

# Oblig 1

Oskar Idland

**Problem 1**

a)

b)

c)

d)

**Problem 2**

a)

We begin with the convergence test.

$$\lim_{n \rightarrow \infty} \left| \frac{a_{n+1}}{a_n} \right| < 1$$

$$\lim_{n \rightarrow \infty} \left| \frac{3^n (z + 4 - 2i)^{2n+2}}{3^{n+1} (z + 4 - 2i)^{2n}} \right| = \lim_{n \rightarrow \infty} \left| \frac{(z + 4 - 2i)^2}{3} \right| < 1$$

$$\lim_{n \rightarrow \infty} |z + 4 - 2i| < \sqrt{3}$$

b)

$$\lim_{n \rightarrow \infty} \left| \frac{(z - 3 + i)(n^2 + 2n)}{(n + 1)^2 + 4n^2} \right| = \lim_{n \rightarrow \infty} \left| \frac{(z - 3 + i)(n^2 + 2n)}{n^2 + 2n + 1 + 4n^2} \right|$$

c)

$$\lim_{n \rightarrow \infty} \left| \frac{\ln(n + 1)nz^{n+1}}{\ln(n)z^n(n + 1)} \right| < 1$$

**Problem 3**

a)

b)

c)