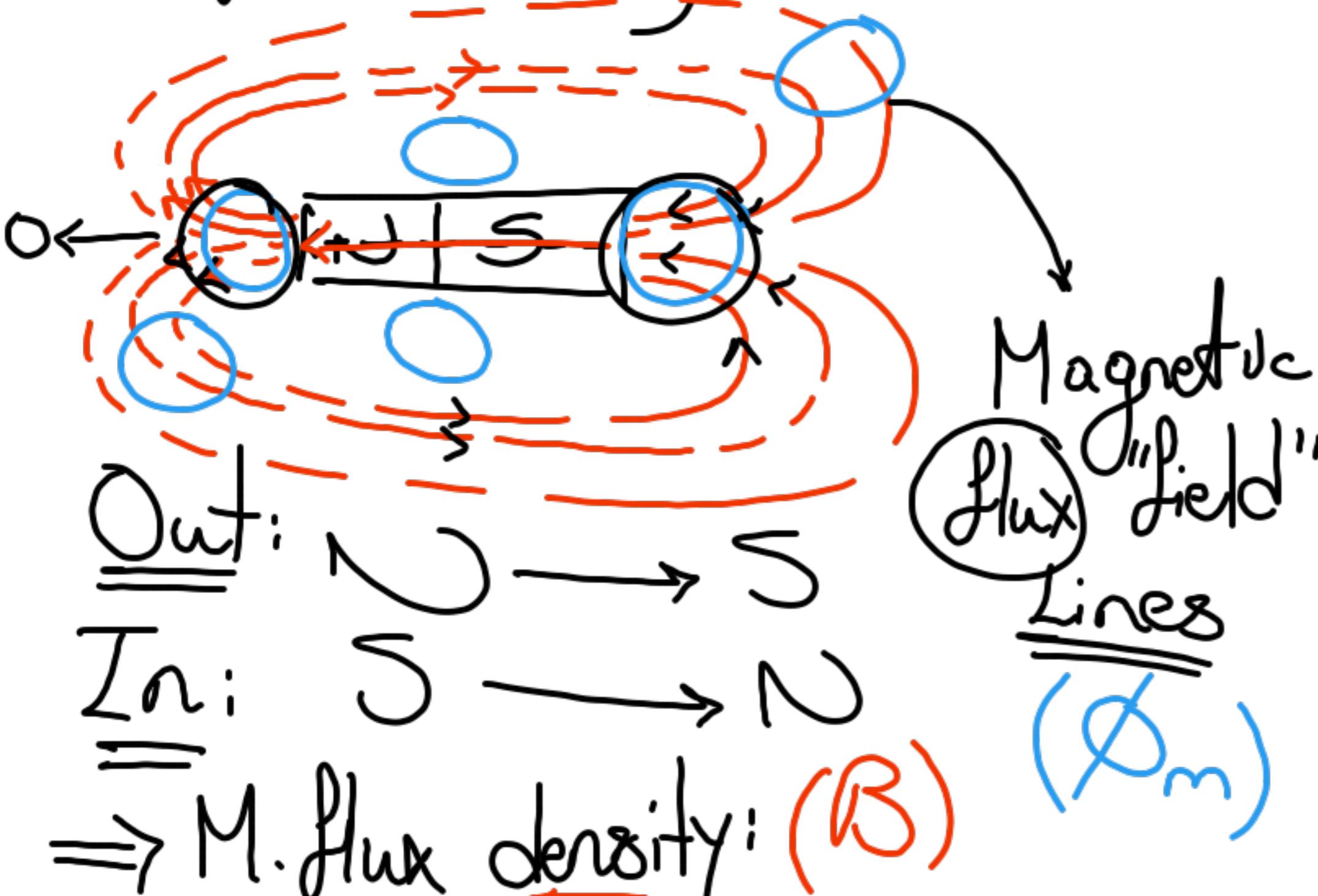


# Bar Magnet



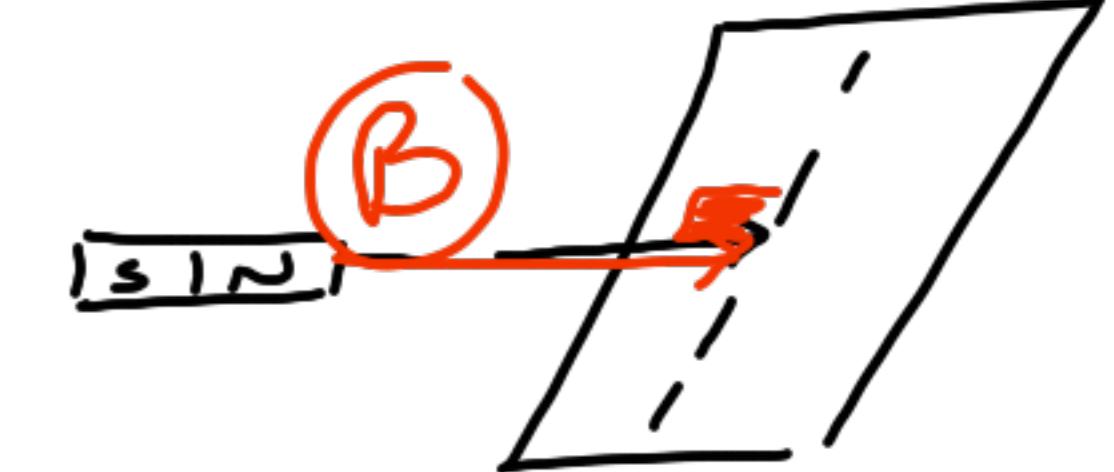
M. flux density:  $(\beta)$

$$\beta = \frac{\phi_{m\perp}}{A}$$

$$\text{Tesla} = \frac{\text{weber}}{\text{m}^2}$$

$$\beta = \frac{\phi_{m\perp}}{A}$$

$$\phi_m = BA$$



$$\phi = BA \cos \theta$$

or

$$\phi = BA \sin \theta$$

MF Area



$$\phi = BA \sin \theta$$

= zero

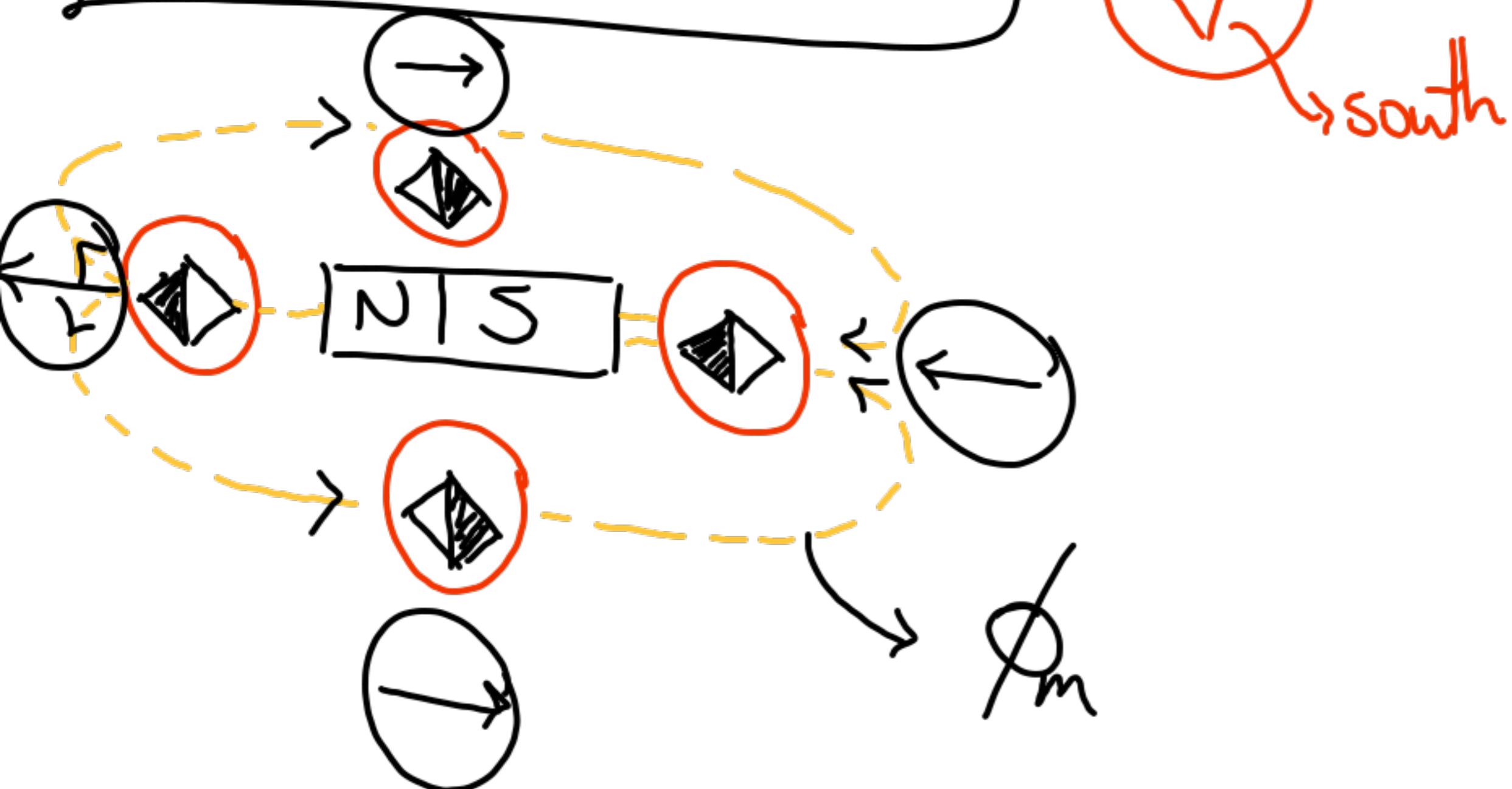
$$\phi = BA \cos\theta$$

normal  
to Area  
MF

$\sin\theta$

Area  
MF

$1 \text{ Weber} = 1 \text{ Tesla} \cdot \text{m}^2$



Conductor + Current

$$= \bar{M} F$$

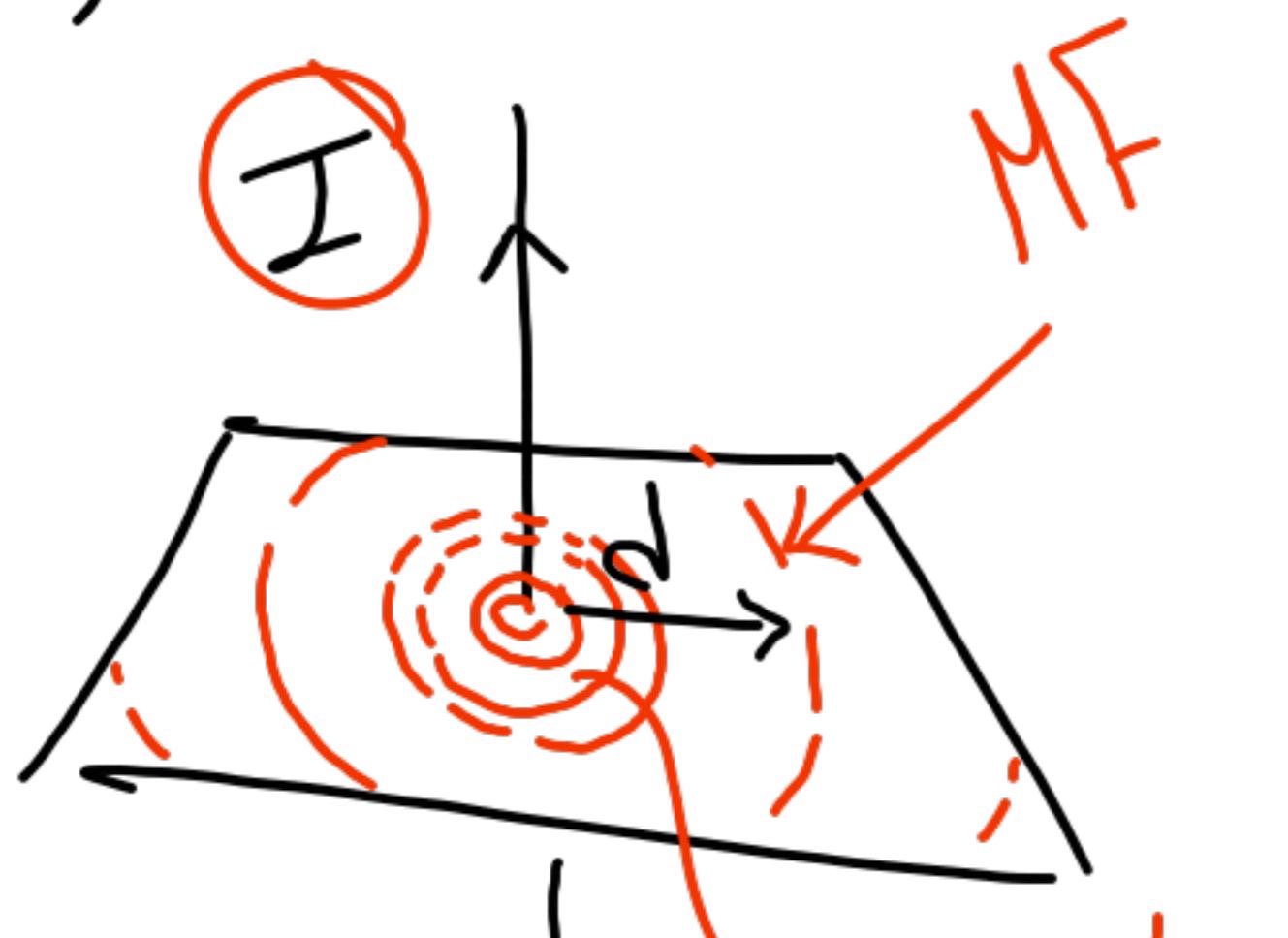
St. wire

Circular coil

Solenoid

# I St. wire

## a) Shape



- 1) Concentric circles
- 2) Crowded near the wire
- 3) As  $I \uparrow$ , more crowded
- 4) As  $d \uparrow$ , less crowded.

b) Law:

$$B \propto I \quad B \propto \frac{1}{d}$$

$$B \propto \frac{I}{d}$$

$$\boxed{B = \frac{\mu}{2\pi} \frac{I}{d}}$$

→ Magnetic permeability

$$\mu = \frac{B 2\pi d}{I}$$

\*  $\frac{tesla.m}{Amp}$        $\frac{wb \cdot m}{m^2 \cdot Amp}$  \*

$$B = \frac{\mu_0 \times 10^{-7} I}{2\pi d}$$

$$\boxed{B = 2 \times 10^{-7} \frac{I}{d}}$$

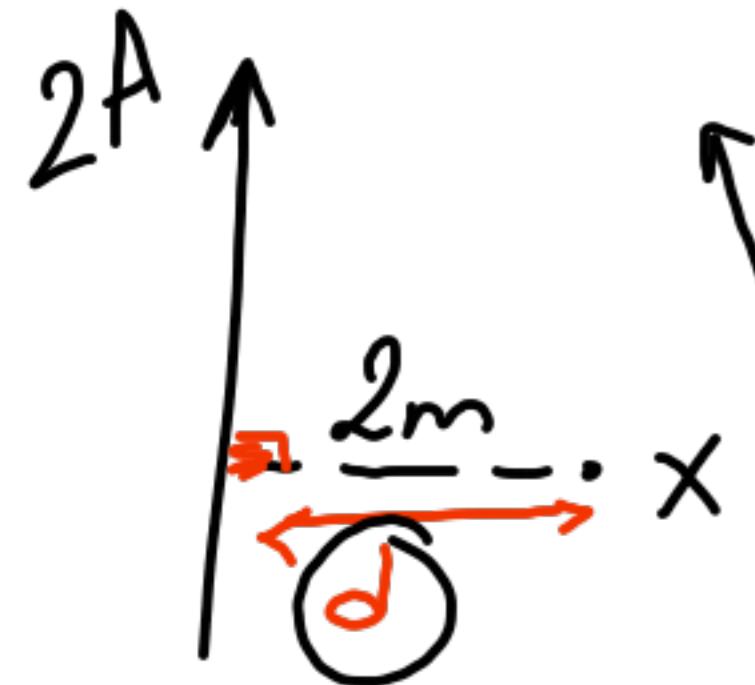
→ factors:

1)  $M$

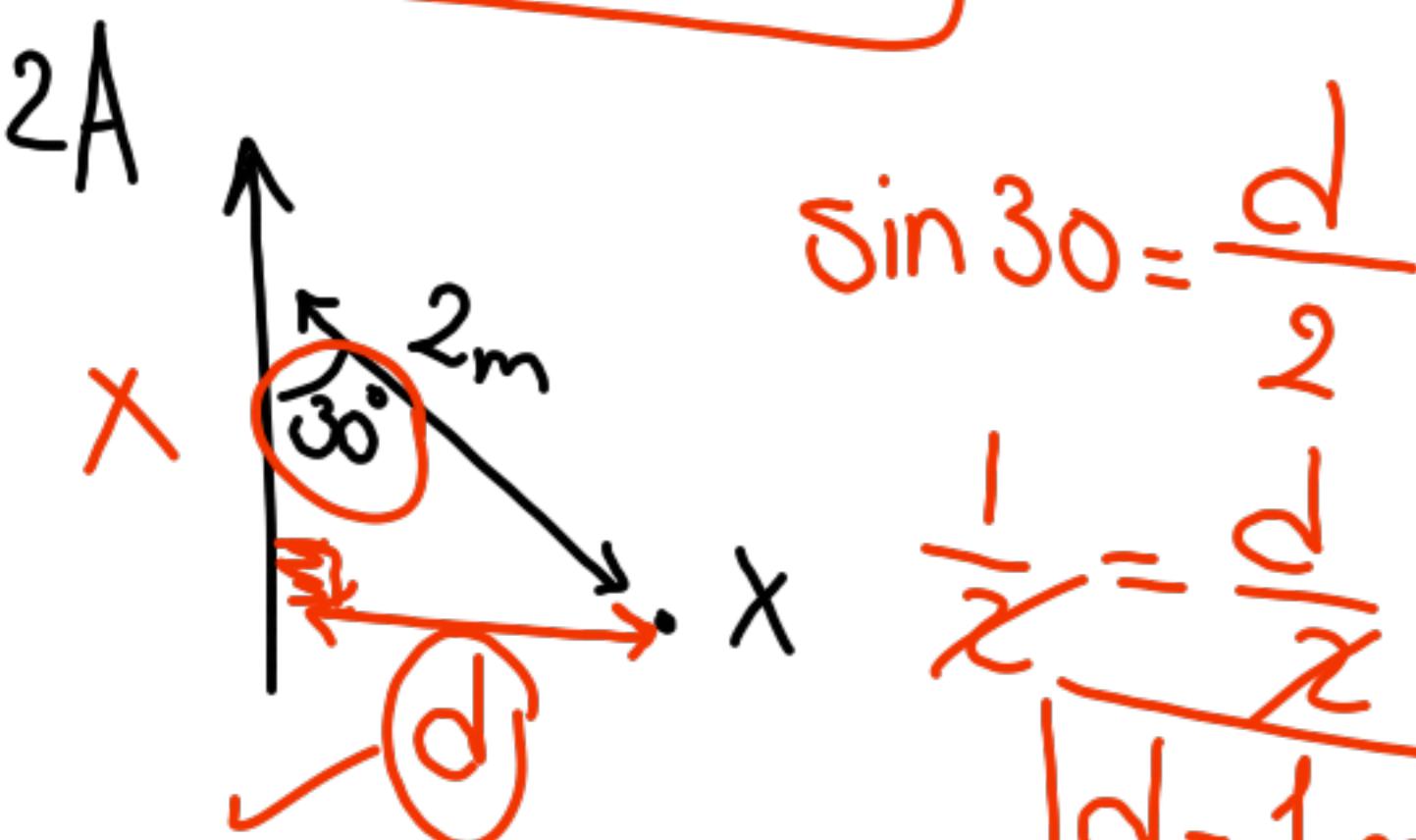
2)  $I$

3) Normal distance

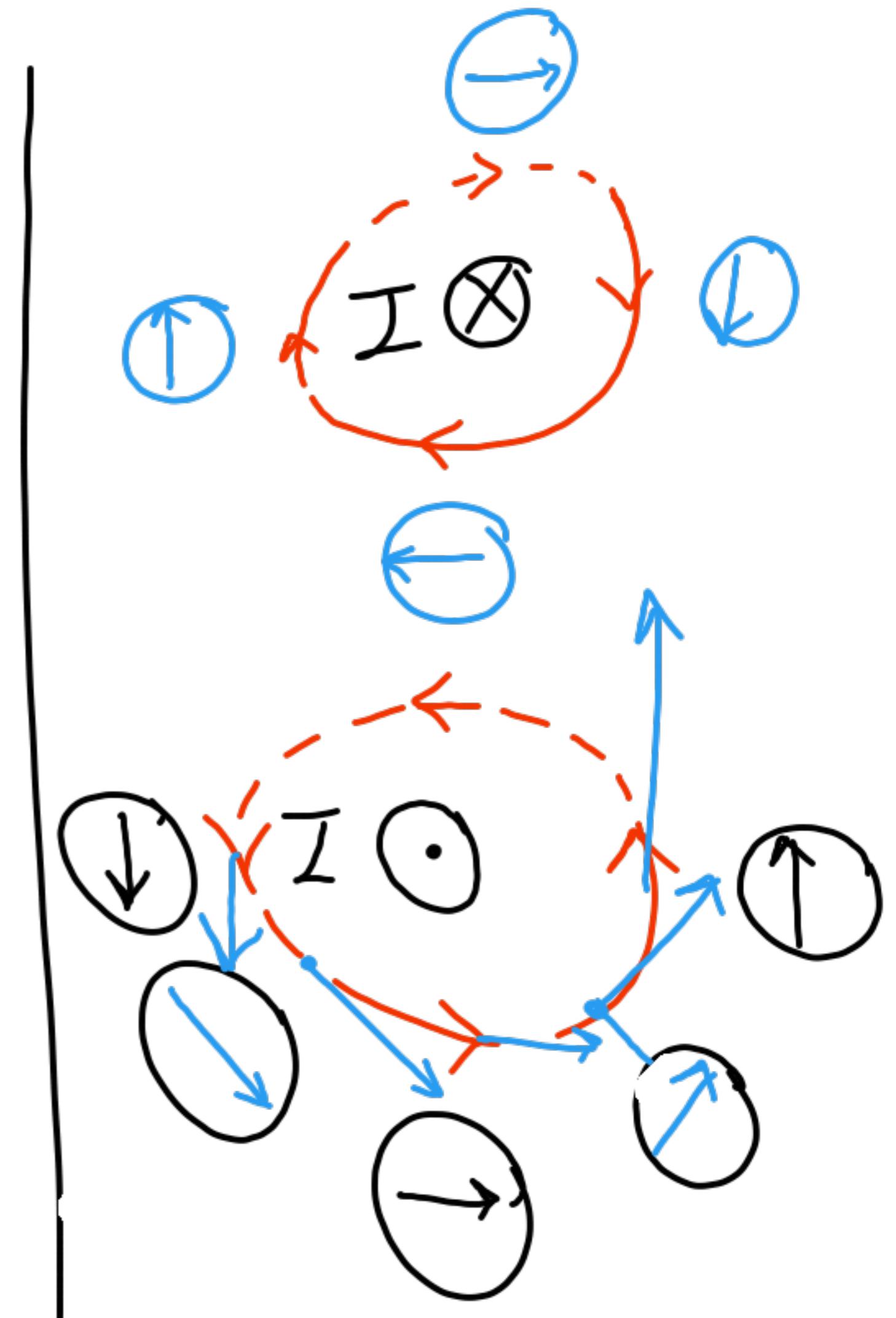
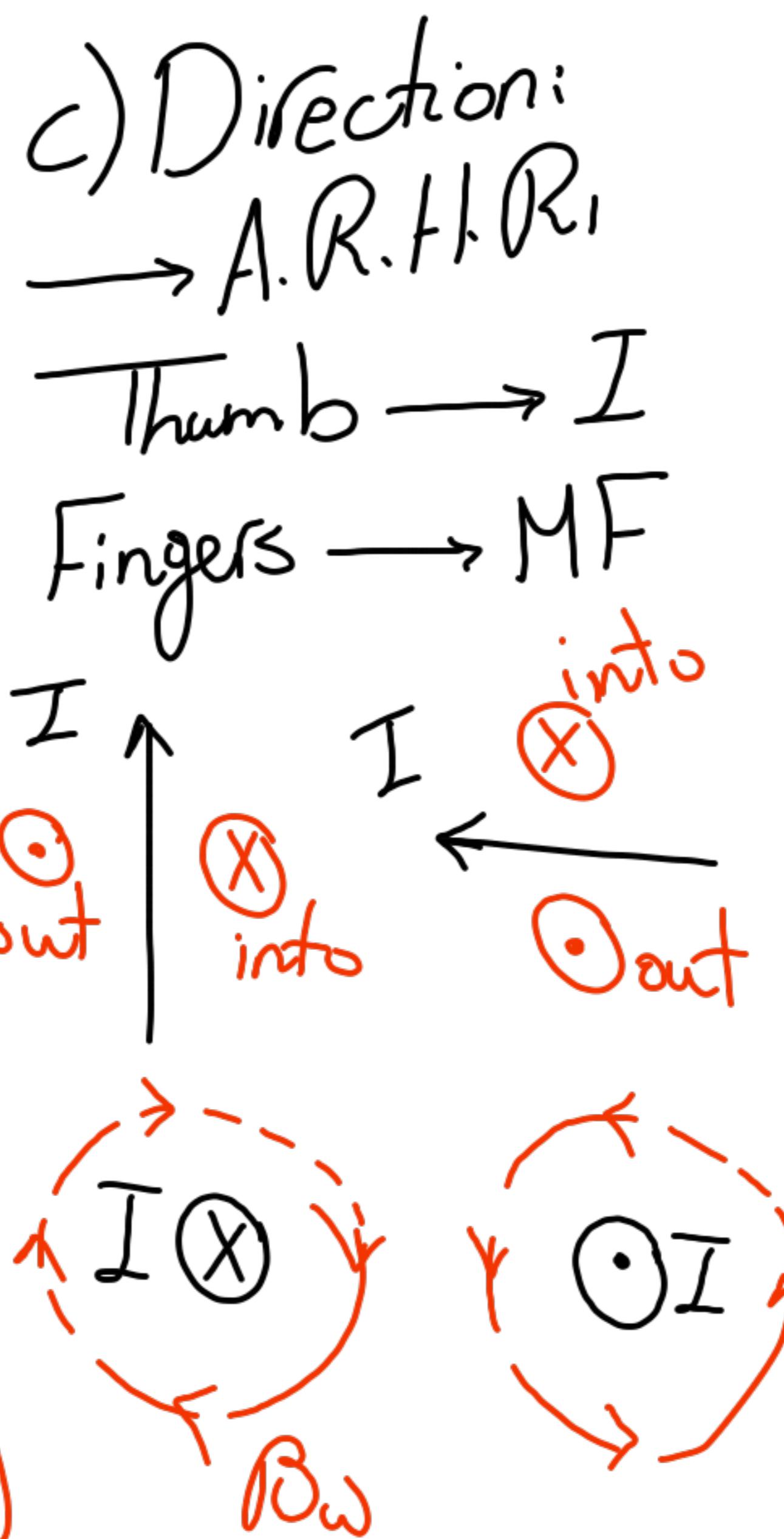
$$\frac{wb}{Amp \cdot m}$$



$$B = 2 \times 10^{-7} \times \frac{2}{2} = 2 \times 10^{-7} \text{ T}$$

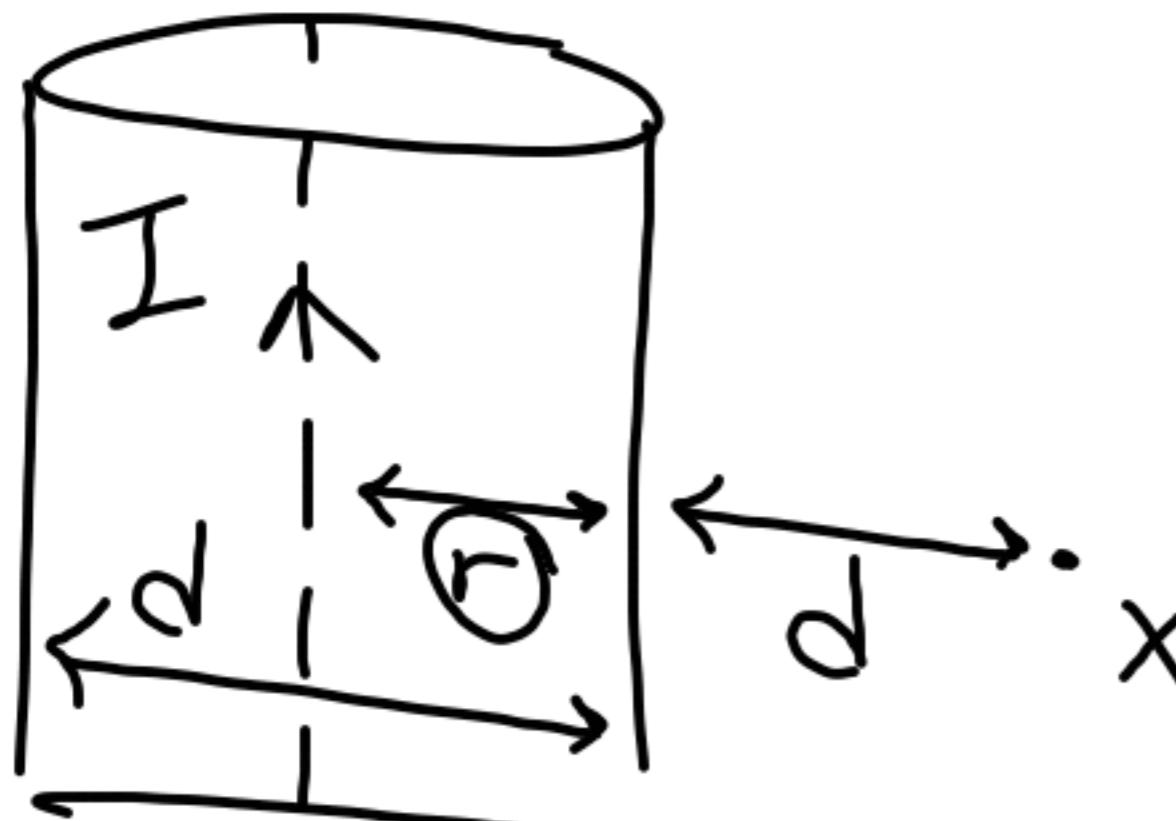


$$B = 2 \times 10^{-7} \times \frac{2}{1} = 4 \times 10^{-7} \text{ T}$$



## Problems:

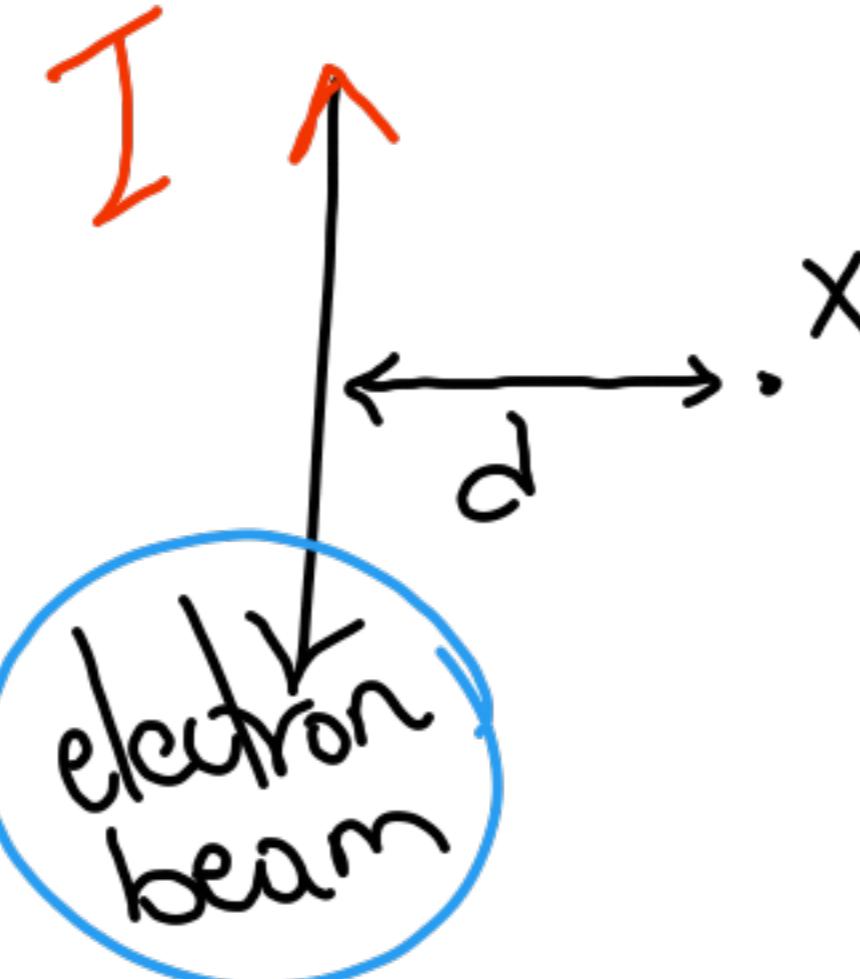
1) Wire of given ( $r$ )



$$\mathcal{B} = 2 \times 10^{-7} \times \frac{I}{d+r}$$

$$r = \frac{\text{diameter}}{2}$$

2) Electron beam



$$\mathcal{B} = 2 \times 10^{-7} \times \frac{I}{d}$$

current  $I$   
جسيم جاري  
التيار  
é جسيم جاري

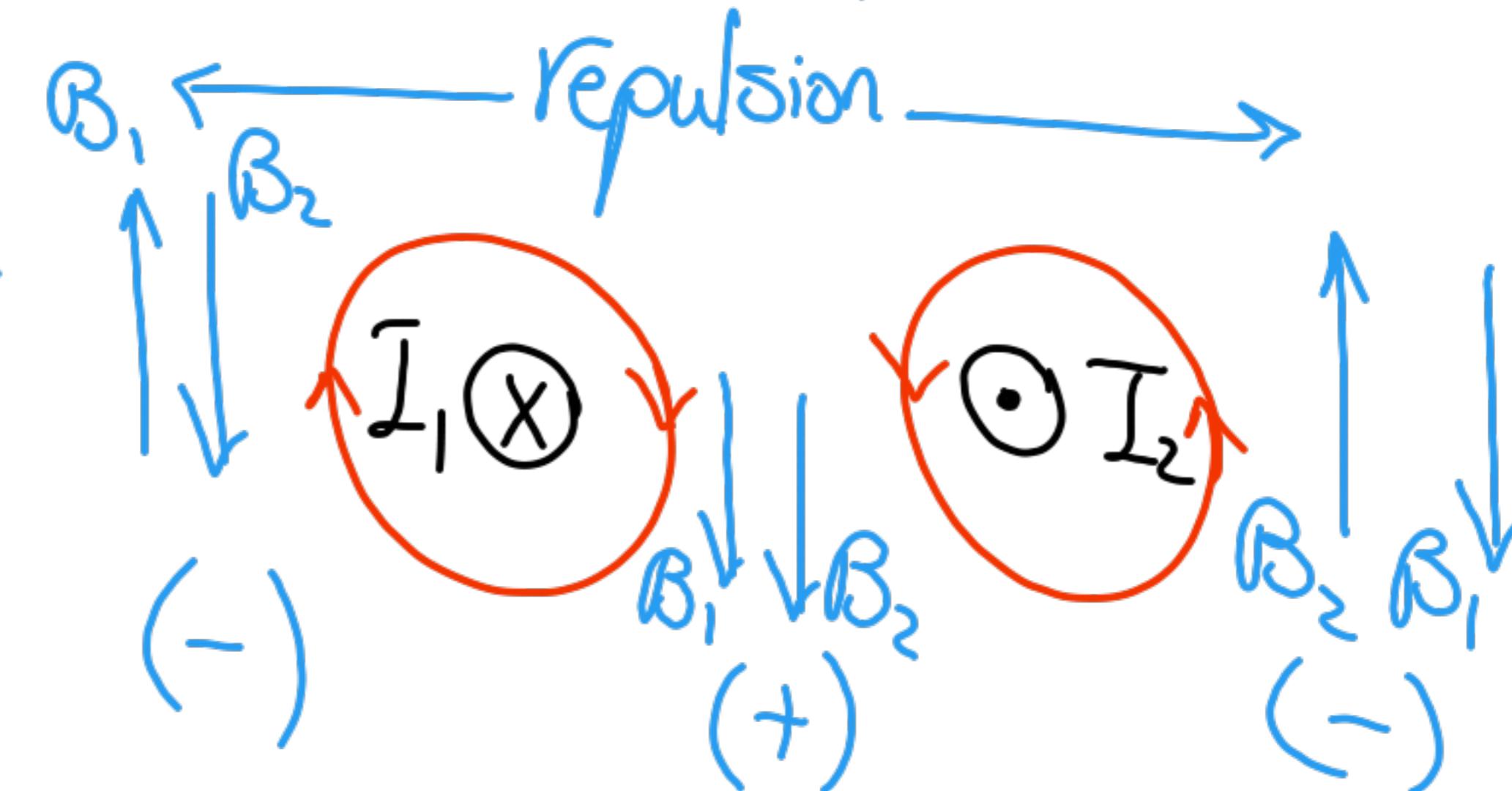
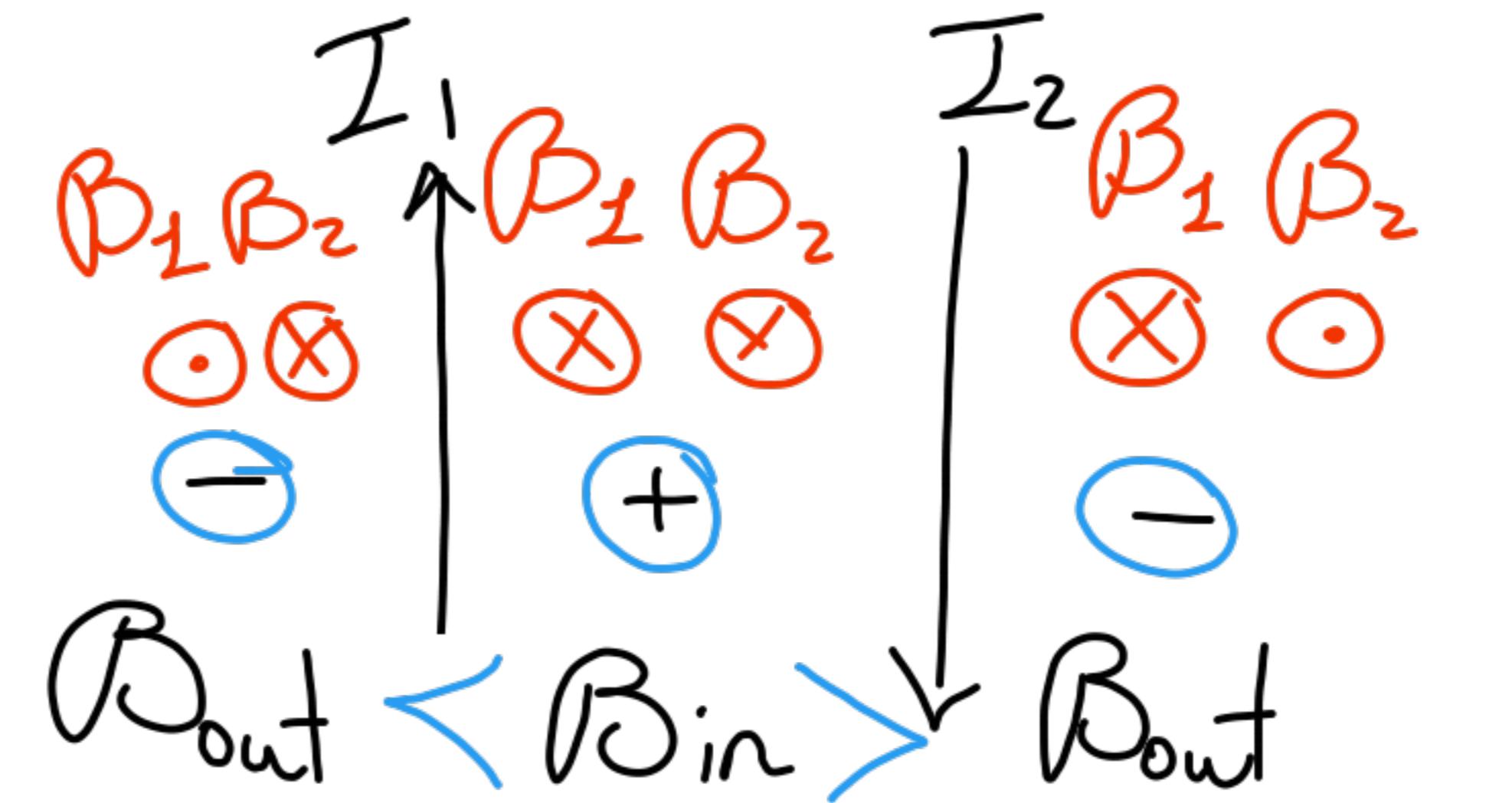
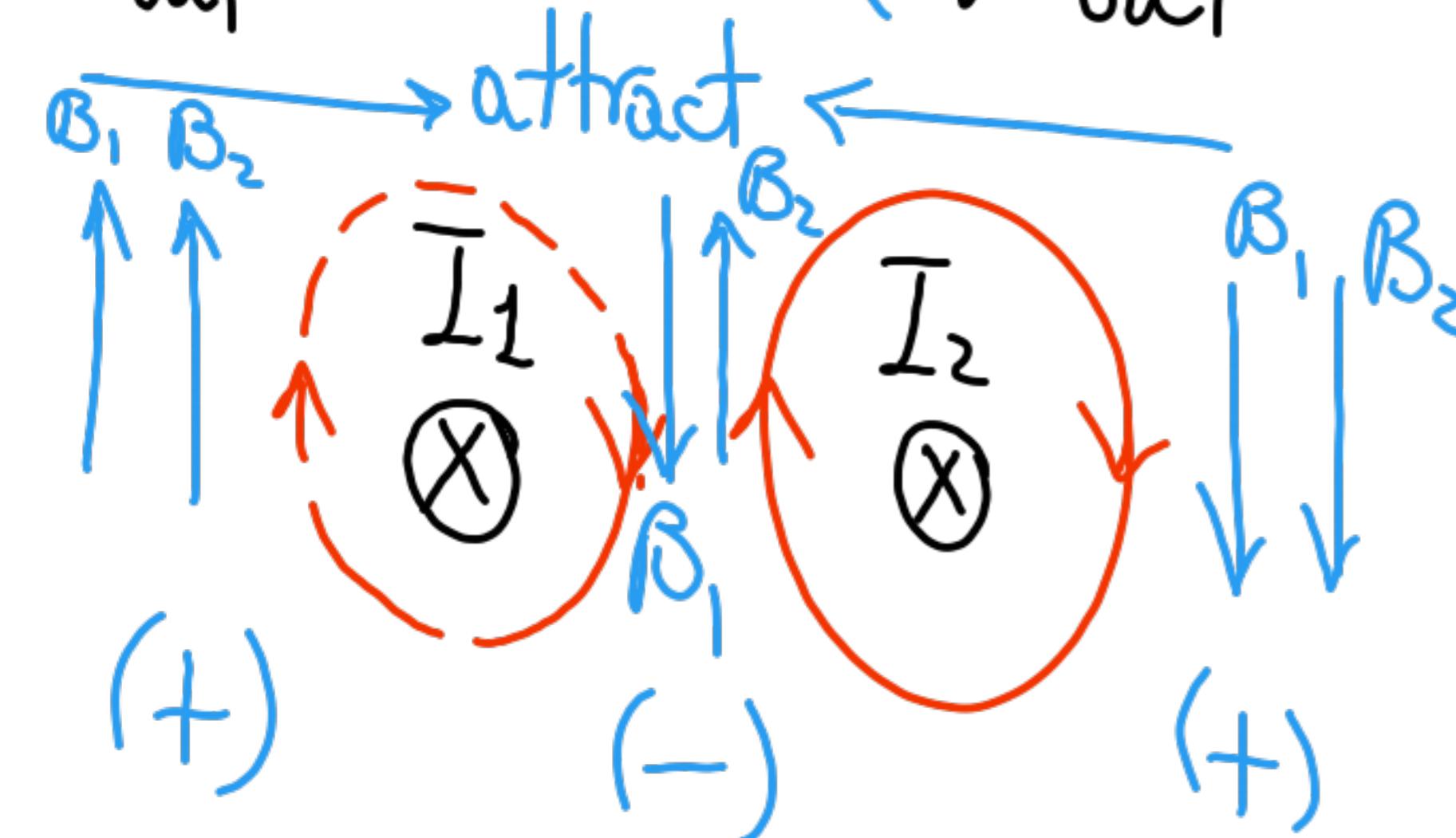
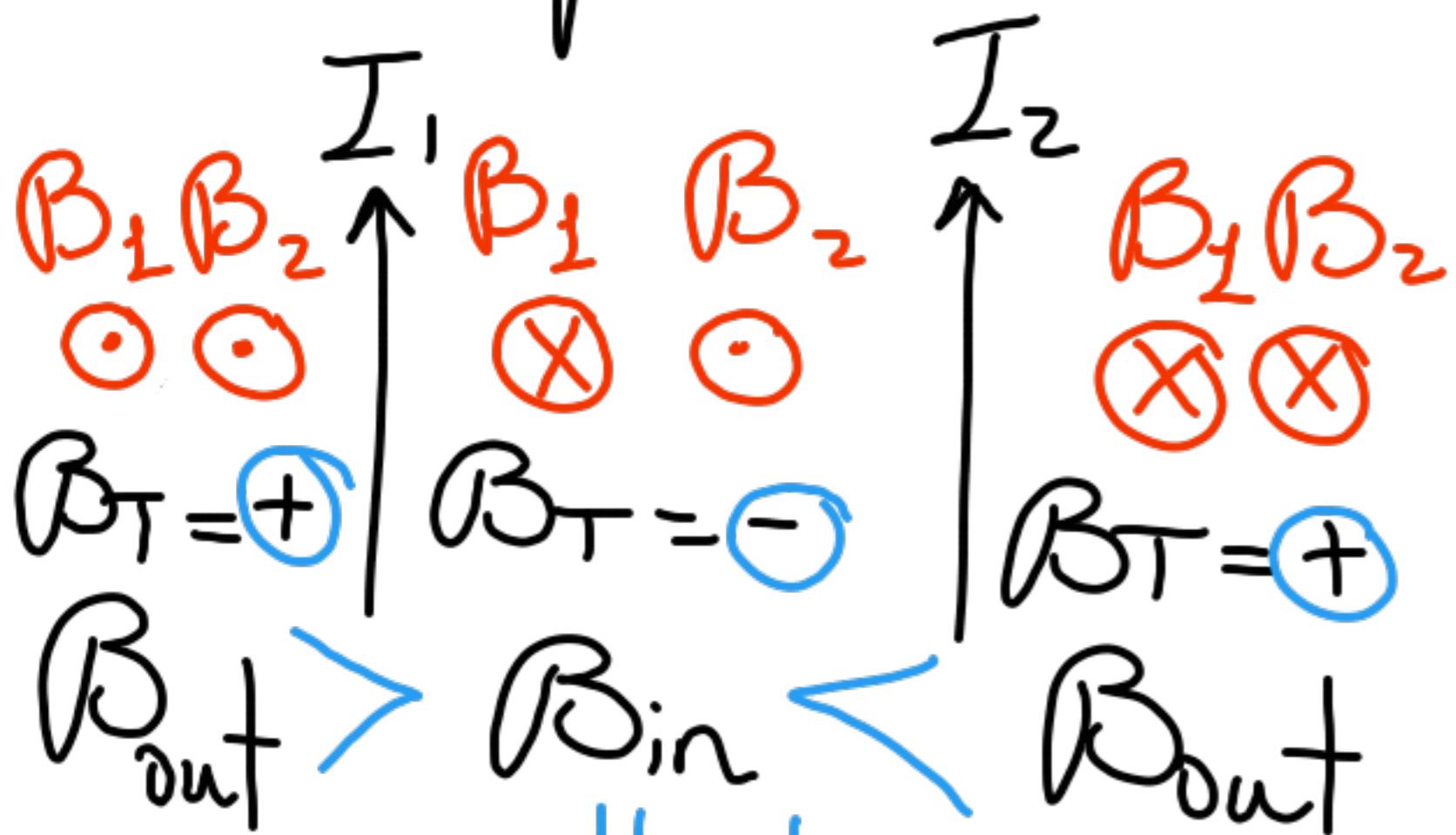
$$1.6 \times 10^{-19} C$$

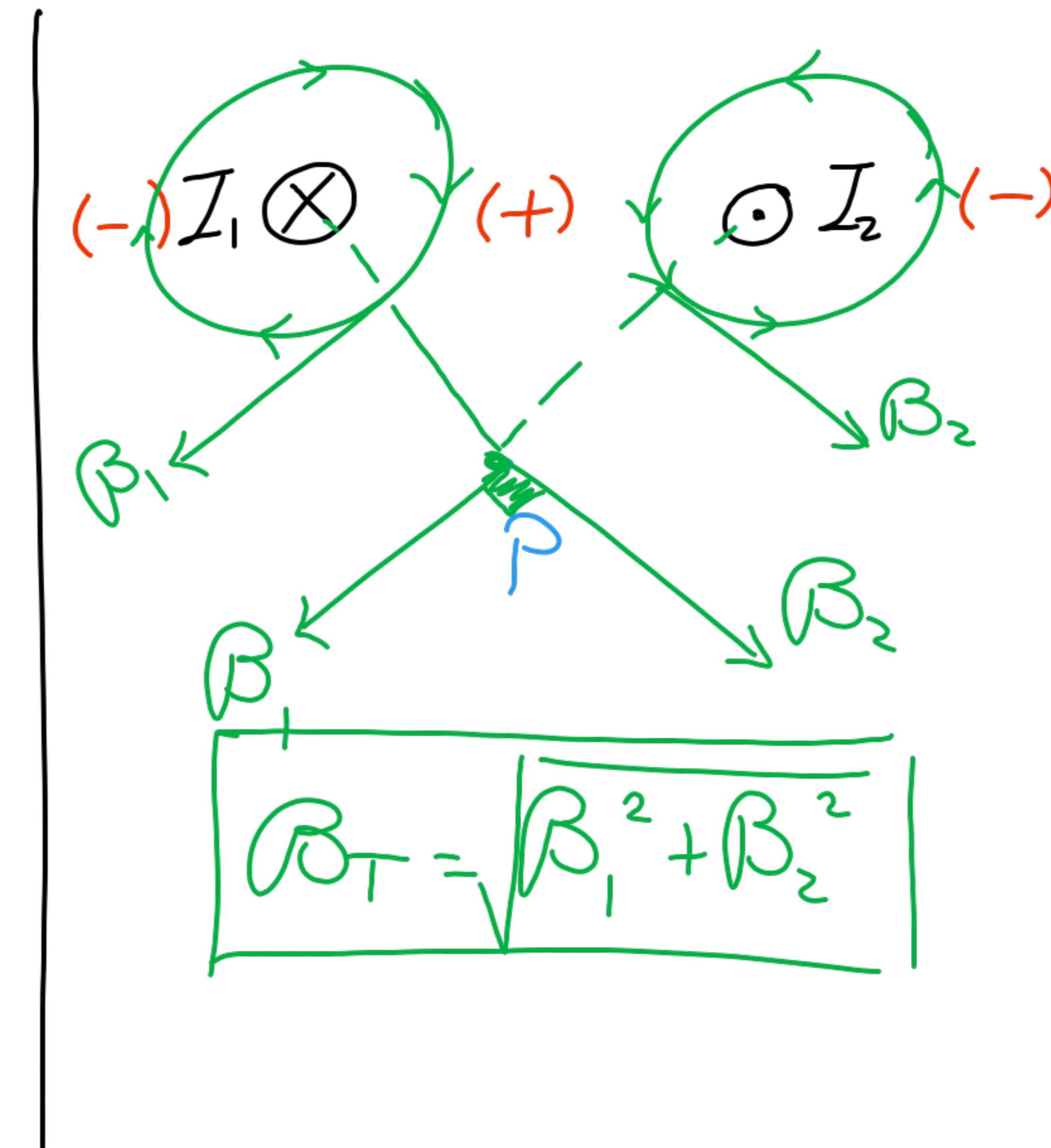
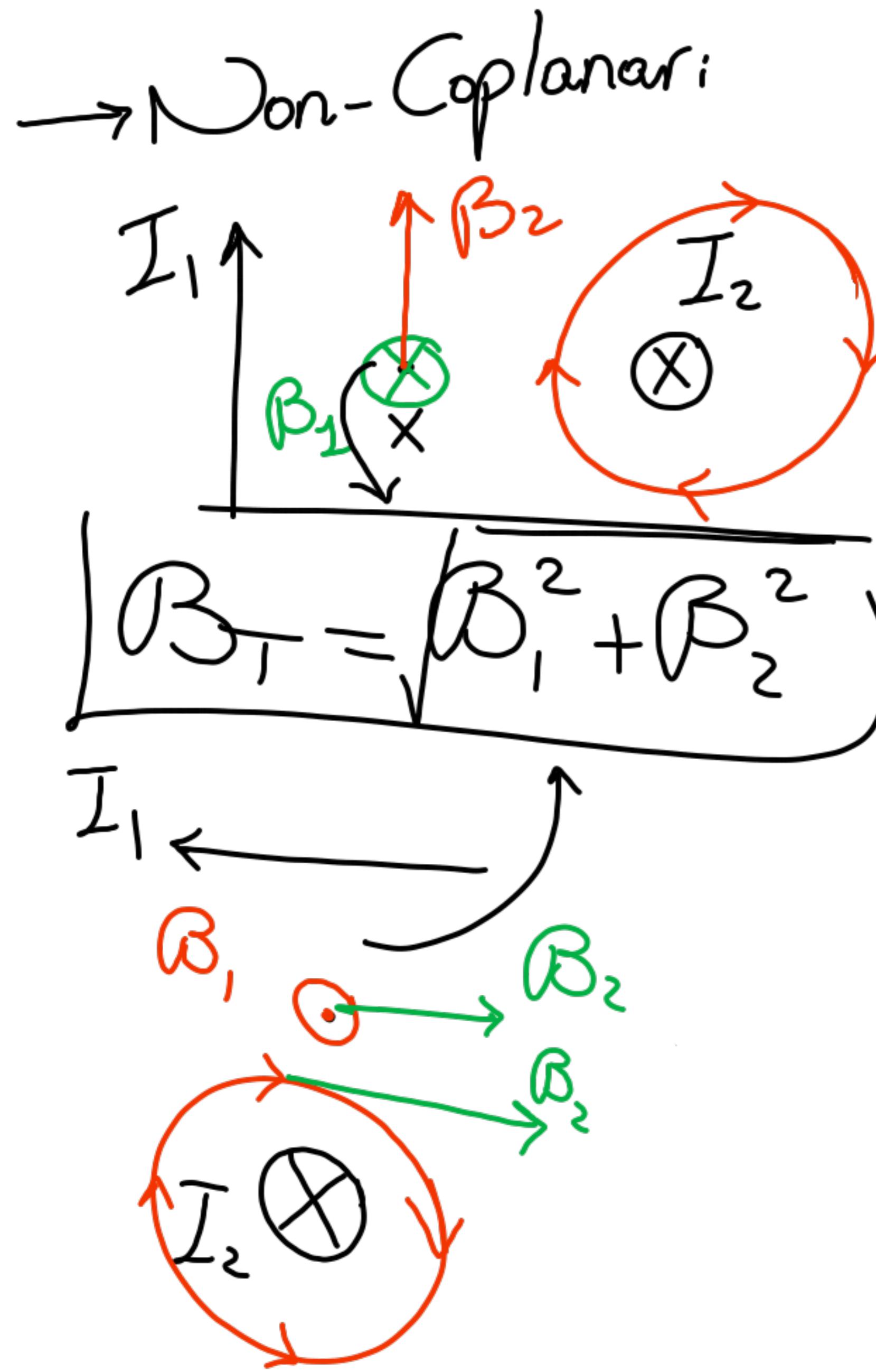
$$I = \frac{Q}{t} = \frac{n \times e}{t}$$

rate of electrons

3 Two wires

→ Coplanar



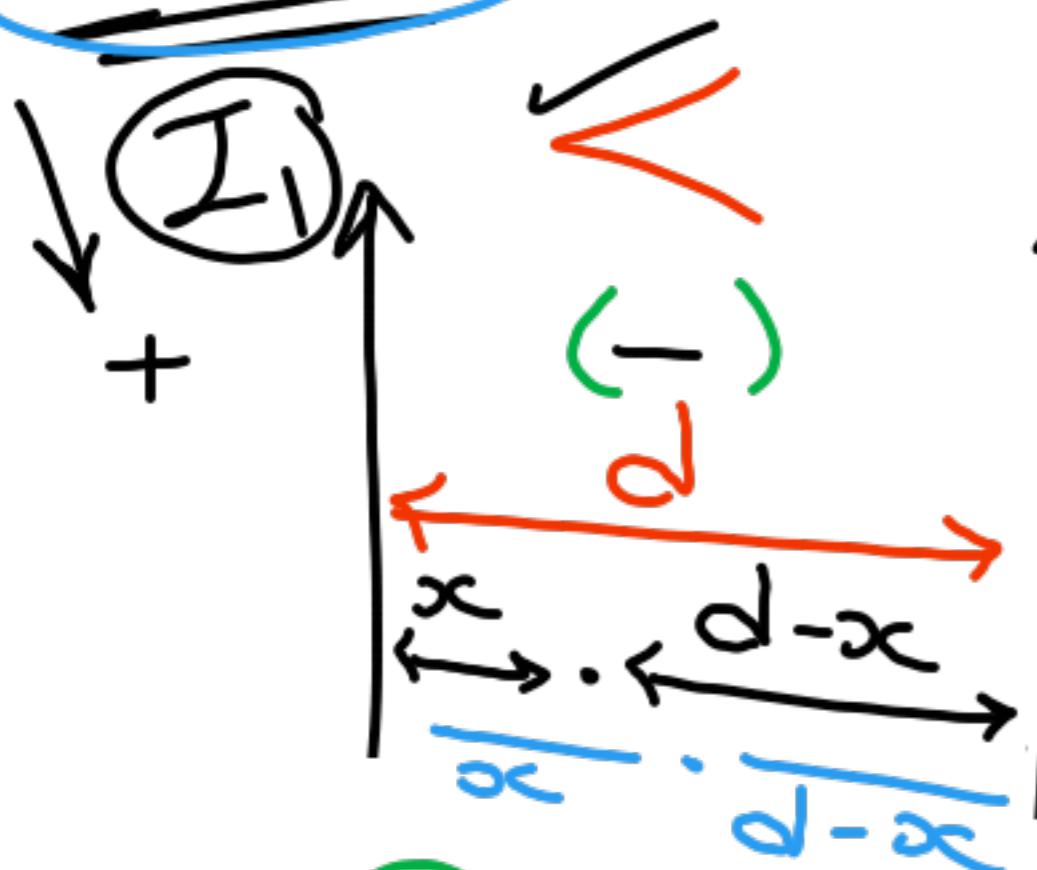


→ Neutral point  $\rightarrow \beta_T = 0$

Opp MF (-)

near the weaker current

Same



$$I_1 \uparrow \quad I_2 \uparrow$$

+      +

if  $I_1 = I_2$   
 $x = d - x$   
 $\therefore$  Neutral at midpoint

$$\beta_T = 0$$

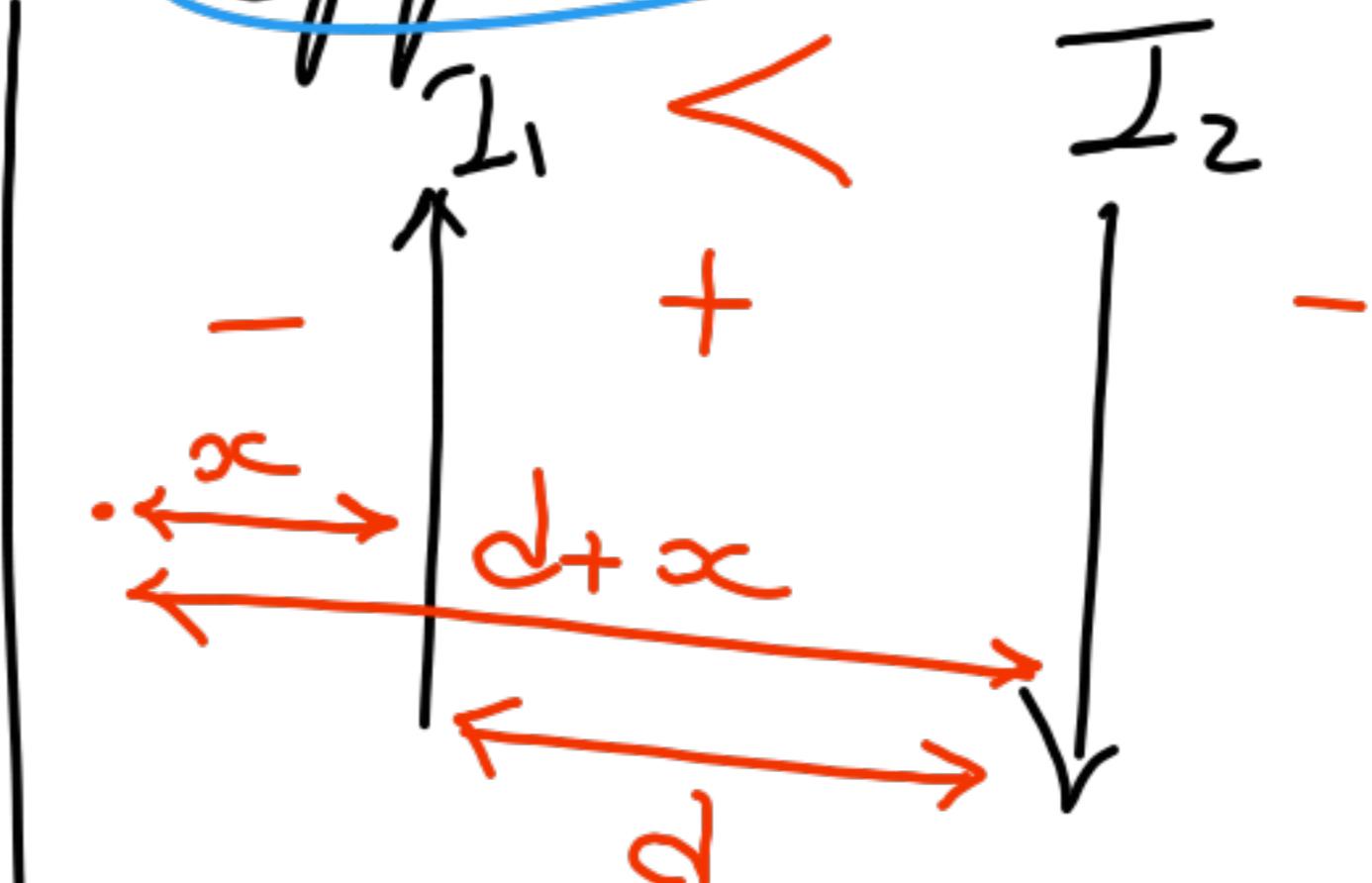
$$\beta_1 - \beta_2 = 0$$

$$\beta_1 = \beta_2$$

~~$$2 \times 10^7 \frac{I_1}{d_1} = 2 \times 10^7 \frac{I_2}{d_2}$$~~

$$\boxed{\frac{I_1}{x} = \frac{I_2}{d-x}}$$

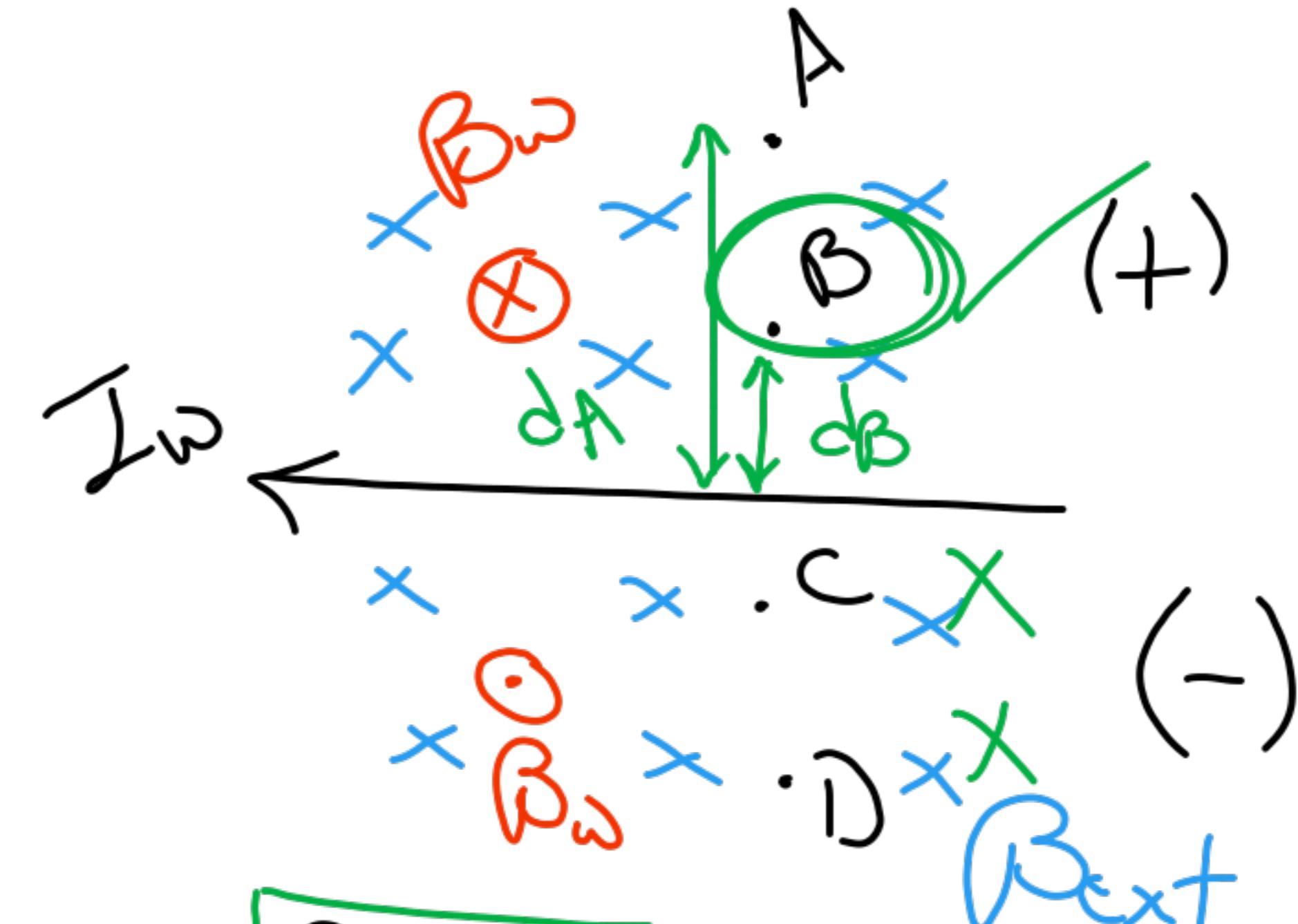
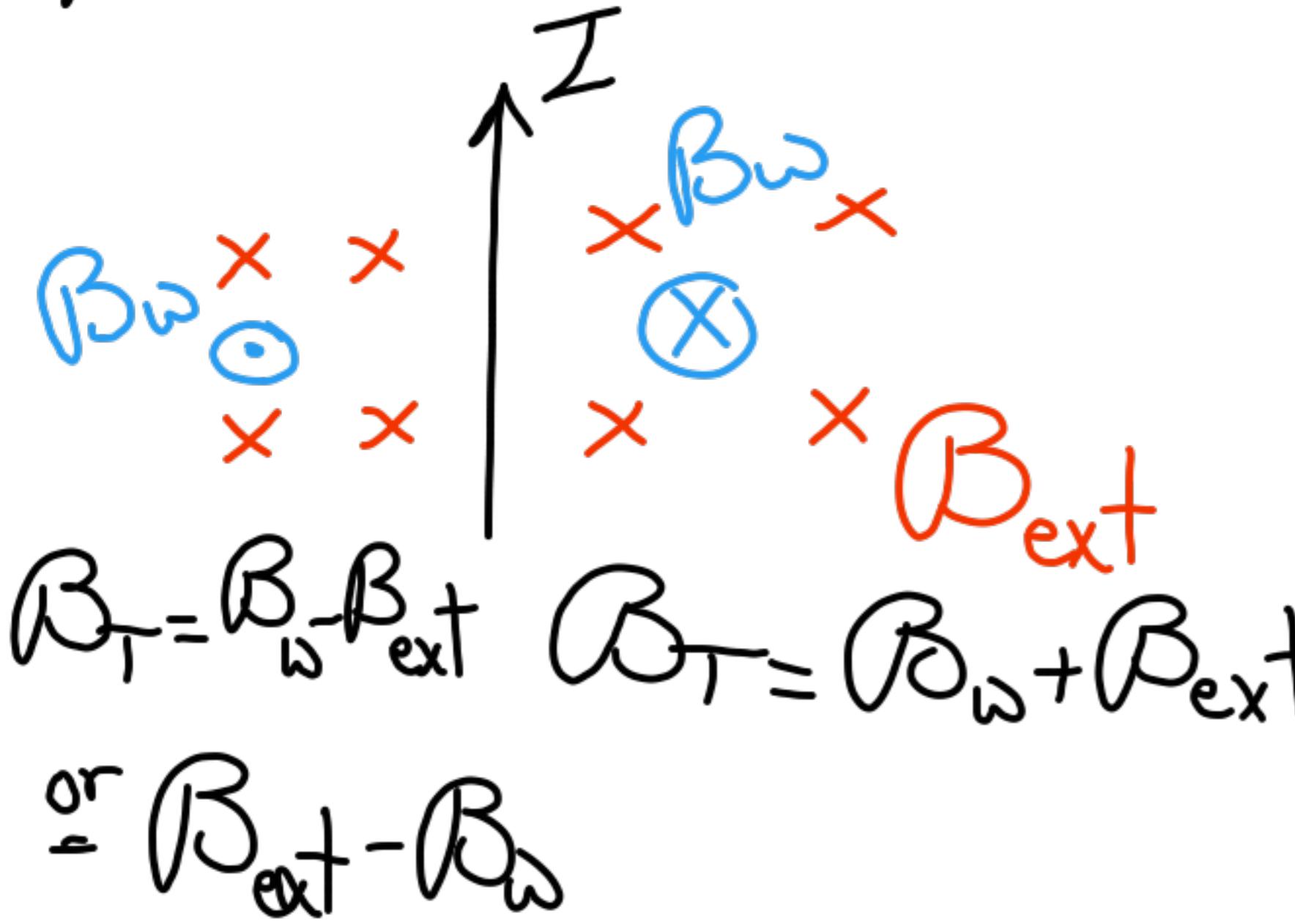
Opposite



$$\boxed{\frac{I_1}{x} = \frac{I_2}{d+x}}$$

if  $I_1 = I_2$   
 $\therefore x \neq d+x$   
 $\therefore$  No neutral point.

# 4 Wire + MF



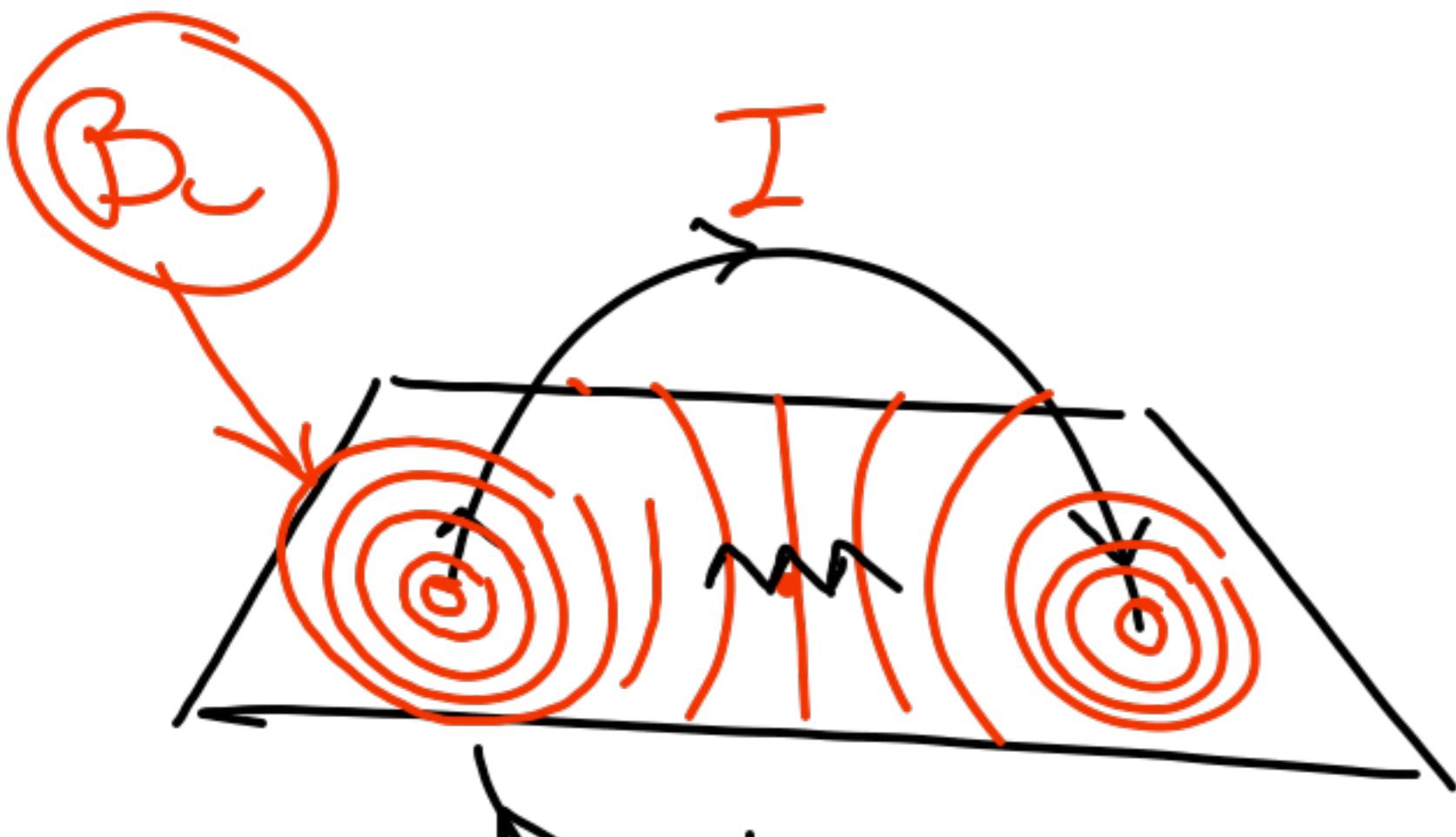
$$\boxed{\beta_A, \beta_B > \beta_C, \beta_D}$$

$$\therefore d_B < d_A$$

$$\boxed{\therefore \beta_B > \beta_A}$$

## 2 Circular Coil

### a) Shape



$\rightarrow$  properties:

- 1) Concentric X
- 2) Uniform parallel

- 3) M. flux  $\perp$  plane
- 4) Very similar to short bar magnet

b) Law:

$$B_c = \frac{\mu_0 N I}{2r}$$

$$N = \frac{L_{\text{wire}}}{2\pi r} = \frac{6}{360^\circ}$$

$$N = \frac{90^\circ}{360^\circ} = \frac{1}{4}$$

$$N = \frac{270^\circ}{360^\circ} = \frac{3}{4}$$

c) Direction:

R.H.S.R.

→ Clockwise

Anticlockwise

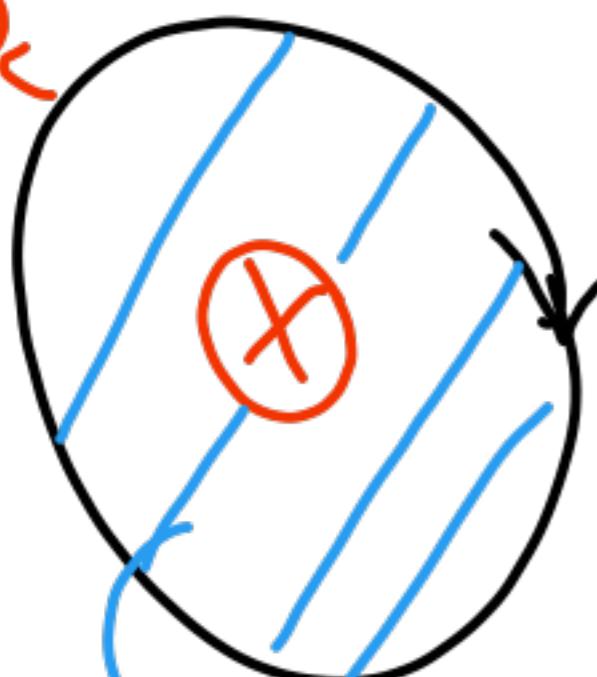


South

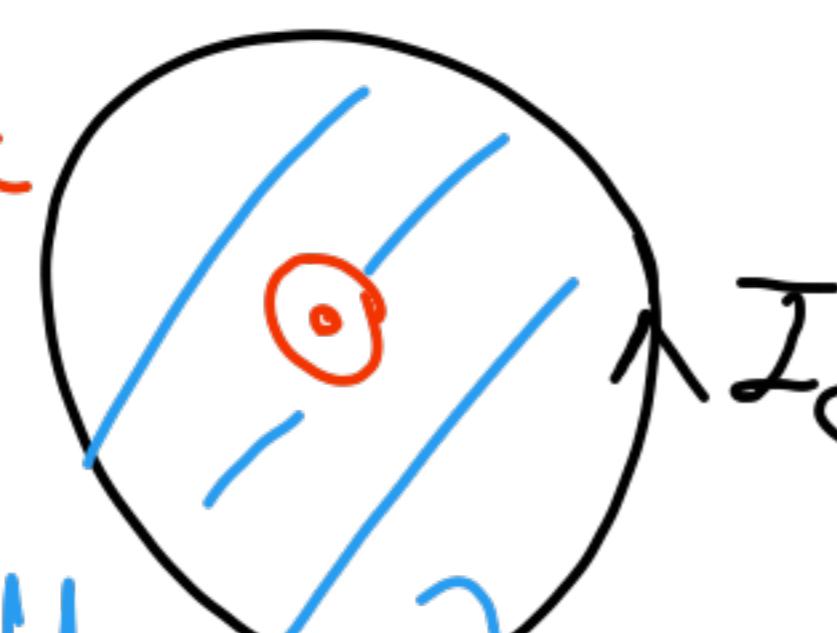


North

$B_c$



$B_c$



$I_c$

South

North

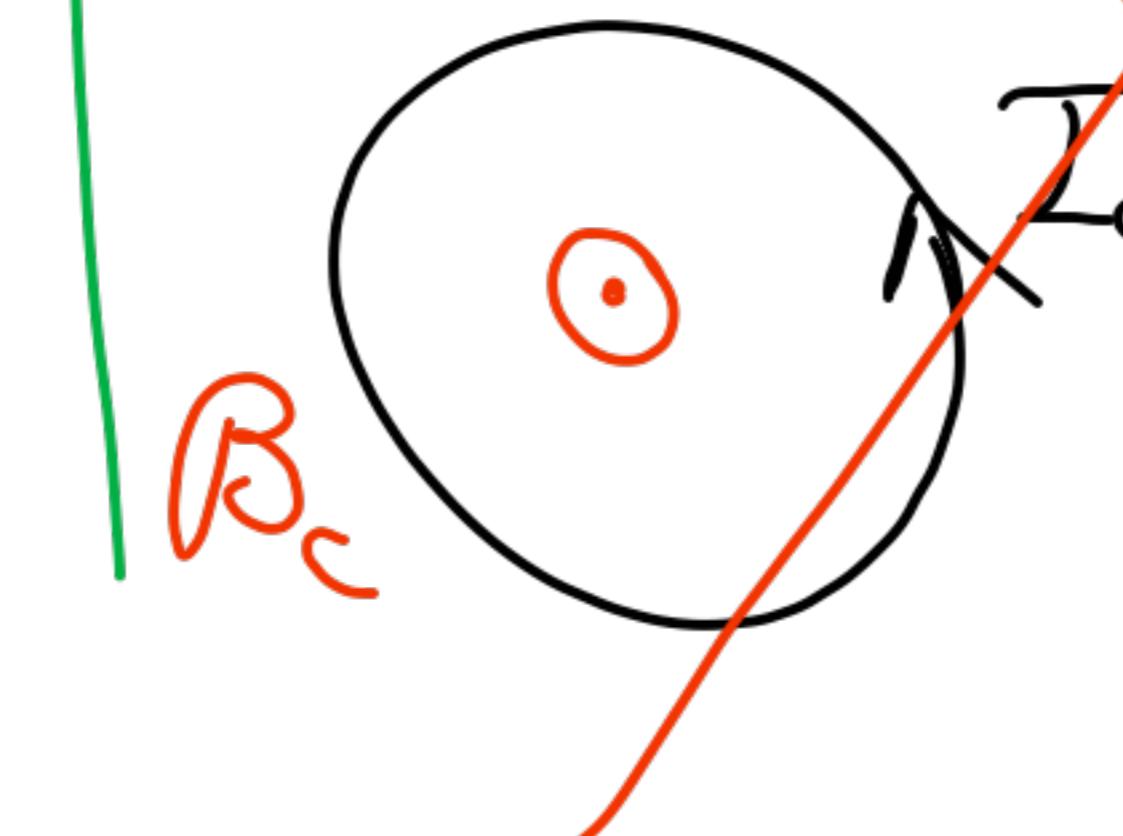
→ A.R.H.R:

Fingers →

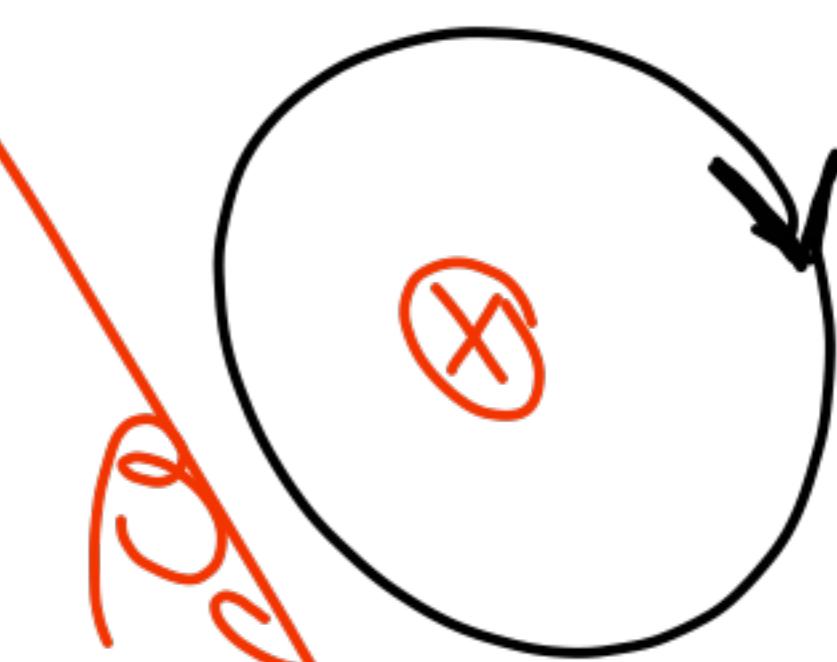
Current

Thumbs →

MF



$B_c$

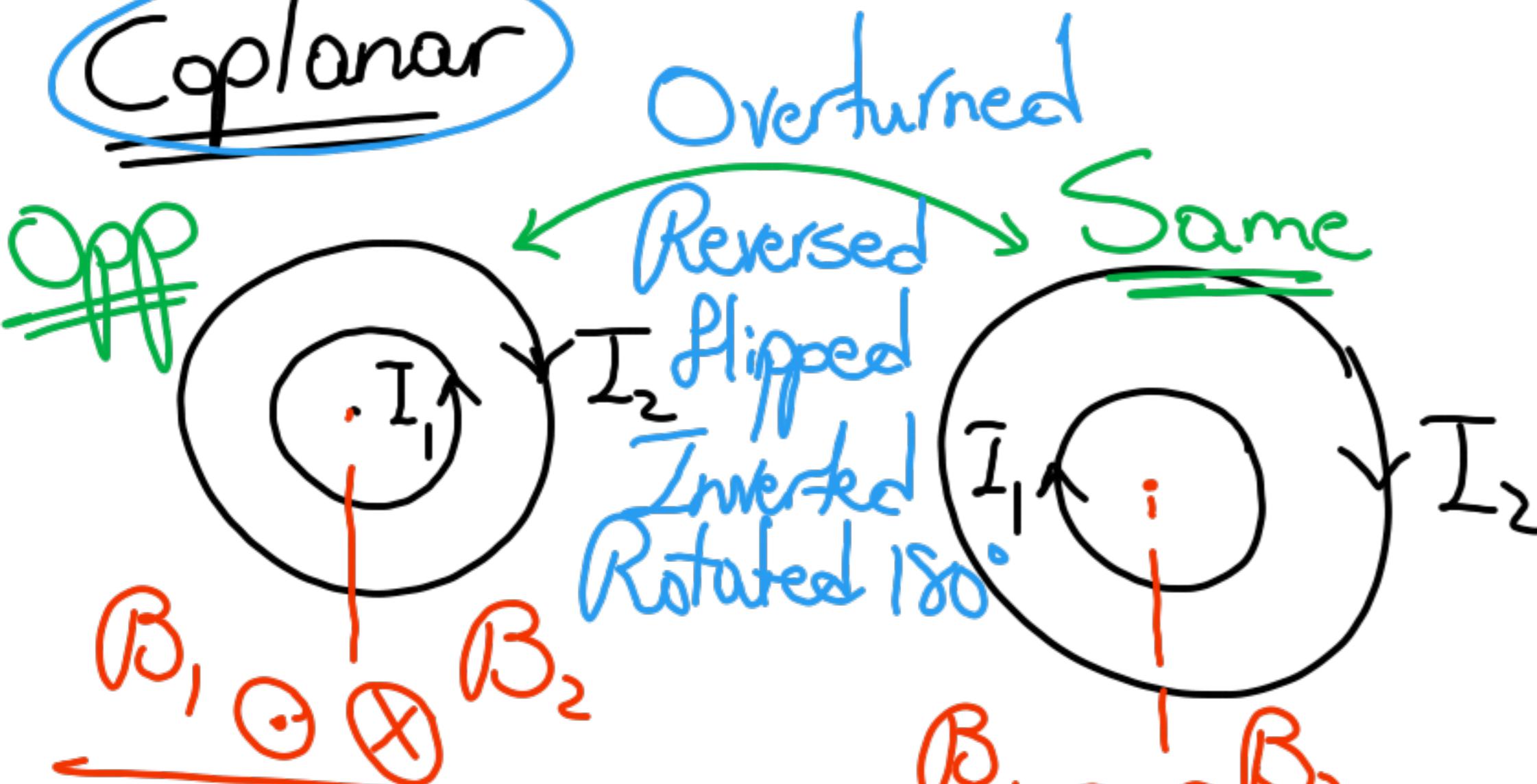


$B_c$

# Problems

## 1 Concentric Coils

Coplanar



$$\beta_T = \beta_1 - \beta_2$$

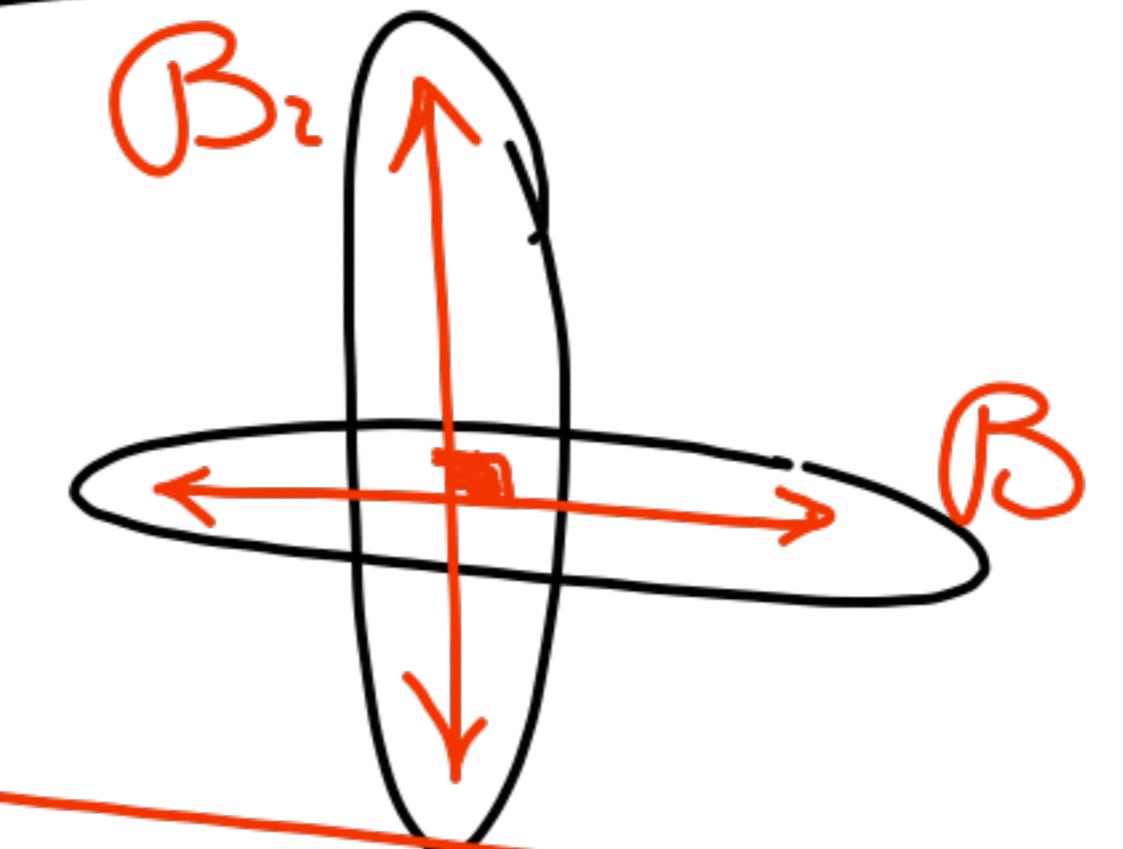
$$\text{or } \beta_2 - \beta_1$$

(opp)  $b_{-}$

$$\beta_T = \beta_1 + \beta_2$$

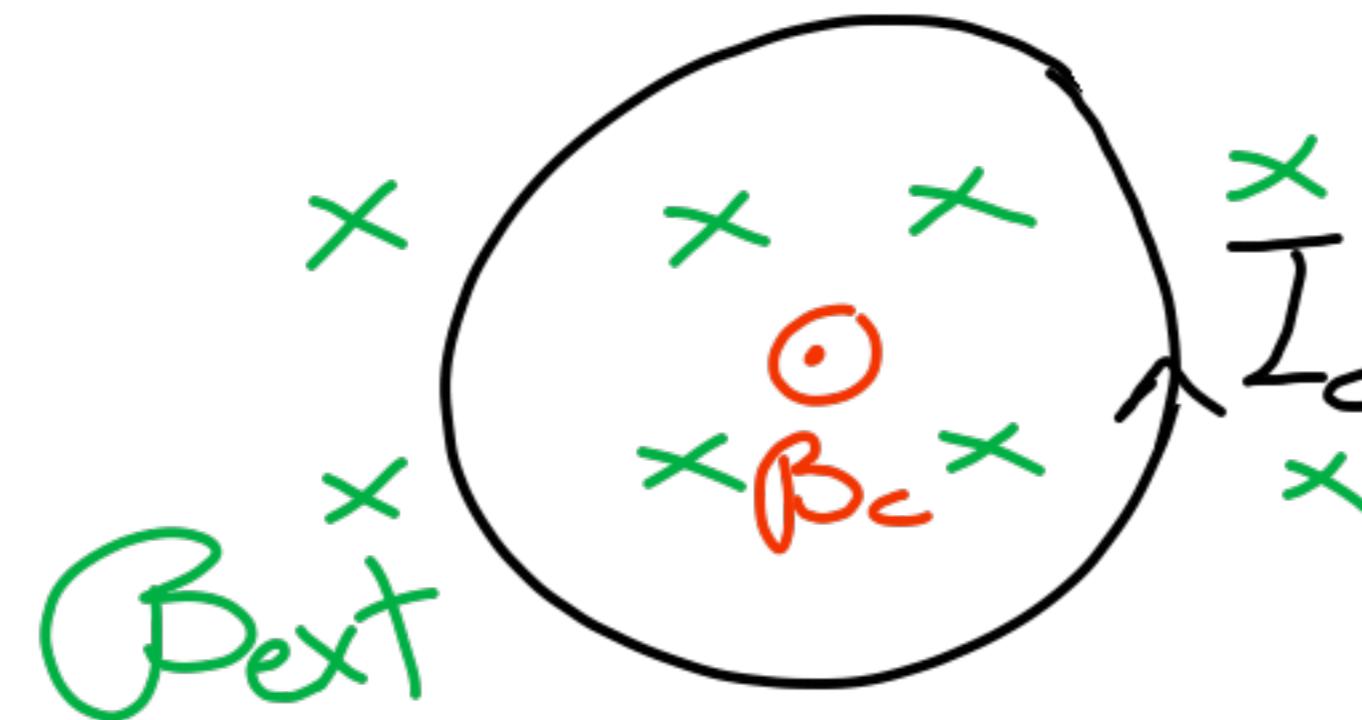
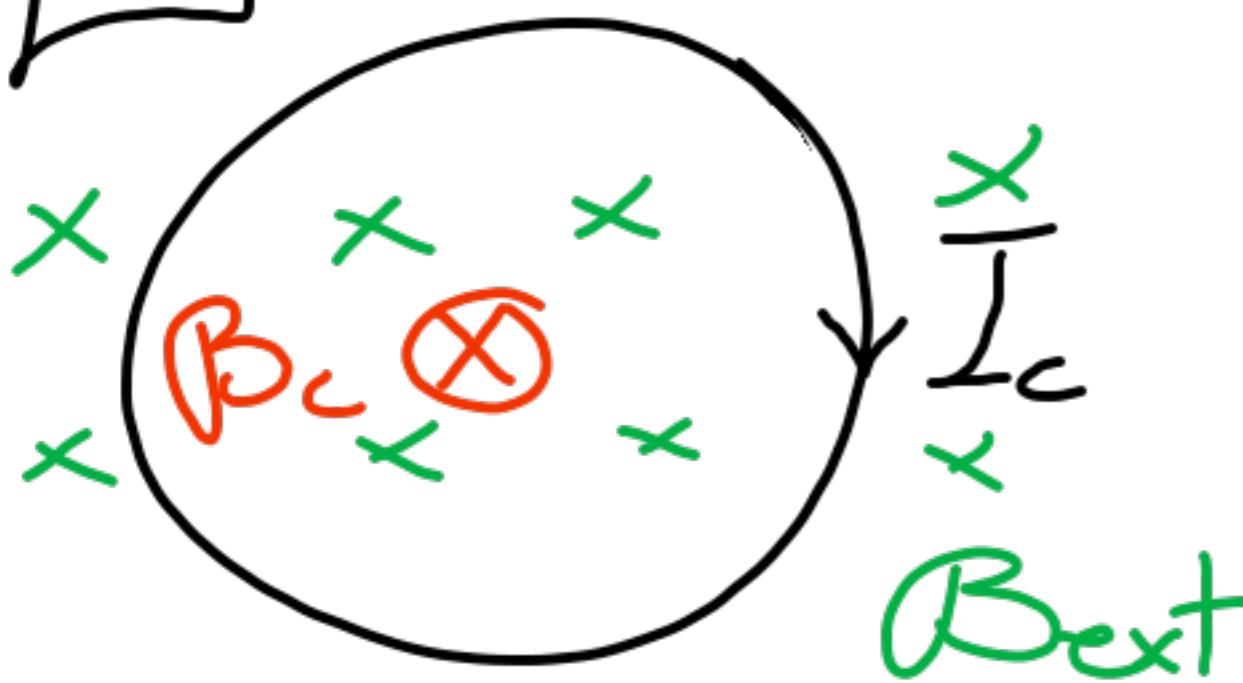
Same  $|+|$

Non-Coplanar

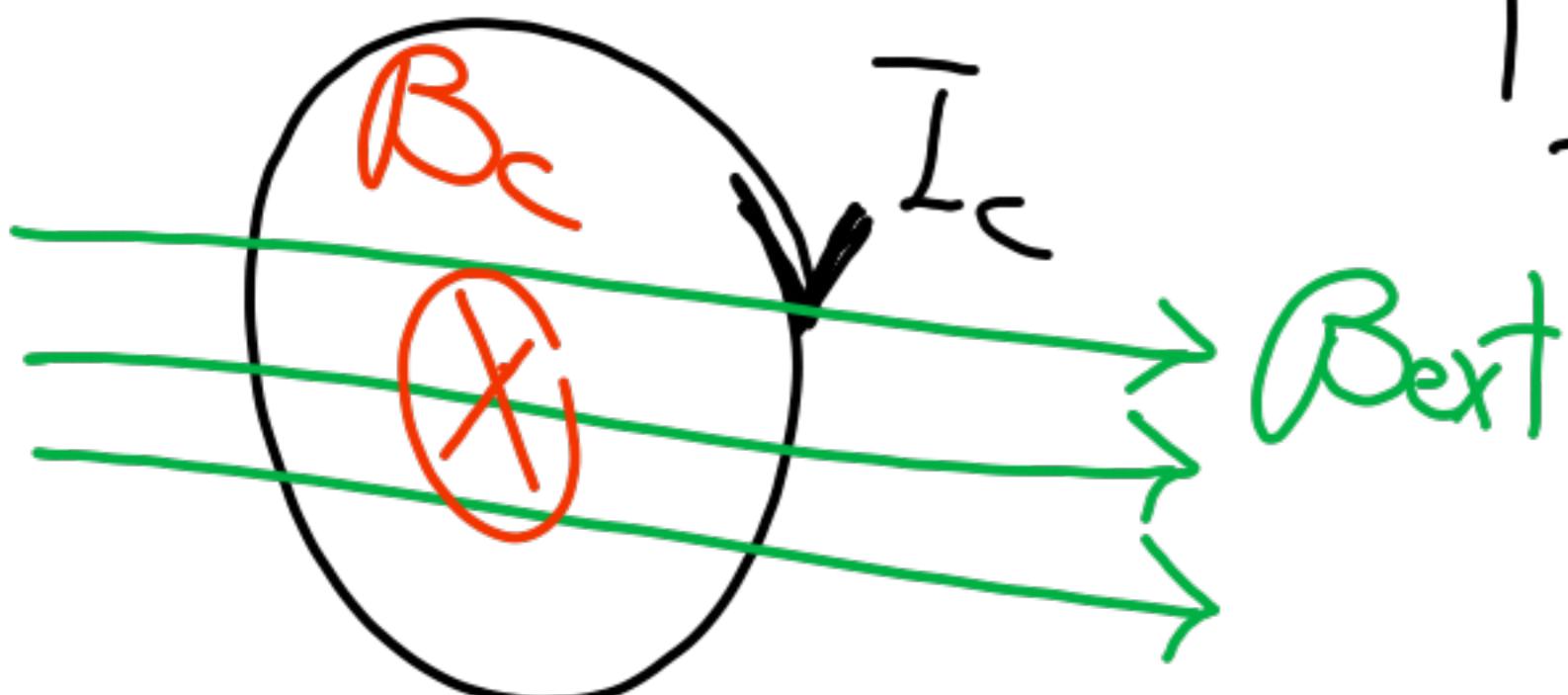


$$\beta_T = \sqrt{\beta_1^2 + \beta_2^2}$$

## 2 Coil + External MF



$$\beta_T = \beta_c + \beta_{ext}$$

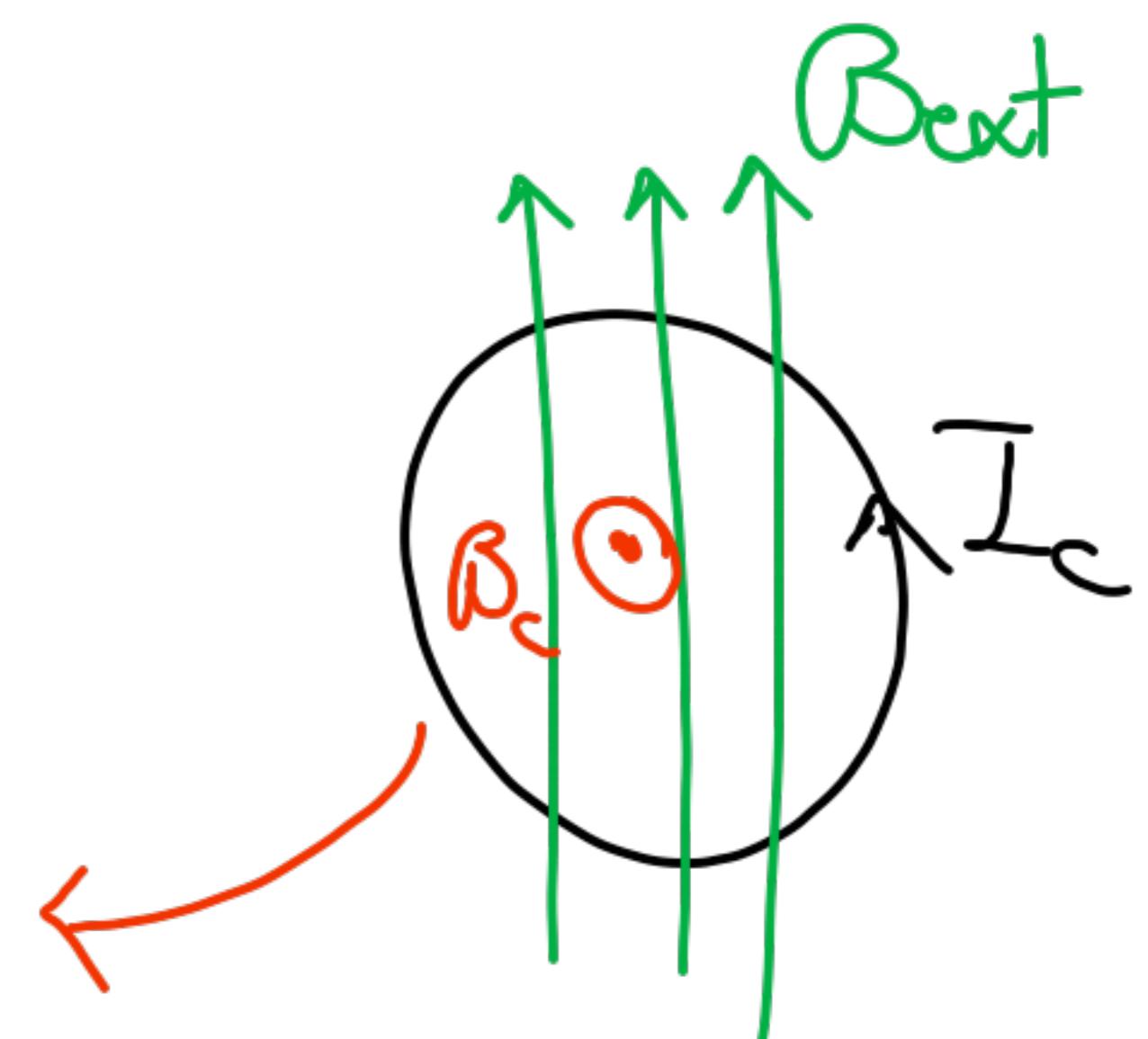


$$\beta_T = \beta_c - \beta_{ext}$$

or

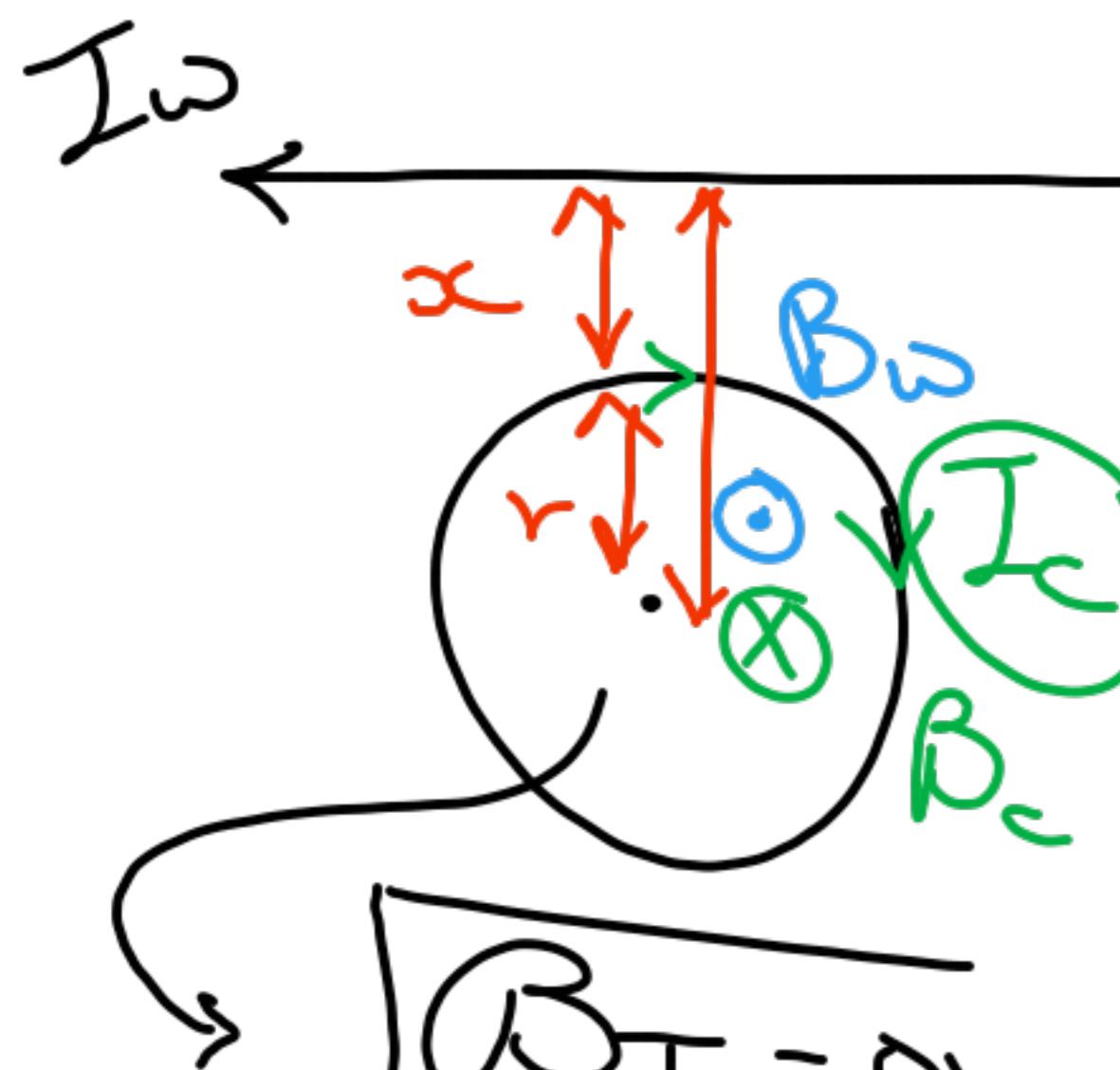
$$\beta_{ext} - \beta_c$$

$$\beta_T = \sqrt{\beta_c^2 + \beta_{ext}^2}$$



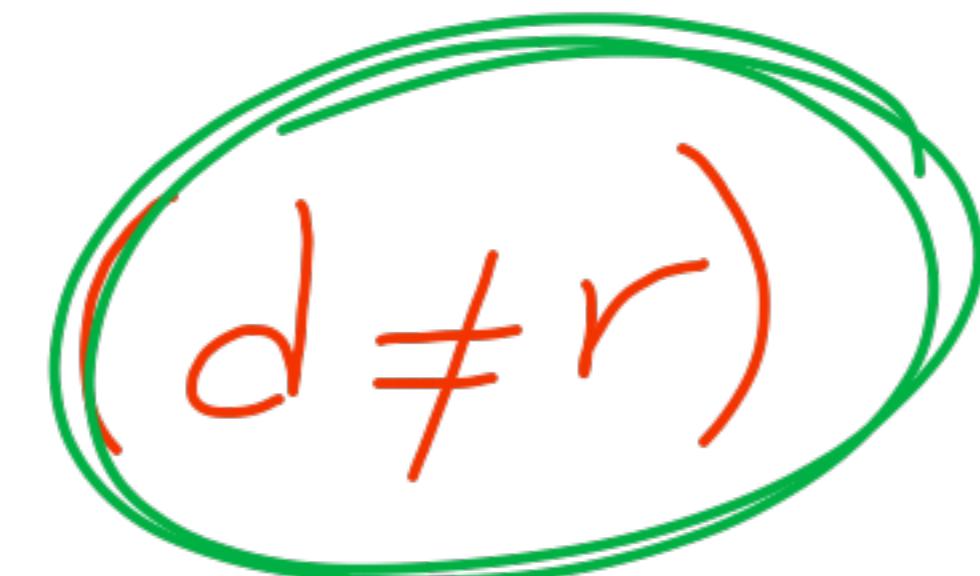
### 3 Coil + Wire

a) Not Tangent



$$\beta_c - \beta_\omega = 0$$

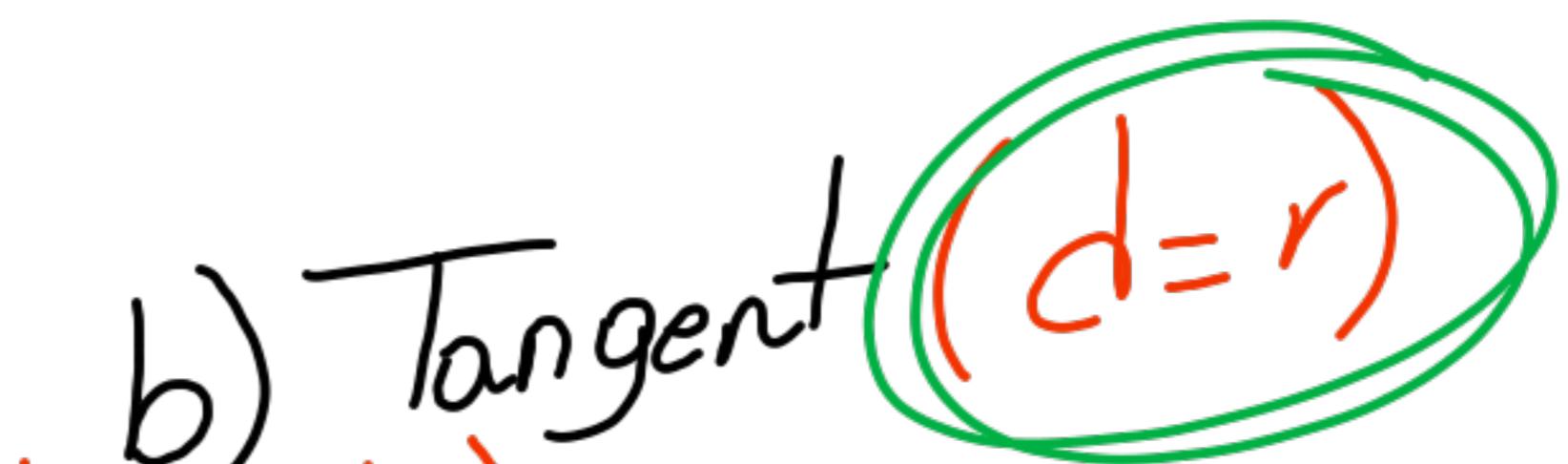
$$\beta_c = \beta_\omega$$



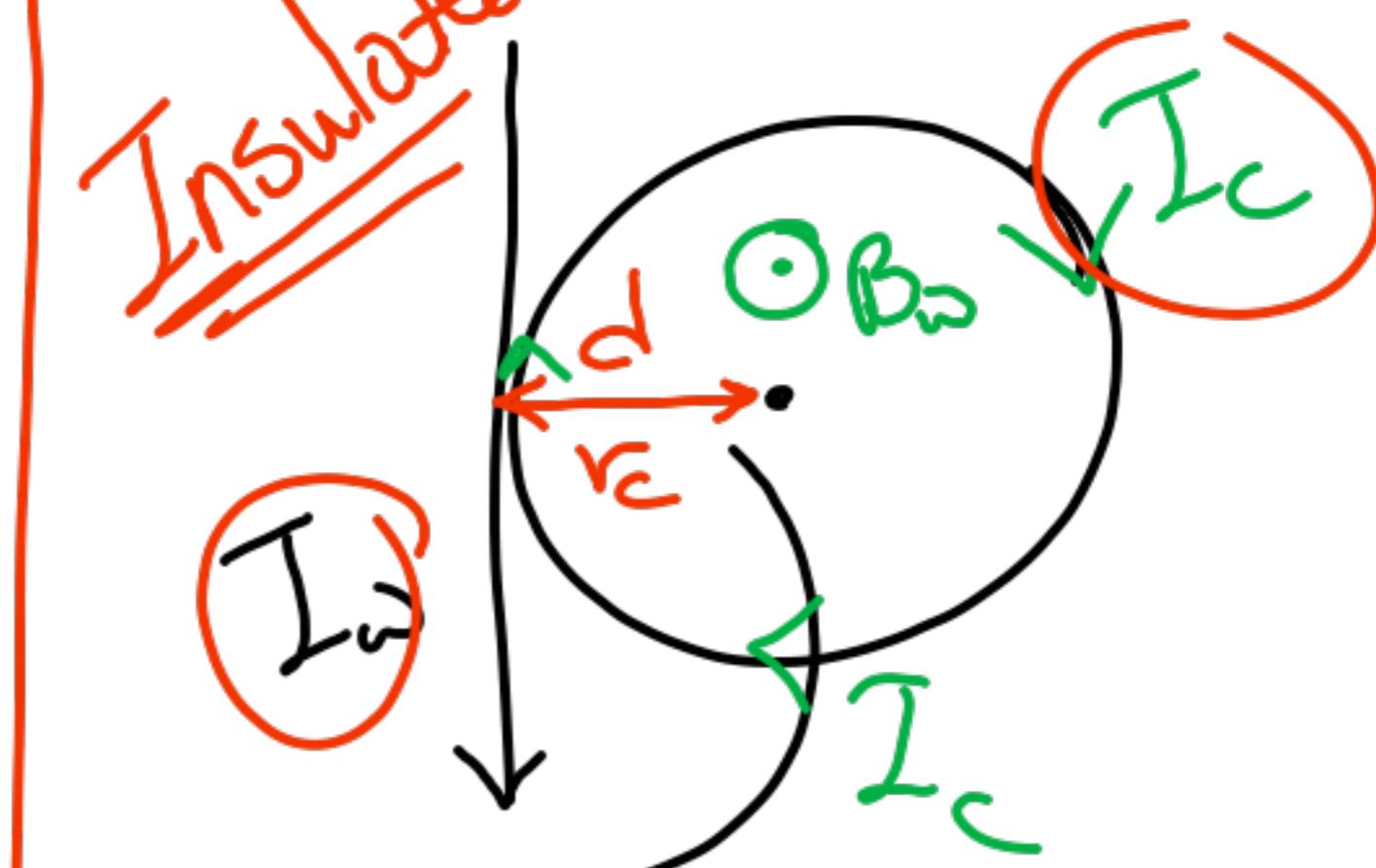
$$\frac{N_c I_c}{2r_c} = \frac{\mu I_\omega}{2\pi d}$$

$$\frac{N_c I_c}{r_c} = \frac{I_\omega}{\pi d}$$

$$*\boxed{\frac{N_c I_c}{r_c} = \frac{I_\omega}{\pi(r_c+x)}}$$



b) Tangent

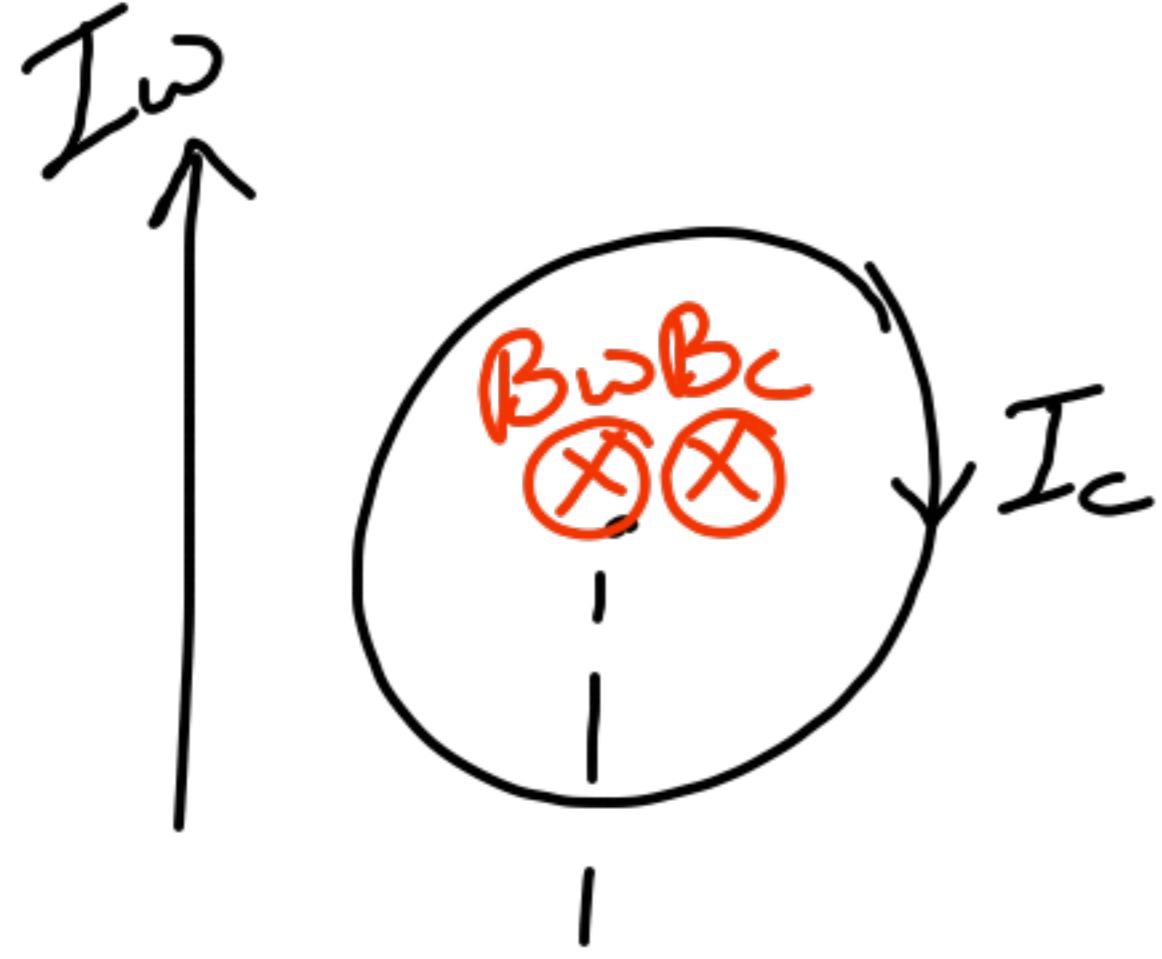


$$\beta_T = 0$$

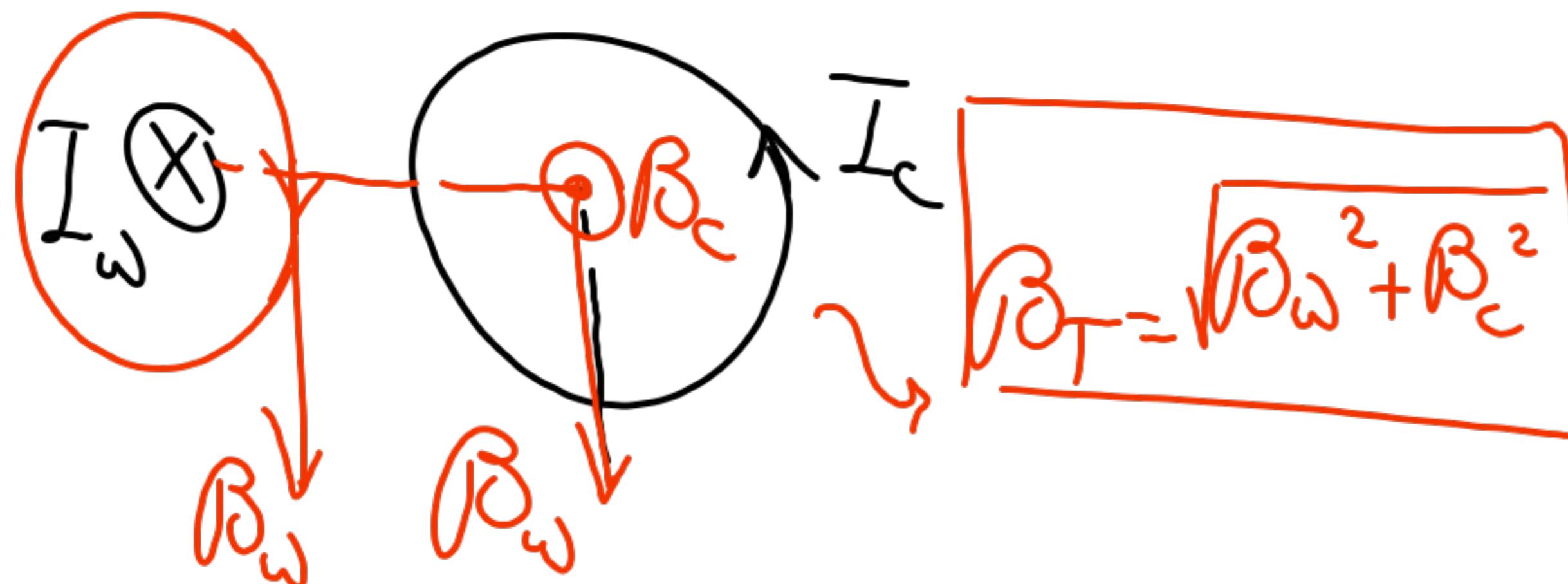
$$\beta_\omega = \beta_c$$

~~$$\frac{\mu}{2\pi} \frac{I_\omega}{d} = \frac{N_c I_c}{2r_c}$$~~

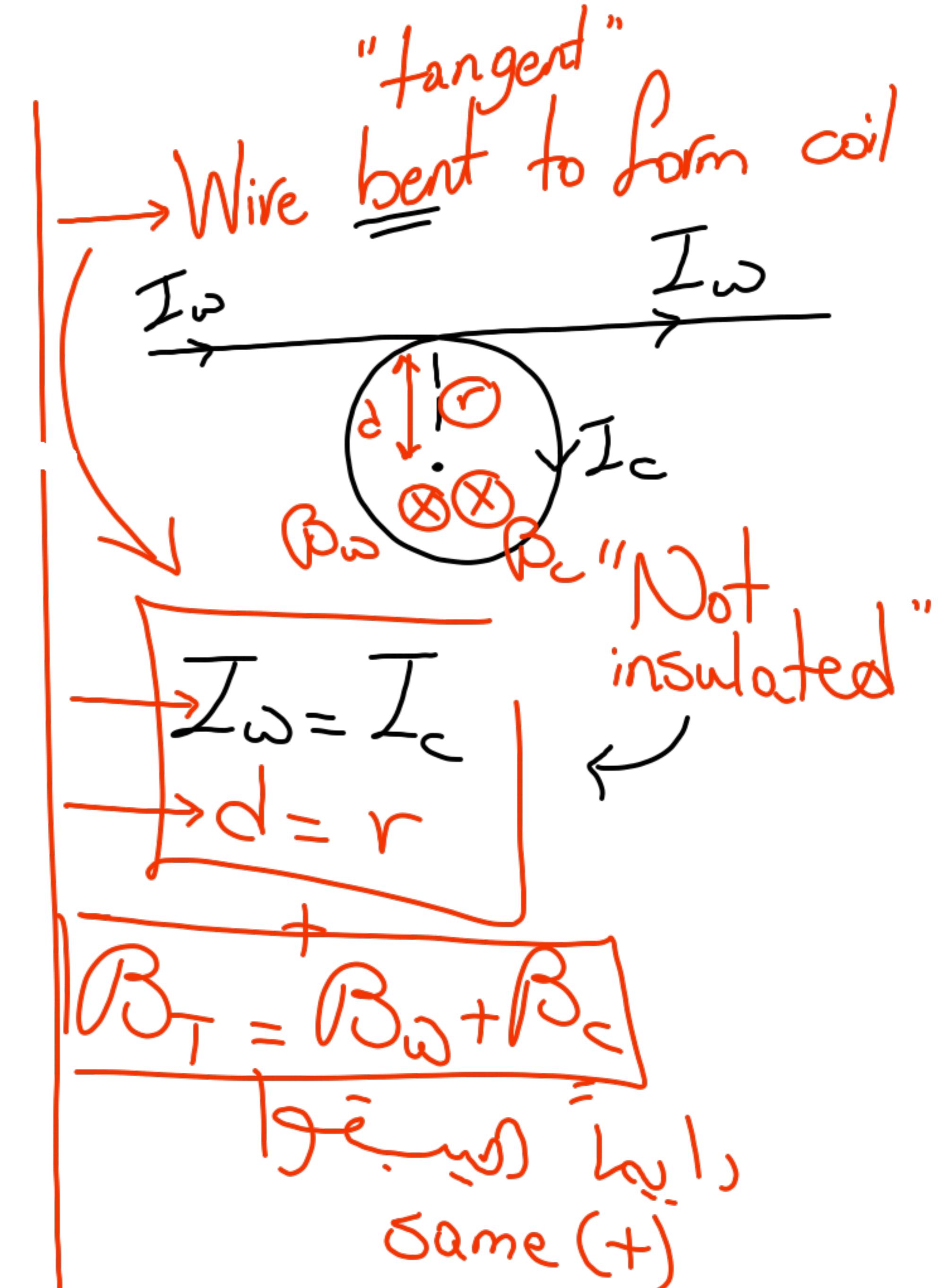
~~$$\boxed{\frac{I_\omega}{\mu} = N_c I_c}$$~~



$$\boxed{\beta_T = \beta_\omega + \beta_c}$$



$$\boxed{\beta_T = \sqrt{\beta_\omega^2 + \beta_c^2}}$$



# A Ratio

a) Coil unwound then again rewound

"Reshaped" "Recoiled"

$$\mathcal{B} = \frac{\mu_0 N I}{2r} \rightarrow \frac{\mathcal{B}_1}{\mathcal{B}_2} = \frac{N_1 I_1 r}{N_2 I_2 r_1}$$

$\therefore$  Wire,  $I$  are const.

$$\frac{\mathcal{B}_1}{\mathcal{B}_2} = \frac{N_1 r}{N_2 r_1}$$

$$\frac{\mathcal{B}_1}{\mathcal{B}_2} = \frac{N_1^2}{N_2^2}$$

$$\frac{\mathcal{B}_1}{\mathcal{B}_2} = \frac{r_2^2}{r_1^2}$$

$$N = \frac{L_{\text{wire}}}{2\pi r}$$

$$\frac{N_1}{N_2} = \frac{r_2}{r_1}$$

b) Coil turns  
 { Cut, Removed }  
 { Added, Extra wire }  
 "Keeping radius const"

$$\frac{\mathcal{B}_1}{\mathcal{B}_2} = \frac{N_1 I_1 r}{N_2 I_2 r_1}$$

$$\frac{N_1}{N_2} = \frac{I_2}{I_1}$$

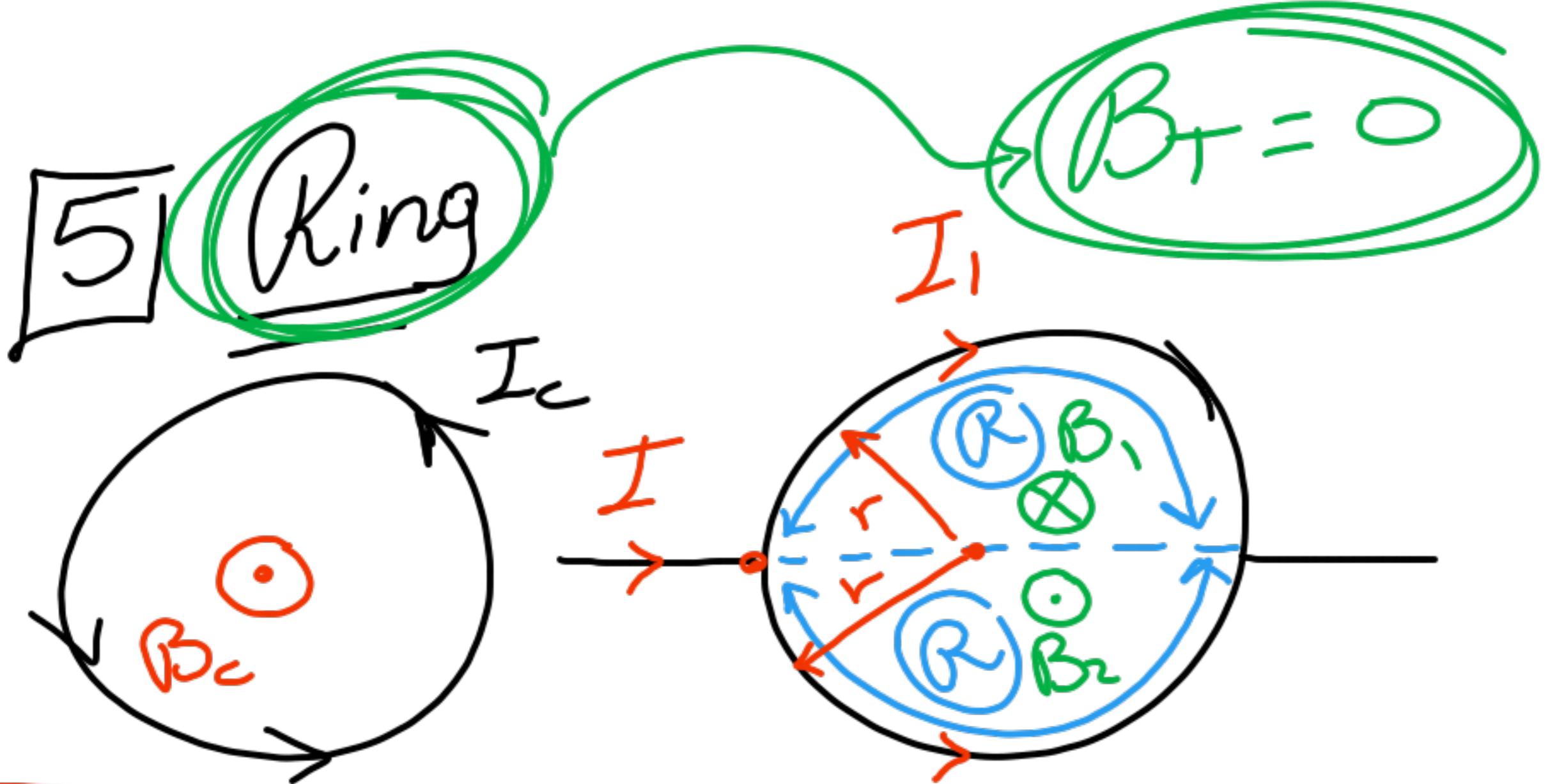
Same Battery  
 $V$  const.  $\rightarrow V = I R$

$$\frac{\mathcal{B}_1}{\mathcal{B}_2} = \frac{I_2 I_1}{I_1 I_2} = \boxed{1}$$

Unchanged

Same Current  
 $I$  const.

$$\frac{\mathcal{B}_1}{\mathcal{B}_2} = \frac{N_1}{N_2}$$



$$\boxed{B_c = \frac{\mu N I}{2r}}$$

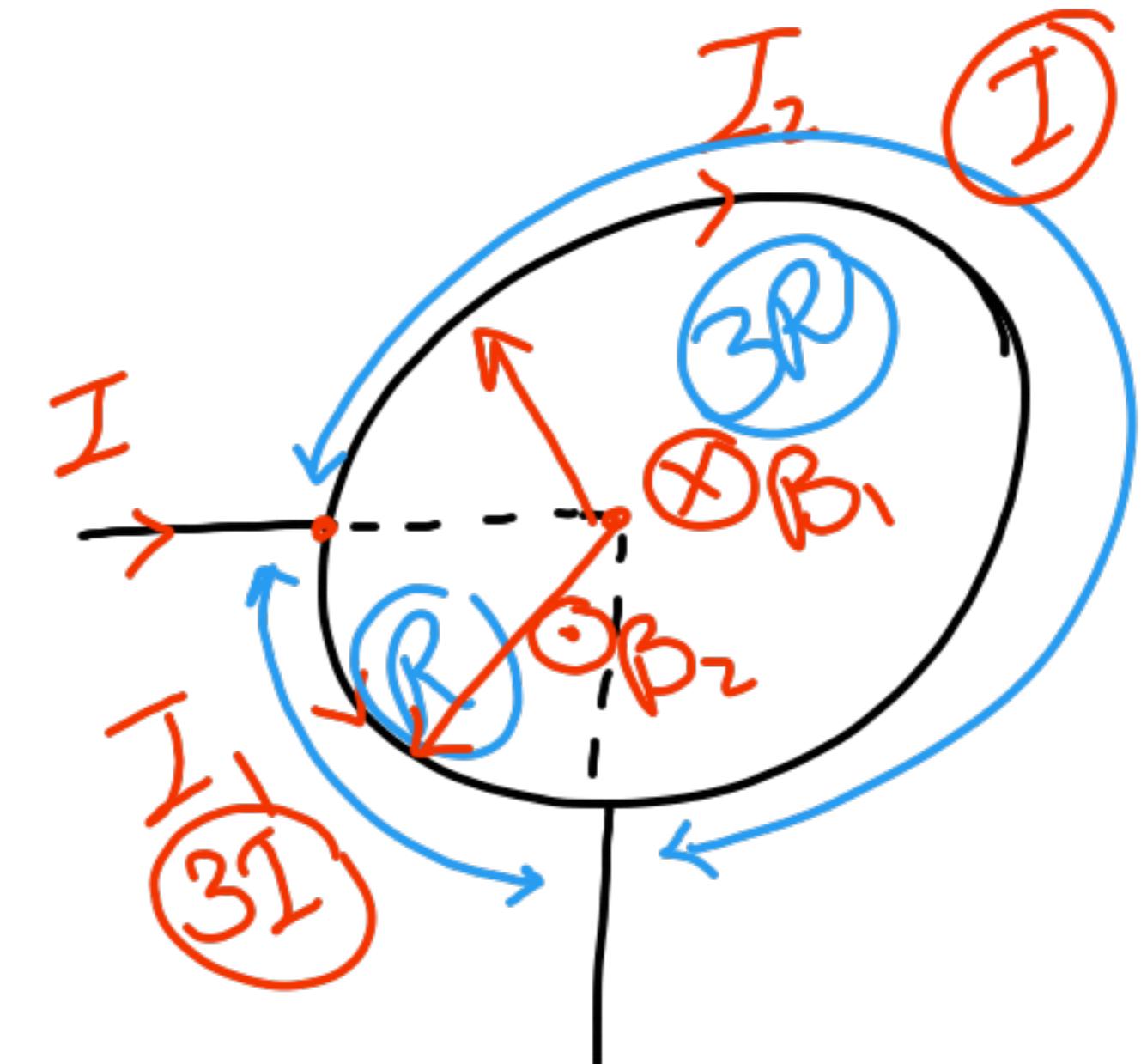
$$\begin{aligned} &I_2 \\ &\because R_1 = R_2 = R \\ &\therefore I_1 = I_2 \end{aligned}$$

$$N_1 = \frac{1}{2} \quad N_2 = \frac{1}{2}$$

$$r_1 = r_2$$

$$\therefore B_1 = B_2 \text{ "opp"}$$

$$\boxed{B_T = B_1 - B_2 = zero}$$

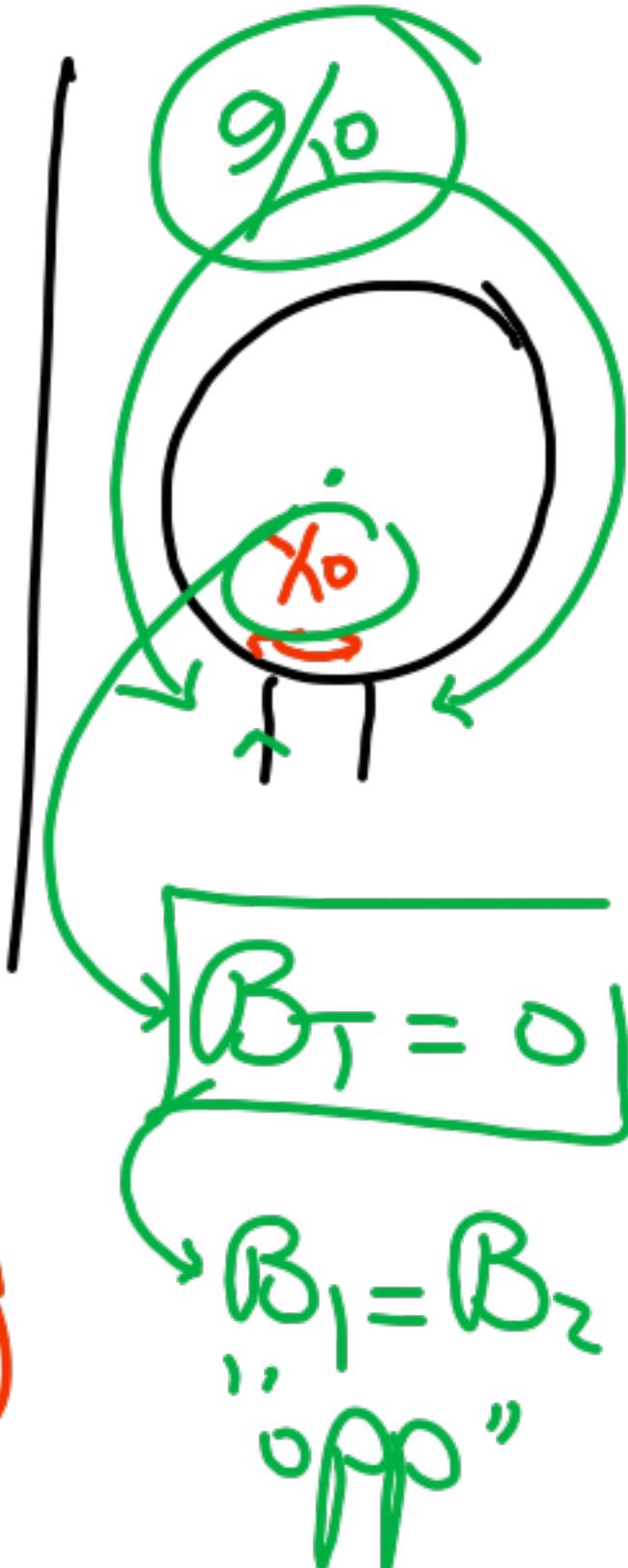


$$\begin{aligned} &N_1 = \frac{1}{4} \\ &I_1 = 3I \end{aligned}$$

$$\begin{aligned} &N_2 = \frac{3}{4} \\ &I_2 = I \end{aligned}$$

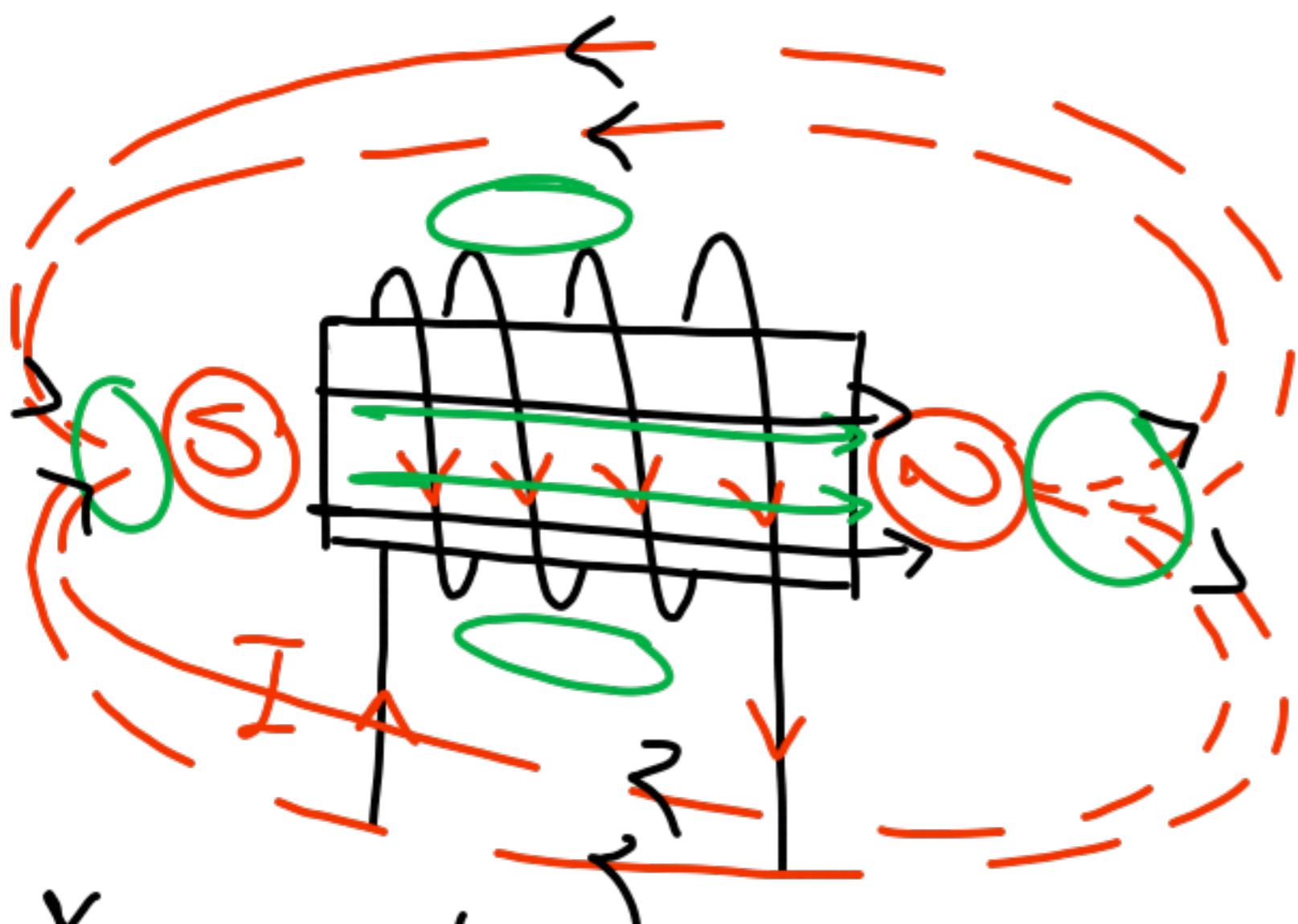
$$\begin{aligned} &r_1 = r_2 \\ &\therefore B_1 = B_2 \text{ "opp" } \end{aligned}$$

$$\boxed{\therefore B_T = 0}$$



### 3] Solenoid

#### a) Shape



\*Properties:

- 1) Bar magnet
- 2) Form closed paths
- 3) Emerges from N → S

b) Law:

$$B_S = \frac{\mu_0 N I}{L_s}$$

or

$$B_S = \mu n I$$

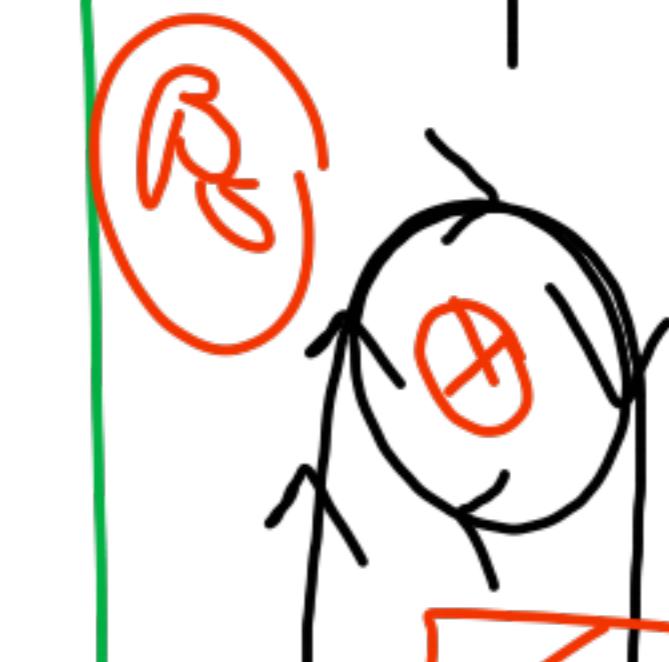
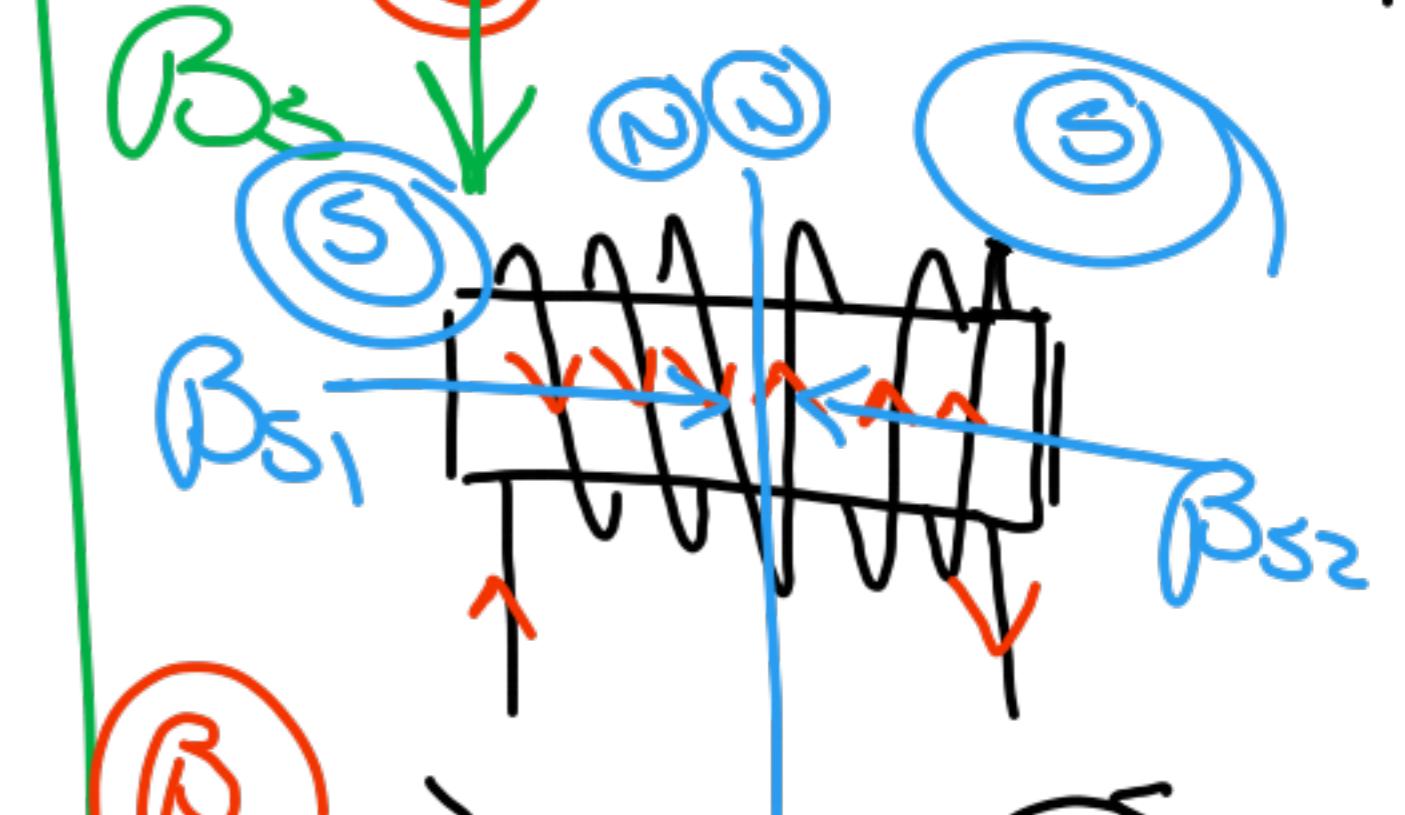
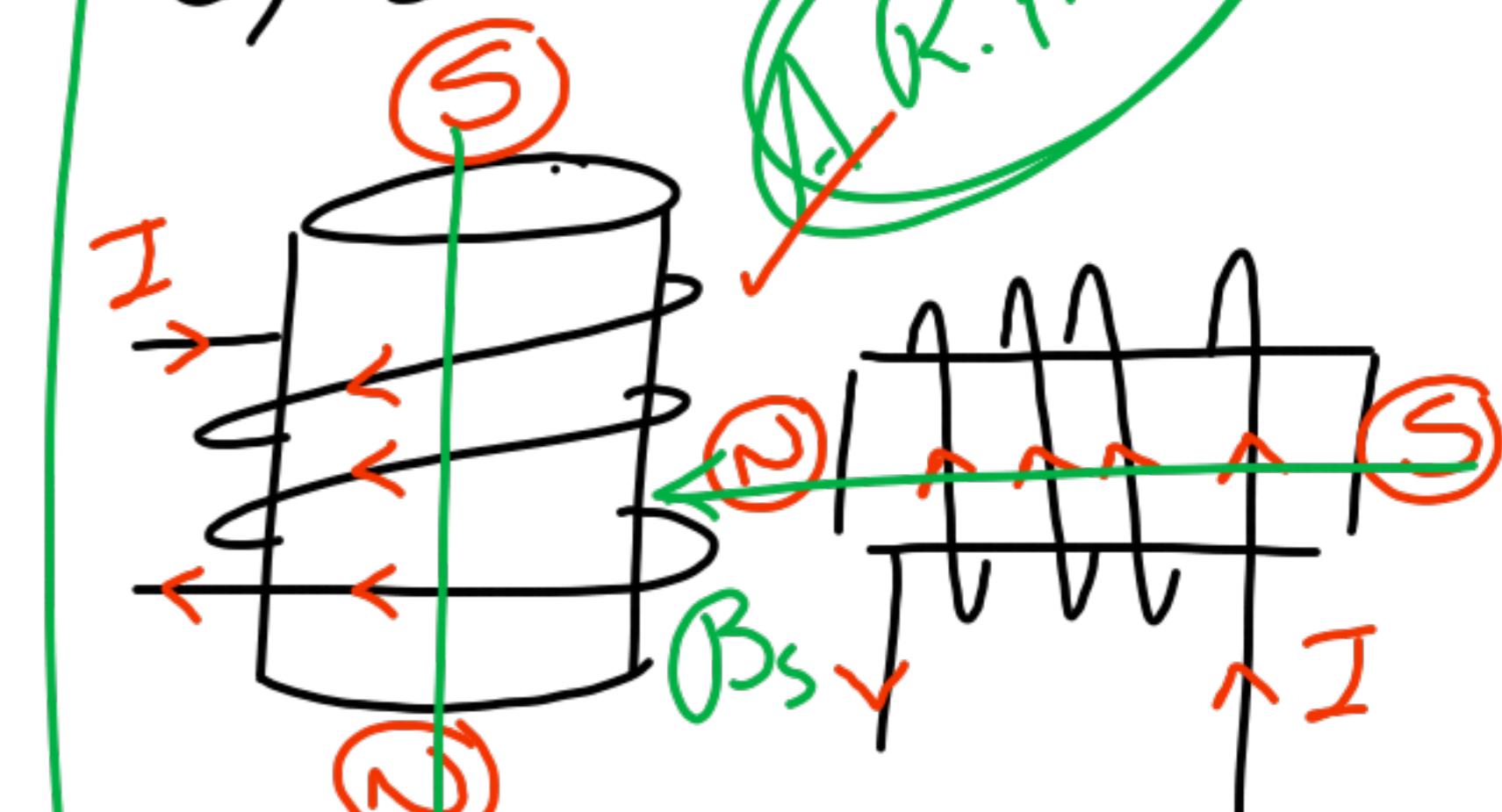
→ No. of turns per unit length

$$n = \frac{N}{L_s}$$

$$\frac{N}{\text{cm}} \xrightarrow{\times 10^{-2}} \frac{N}{\text{m}}$$

$\times 10^2$

c) Direction:

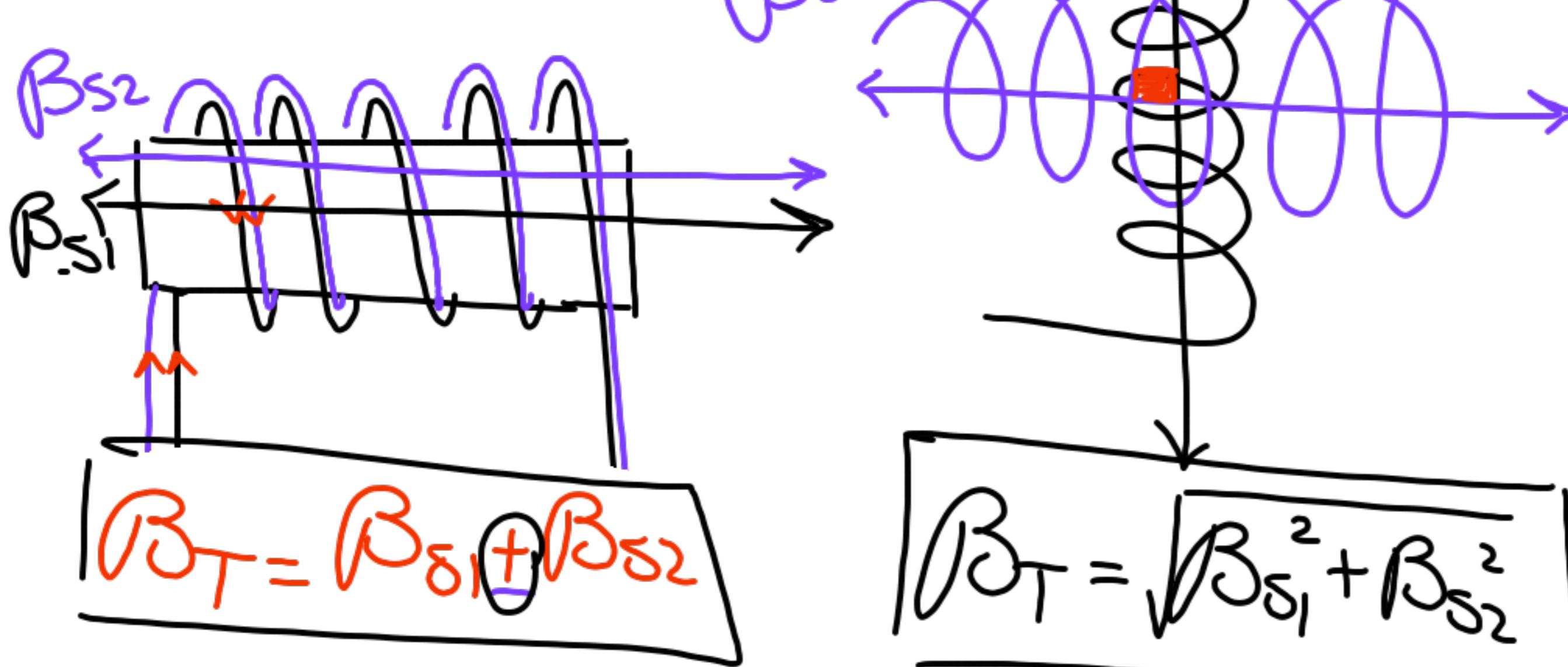


$\checkmark R.H.S.R$

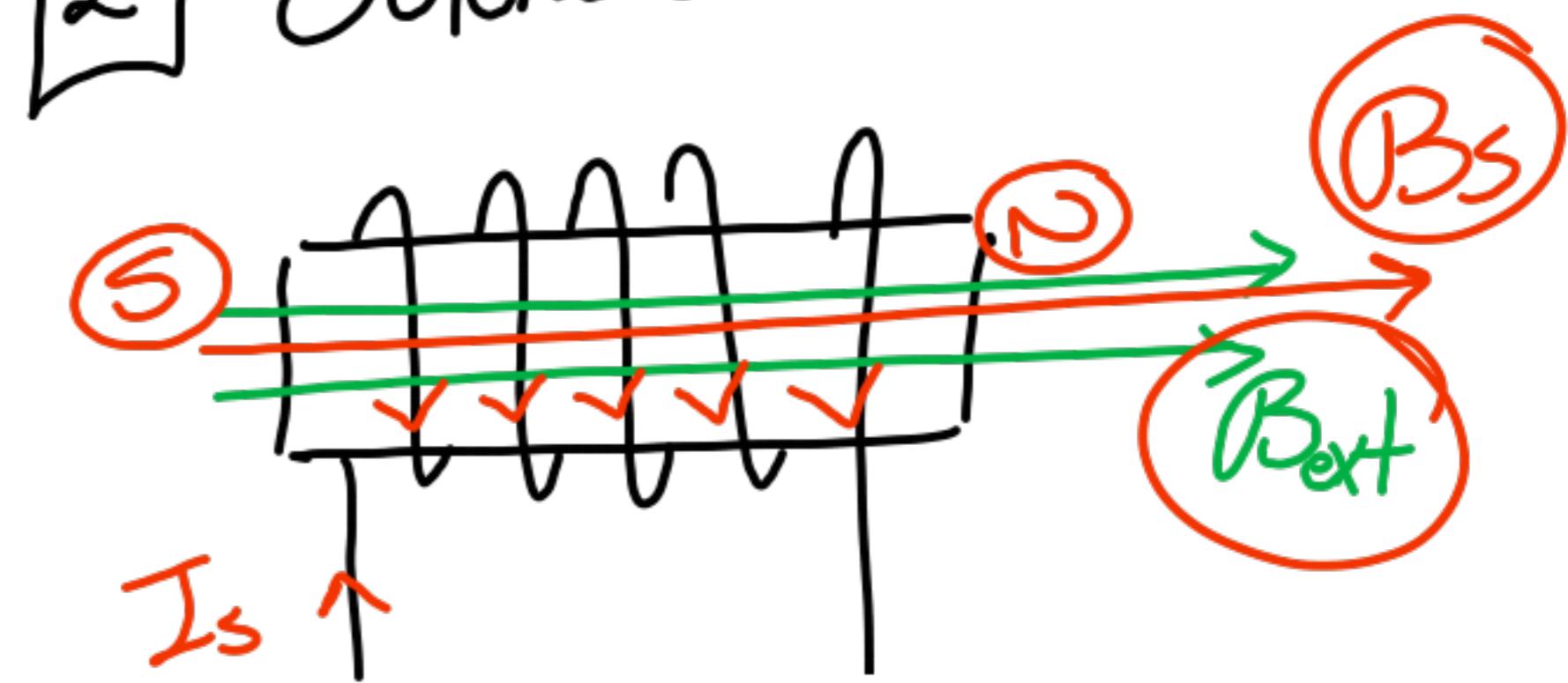
# Problems

## 1 Two Solenoids

Co-axial



## 2 Solenoid + $B_{ext}$



$$B_T = B_S + B_{ext}$$

