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**EE 254**

# **Electronic Instrumentation**

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***Lecture Note #12***

## 4. Data Converters

- \*\*\* Analogue to Digital (A/D) Conversion (ADC)
- \*\*\* Digital to Analogue (D/A) Conversion (DAC)
- \*\*\* Sample and Hold Circuit

# Analogue-to-Digital Converters

1. Parallel or Flash ADC
2. Counting ADC
3. Dual-Slope ADC
4. Successive Approximation A/D Converter
5. Semi-flash ADC
6. Delta-Sigma ADC
7. Pipelined ADC

# Digital-to-Analogue Converters

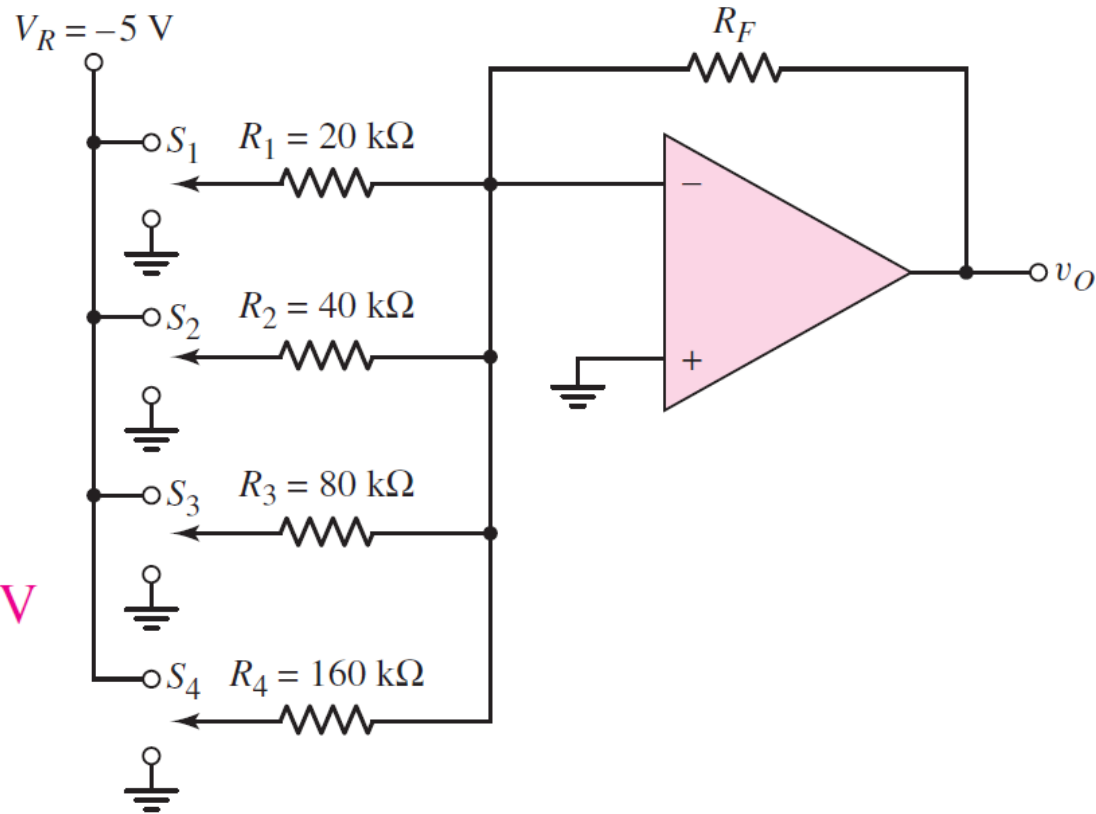
1. Weighted-Resistor DAC
2. R–2R Ladder Network DAC
3. Segmented DAC
4. Delta-Sigma DAC

# Digital-to-Analog Converters

## Weighted-Resistor 4-Bit D/A

- ✿ A simple 4-bit D/A converter.
- ✿ With  $R_F = 10\text{ k}\Omega$ , the output voltage:

$$v_O = \left( \frac{b_1}{2} + \frac{b_2}{4} + \frac{b_3}{8} + \frac{b_4}{16} \right) (5)\text{ V}$$

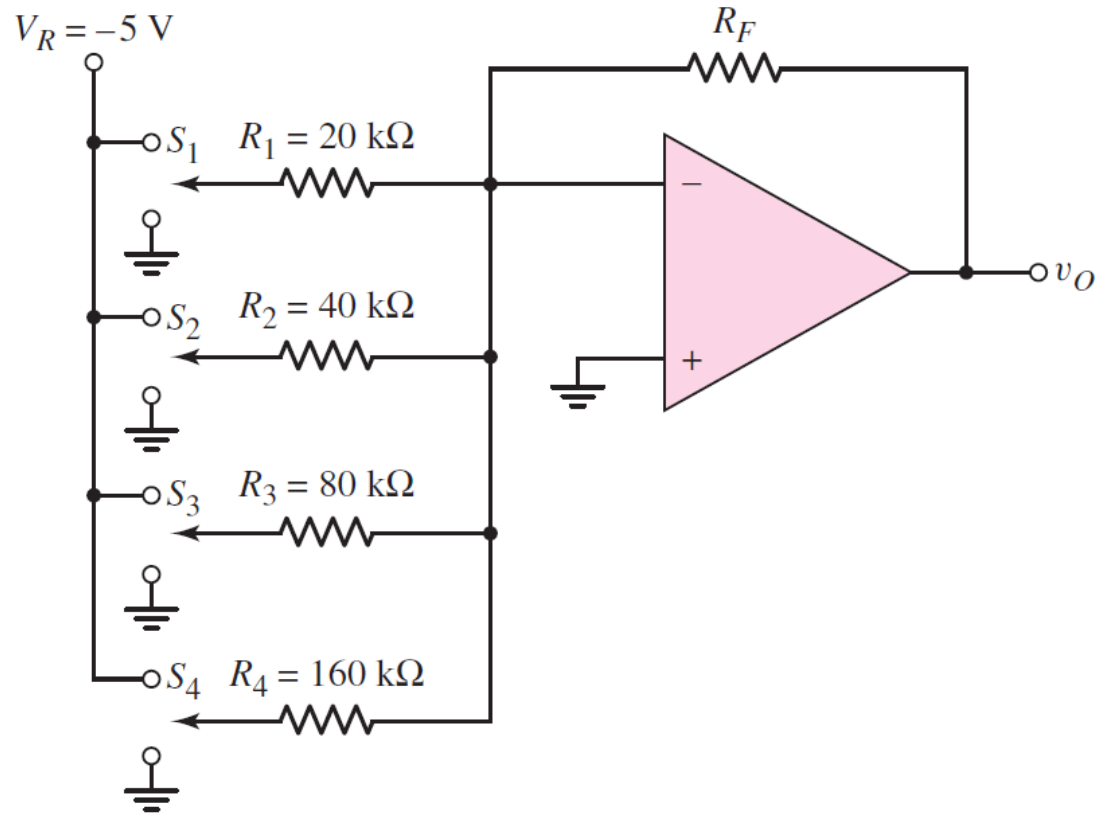


- ✿ Accuracy of the circuit can be achieved by the precision of the weighted resistors and the feedback resistor.
- ✿ When the  $N$  increases, the size of the weighted input resistance increases for lesser significant bits.

# Digital-to-Analog Converters

## Weighted-Resistor 4-Bit D/A

- ✿ The accuracy for large resistance values becomes more difficult to maintain.
- ✿ The size of this D/A converter is in general limited to a 4-bit input.
- ✿ Another factor that determines the **accuracy** of the D/A circuit is the **precision of the switches**.

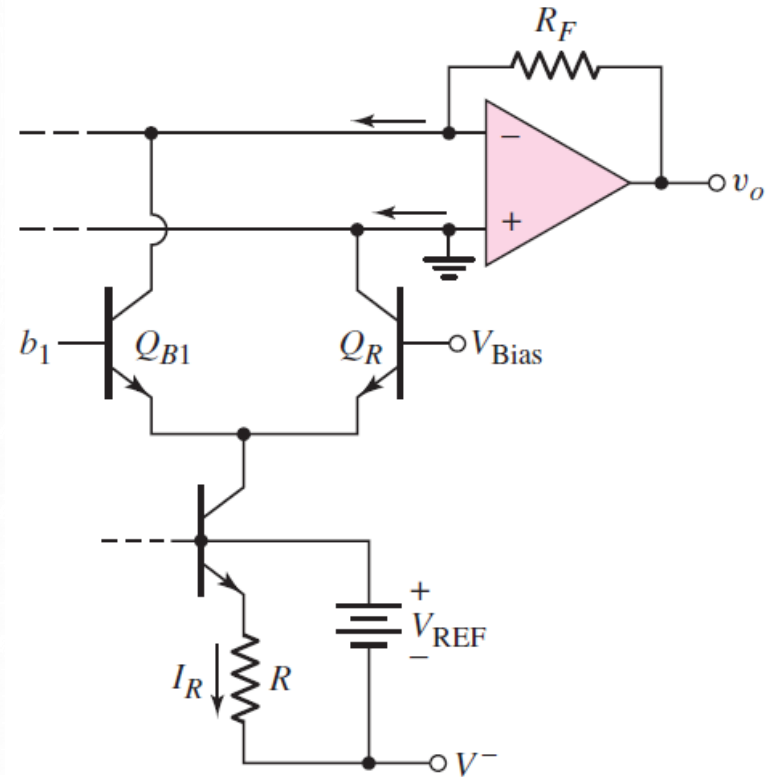




# Digital-to-Analog Converters

## Weighted-Resistor 4-Bit D/A

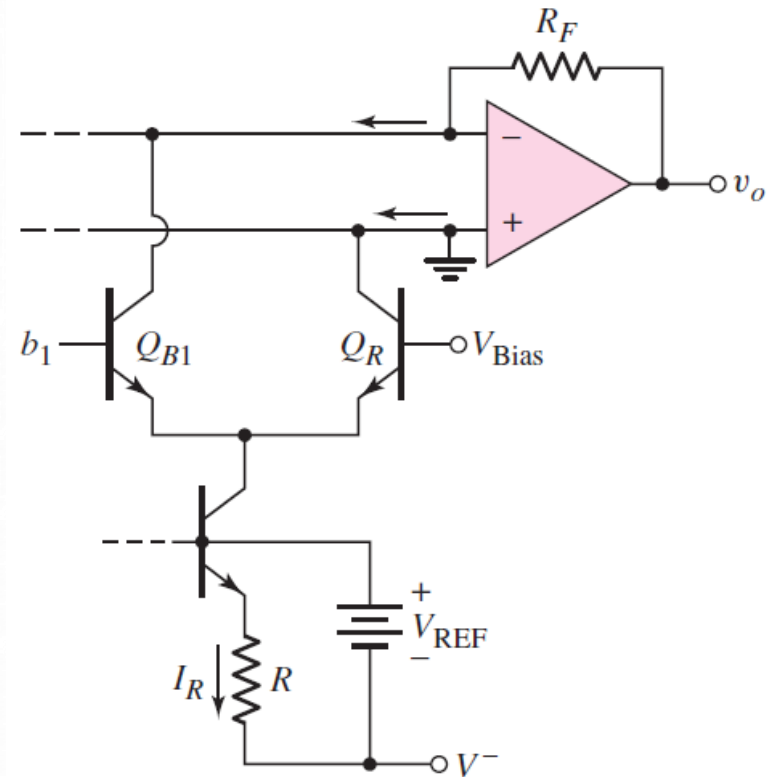
- ✿ An example of a current switch, showing only the MSB.
- ✿ If the bit  $b_1$  is a logic 1 ( $> V_{Bias}$ ), then  $Q_{B1}$  is turned on and  $Q_R$  is turned off so that the current  $I_R$  is switched through  $Q_{B1}$ .
- ✿ This current becomes a component of the current through the feedback resistor.
- ✿ If  $b_1$  is a logic 0 ( $< V_{Bias}$ ), then  $Q_{B1}$  is turned off and  $Q_R$  is turned on so that the current is switched to ground.
- ✿ Because of the virtual ground, we may note that the collector voltages of  $Q_{B1}$  and  $Q_R$  are essentially identical.



# Digital-to-Analog Converters

## Weighted-Resistor 4-Bit D/A

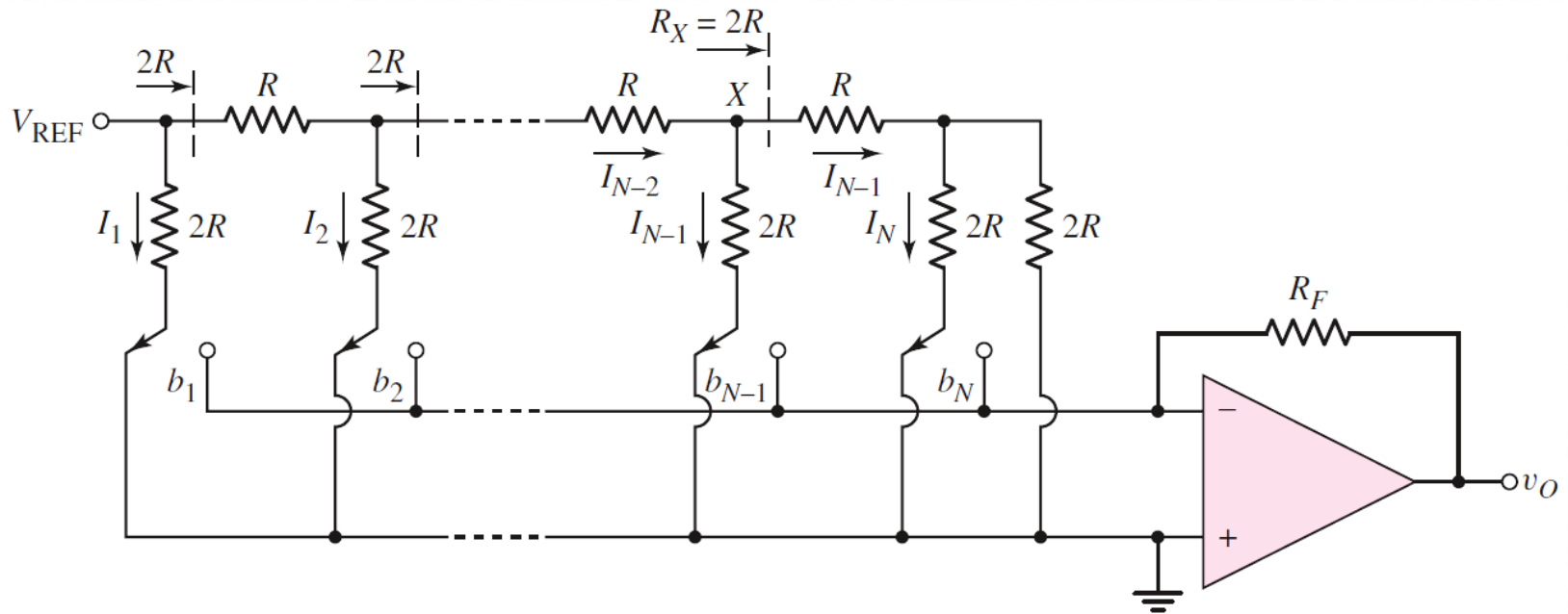
- For the circuit to operate properly, the base-emitter voltage of all the transistors must be the same.
- Since the currents are smaller for the lesser significant bits, the base-emitter areas must be reduced in order to maintain the same current density.





# Digital-to-Analog Converters

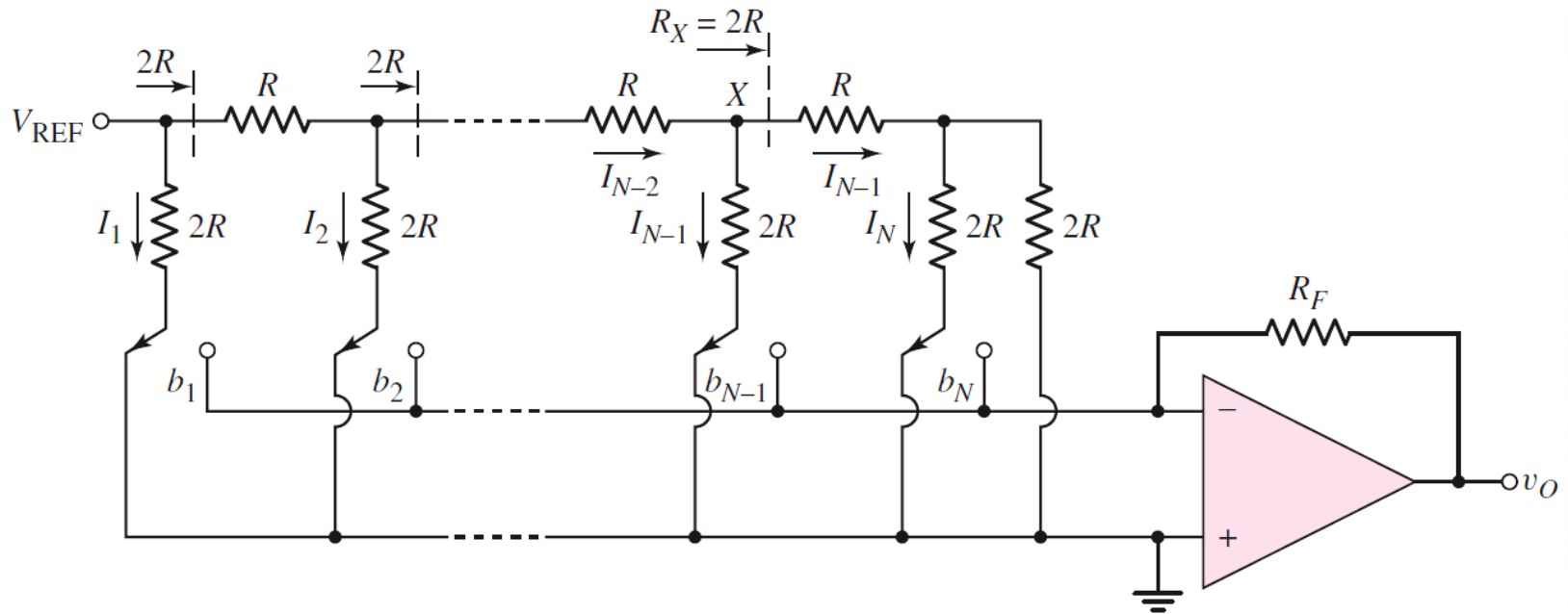
## R-2R Ladder Network D/A



- ✿ This configuration eliminates the widespread in weighted input resistor values in the previous circuit.
- ✿ Assuming the switches are ideal, the current in each resistor is a constant because of the virtual ground concept.

# Digital-to-Analog Converters

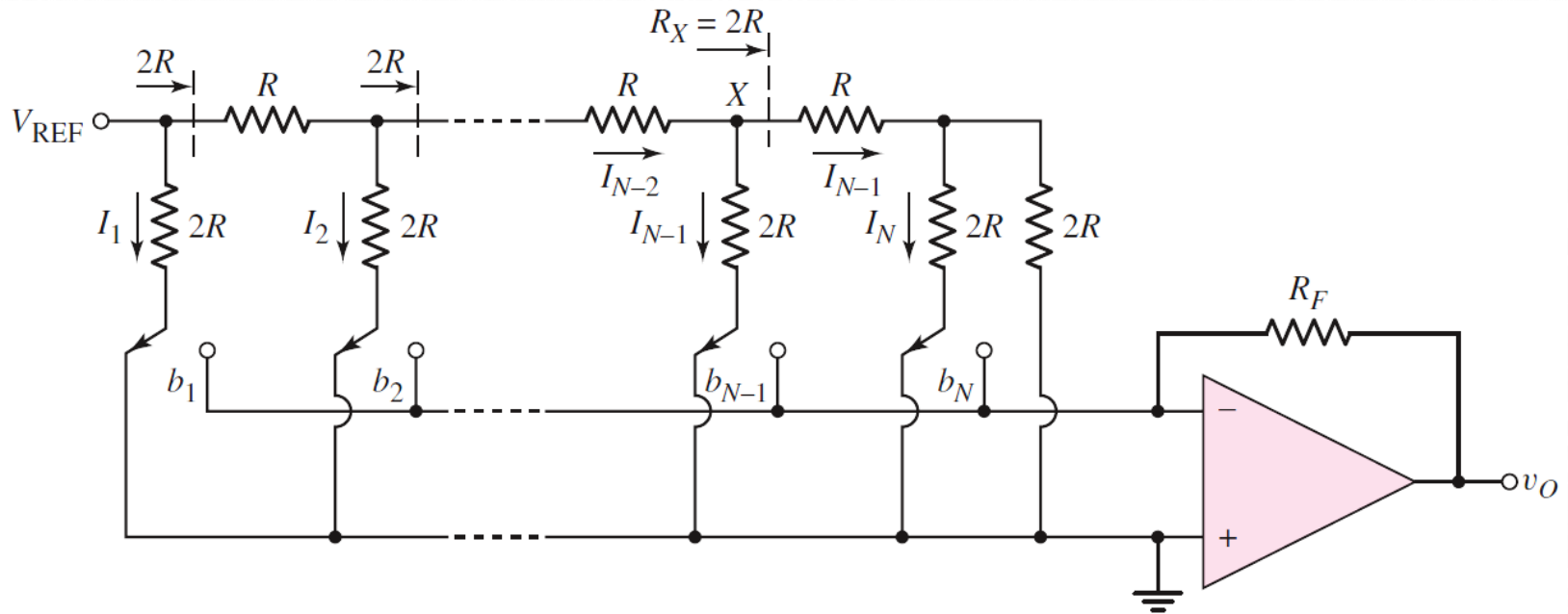
## R-2R Ladder Network D/A



- ✿ Consider node  $X$ , the resistance denoted as  $R_X$  is  $R_X = 2R$ .
- ✿ This same resistance occurs at every node in the circuit as indicated.
- ✿ Therefore, the current entering each node splits evenly as shown at node  $X$ .

# Digital-to-Analog Converters

## R-2R Ladder Network D/A

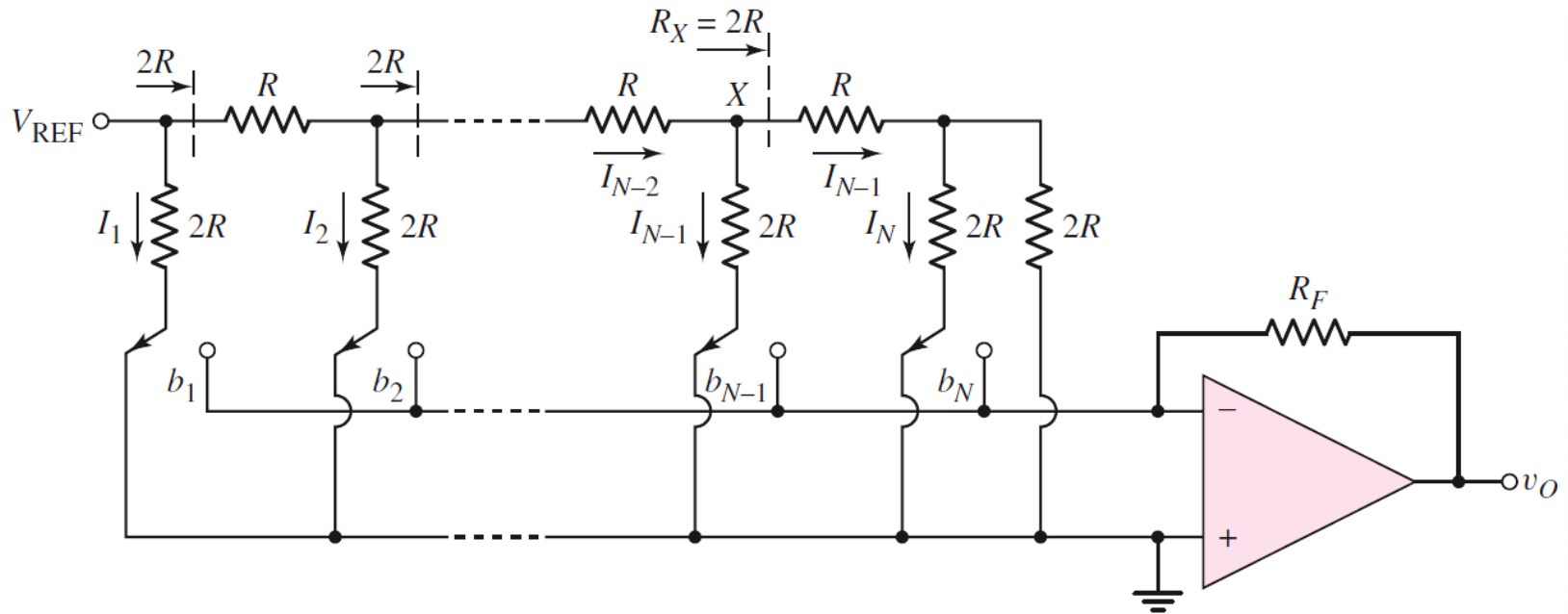


- Then the current entering each node is  $I_{N-1} = \frac{1}{2} I_{N-2}$
- This effect again occurs at every node in the circuit. Then,

$$I_1 = 2I_2 = 4I_3 = \dots = 2^{N-2}I_{N-1} = 2^{N-1}I_N$$

# Digital-to-Analog Converters

## R-2R Ladder Network D/A



✿ Setting the feedback resistance to  $R_F = R$ , we have the output voltage:

$$v_O = (-V_{REF}) \left( \frac{b_1}{2} + \frac{b_2}{4} + \dots + \frac{b_N}{2^N} \right)$$

## Example 01 :: DAC

An analog signal in the range 0 to 5 V is to be converted to a digital signal with a quantization error of less than one percent.

- (a) What is the required number of bits?
- (b) What input voltage value represents 1 LSB?
- (c) What digital output represents an input voltage of 3.5424 V?

## Example 02 :: DAC

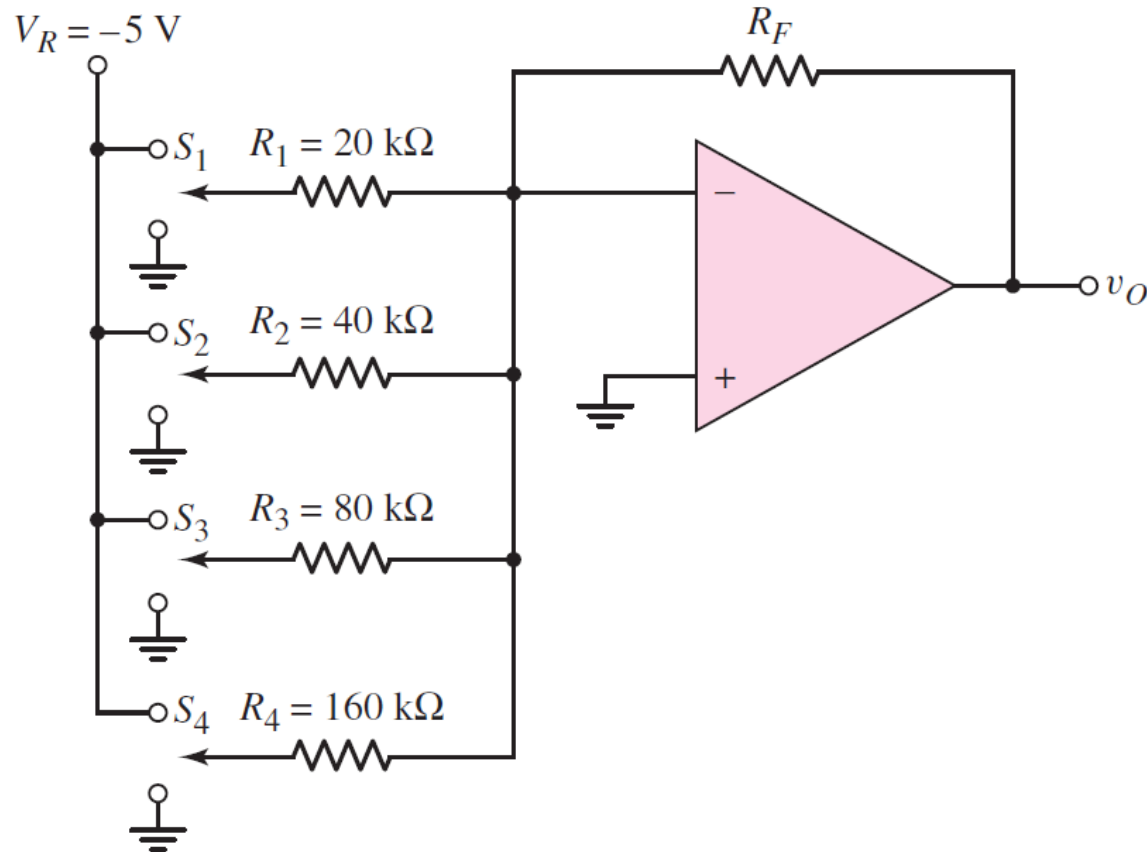
An analog signal in the range 0 to 3.3 V is to be converted to a digital signal with a quantization error of less than 0.5 percent.

- (a) What is the required number of bits?
- (b) What input voltage value represents 1 LSB?
- (c) What digital output represents an input voltage of 2.5321 V?



## Example 03 :: DAC

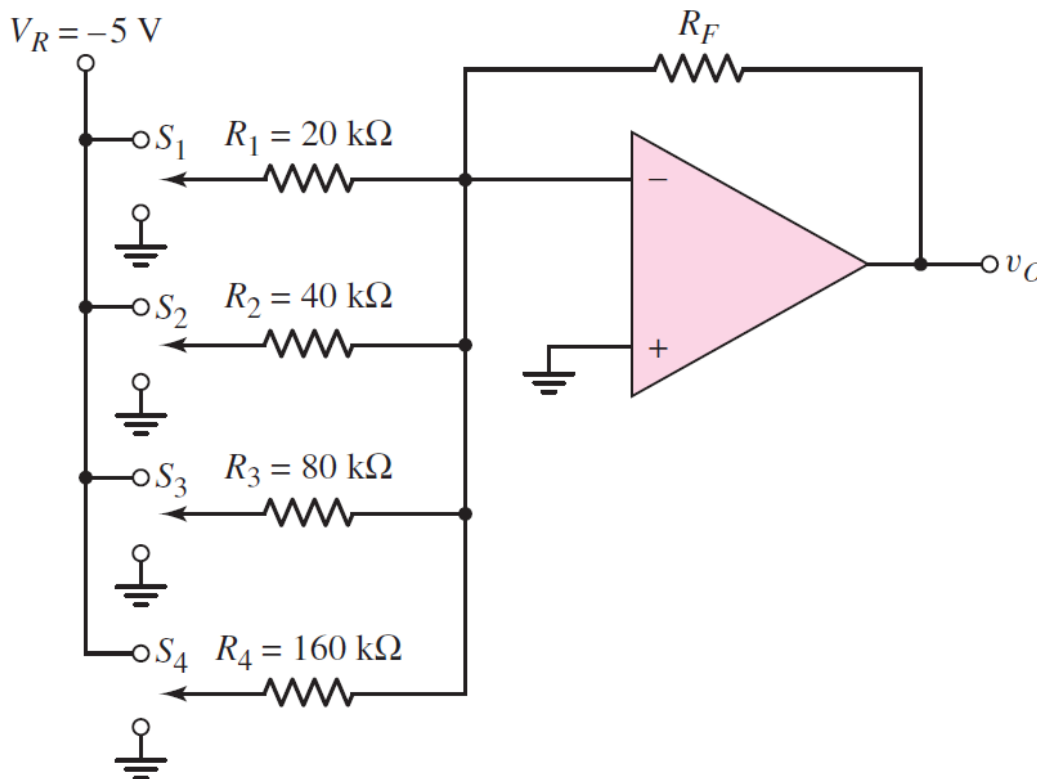
- a) What is the output voltage of the 4-bit weighted-resistor D/A in the Figure below if the input is 0110? Assume  $R_F = 10\text{k}\Omega$ .
- b) The input signal changes to 1001. What is the output voltage?



## Example 04 :: DAC

Consider the 4-bit weighted-resistor D/A converter in Figure below. Let  $R_F = 10\text{ k}\Omega$

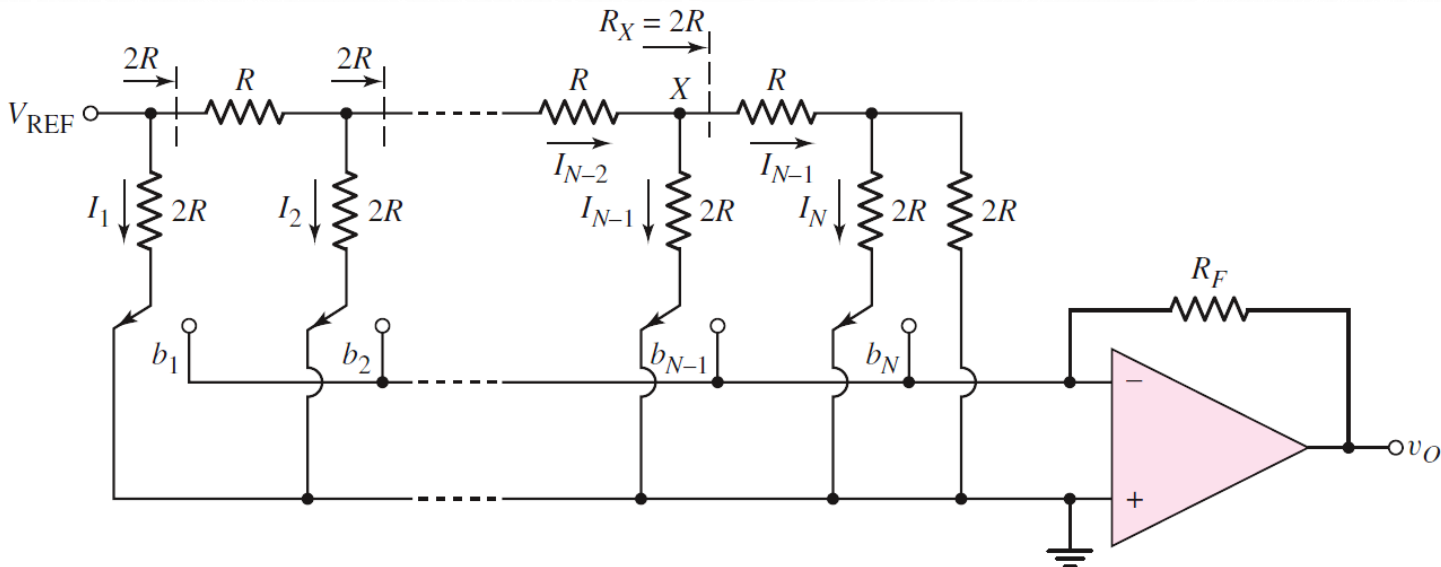
- What is the maximum allowed tolerance ( $\pm$ percent) in the value of  $R_1$  so that the maximum error in the output is limited to  $\pm 1/2$  LSB?
- Repeat part (a) for the resistor  $R_4$ .



## Example 05 :: DAC

The  $N$ -bit D/A converter with an R–2R ladder network in Figure is to be designed as a 6-bit D/A device. Let  $V_{REF} = -5.0V$  and  $R = R_F = 5.0\text{ k}\Omega$ .

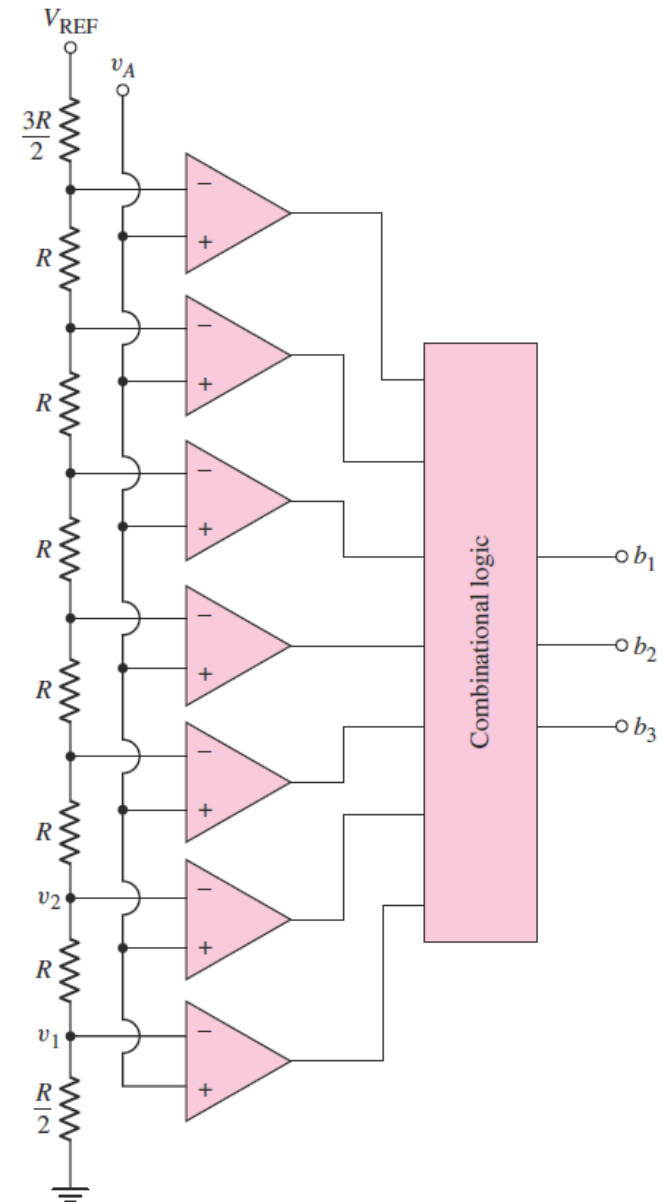
- What are currents  $I_1, I_2, I_3, I_4, I_5$ , and  $I_6$ ?
- The input changes by 1 LSB. What is the change in the output voltage?
- What is the output voltage if the input is 010011?
- What is the change in output voltage if the input changes from 101010 to 010101?



## Example 06 :: ADC

The 3-bit flash A/D converter in Figure has a reference voltage of  $V_{REF} = 3.3\text{ V}$ . The 3-bit output is 101.

What is the range of  $v_A$  that produces this output?



## Example 07 :: ADC

A 10-bit counting A/D converter has an analog input in the range  $0 \leq v_A \leq 5\text{ V}$  and has a clock frequency of  $1\text{ MHz}$ .

- (a) What is the maximum conversion time?
- (b) If the output is 0010010010, what is the range of the input signal  $v_A$  (assume a quantization error of  $\pm 1/2\text{ LSB}$ ).
- (c) How many clock pulses are required to produce an output of 0100100100?

