

Assignment 1 Practical Systems Biology

Student Exam Number: B161216

```
In [1]: import numpy as np
import matplotlib.pyplot as plt
%matplotlib inline
```

Probability

```
In [2]: dna1 = str(np.load('dna1.npy'))
dna2 = str(np.load('dna2.npy'))
```

Question 1.1

```
In [3]: #define a function that reports the probability of finding a base (b) in a sequence (seq)
        def base_prob(seq, b, seq name):
            i = 0
            for n in seq:
                if n == b:
                    i += 1
            prob = i/len(seq)
            print ("The probability of finding {} in {} is {}".format(b, seq name, prob))
In [4]: | #call probability reporter for each base and each sequence
        bases = "ACTG"
        for base in bases:
           base prob(dna1, base, "dna1")
        print()
        for base in bases:
           base_prob(dna2, base, "dna2")
        The probability of finding A in dnal is 0.308125
        The probability of finding C in dna1 is 0.223625
        The probability of finding T in dna1 is 0.29925
        The probability of finding G in dna1 is 0.169
        The probability of finding A in dna2 is 0.30875
        The probability of finding C in dna2 is 0.217
        The probability of finding T in dna2 is 0.3105
        The probability of finding G in dna2 is 0.16375
```

Question 1.2

```
In [6]: #define fragment to search for
    fragment = "TTTT"

    #search for fragment's sequence in each
    base_prob2(dna1, fragment, "dna1")
    base_prob2(dna2, fragment, "dna2")

The probability of finding 'TTTT' in dna1 is 0.009875
    The probability of finding 'TTTT' in dna2 is 0.02775
```

Considering that the probability of finding a given sequence of base pairs in another random sequence (each base is independent from the rest of the sequence) is $(1/4)^n$, where n is the given sequence's length, the probability of finding a 4-base long sequence (in this case TTTT) would be $(1/4)^4$, or 0.00390625. This probability is closer to the one found in dna1, so this must be the synthetic sequence and dna2 must be the natural one.

Entropy

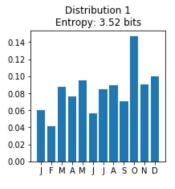
Question 2.1

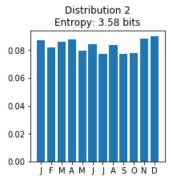
Question 2.2

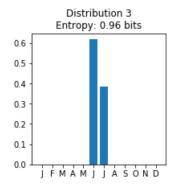
```
In [8]: dl= np.load('annualprobs.npy')

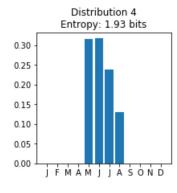
#set the x-axis labels for figures
months = ["J", "F", "M", "A", "M", "J", "A", "S", "O", "N", "D"]
x_axis = np.linspace(0, len(months)-1, len(months))

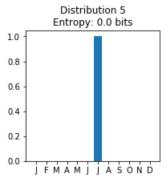
#for each distribution (dist) 1 to 6, calculate its entropy and plot it
for dist in range(len(dl)):
    #rounding entropy values to 2 decimal places
    ent = round(entropy(dl[dist]), 2)
    plt.figure(figsize = (3,3))
    plt.title("Distribution {}\nentropy: {} bits".format(dist+1, ent))
    plt.bar(x_axis, dl[dist])
    plt.xticks(x_axis, months)
    plt.show()
```

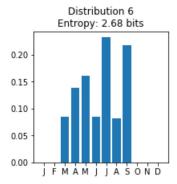












The entropy seems to be higher if the probabilities are similar for each state of the distribution, as best represented in Distribution 2 (with the highest entropy).

If there is a strong bias to one or some of the states (probability is concentrated in a few states), as in Distributions 5 or 3, respectively, the entropy is lower. This makes sense with the definition of entropy as "a measure of how disorganized something is".

Measuring the dependance between two random variables

```
In [9]: d2 = np.load('XandY.npy')
```

Question 3.1

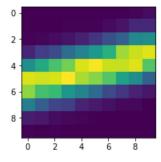
```
In [10]: def correlation(x, y):
             #get means for each list
             mx = np.mean(x)
             my = np.mean(y)
              #variables to store each sum in the correlation
             sum x2 = 0
             sum y2 = 0
             sum_xy = 0
              #get values for every sum
             for n in x:
                 sum x2 += (n - mx) **2
             for n in y:
                 sum y2 += (n - my) **2
             for c in range(len(x)): \#x and y need to have the same amount of elements
                 sum_xy += (x[c] - mx) * (y[c] - my)
              #return the final calculation of the correlation
             return sum xy/(sum x2*sum y2) ** (1/2)
```

Question 3.2

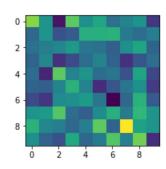
Plotting for every dataset instead of just one

```
In [11]: for set in range(0, len(d2), 2):
    hist, xedges, yedges = np.histogram2d(d2[set], d2[set+1], bins = 10)
    hist = np.rot90(hist)
    print("Dataset", int(1+set/2))
    plt.figure(figsize = (3,3))
    plt.imshow(hist, aspect = 'auto')
    plt.show()
```

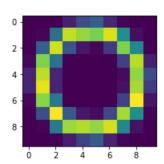
Dataset 1



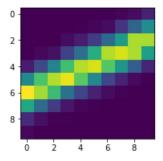
Dataset 2



Dataset 3



Dataset 4



Question 3.3

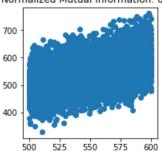
The number of events is the length of each dataset.

The probability that an event falls into a bin should then be equal to the number of events in that bin divided by the total number of events

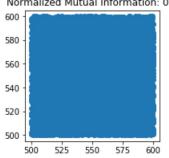
```
In [12]: \#this function returns the mutual information between x and y, normalized by the entropy of
         def normalized_mutual_information(x, y):
             hist, xedges, yedges = np.histogram2d(x, y, bins = 10)
             hist norm = hist/np.sum(hist) #normalize the histogram to get the bins probability distr
             \#calculate conditional entropy of y given x
             cond ent = 0
             for x_val in hist_norm:
                 x_prob = np.sum(x_val)
                 for y_val in x_val:
                     if y val != 0:
                         cond ent += y val*np.log2(x prob/y val)
             \# calculate y entropy and normalized mutual information
             y_probs = np.sum(hist_norm, axis = 0)
             y_ent = entropy(y_probs)
             nmi = (y_ent-cond_ent)/y_ent
             return nmi
In [13]: #approximating final results to 2 decimal points
         cor = round(correlation(d2[0], d2[1]), 2)
         nmi = round(normalized mutual information(d2[0], d2[1]), 2)
         print("Dataset 1")
         print("Correlation:", cor)
         print("Normalized Mutual Information:", nmi)
         Dataset 1
         Correlation: 0.52
         Normalized Mutual Information: 0.09
```

Question 3.4

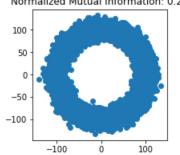
Dataset 1 Correlation Coefficient: 0.52 Normalized Mutual Information: 0.09



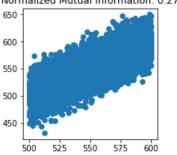
Dataset 2 Correlation Coefficient: -0.01 Normalized Mutual Information: 0.0



Dataset 3 Correlation Coefficient: -0.0 Normalized Mutual Information: 0.25



Dataset 4 Correlation Coefficient: 0.82 Normalized Mutual Information: 0.27



While correlation and mutual information have some measure of dependance between x and y, they behave differently.

Correlation appears to be high only if x and y change together in a linearly, as seen in datasets 1 and 4. As there is no linear correlation between x and y in datasets 2 and 3, the correlation coefficient nears 0. Correlation is ultimately a measure of how much x changes along with y, asking the question "if x is high (compared to its mean), will y be high/low too?". It can be seen how this applies for dataset 4 and not for dataset 3.

The normalized mutual information, in the other hand, still has distinguishable values for datasets 1 and 4, but now also for dataset 3. Visually, dataset 3 seems relatively "organized". We can know a lot about y if we know x, even if they do not correlate linearly, and that is why the normalized mutual information nears the one seen in dataset 4. As the probabilities are still concentrated in a few positions of the probability-space, the entropy is reduced if we know the values for x. For example, if we know that x is a middle-value in dataset 3, we would certainly know that y would have an extreme value.