAPE

PCERA CPERA EPCRA PECRA CEPRA ECPRA RCPEA CRPEA PRCEA RPCEA CPREA PCREA PERCA EPRCA RPECA PRECA ERPCA REPCA RECPA ERCPA CREPA RCEPA FCRPA CERPA AFRPC FARPC RAFPC AREPC FRAPC REAPC PEARC EPARC APERC PAERC EAPRC AEPRC ARPEC RAPEC PAREC APREC RPAEC PRAEC PREAC RPEAC EPRAC PERAC REPAC ERPAC CRPAE RCPAE PCRAE CPRAE RPCAE PRCAE ARCPE RACPE CARPE ACRPE RCAPE CRAPE CPARE PCARE ACPRE CAPRE PACRE APCRE APRCE PARCE RAPCE ARPCE PRACE RPACE FPACR PEACR AFPCR FAPCR PAFCR APFCR CPFAR PCFAR ECPAR CEPAR PECAR EPCAR EACPR AECPR CEAPR ECAPR ACEPR CAEPR CAPER ACPER PCAER CPAER APCER PACER RACEP ARCEP CRAEP RCAEP ACREP CAREP EARCP AERCP REACP ERACP ARECP RAECP RCEAP CREAP ERCAP RECAP CERAP ECRAP ECARP CEARP AECRP EACRP CAERP ACERP

CAN CAP CAPE CAR

PCERA CPERA EPCRA PECRA CEPRA ECPRA RCPEA CRPEA PRCEA RPCEA CPREA PCREA PERCA EPRCA RPECA PRECA ERPCA REPCA RECPA ERCPA CREPA RCEPA FCRPA CERPA AFRPC FARPC RAFPC AREPC FRAPC REAPC PEARC EPARC APERC PAERC EAPRC AEPRC ARPEC RAPEC PAREC APREC RPAEC PRAEC PREAC RPEAC EPRAC PERAC REPAC ERPAC CRPAE RCPAE PCRAE CPRAE RPCAE PRCAE ARCPE RACPE CARPE ACRPE RCAPE CRAPE CPARE PCARE ACPRE CAPRE PACRE APCRE APRCE PARCE RAPCE ARPCE PRACE RPACE FPACR PEACR AFPCR FAPCR PAFCR APFCR CPFAR PCFAR ECPAR CEPAR PECAR EPCAR EACPR AECPR CEAPR ECAPR ACEPR CAEPR CAPER ACPER PCAER CPAER APCER PACER RACEP ARCEP CRAEP RCAEP ACREP CAREP EARCP AERCP REACP ERACP ARECP RAECP RCEAP CREAP ERCAP RECAP CERAP ECRAP ECARP CEARP AECRP EACRP CAERP ACERP

CAN CAP CAPE CAR CARE

PCERA CPERA EPCRA PECRA CEPRA ECPRA RCPEA CRPEA PRCEA RPCEA CPREA PCREA PERCA EPRCA RPECA PRECA ERPCA REPCA RECPA ERCPA CREPA RCEPA FCRPA CERPA AFRPC FARPC RAFPC AREPC FRAPC REAPC PEARC EPARC APERC PAERC EAPRC AEPRC ARPEC RAPEC PAREC APREC RPAEC PRAEC PREAC RPEAC EPRAC PERAC REPAC ERPAC CRPAE RCPAE PCRAE CPRAE RPCAE PRCAE ARCPE RACPE CARPE ACRPE RCAPE CRAPE CPARE PCARE ACPRE CAPRE PACRE APCRE APRCE PARCE RAPCE ARPCE PRACE RPACE FPACR PEACR AFPCR FAPCR PAFCR APFCR CPFAR PCFAR ECPAR CEPAR PECAR EPCAR EACPR AECPR CEAPR ECAPR ACEPR CAEPR CAPER ACPER PCAER CPAER APCER PACER RACEP ARCEP CRAEP RCAEP ACREP CAREP EARCP AERCP REACP ERACP ARECP RAECP RCEAP CREAP ERCAP RECAP CERAP ECRAP ECARP CEARP AECRP EACRP CAERP ACERP

CAN CAP CAPE CAR CARE CLAP

PCERA CPERA EPCRA PECRA CEPRA ECPRA RCPEA CRPEA PRCEA RPCEA CPREA PCREA PERCA EPRCA RPECA PRECA ERPCA REPCA RECPA ERCPA CREPA RCEPA FCRPA CERPA AFRPC FARPC RAFPC AREPC FRAPC REAPC PEARC EPARC APERC PAERC EAPRC AEPRC ARPEC RAPEC PAREC APREC RPAEC PRAEC PREAC RPEAC EPRAC PERAC REPAC ERPAC CRPAE RCPAE PCRAE CPRAE RPCAE PRCAE ARCPE RACPE CARPE ACRPE RCAPE CRAPE CPARE PCARE ACPRE CAPRE PACRE APCRE APRCE PARCE RAPCE ARPCE PRACE RPACE FPACR PEACR AFPCR FAPCR PAFCR APFCR CPFAR PCFAR ECPAR CEPAR PECAR EPCAR EACPR AECPR CEAPR ECAPR ACEPR CAEPR CAPER ACPER PCAER CPAER APCER PACER RACEP ARCEP CRAEP RCAEP ACREP CAREP EARCP AERCP REACP ERACP ARECP RAECP RCEAP CREAP ERCAP RECAP CERAP ECRAP ECARP CEARP AECRP EACRP CAERP ACERP

CAN CAP CAPE CAR CARE CLAP EACH

PCERA CPERA EPCRA PECRA CEPRA ECPRA RCPEA CRPEA PRCEA RPCEA CPREA PCREA PERCA EPRCA RPECA PRECA ERPCA REPCA RECPA ERCPA CREPA RCEPA FCRPA CERPA AFRPC FARPC RAFPC ARFPC FRAPC REAPC PEARC EPARC APERC PAERC EAPRC AEPRC ARPEC RAPEC PAREC APREC RPAEC PRAEC PREAC RPEAC EPRAC PERAC REPAC ERPAC CRPAE RCPAE PCRAE CPRAE RPCAE PRCAE ARCPE RACPE CARPE ACRPE RCAPE CRAPE CPARE PCARE ACPRE CAPRE PACRE APCRE APRCE PARCE RAPCE ARPCE PRACE RPACE FPACR PEACR AFPCR FAPCR PAECR APECR CPEAR PCEAR ECPAR CEPAR PECAR EPCAR EACPR AECPR CEAPR ECAPR ACEPR CAEPR CAPER ACPER PCAER CPAER APCER PACER RACEP ARCEP CRAEP RCAEP ACREP CAREP EARCP AERCP REACP ERACP ARECP RAECP RCEAP CREAP ERCAP RECAP CERAP ECRAP ECARP CEARP AECRP EACRP CAERP ACERP

CAN CAP CAPE CAR CARE CLAP EACH EAR

PCERA CPERA EPCRA PECRA... (5! = 120)

NPCERA

NPCERA PNCERA CNPERA NCPERA... (6! = 720)

NPCERAH

NPCERAH PNCERAH CNPERAH NCPERAH... (7! = 5,040)

O(k): k!

Factorial

```
4! = 24
       5! = 120
       6! = 720
      7! = 5,040
      8! = 40,320
     9! = 362,880
    10! = 3,628,800
   11! = 39,916,800
   12! = 479,001,600
  13! = 6,227,020,800
 14! = 87,178,291,200
15! = 1,307,674,368,000
```

The worst part is, we can't just do this permutation once.

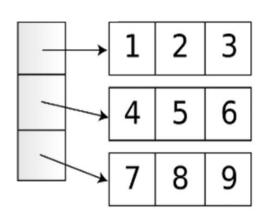
Above 11 or 12 characters, that'd be too many strings to hold in memory all at once.

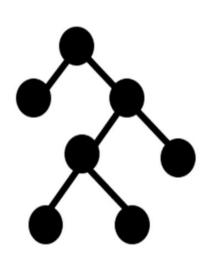
So we're going to have to re-permute input for each word we check. O(n * k!)

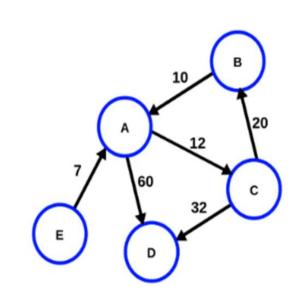
Actually, it's not that bad. (but it's still bad)

Permutation of the input can stop once the length of the word is reached.

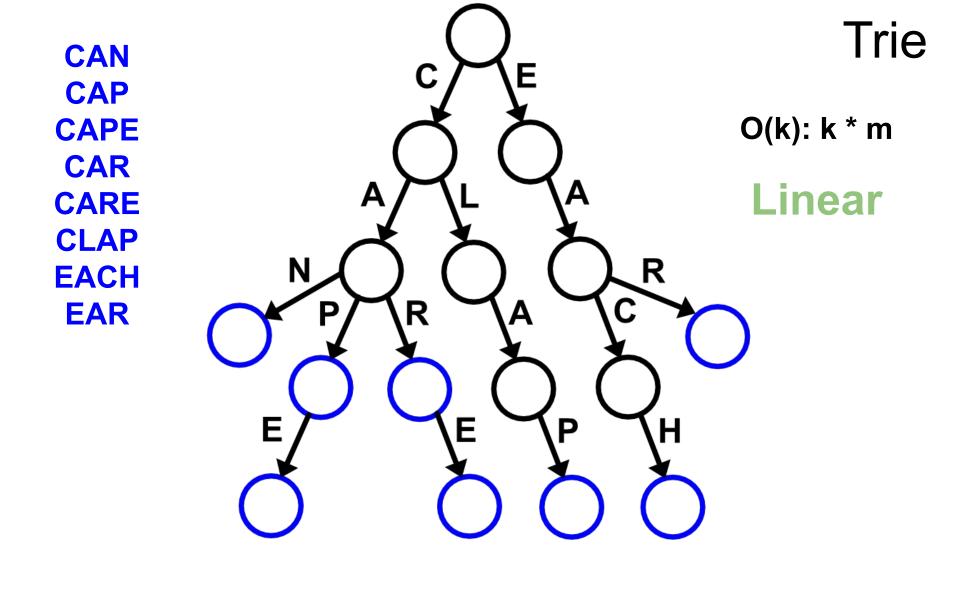
Also, we can abandon any partial permutation result that doesn't match the beginning of each word.





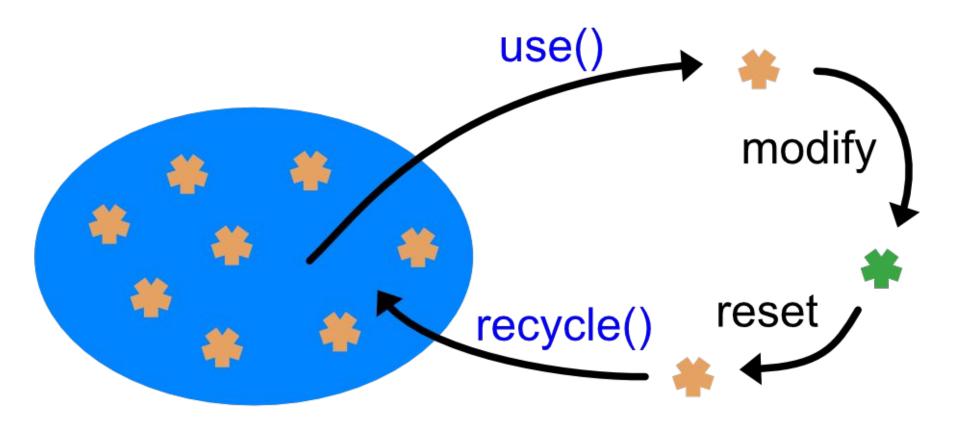


Data Structures

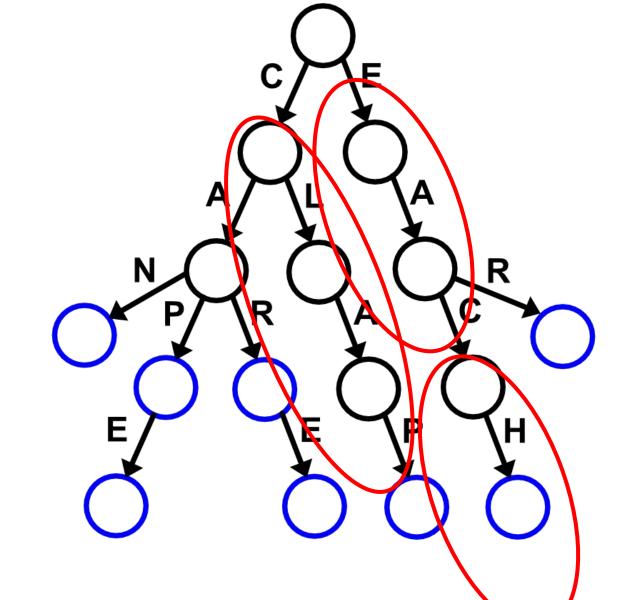


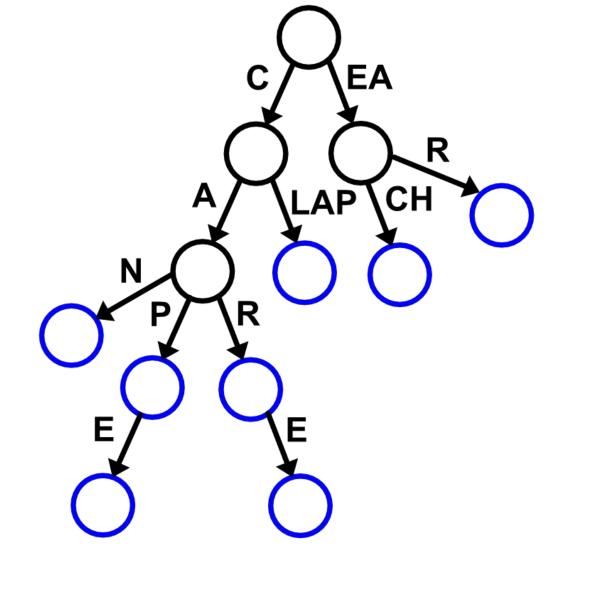


Minimizing Garbage Collection



Object Pool





CAN

CAP

CAPE

CAR

CARE

CLAP

EACH

EAR

Radix

Tree

CAN CAP CAPE CAR CARE CLAP EACH EAR

DAFSA / DAWG

H _ _



explain

e xplain xe plain pxe lain Ipxe ain alpxe in ialpxe n nialpxe

GADDAG

https://en.wikipedia.org/wiki/GADDAG



Bonus: Dwordly





The End