

FYS3150 - Project 1

Andrew Quan, Oskar Idland, Hishem Kløvnnes, Håvard Skåli
(Dated: August 24, 2023)

[GitHub Repository](#)

PROBLEM 1

We have the one-dimensional Poisson equation

$$-\frac{d^2 u}{dx^2} = 100e^{-10x}, \quad x \in [0, 1] \quad (1)$$

where the right hand side of the equation is the source term $f(x)$. We have the boundary conditions $u(0) = 0$ and $u(1) = 0$. Integrating both sides of (1) with respect to x twice we get

$$\begin{aligned} \frac{d^2 u}{dx^2} &= -100e^{-10x} \\ \iint \left(\frac{d^2 u}{dx^2} \right) dx^2 &= -100 \iint e^{-10x} dx^2 \\ \int \left(\frac{du}{dx} \right) dx &= -100 \int \left(-\frac{1}{10} e^{-10x} + C \right) dx \\ u(x) &= -100 \left(\frac{1}{100} e^{-10x} + Cx + D \right) \\ u(x) &= Cx + D - e^{-10x} \end{aligned} \quad (2)$$

Where C and D are some arbitrary constants. Invoking the boundary conditions we get

$$\begin{aligned} u(0) &= D - 1 = 0 \Rightarrow D = 1 \\ u(1) &= C + 1 - e^{-10} = 0 \Rightarrow C = e^{-10} - 1 \end{aligned}$$

Thus, plugging these constants into the general solution and rearranging the terms, the final solution becomes

$$u(x) = 1 - x(1 - e^{-10}) - e^{-10x} \quad (3)$$

just like we wanted to show.

PROBLEM 2

Problem a

Write a solution for problem 1a here.

Problem b

Write a solution for problem 1b here.

We write equations using the LaTeX `equation` (or `align`) environments. Here is an equation with numbering

$$\mathbf{F} = \frac{d\mathbf{p}}{dt}, \quad (4)$$

and here is one without numbering:

$$\oint_C \mathbf{F} \cdot d\mathbf{r} = 0.$$

TABLE I. Write a descriptive caption here, explaining the content of your table.

Number of points	Output
10	0.3086
100	0.2550

Sometimes it is useful to refer back to a previous equation, like we’re demonstrating here for equation 4.

Also, note the LaTeX code we used to get correct quotation marks in the previous sentence. (Simply using the " key on your keyboard will give the wrong result.) Figures should preferably be vector graphics (e.g. a .pdf file) rather than raster graphics (e.g. a .png file).

By the way, don’t worry too much about where LaTeX decides to place your figures and tables — LaTeX knows more than we do about proper document layout. As long as you label all your figures and tables and refer to them in the text, it’s all good. Of course, in some cases it can be worth trying to force a specific placement, to avoid the figure/table appearing many pages away from the main text discussing it, but this isn’t something you should spend time on until the very end of the writing process.

Next up is a table, created using the `table` and `tabular` environments. We refer to it by table I.

Finally, we can list algorithms by using the `algorithm` environment, as demonstrated here for algorithm 1.

Algorithm 1 Some algorithm	
Some maths, e.g $f(x) = x^2$.	▷ Here’s a comment
for $i = 0, 1, \dots, n - 1$ do	
Do something here	
while Some condition do	
Do something more here	
Maybe even some more math here, e.g $\int_0^1 f(x)dx$	