# Lista de Exemplos U04-Parte 01

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4.1 - Conceito de Variável Aleatória (V.A.) e

4.2 - Probabilidade associada à variável aleatória (V.A.)

Questão 1 – Um experimento (E) consiste em jogar uma moeda 4 vezes.

**A)** Especifique o espaço amostral (S), onde C corresponde a "cara"e K corresponde a "coroa".

RESPOSTA

```
S = [

KKKK, KKKC, KKCK, KKCC,

KCKK, KCCK, KCKC, KCCC,

CCCC, CCCK, CCKC, CCKK,

CKCC,CKCK, CKKC, CKKK

]
```

**B)** Seja a Variável Aleatória (X) a ocorrencia de "coroas" nas 4 jogadas. Especifique os resultados de S, os valores de X correspondentes (contradomínio  $R_x$ ) e a probabilidade de cada valor de X.

RESPOSTA

### Questão 2 – Um experimento (E) consiste em jogar 3 dados (de 6 faces).

**A)** Especifique o espaço amostral S. Especificando a ocorrencia das faces pelo número correspondente (1, 2, 3, 4, 5 ou 6).

#### RESPOSTA

```
\mathbf{E} = [
(000), (001), (002), (003), (004), (005), (006),
(010), (011), (012), (013), (014), (015), (016),
(020), (021), (022), (023), (024), (025), (026),
(030), (031), (032), (033), (034), (035), (036),
(040), (041), (042), (043), (044), (045), (046),
(050), (051), (052), (053), (054), (055), (056),
(060), (061), (062), (063), (064), (065), (066),
(100), (101), (102), (103), (104), (105), (106),
(110), (111), (112), (113), (114), (115), (116),
(120), (121), (122), (123), (124), (125), (126),
(130), (131), (132), (133), (134), (135), (136),
(140), (141), (142), (143), (144), (145), (146),
(150), (151), (152), (153), (154), (155), (156),
(160), (161), (162), (163), (164), (165), (166),
(200), (201), (202), (203), (204), (205), (206),
(210), (211), (212), (213), (214), (215), (216),
(220), (221), (222), (223), (224), (225), (226),
(230), (231), (232), (233), (234), (235), (236),
(240), (241), (242), (243), (244), (245), (246),
(250), (251), (252), (253), (254), (255), (256),
(260), (261), (262), (263), (264), (265), (266),
(300), (301), (302), (303), (304), (305), (306),
(310), (311), (312), (313), (314), (315), (316),
(320), (321), (322), (323), (324), (325), (326),
(330), (331), (332), (333), (334), (335), (336),
(340), (341), (342), (343), (344), (345), (346),
(350), (351), (352), (353), (354), (355), (356),
(360), (361), (362), (363), (364), (365), (366),
(400), (401), (402), (403), (404), (405), (406),
(410), (411), (412), (413), (414), (415), (416),
```

```
(420), (421), (422), (423), (424), (425), (426),
(430), (431), (432), (433), (434), (435), (436),
(440), (441), (442), (443), (444), (445), (446),
(450), (451), (452), (453), (454), (455), (456),
(460), (461), (462), (463), (464), (465), (466),
(500), (501), (502), (503), (504), (505), (506),
(510), (511), (512), (513), (514), (515), (516),
(520), (521), (522), (523), (524), (525), (526),
(530), (531), (532), (533), (534), (535), (536),
(540), (541), (542), (543), (544), (545), (546),
(550), (551), (552), (553), (554), (555), (556),
(560), (561), (562), (563), (564), (565), (566),
(600), (601), (602), (603), (604), (605), (606),
(610), (611), (612), (613), (614), (615), (616),
(620), (621), (622), (623), (624), (625), (626),
(630), (631), (632), (633), (634), (635), (636),
(640), (641), (642), (643), (644), (645), (646),
(650), (651), (652), (653), (654), (655), (656),
(660), (661), (662), (663), (664), (665), (666)
print("E = [")
for i in range(7):
  for j in range(7):
     for n in range(7):
       print(f"({i}{j}{n}), ", end=" ")
     print()
  print("\n")
print("]")
```

**B)** Seja a Variável Aleatória (X) a soma dos valores das duas primeiras faces menos o valor da terceira. Especifique os resultados de S, os valores de X correspondentes (contradomínio  $R_x$ ) e a probabilidade de cada valor de X.

#### RESPOSTA

### Contradomínio $R_x$

$$Rx = [0, -1, -2, -3, -4, -5, -6, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12]$$

#### Probabilidade de cada valor de X

```
X_0 = 0.00291545, X_1 = 0.00874636, X_2 = 0.01749271
```

```
X_3 = 0.02915452, X_4 = 0.04373178, X_5 = 0.06122449
X_6 = 0.08163265, X_7 = 0.09620991, X_8 = 0.10495627
X_9 = 0.10787172, X_{10} = 0.10495627, X_{11} = 0.09620991
X_{12} = 0.08163265, X_{13} = 0.06122449, X_{14} = 0.04373178
X_{15} = 0.02915452, X_{16} = 0.01749271, X_{17} = 0.00874636
X_{18} = 0.00291545
Resultado de S
s = []
for i in range(7):
  for j in range(7):
    for n in range(7):
      soma = (i+j)-n
      s.append(soma)
      print(f"x({i}{j}{n}) = {soma}, ", end="")
    print()
  print("\n")
unicos lista = list(dict.fromkeys(s))
print("Rx", unicos lista)
Encontrando o Contradomínio R_x e as Probabilidades de cada valor de X
import numpy as np
0], dtype="float64")
for i in s:
  if (i == -6):
    prob[0] += 1/len(s)
  elif (i == -5):
    prob[1] += 1/len(s)
  elif (i == -4):
    prob[2] += 1/len(s)
  elif (i == -3):
    prob[3] += 1/len(s)
  elif (i == -2):
    prob[4] += 1/len(s)
  elif (i == -1):
    prob[5] += 1/len(s)
  elif (i == 0):
    prob[6] += 1/len(s)
  elif (i == 1):
```

```
prob[7] += 1/len(s)
  elif (i == 2):
    prob[8] += 1/len(s)
  elif (i == 3):
    prob[9] += 1/len(s)
  elif (i == 4):
    prob[10] += 1/len(s)
  elif (i == 5):
    prob[11] += 1/len(s)
  elif (i == 6):
    prob[12] += 1/len(s)
  elif (i == 7):
    prob[13] += 1/len(s)
  elif (i == 8):
    prob[14] += 1/len(s)
  elif (i == 9):
    prob[15] += 1/len(s)
  elif (i == 10):
    prob[16] += 1/len(s)
  elif (i == 11):
    prob[17] += 1/len(s)
  elif (i == 12):
    prob[18] += 1/len(s)
print(f"\nProbabilidade para os Xs =\n {prob}\n")
print(f"Soma das Probabilidades: {prob.sum()}")
Probabilidade para os Xs =
 [0.00291545 0.00874636 0.01749271 0.02915452 0.04373178 0.06122449
 0.08163265 0.09620991 0.10495627 0.10787172 0.10495627 0.09620991
 0.08163265 0.06122449 0.04373178 0.02915452 0.01749271 0.00874636
 0.002915451
Soma das Probabilidades: 1.00000000000000004
```

#### 4.3 - Variáveis aleatórias discretas e contínuas e

## 4.4 - Funções de variáveis aleatórias (V.A.) - fdp e FDP

Questão 3 - Com base na Questão 1. Determine:

**A)** 
$$p(x_i)$$
 – fdp de  $X$ .

RESPOSTA

```
x_i |
P[X = x_i]
B) F(x_i) -FDP de X.
     RESPOSTA
x_i |
F[X = x_i]
prob_q1 = np.array([1/16, 1/4, 3/8, 1/4, 1/16], dtype="float64")
fdp q1 = prob q1*100.0
print(f"\np(xi)- fdp de X:")
for i in fdp q1:
  print(f"{i}% ", end=" ")
FDP q1 = np.zeros(5)
for i in range(0, 5):
  FDP q1[i] = fdp q1[:i+1].sum()
print(f"\n\nF(xi)-FDP de X:")
for i in FDP q1:
  print(f"{i}% ", end=" ")
p(xi) – fdp de X:
6.25% 25.0% 37.5% 25.0% 6.25%
F(xi)-FDP de X:
6.25% 31.25% 68.75% 93.75% 100.0%
Questão 4 - Com base na Questão 2. Determine:
a) p(x_i) – fdp de X.
     RESPOSTA
```

x\_i 0

 $P[X = x_i]$  0.29%

```
10
x_i
P[X = x i]
                                                10.49%
fdp_q2 = prob*100
print(f"\n\p(xi) - fdp de X:")
for i in range (19):
  print(f"{format(fdp_q2[i], '.2f')}% ", end=" ")
  if (i == 9):
    print()
p(xi) – fdp de X:
0.29% 0.87% 1.75% 2.92% 4.37% 6.12% 8.16% 9.62% 10.50% 10.79%
10.50% 9.62% 8.16% 6.12% 4.37% 2.92% 1.75% 0.87% 0.29%
b) F(x_i) -FDP de X.
     RESPOSTA
FDP q2 = np.zeros(19)
for i in range (0, 19):
  FDP q2[i] = fdp q2[:i+1].sum()
print("\nF(xi)- FDP de X: ")
for i in range (19):
  print(f"{format(FDP q2[i], '.2f')}% " , end=" ")
  if (i == 9):
    print()
F(xi) - FDP de X:
0.29% 1.17% 2.92% 5.83% 10.20% 16.33% 24.49% 34.11% 44.61%
55.39%
65.89% 75.51% 83.67% 89.80% 94.17% 97.08% 98.83% 99.71%
100.00%
Questão 5 - Uma função distribuição de probabilidade acumulada FDP é definida da seguinte
forma:
     X < a \rightarrow F = 0;
   a \le X \le b \to F = \frac{x-a}{b-a};
```

•  $X > b \rightarrow F = 1$ ;

- a) Calcule f(x) fdp de X.
  - RESPOSTA
- b) Calcule  $P[1 < X \le 3]$  para a=1 e b=5.
  - RESPOSTA
- c) Calcule  $P[-1 < X \le 2]$  para a=1 e b=5.
  - RESPOSTA
- d) Calcule  $P[-\infty < X \le 1, 5]$  para a=1 e b=5.
  - RESPOSTA
- e) Calcule  $P[0 < X \le 6]$  para a = 1 e b = 5.
  - RESPOSTA

Questão 6 - O tempo de transmissão X de mensagens em um sistema de comunicação obedece a lei de probabilidade exponencial com parâmetro  $\lambda$ , isto é  $P[X>x]=e-\lambda x, x>0$ . Calcule,  $T=1/\lambda$ .

- a) Defina F(x) FDP de X
  - RESPOSTA

- b) Calcule f(x) fdp de X.
  - RESPOSTA
- c) Calcule  $P[T < X \le 2T]$  para  $T = T = 1/\lambda$ .
  - RESPOSTA