

# Analyzing time series of tree growth - Concepts, peculiarities and methods

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# Structure

- **Concepts**

- Tree growth and tree growth parameters
- Tree-rings and growth zones
- Cross-dating
- Principles of dendrochronology/-ecology

- **Peculiarities**

- Growth trends
- Multiple states
- Sensitive/transient response, autocorrelation

- **Methods**

- Detrending
- Chronology building
- Response function

# Tree growth and tree growth parameters

- **Tree growth**
  - primary growth/secondary growth
  - leaf/needle, branch, stem, bark, root growth





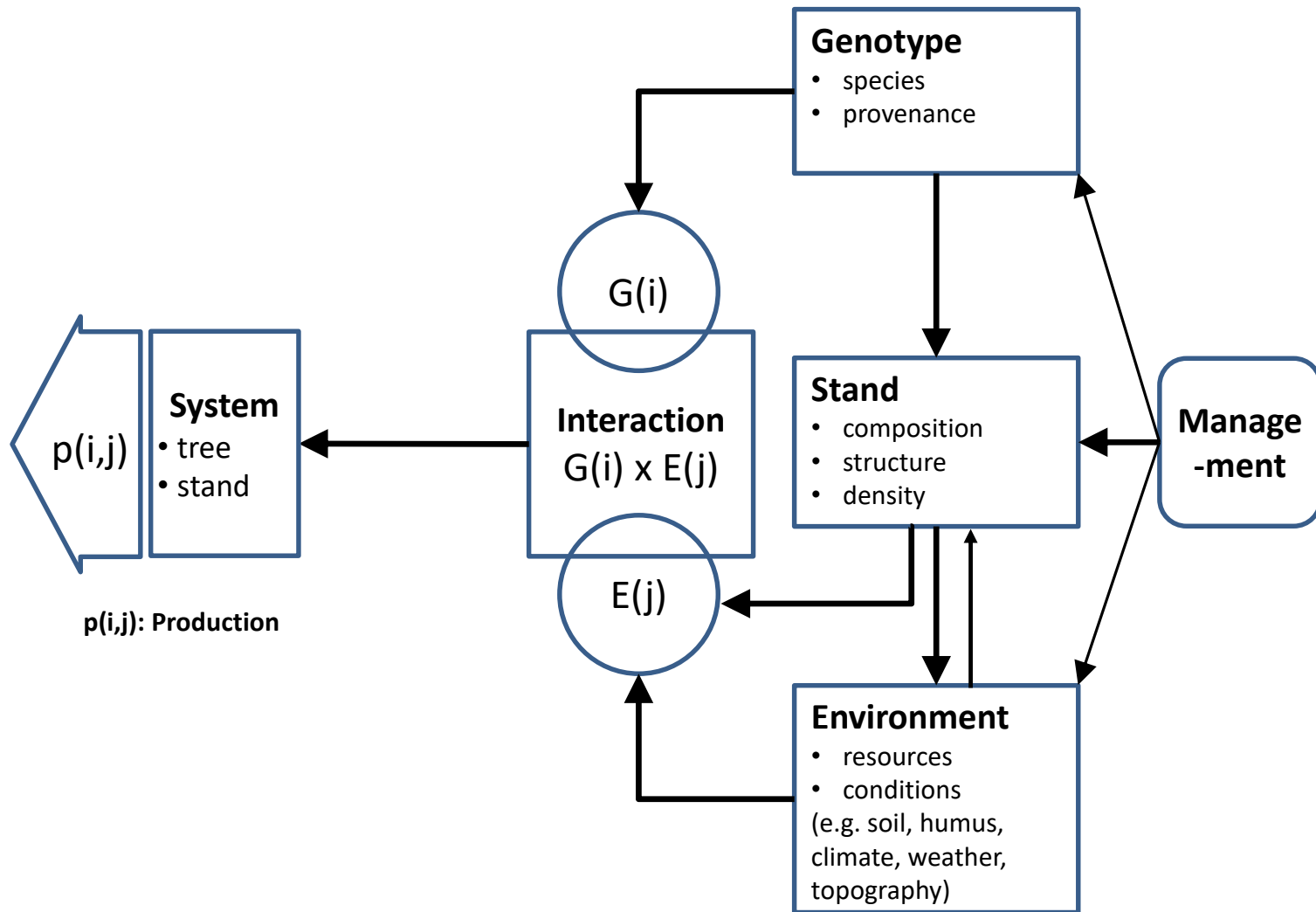
**Age: 68 years**

**Calendar year: 1937**

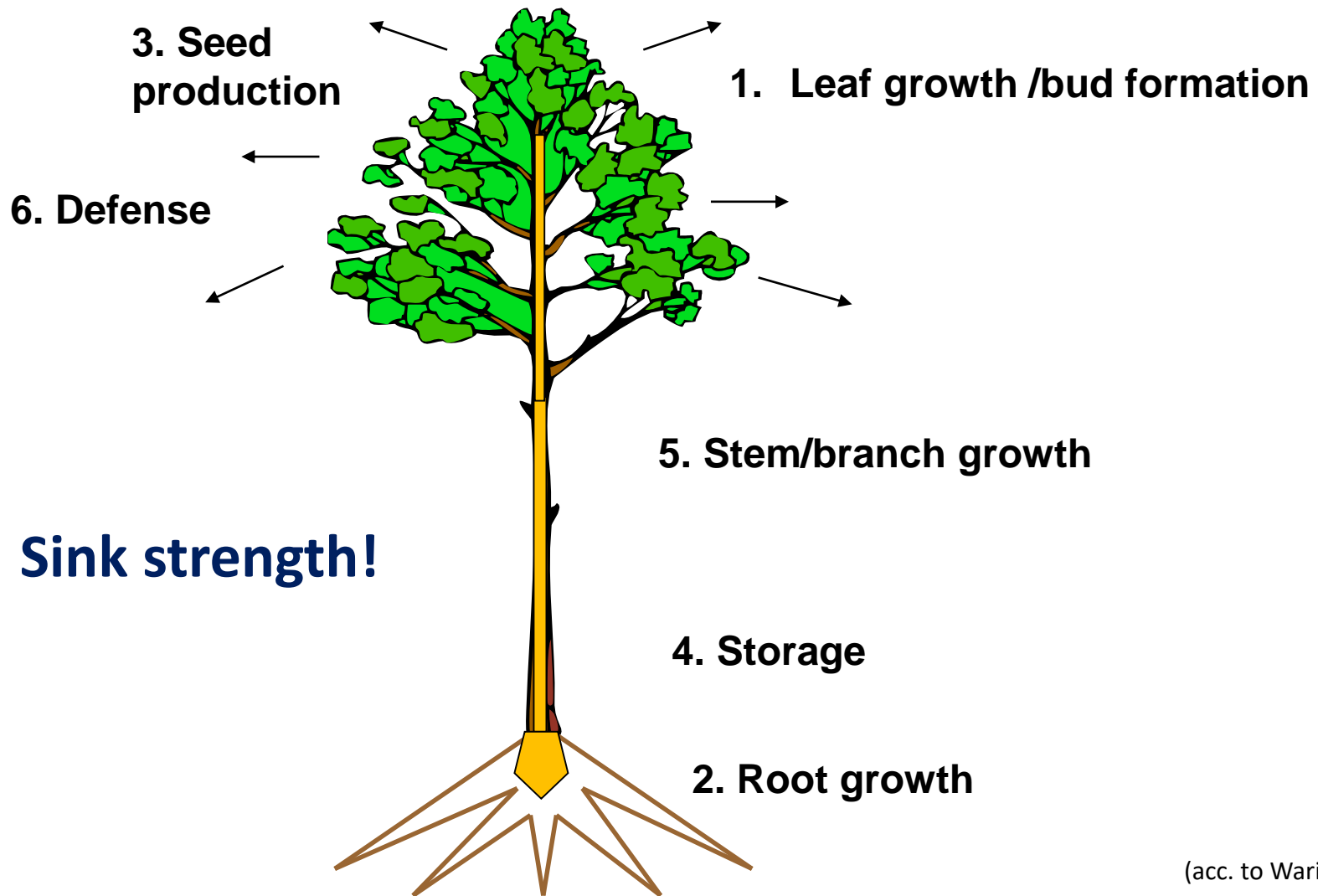
(Douglas fir, Mooswald, date  
of cutting: 27.04.2006)



# System analysis: Production process



# System analysis: Biomass partitioning in trees



(acc. to Waring 1986)

# Tree growth and tree growth parameters

- **Tree growth**

- primary growth/secondary growth
- leaf/needle, branch, stem, bark, root growth

- **Tree growth parameters**

- diameter growth/diameter increment, e.g.,  $d_{age\ 100}$ ,  $ir$ , TRW
- basal area growth/basal area increment, e.g.,  $ig$ ,  $iG$
- height growth/height increment, e.g.,  $h_{age\ 100}$ ,  $ih$
- volume growth/volume increment, e.g.,  $v_{age\ 100}$ ,  $iv$ ,  $iV$
- biomass growth/biomass increment

- **Analysis of tree growth:**

- **Retrospective methods**

- Stem analysis
- Increment cores

- **In situ methods**

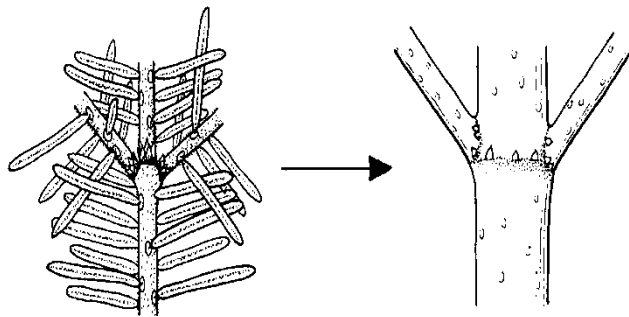
- Repeated measurements, e.g., long-term forest research plots, inventory
- Continuous measurements, e.g., point dendrometer, permanent circumference band

# Stem analysis

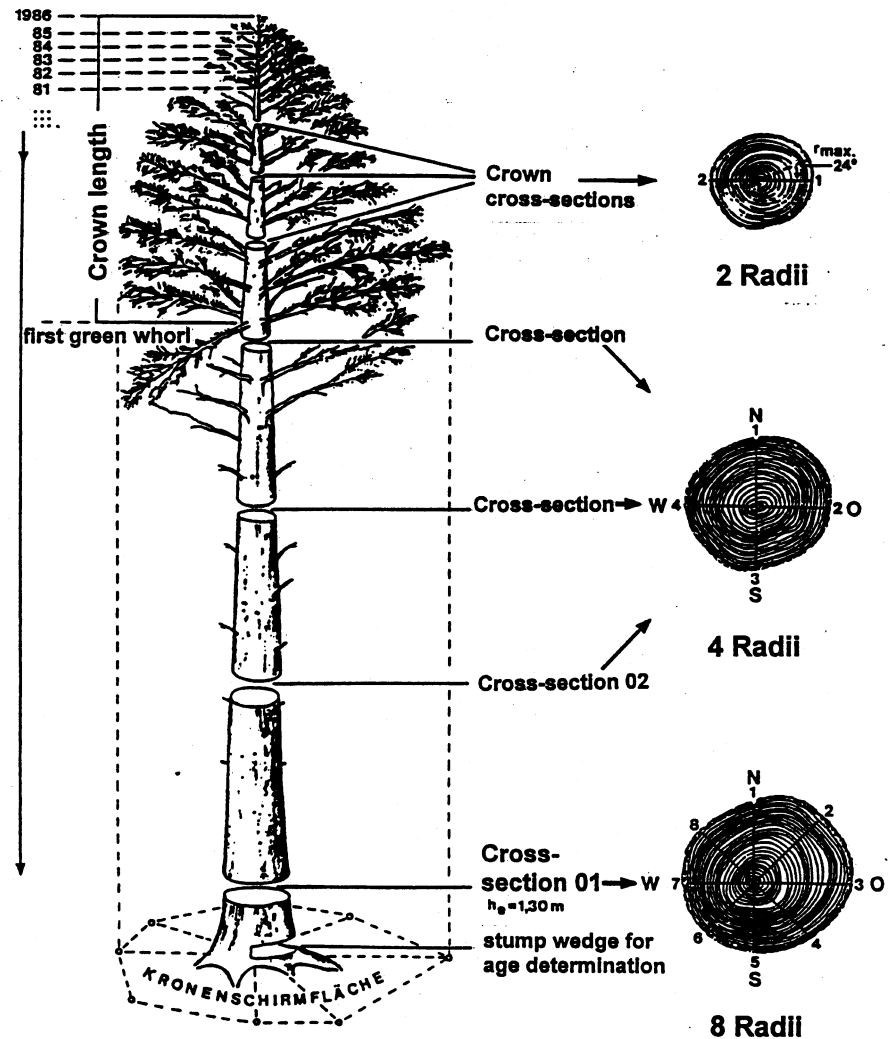
Height analysis

Analysis of stem cross-sections

Traces of bud scales



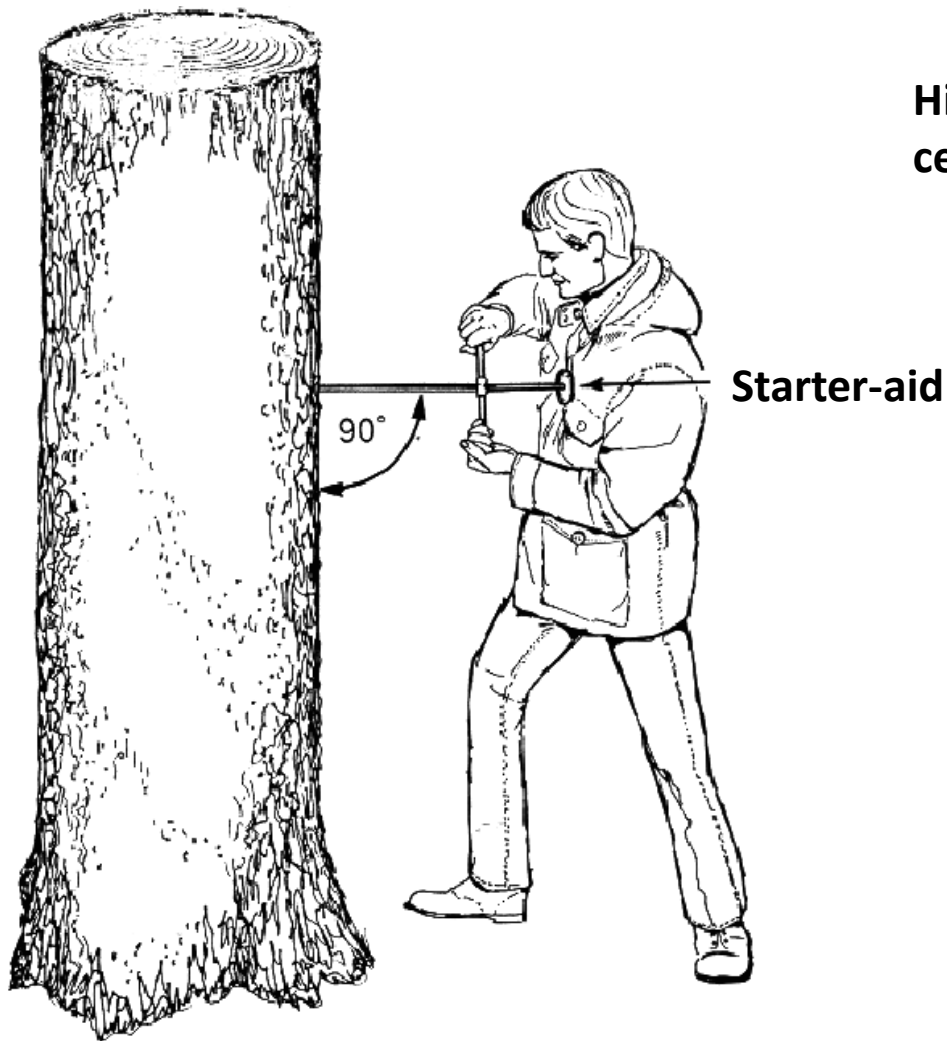
(Roloff 2001)



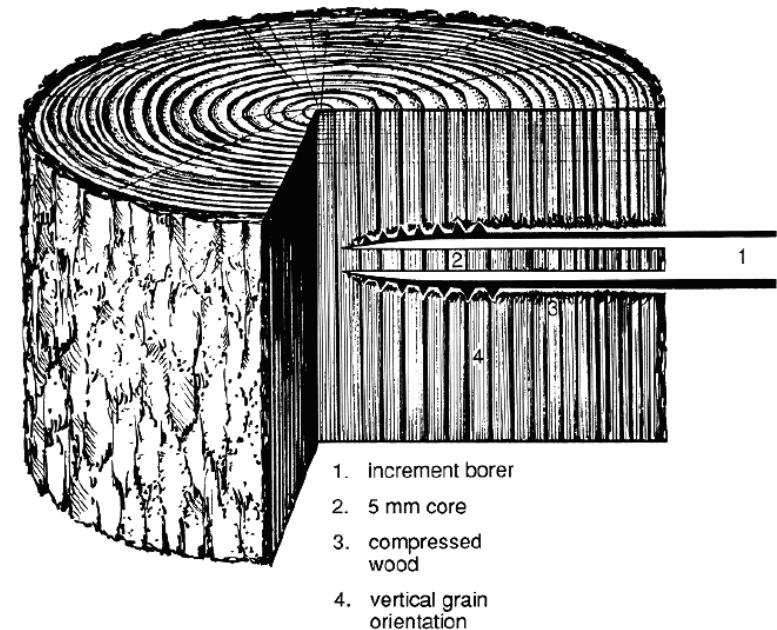
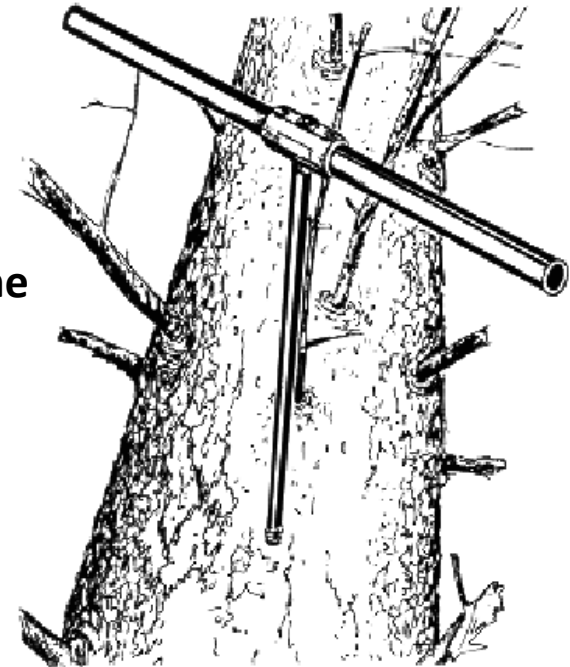
(Gerecke 1988)



# Application of **increment borer**



Hitting the  
centre



# Dendrometer measurements

## Point dendrometer



**Dendrometer-  
mounting**

**Sensor-head**

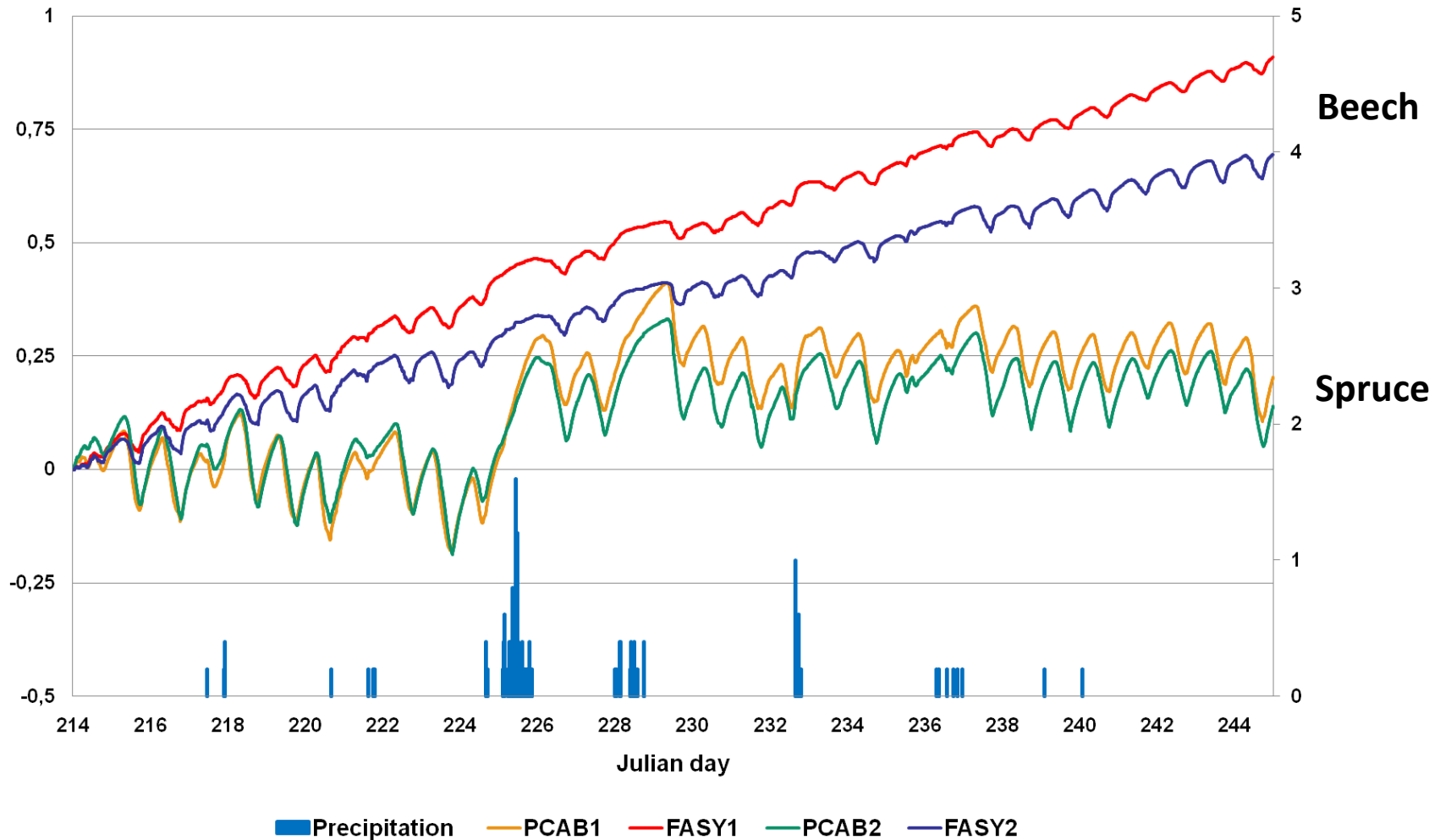
**Cable to datalogger**



**5 cm**

(Hauser 2002)

# Dendrometer measurements



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**Cold winter:**  
→ tree-ring boundary **distinct**

This image shows a cross-section of a tree trunk with two prominent tree rings. The upper ring, representing a cold winter, has a very clear and sharp boundary between its light-colored growth zone and the darker, denser zone of the previous year. The lower ring, representing a mild winter, has a much more blurred and indistinct boundary, making it difficult to see where one year's growth ends and the next begins.

**Mild winter:**  
→ tree-ring boundary **fuzzy**



Annual periodicity!

Tree-rings?

Growth  
zones?

Other growth  
rhythm“

(Cross-section: *Vitex limoniifolia*, Thailand)

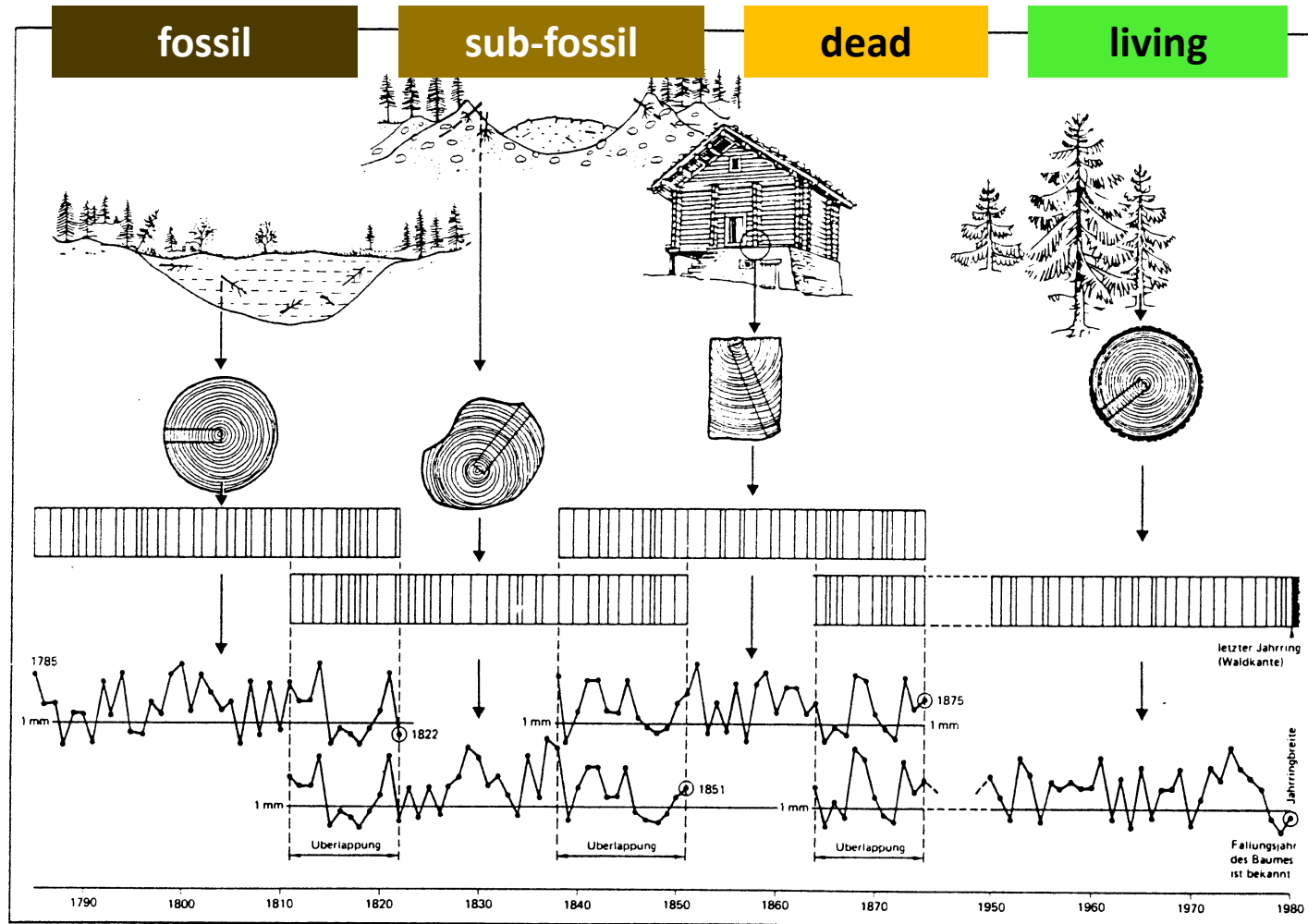


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# Cross-dating and chronology building



(Schweingruber 1989)

# Missing rings?

A tree ring which in a sample is absent due to **failure of cambial activity**.



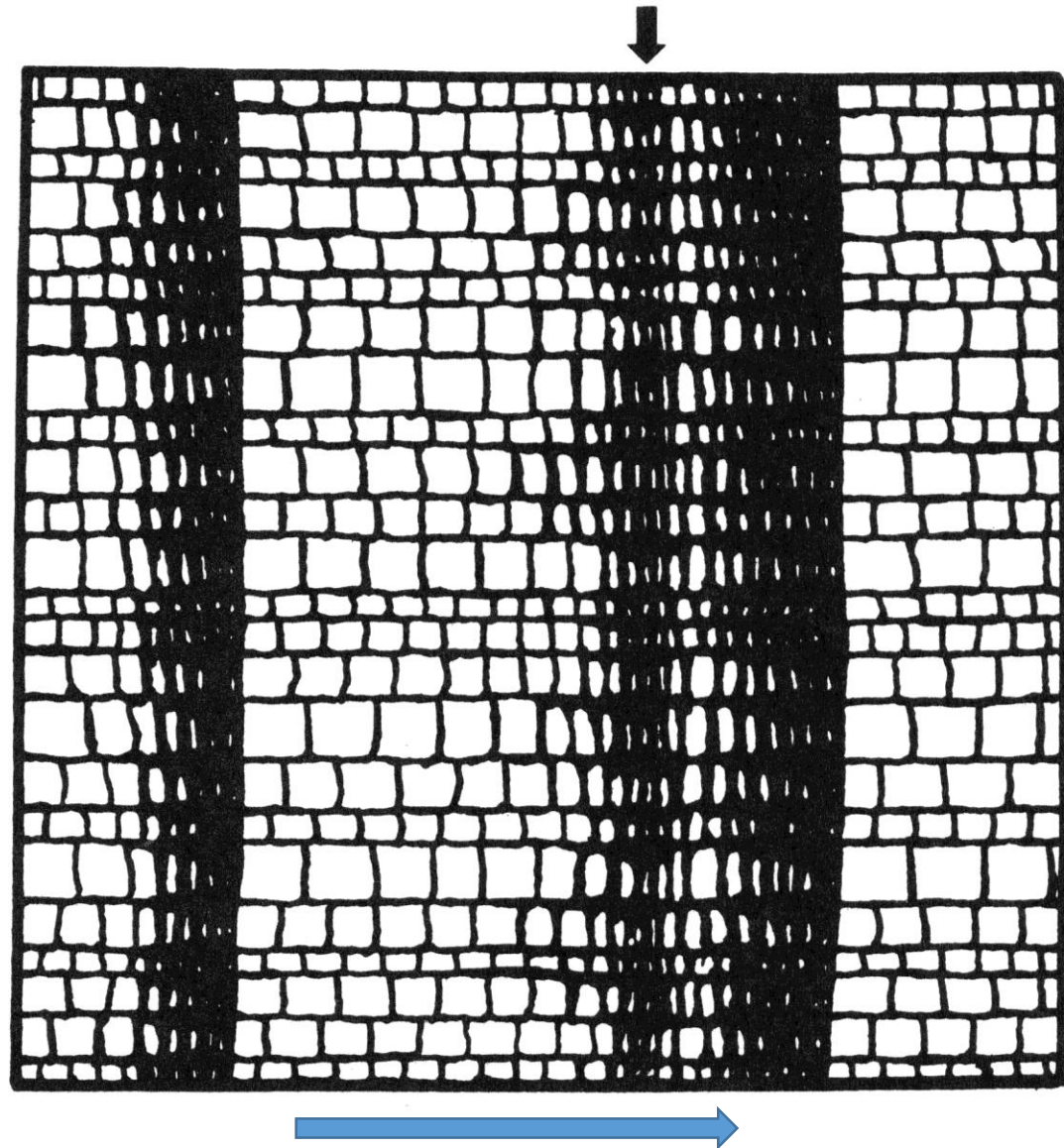
Missing rings can be located by **cross-dating**.

The term "missing ring" is used for tree rings which are **absent on the whole sample**.

When a tree ring is discontinuous (partial, incomplete), it is a **wedging ring**.

# False rings?

Cells leading into the false ring will **gradually decrease** in size and then **gradually increase back** to earlywood cells.



(Speer *et al.* 2004)

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- Principles of dendrochronology/-ecology

# Principles of dendrochronology/-ecology

1. The principle of aggregate tree growth
2. The uniformitarian principle
3. The principle of ecological amplitude, and
4. The principle of site selection

<http://web.utk.edu/~grissino/>



# Principles of dendrochronology/-ecology

## The principle of aggregate tree growth

“Any individual tree growth series can be decomposed into an aggregate of environmental factors that affected the patterns of tree growth over time”.

(e.g. [web.utk.edu/~grissino/](http://web.utk.edu/~grissino/))

$$R_t = A_t + C_t + \delta D1_t + \delta D2_t + E_t \quad (1) \quad \text{(acc. to Cook 1990)}$$

$R_t$  = growth response variable, e.g. radial increment, in year  $t$

$A_t$  = **age trend component** in year  $t$

$C_t$  = **climate factor** in year  $t$

$D1_t$  = **tree individual disturbance** in year  $t$

$D2_t$  = **stand wide disturbance** in year  $t$

$\delta$  = binary indicator ( $\delta = 1$ : presence,  $\delta = 0$ : absence)

$E_t$  = error term (white noise process) in year  $t$

# Principles of dendrochronology/-ecology

## The principle of aggregate tree growth

“Any individual tree growth series can be decomposed into an aggregate of environmental factors that affected the patterns of tree growth over time”.

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$$R_t = A_t + C_t + \delta D1_t + \delta D2_t + E_t \quad (1) \quad \text{(acc. to Cook 1990)}$$

**Dendroclimatology:** „maximize the climate signal by minimizing the other factors through chronology building, *i.e.* (1) detrending/standardization, and (2) aggregation”.

**Trend component:**

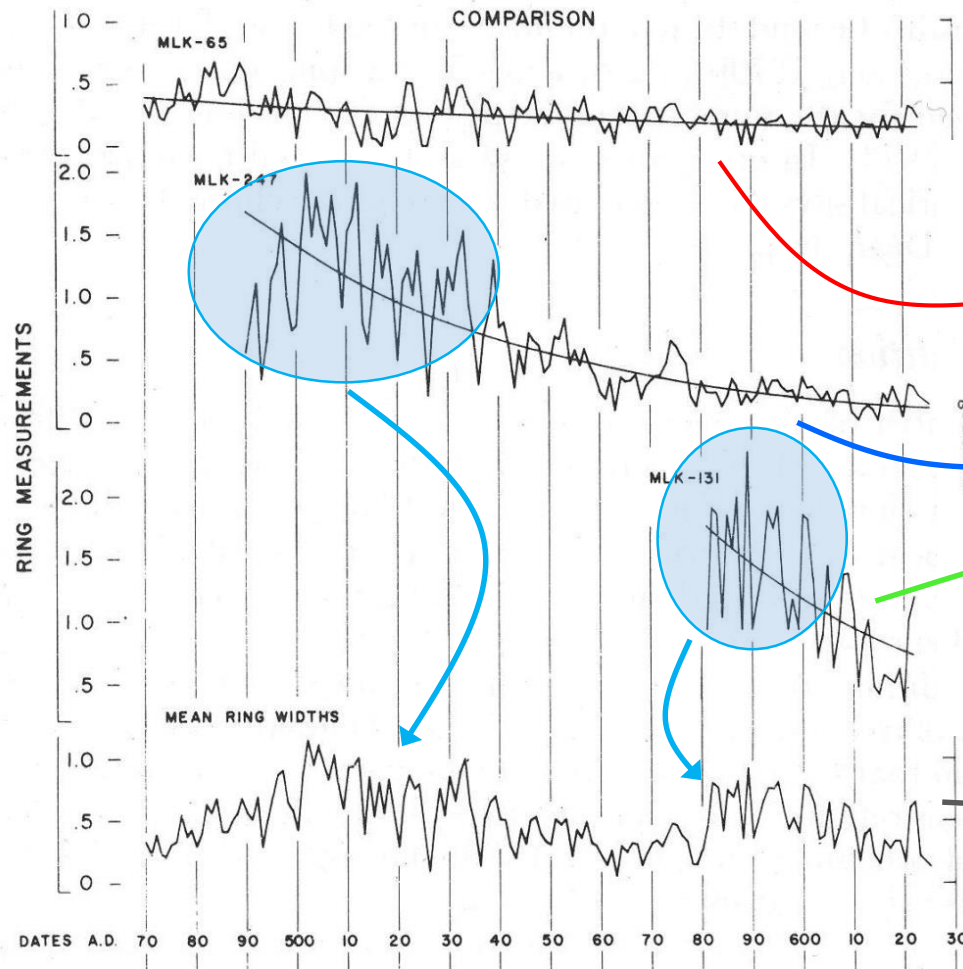
$$G_t = f(A_t, \delta D1_t, \delta D2_t) \quad (2)$$

$\delta$  = binary indicator ( $\delta = 1$ : presence,  $\delta = 0$ : absence)

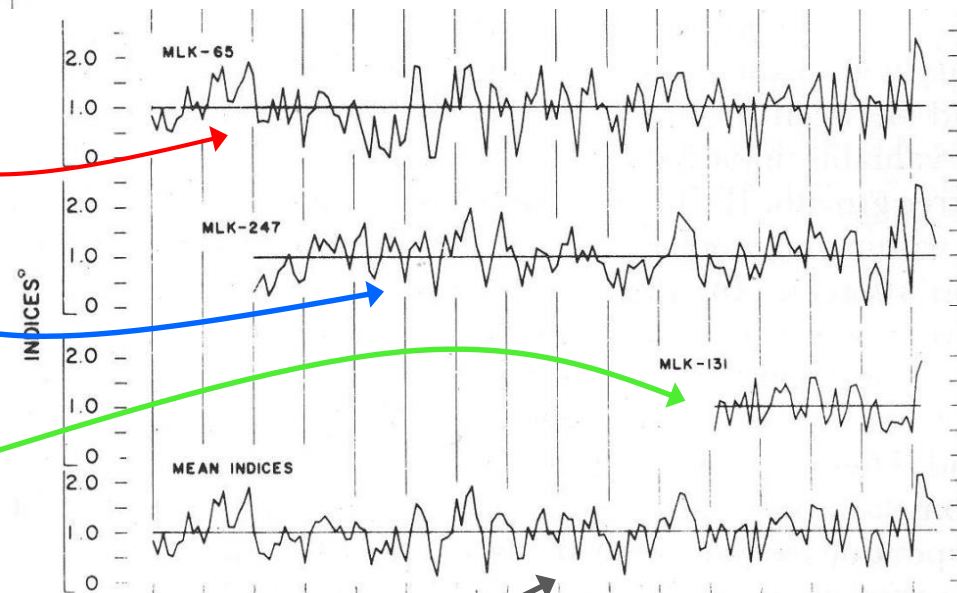
$E_t$  = error term (white noise process) in year  $t$

# Standardization - Detrending

Raw (measurement-) values



Detrended (standardized) Index values



(Fritts 1976)

# Standardization - Detrending

## Models for nonstationary series (series with a trending mean):

### Trend stationarity:

The mean trend is deterministic, i.e., once the trend is estimated and removed from the data, the residual series is a stationary stochastic process

### Difference stationarity:

The mean trend is stochastic, i.e. once the series is differenced  $D$  times, the series yields a stationary stochastic process



**Concept rarely applied in dendroecology!**

# The principle of aggregate tree growth - Critics

$$R_t = A_t + C_t + \delta D1_t + \delta D2_t + E_t \quad (1) \quad (\text{acc. to Cook 1990})$$

## “Age trend” component ( $A_t$ ) in year $t$ :

The endogenous trend component comprises effects of **chronological AND of physiological age** (i.e. dimension related trend). **Alternative:** e.g., multi-step detrending

## “Climate factor” ( $C_t$ ) in year $t$ :

The climate factor is an amalgamation of effects of **weather** (operating at high frequencies) **AND climate** (operating at low frequencies). Effects can be **delayed and long-lasting** (lag and carry-over effects). **Alternative:** e.g., distributed-lag model

## Disturbances:

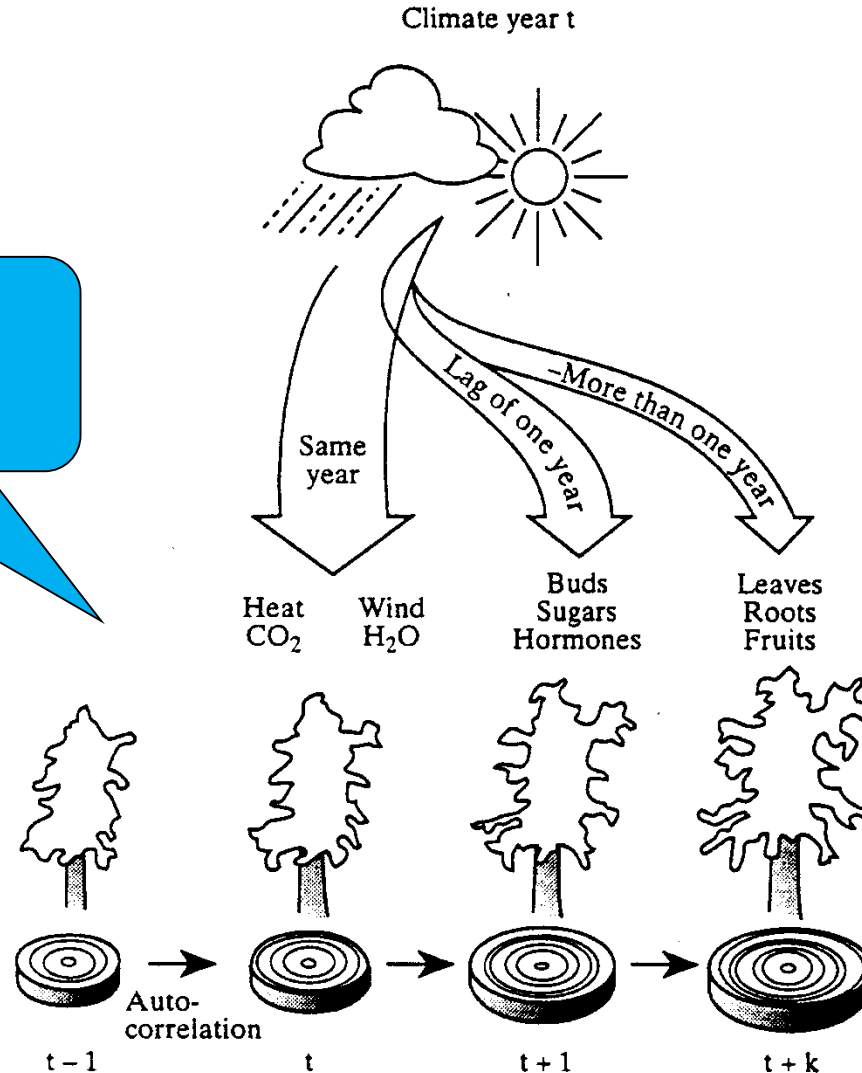
Disturbances can have **long-lasting effects**. Weather factors, e.g. late frost, can also cause disturbance. **Alternative:** e.g., threshold autoregression model

## Additive aggregation:

The assumption of **additive linkage without interaction** of components is biologically not meaningful. **Alternative:** multiplicative aggregation

# Time lagged effects: memory/autocorrelation

- endogenous factors  
AND
- exogenous factors



(Fritts 1976)



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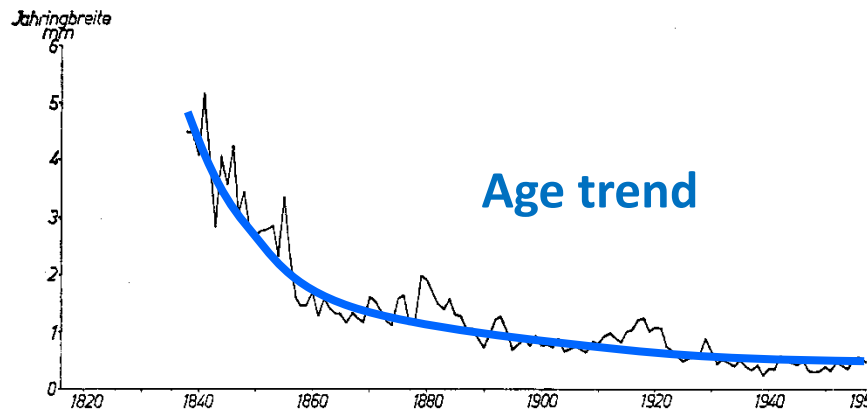


(Douglas fir, Mooswald, date  
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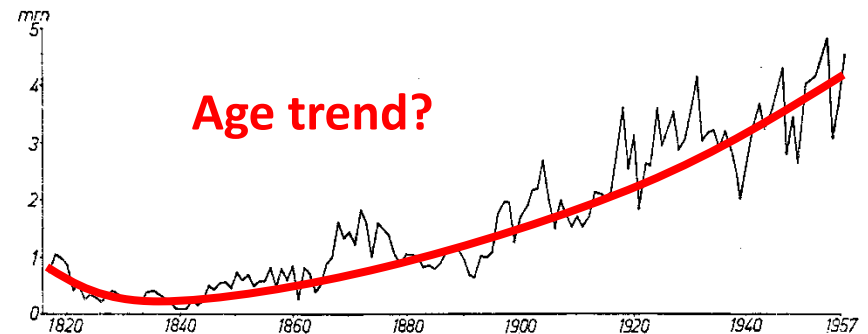
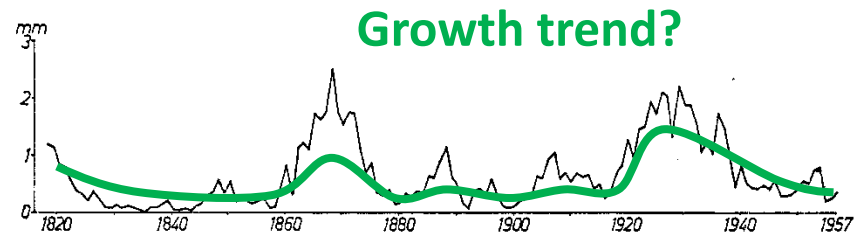


# Radial increment of forest trees in the Black Forest

## Age class forest (Fir)

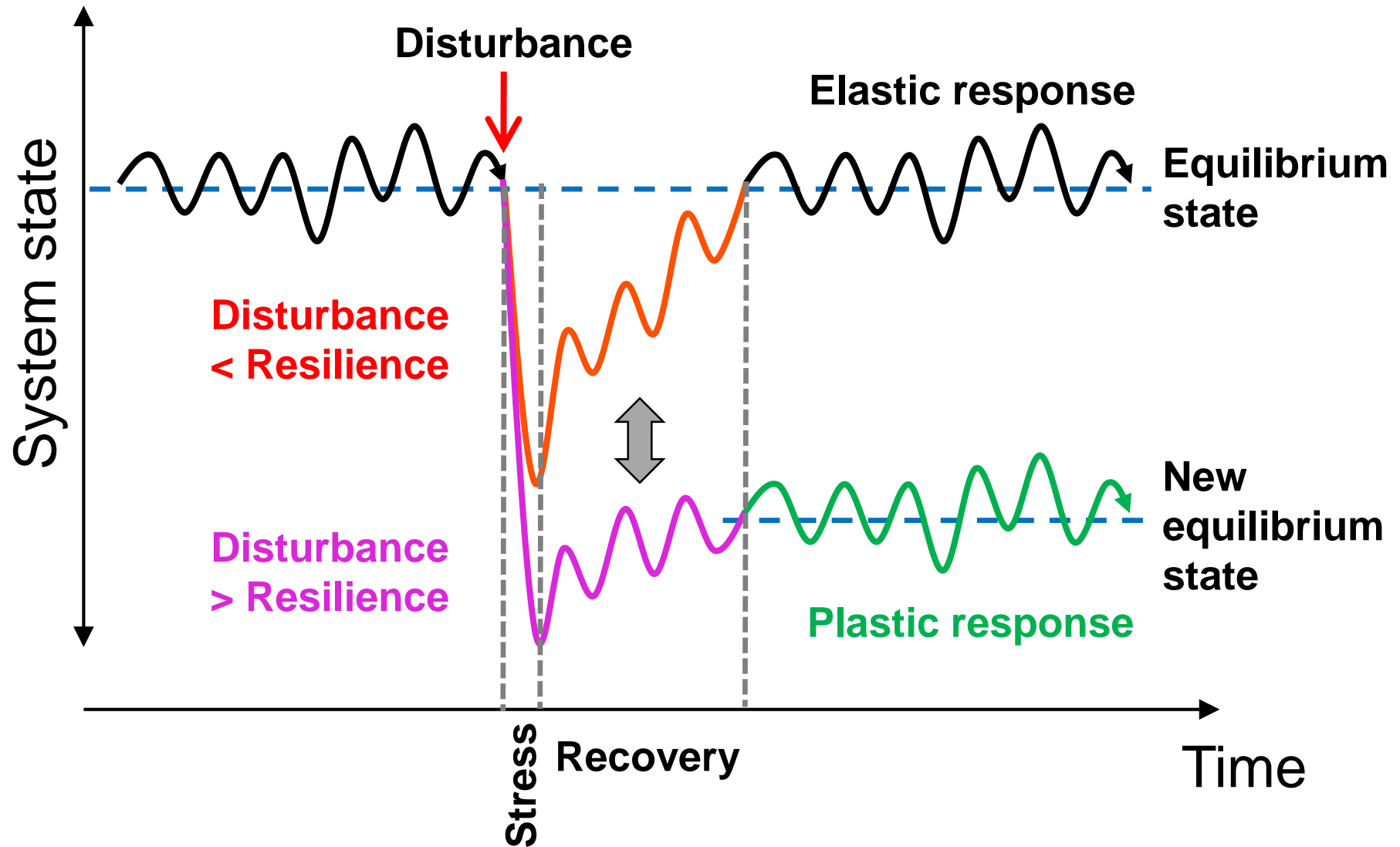


## Plenterwald (Fir)



(acc. to Mitscherlich, 1978)

# Disturbances and resilience of forest ecosystems



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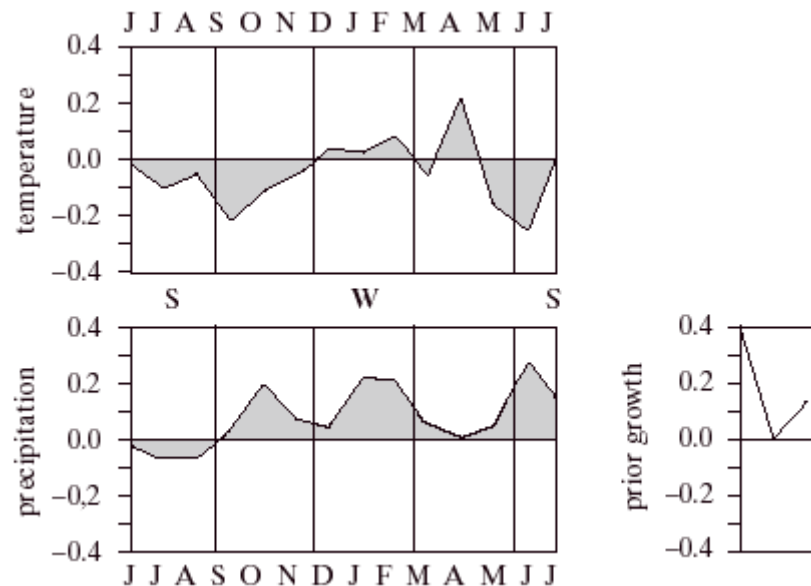
- **Methods**

- Detrending
- Chronology building
- Response function

(adapted after Puettmann et al. 2015)

# Response function analysis

- **multiple regression technique** using the **principal components (PCs)** of **monthly climatic data** to estimate **indexed values of ring-width** growth.
- the regression coefficients are then multiplied by the PCs of climate to obtain a new set of regression coefficients related to the original monthly climatic data variables.



Results from response function analyses (A) for temperature and precipitation (previous June to current July) and autocorrelation analyses (B) for a 3-year period (semi-arid sites in the American Southwest). (Fritts 1976)

([http://www.wsl.ch/dendro/products/dendro\\_glossary](http://www.wsl.ch/dendro/products/dendro_glossary))



# Weblinks

## **Ultimate Tree-Ring Web Pages**

<http://web.utk.edu/~grissino/>

## **Multilingual Glossary of Dendrochronology**

[http://www.wsl.ch/dendro/products/dendro\\_glossary](http://www.wsl.ch/dendro/products/dendro_glossary)

## **Dendrochronology Program Library**

<http://www.ltrr.arizona.edu/pub/dpl/>

## **Dendrochronology Program Library in R**

<https://cran.r-project.org/web/packages/dplR/index.html>

## **Climate explorer**

<https://climexp.knmi.nl/start.cgi>

## **International Tree-Ring Data Bank**

<http://www.ncdc.noaa.gov/paleo/treering.html>

## **Gesellschaft für Jahrringforschung / Association for Tree-Ring Research**

<http://www.tree-ring.org/>