

# PROJECT 1 REPORT

## SMALL STANDARD CELL LIBRARY

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CSCE 337/3404 – Digital Design II  
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- ➔ Height of all the cells is 444.
- ➔ Width of the inverter cells is 28.
- ➔ Width of the NAND cells is 44.
- ➔ Width of the NOR cells is 44.
- ➔ Width of the fourth function f cells is 56.
- ➔ Width of the fourth function g cells is 56.
- ➔ Width of the fourth function h cells is 80.

# 1- Inverter Cell

## Stick Diagram

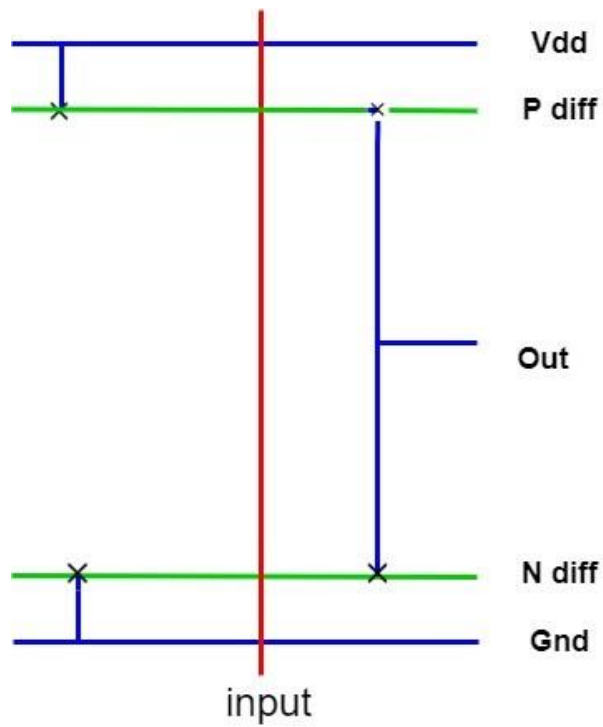


Figure 1

$$height = 32\lambda$$

## Schematic

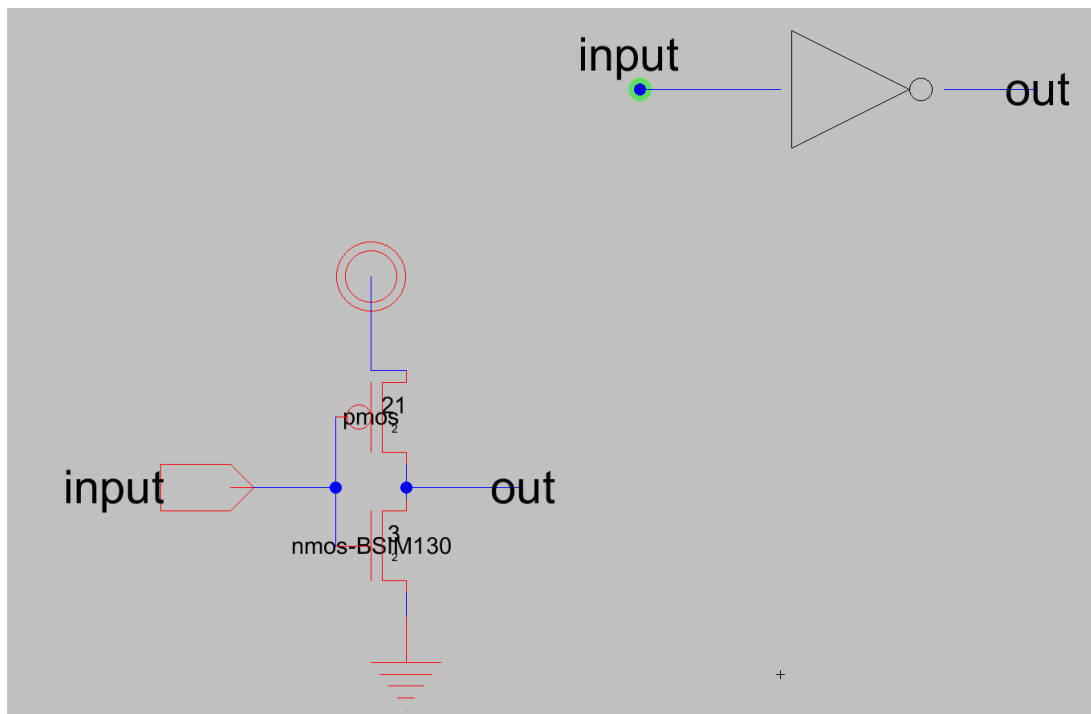


Figure 2

**Size 1:**  
**Layout**

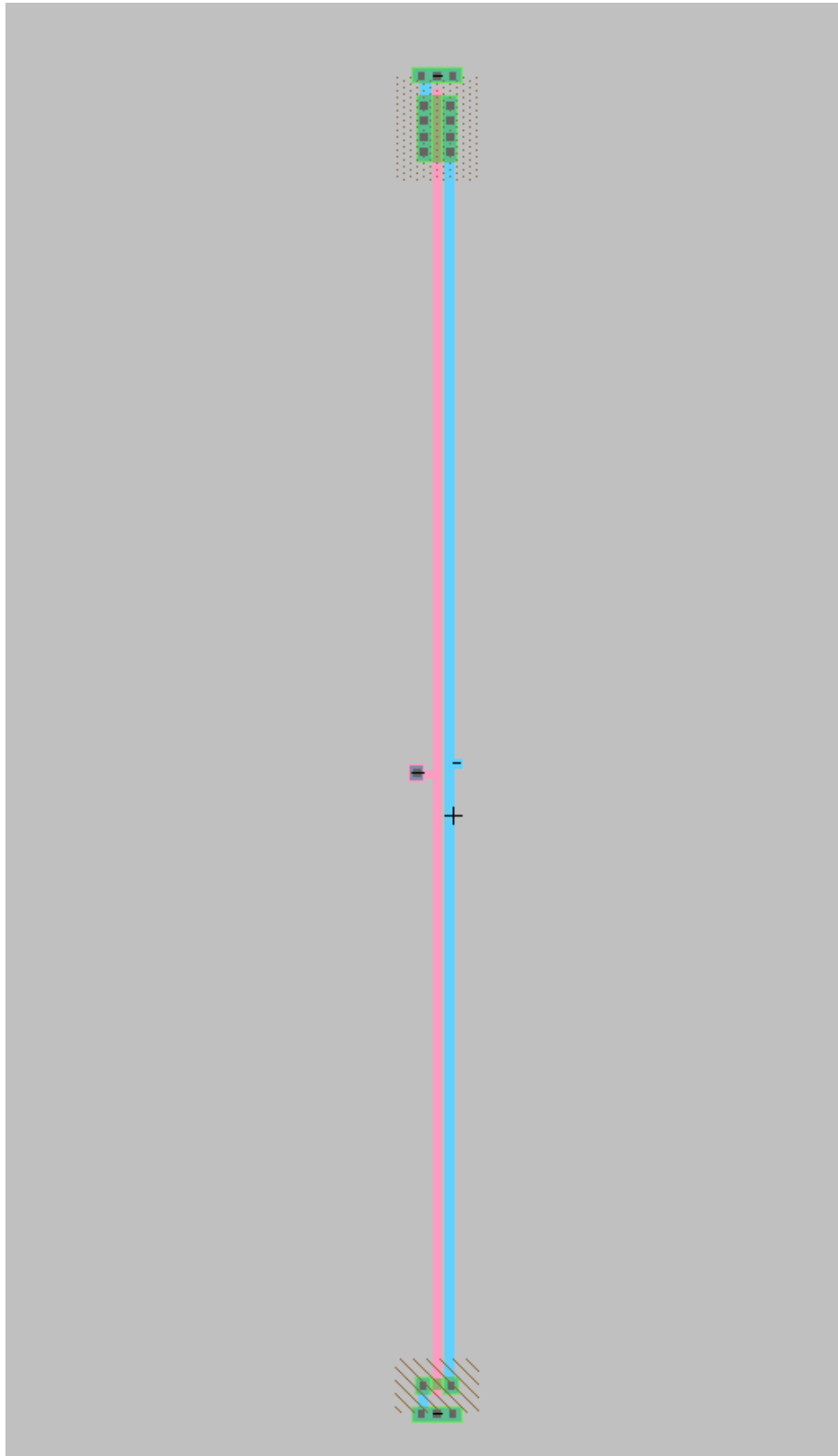


Figure 3

## Propagation Delays

**T<sub>pdf</sub>**

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	7.90555e-010	1.18018e-009	1.95818e-009	3.55311e-009
100 ps	4.45051e-010	8.6712e-010	1.67825e-009	3.31425e-009
400 ps	4.8946e-010	8.99315e-010	1.70968e-009	3.34294e-009
800 ps	5.54836e-010	9.63462e-010	1.75826e-009	3.38683e-009

**T<sub>pdr</sub>**

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	2.1553e-010	4.35801e-010	7.78736e-010	1.31496e-009
100 ps	1.53248e-010	2.87238e-010	5.63054e-010	1.0856e-009
400 ps	1.87511e-010	3.20133e-010	5.96633e-010	1.12708e-009
800 ps	2.17578e-010	3.69864e-010	6.33786e-010	1.17742e-009

## Linear Delay Model

Using  $T_{pdf}$ :

$$7.9055e-10 = k_1 \times 130 e^{-15} + 0 + k_3 \rightarrow (1)$$

$$4.8949 e-10 = k_1 \times 130 e^{-15} + k_2 \times 400 e^{-12} + k_3 \rightarrow (2)$$

$$1.75826 e-9 = k_1 \times 520 e^{-15} + k_2 \times 800 e^{-12} + k_3 \rightarrow (3)$$

$$k_1 = 4025.36$$

$$k_2 = -0.75$$

$$k_3 = 2.6725 e-10$$

$$T_{pdf} = 4025.36 \times \text{cload} - 0.75 \times \text{transition time} + 2.6725 e-10$$

Using  $T_{pdr}$ :

$$7.78736e-10 = k_1 \times 520 e^{-15} + 0 + k_3$$

$$5.63 e-10 = k_1 \times 520 e^{-15} + k_2 \times 100e^{-12} + k_3$$

$$1.87e-10 = k_1 \times 130 e^{-15} + k_2 \times 400 e^{-12} + k_3$$

$$K_1 = 1.72 e-28$$

$$K_2 = -1.2533$$

$$K_3 = 6.83 e-10$$

$$T_{pdr} = 1.72 e-28 \times \text{cload} - 1.2533 \times \text{transition time} + 6.83 e-10$$

**Size 2:  
Layout**

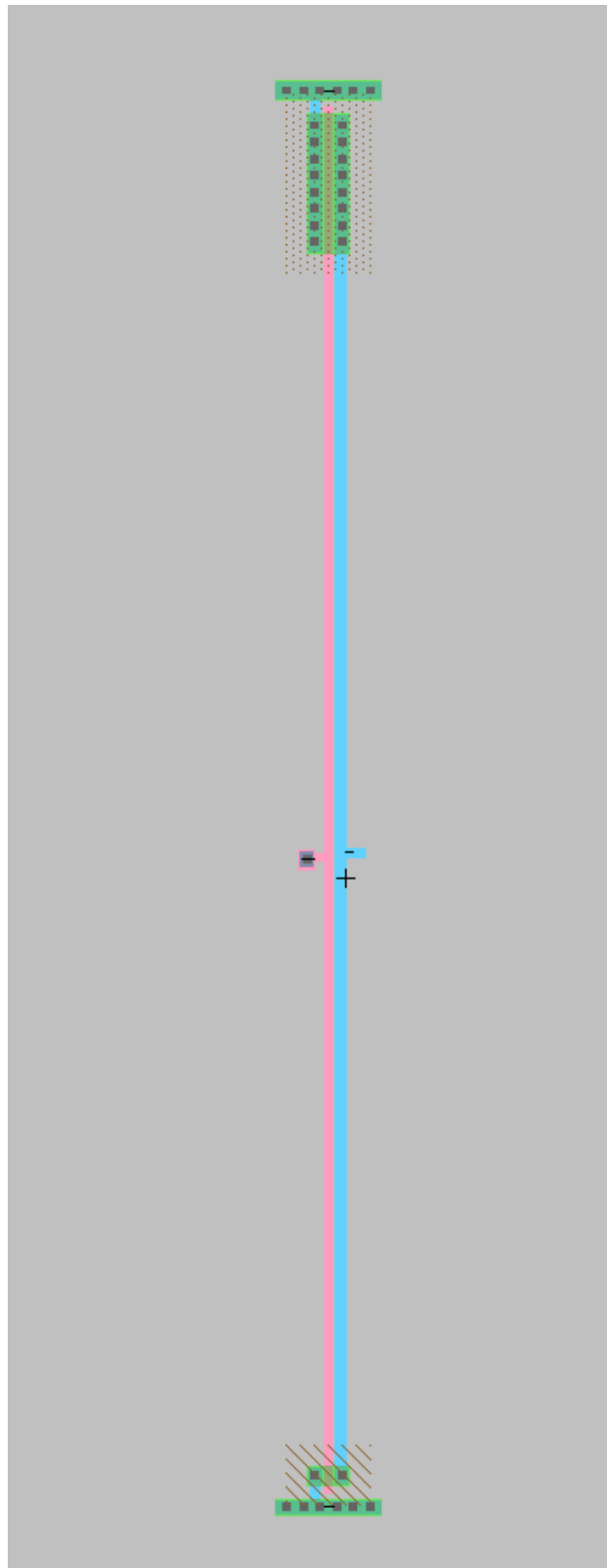


Figure 4

## Propagation Delays

**T<sub>pdf</sub>**

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	5.69191e-010	7.79735e-010	1.1636e-009	1.92831e-009
100 ps	2.35652e-010	4.38918e-010	8.53784e-010	1.64567e-009
400 ps	2.7836e-010	4.7622e-010	8.88574e-010	1.67745e-009
800 ps	3.5887e-010	3.5887e-010	9.38817e-010	1.73187e-009

**T<sub>pdr</sub>**

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	6.03102e-011	2.11266e-010	4.34727e-010	7.75821e-010
100 ps	8.40354e-011	1.51996e-010	2.88591e-010	5.62606e-010
400 ps	1.11931e-010	1.87618e-010	3.19425e-010	5.93691e-010
800 ps	1.1537e-010	1.1537e-010	3.69549e-010	6.33402e-010



## Linear Delay Model

Using Tpdf:

$$7.9055e-10 = k_1 \times 130 \text{ e }^{-15} + 0 + k_3 \rightarrow (1)$$

$$4.8949 \text{ e }^{-10} = k_1 \times 130 \text{ e }^{-15} + k_2 \times 400 \text{ e }^{-12} + k_3 \rightarrow (2)$$

$$1.75826 \text{ e }^{-9} = k_1 \times 520 \text{ e }^{-15} + k_2 \times 800 \text{ e }^{-12} + k_3 \rightarrow (3)$$

$$k_1 = 4025.36$$

$$k_2 = -0.75$$

$$k_3 = 2.6725 \text{ e }^{-10}$$

$$T_{pdf} = 4025.36 \times \text{cload} - 0.75 \times \text{transition time} + 2.6725 \text{ e }^{-10}$$

Using Tpdr:

$$7.78736e-10 = k_1 \times 520 \text{ e }^{-15} + 0 + k_3$$

$$5.63 \text{ e }^{-10} = k_1 \times 520 \text{ e }^{-15} + k_2 \times 100e-12 + k_3$$

$$1.87e-10 = k_1 \times 130 \text{ e }^{-15} + k_2 \times 400 \text{ e }^{-12} + k_3$$

$$K_1 = 1.72 \text{ e }^{-28}$$

$$K_2 = -1.2533$$

$$K_3 = 6.83 \text{ e }^{-10}$$

$$T_{pdr} = 1.72 \text{ e }^{-28} \times \text{cload} - 1.2533 \times \text{transition time} + 6.83 \text{ e }^{-10}$$

**Size 4:  
Layout**

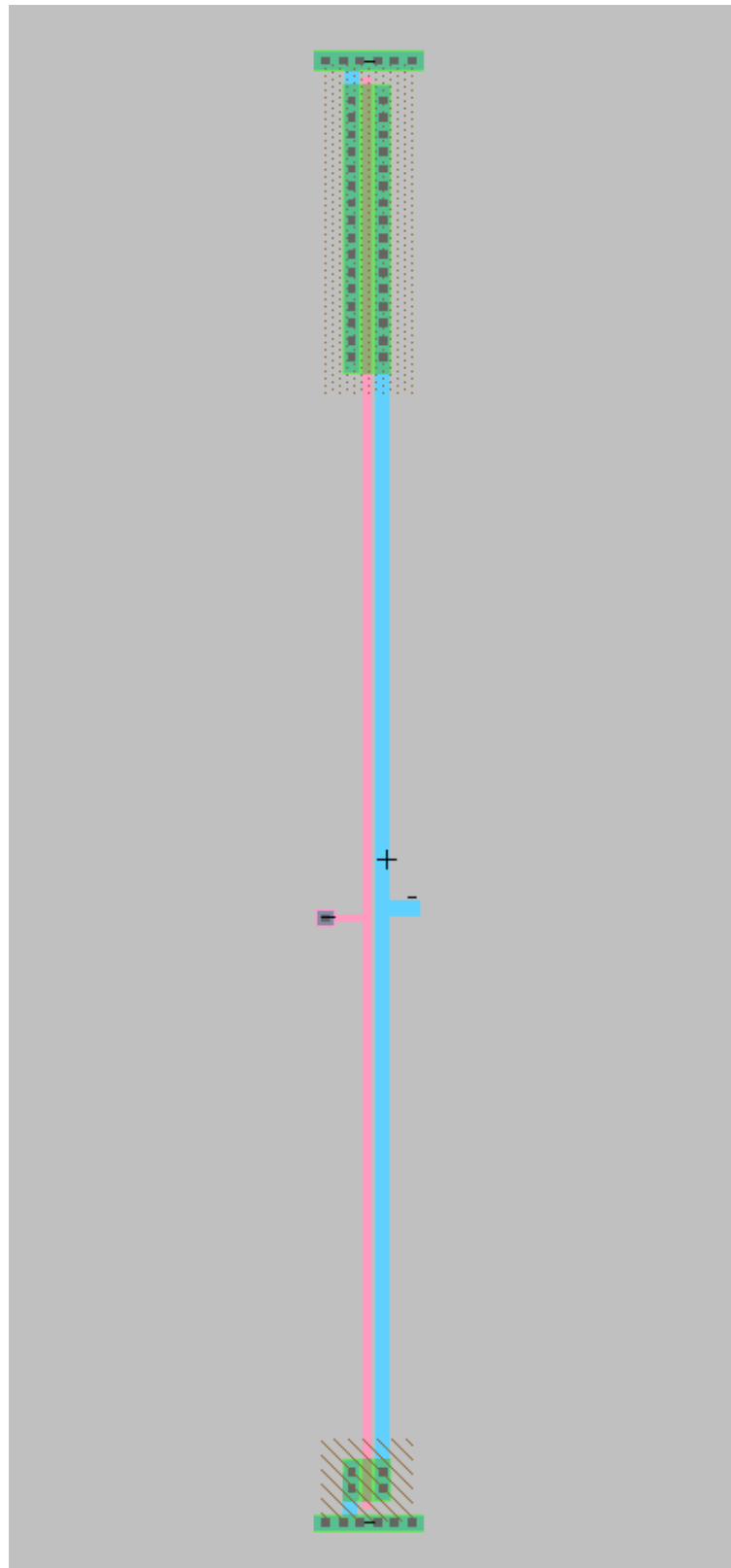


Figure 5

## Propagation Delays

$T_{pdf}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	7.81008e-010	4.47151e-010	5.71686e-010	1.14031e-009
100 ps	1.28271e-010	2.29438e-010	4.33323e-010	8.41132e-010
400 ps	1.84811e-010	2.77074e-010	4.73283e-010	8.81281e-010
800 ps	2.56536e-010	3.5693e-010	5.43175e-010	9.33578e-010

$T_{pdr}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	2.1573e-010	3.6865e-011	6.36e-011	4.37739e-010
100 ps	5.05777e-011	8.37669e-011	1.51297e-010	2.87851e-010
400 ps	6.12656e-011	1.11064e-010	1.86916e-010	3.18027e-010
800 ps	4.61733e-011	1.15452e-010	2.16436e-010	3.69303e-010

## Linear Delay Model

### Using Tpdf

$$7.81e-10 = 130 e-15 \times k_1 + 0 + k_3$$

$$4.33e-10 = 520 e-15 + 100e-12 \times k_2 + k_3$$

$$1.848e-10 = 130 e-15 k_1 + 400e-12 k_2 + k_3$$

$$K_1 = -510$$

$$K_2 = -1.4905$$

$$k_3 = 8.47e-10$$

$$T_{pdf} = -510 \times \text{cload} - 1.4905 \times \text{transition time} + 8.47e-10$$

### Using Tpdr

$$2.157e-10 = 130 e-15 k_1 + 0 + k_3$$

$$5.057 e-11 = 130e-15 k_1 + 100e-12 \times k_2 + k_3$$

$$8.376e-11 = 260e-15 k_1 + 100e-12 \times k_2 + k_3$$

$$K_1 = 254.85$$

$$K_2 = -1.6513$$

$$k_3 = 1.8257e-10$$

$$T_{pdr} = 254.85 \times \text{cload} - 1.6513 \times \text{transition time} + 1.8257e-10$$

**Size 8:  
Layout**

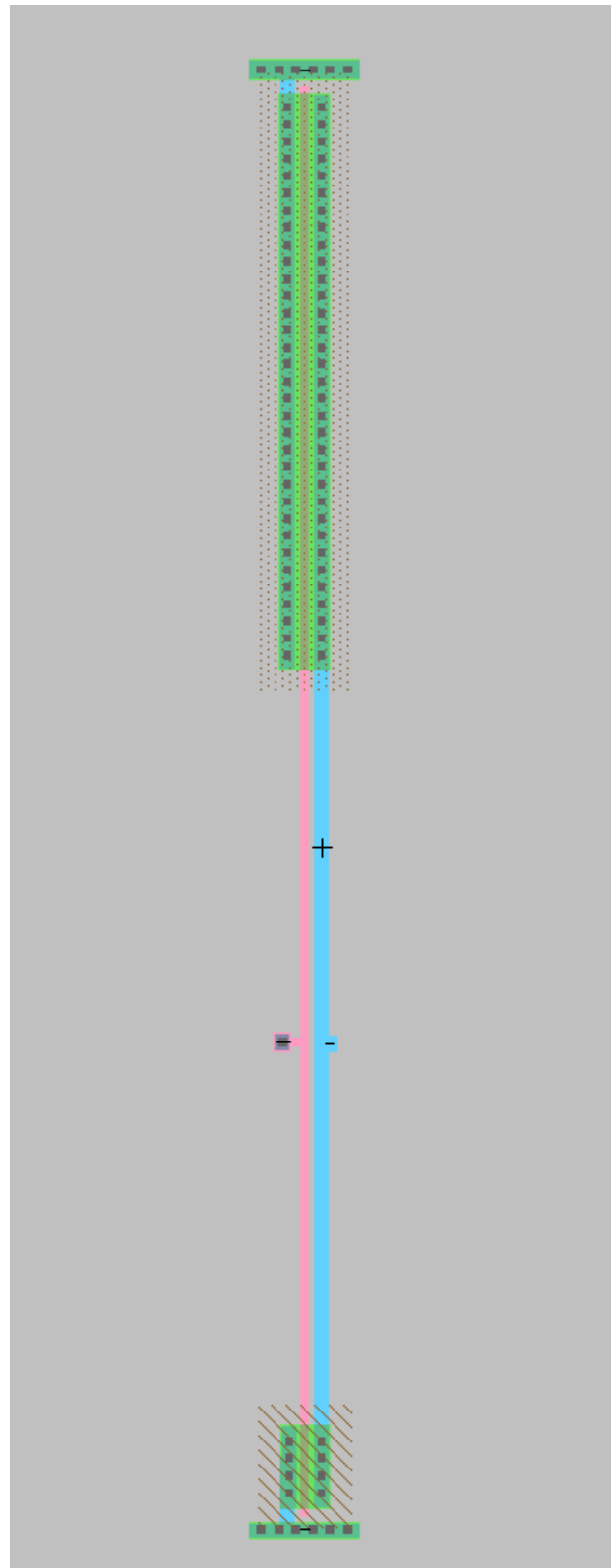


Figure 6

## Propagation Delays

$T_{pdf}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	3.77419e-010	4.52759e-010	5.72087e-010	7.84015e-010
100 ps	7.83796e-011	1.27649e-010	2.31712e-010	4.30783e-010
400 ps	1.34458e-010	1.84163e-010	2.76305e-010	4.70603e-010
800 ps	2.00911e-010	2.57082e-010	3.57556e-010	5.41174e-010

$T_{pdr}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	1.04624e-010	3.73203e-011	6.30392e-011	2.15752e-010
100 ps	3.20593e-011	5.08357e-011	8.29229e-011	1.49394e-010
400 ps	2.74952e-011	6.14081e-011	1.11326e-010	1.86892e-010
800 ps	2.4333e-012	4.6723e-011	1.15879e-010	2.17464e-010

## Linear Delay Model

### Using Tpdf

$$7.84e-10 = 1040e-15 k_1 + 0 + k_3$$

$$4.308e-10 = 1040e-15 k_1 + 100e-12 k_2 + k_3$$

$$1.345e-10 = 130e-15 k_1 + 400e-12 k_2 + k_3$$

$$K_1 = -838.79$$

$$K_2 = -3.532$$

$$K_3 = 1.65e-9$$

$$T_{pdf} = -838.79 \times \text{cload} - 3.532 \times \text{transition time} + 1.65e-9$$

### Using Tpdr

$$6.30e-11 = 520e-15 k_1 + 0 + k_3$$

$$3.205e-11 = 130e-15 k_1 + 100e-12 k_2 + k_3$$

$$1.158e-10 = 520e-15 k_1 + 800e-12 k_2 + k_3$$

$$K_1 = 96.282$$

$$K_2 = 0.066$$

$$K_3 = 1.2933e-11$$

$$T_{pdr} = 96.282 \times \text{cload} + 0.066 \times \text{transition time} + 1.2933e-11$$

## 2- 3 Input NAND Gate

### Stick Diagram

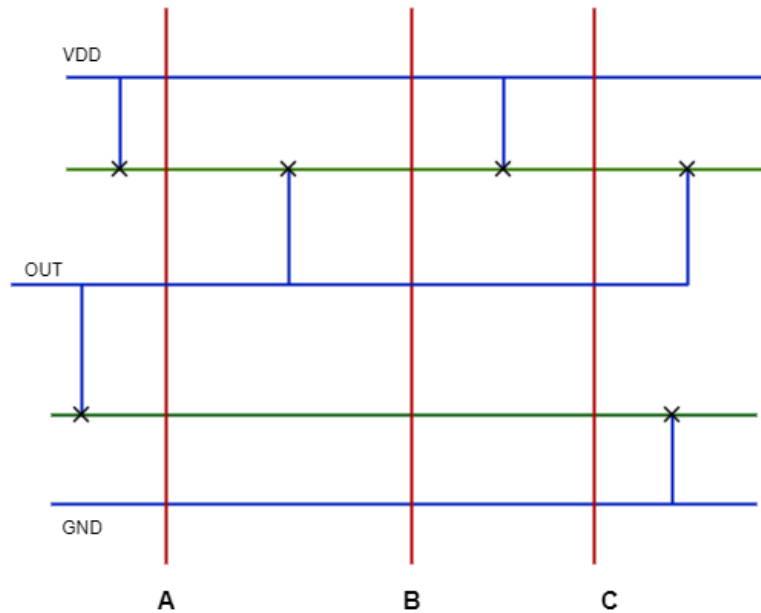


Figure 7

$$height = 40\lambda$$

### Schematic

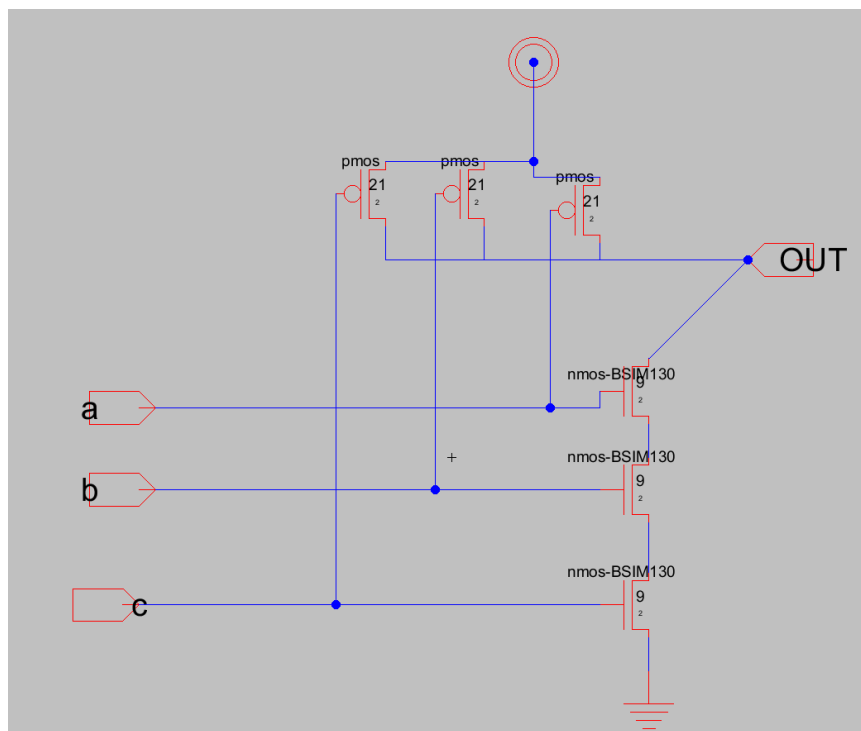


Figure 8



**Size 1:**  
**Layout**

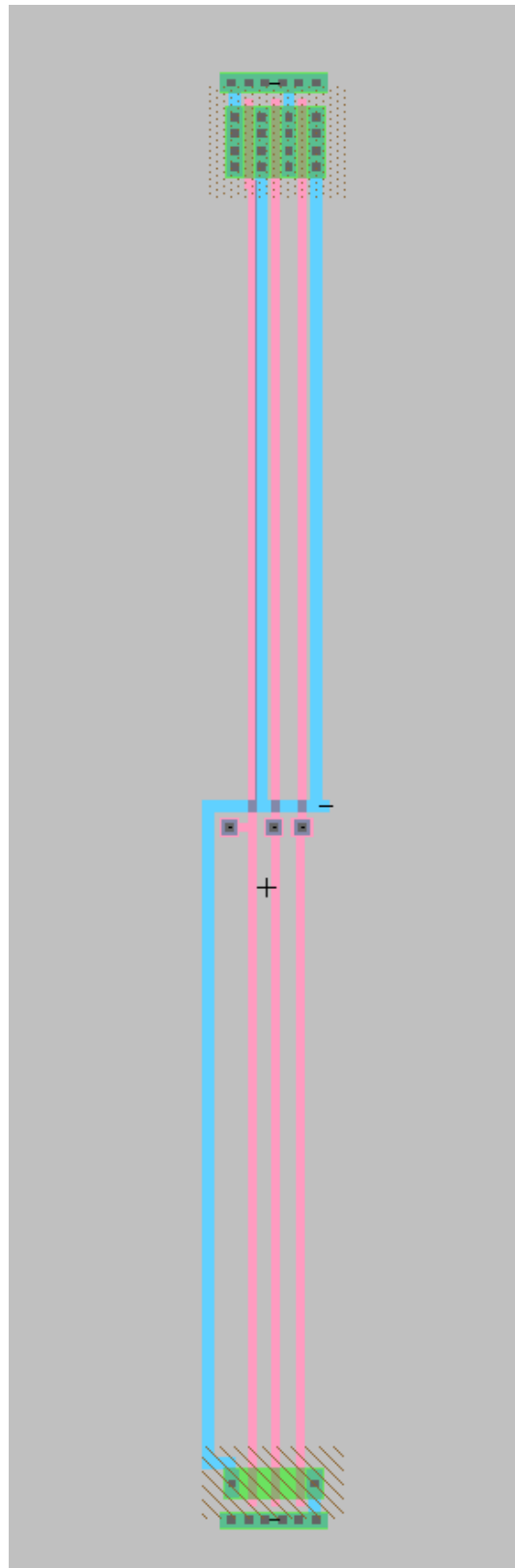


Figure 9

## Propagation Delays

$T_{pdf}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	5.59236e-010	8.42258e-010	1.36011e-009	2.40105e-009
100 ps	3.06382e-010	5.79815e-010	1.13432e-009	2.1963e-009
400 ps	3.4095e-010	6.12033e-010	1.16015e-009	2.21948e-009
800 ps	3.96229e-010	6.63049e-010	1.20673e-009	2.25347e-009

$T_{pdr}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	2.78928e-010	4.84481e-010	8.06024e-010	1.33432e-009
100 ps	1.58218e-010	2.95292e-010	5.73163e-010	1.0996e-009
400 ps	1.96144e-010	3.26242e-010	6.04355e-010	1.13415e-009
800 ps	2.37571e-010	3.82808e-010	6.4414e-010	1.18362e-009

## Linear Delay Model

### Using Tpdf

$$3.06382e-010 = (K1 * 130e-15) + (K2 * 100e-12) + K3$$

$$8.42258e-010 = (K1 * 260e-15) + (K2 * 0e-12) + k3$$

$$2.21948e-009 = (K1 * 1040e-15) + (K2 * 400e-12) + K3$$

$$K1 = 2708.250769$$

$$K2 = -1.838034$$

$$K3 = 1.381128e-10$$

$$T_{pdf} = 2708.250769x \text{ cload} - 1.838034x \text{ transition time} + 1.381128e-10$$

### Using Tpdr

$$1.58218e-010 = (K1 * 130e-15) + (K2 * 100e-12) + K3$$

$$4.84481e-010 = (K1 * 260e-15) + (K2 * 0e-12) + k3$$

$$6.4414e-010 = (K1 * 520e-15) + (K2 * 800e-12) + K3$$

$$K1 = 2130.586923$$

$$K2 = -0.492867$$

$$K3 = -6.94e-11$$

$$T_{pdr} = 2130.586923x \text{ cload} - 0.492867x \text{ transition time} - 6.94e-11$$

**Size 2:**  
**Layout**

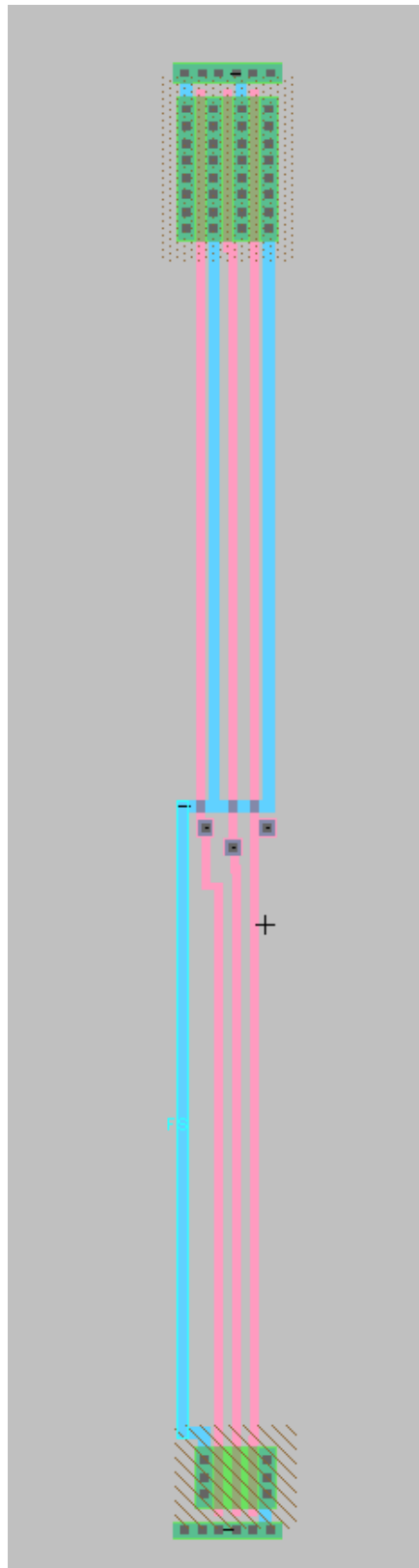


Figure 10

## Propagation Delays

$T_{pdf}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	4.05606e-010	5.57361e-010	8.36313e-010	1.35318e-009
100 ps	1.66418e-010	3.03877e-010	5.78831e-010	1.12502e-009
400 ps	2.04194e-010	3.34308e-010	6.2306e-010	1.15679e-009
800 ps	2.65308e-010	3.92035e-010	6.54074e-010	1.20058e-009

$T_{pdr}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	1.43759e-010	2.77855e-010	4.81907e-010	8.04252e-010
100 ps	8.90937e-011	1.57185e-010	2.93437e-010	5.64261e-010
400 ps	1.23224e-010	1.94862e-010	3.27382e-010	6.00192e-010
800 ps	1.41745e-010	2.35985e-010	3.80932e-010	6.43283e-010

## Linear Delay Model

### Using Tpdf

$$4.05606e-010 = (K1 * 130e-15) + (K2 * 0e-12) + K3$$

$$6.2306e-010 = (K1 * 520e-15) + (K2 * 400e-12) + k3$$

$$1.20058e-009 = (K1 * 1040e-15) + (K2 * 800e-12) + K3$$

$$K1 = 2769.738462$$

$$K2 = -2.15686$$

$$K3 = 4.554e-11$$

$$T_{pdf} = 2769.738462 \times \text{cload} - 2.15686 \times \text{transition time} + 4.554e-11$$

### Using Tpdr

$$8.90937e-011 = (K1 * 130e-15) + (K2 * 100e-12) + K3$$

$$2.77855e-010 = (K1 * 260e-15) + (K2 * 0e-12) + k3$$

$$6.43283e-010 = (K1 * 1040e-15) + (K2 * 800e-12) + K3$$

$$K1 = 998.50$$

$$K2 = -0.5071917$$

$$K3 = 1.824454e-11$$

$$T_{pdr} = 998.50 \times \text{cload} - 0.5071917 \times \text{transition time} + 1.824454e-11$$

**Size 4:**  
**Layout**

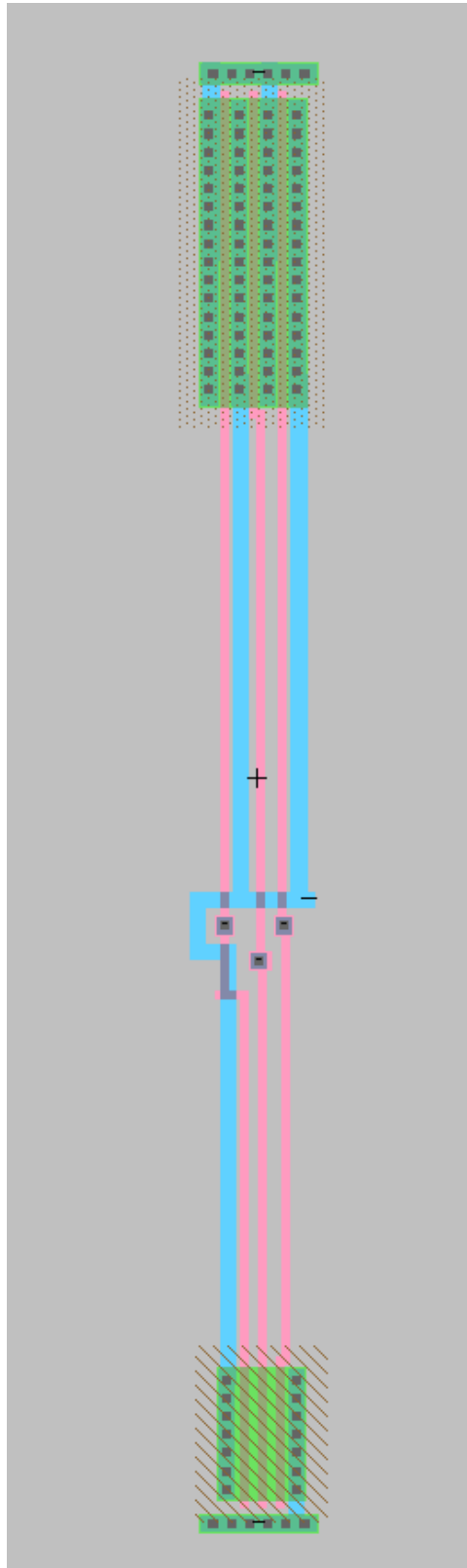


Figure 10

## Propagation Delays

$T_{pdf}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	3.11205e-010	4.07218e-010	5.60634e-010	8.40987e-010
100 ps	9.73306e-011	1.65932e-010	3.03166e-010	5.77622e-010
400 ps	1.39831e-010	2.04946e-010	3.33642e-010	6.06386e-010
800 ps	1.88202e-010	2.65252e-010	3.9457e-010	6.50933e-010

$T_{pdr}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	5.77559e-011	1.98386e-010	2.73082e-010	4.87287e-010
100 ps	5.52297e-011	1.14182e-010	1.56163e-010	2.96364e-010
400 ps	7.70874e-011	1.222669e-10	1.95071e-010	3.25065e-010
800 ps	8.1296e-011	1.41289e-010	2.35328e-010	3.8088e-010



## Linear Delay Model

### Using Tpdf

$$9.73306e-011 = (K1 * 130e-15) + (K2 * 100e-12) + K3$$

$$4.07218e-010 = (K1 * 520e-15) + (K2 * 0e-12) + k3$$

$$6.50933e-010 = (K1 * 1040e-15) + (K2 * 800e-12) + K3$$

$$K1 = 748.0258791$$

$$K2 = -0.181573$$

$$K3 = 1.824454286e-11$$

$$T_{pdf} = 748.0258791 \times \text{cload} - 0.181573 \times \text{transition time} + 1.824454286e-11$$

### Using Tpdr

$$5.52297e-011 = (K1 * 130e-15) + (K2 * 100e-12) + K3$$

$$1.98386e-010 = (K1 * 260e-15) + (K2 * 0e-12) + k3$$

$$3.8088e-010 = (K1 * 1040e-15) + (K2 * 800e-12) + K3$$

$$K1 = 729.52989$$

$$K2 = -0.483174$$

$$K3 = 8.708228e-12$$

$$T_{pdr} = 729.52989 \times \text{cload} - 0.483174 \times \text{transition time} + 8.708228e-12$$

### 3- Input NOR Gate Stick Diagram

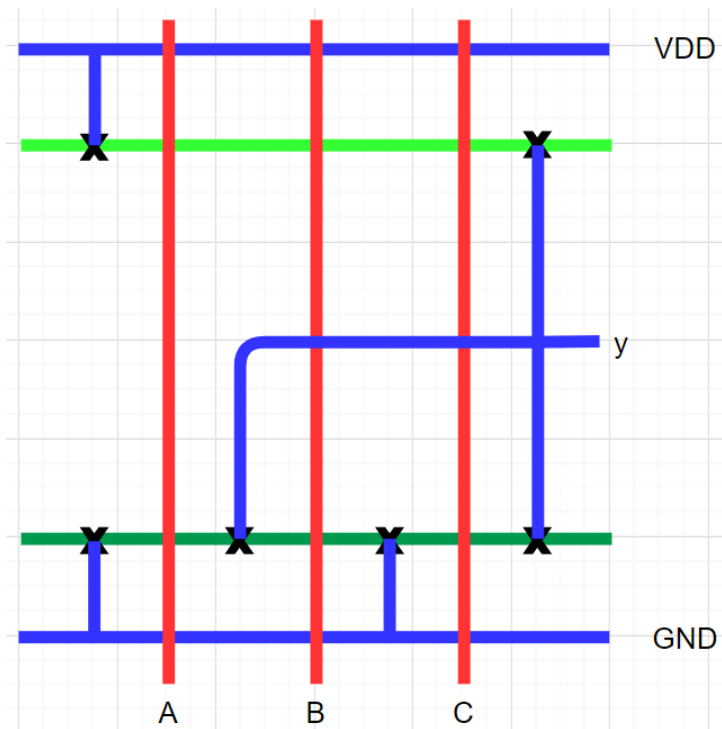


Figure 11

$$height = 40\lambda$$

### Schematic

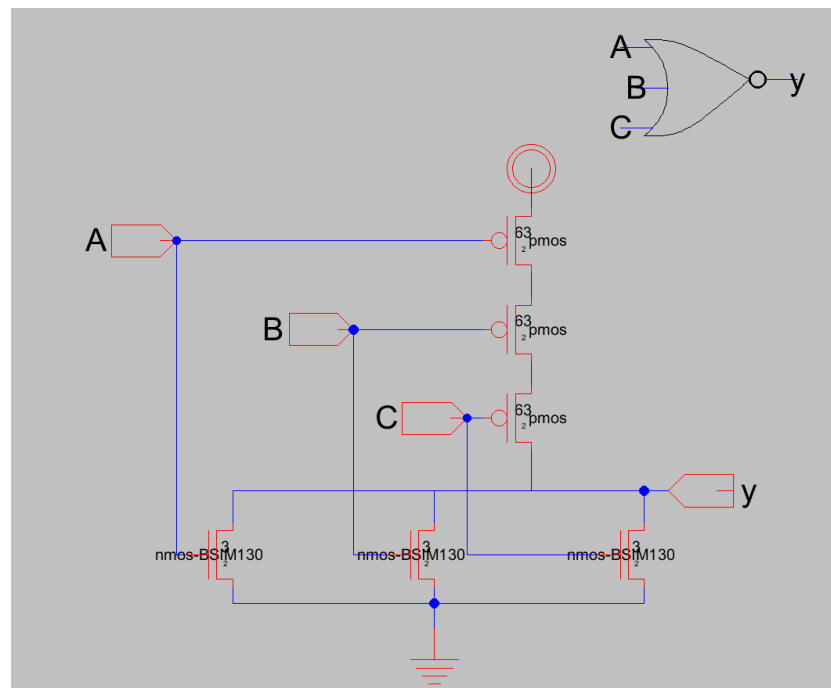


Figure 12

**Size 1:**

**Layout**

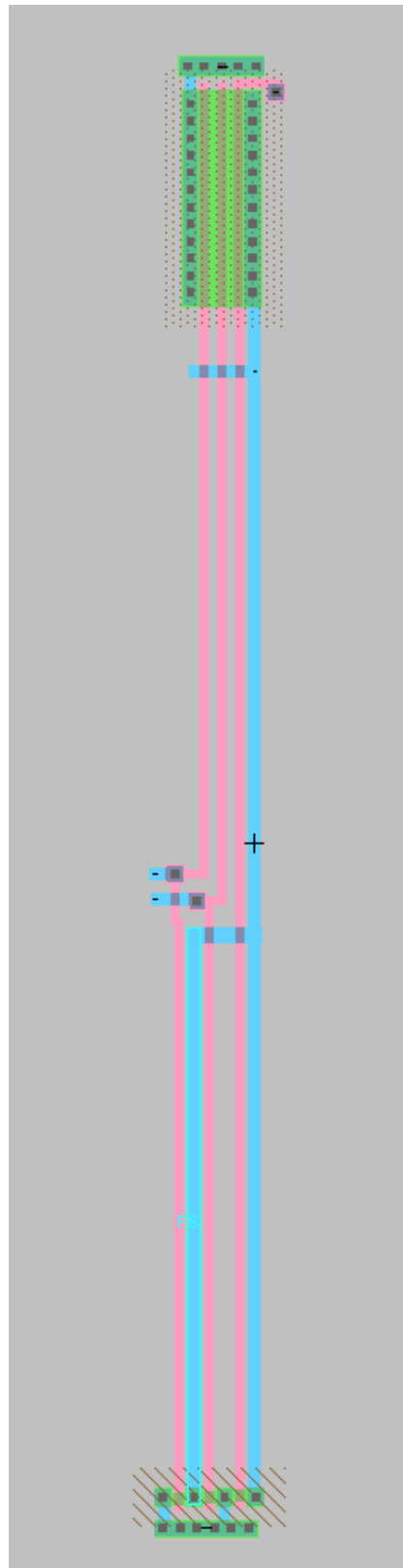


Figure 13

## Propagation Delays

$T_{pdf}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	9.94883e-010	1.34142e-009	2.11285e-009	3.69649e-009
100 ps	5.57007e-010	9.73346e-010	1.7938e-009	3.43064e-009
400 ps	6.03531e-010	1.01712e-009	1.82407e-009	3.46021e-009
800 ps	6.87091e-010	1.08423e-009	1.88151e-009	3.50729e-009

$T_{pdr}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	3.28678e-011	1.41217e-010	4.25393e-010	9.00704e-010
100 ps	1.44074e-010	2.66613e-010	5.04107e-010	9.89129e-010
400 ps	1.3355e-010	2.49147e-010	4.86928e-010	9.74296e-010
800 ps	1.08609e-010	2.40405e-010	4.66806e-010	9.46462e-010

## Linear Delay Model

### Using Tpdf

$$5.57007e-010 = (K1 * 130e-15) + (K2 * 100e-12) + K3$$

$$1.34142e-009 = (K1 * 260e-15) + (K2 * 0e-12) + k3$$

$$3.50729e-009 = (K1 * 520e-15) + (K2 * 800e-12) + K3$$

$$K1 = -729.81$$

$$K2 = 4.621$$

$$K3 = 1.897e-10$$

$$Tpdf = -729.81 \times \text{cload} + 4.621 \times \text{transition time} + 1.897e-10$$

### Using Tpdr

$$1.44074e-010 = (K1 * 130e-15) + (K2 * 100e-12) + K3$$

$$4.25393e-010 = (K1 * 520e-15) + (K2 * 0e-12) + k3$$

$$9.46462e-010 = (K1 * 520e-15) + (K2 * 800e-12) + K3$$

$$K1 = 888.13$$

$$K2 = 0.65145$$

$$K3 = -3.652e-11$$

$$Tpdr = 888.13 \times \text{cload} + 0.65145 \times \text{transition time} - 3.652e-11$$

**Size 2:**  
**Layout**

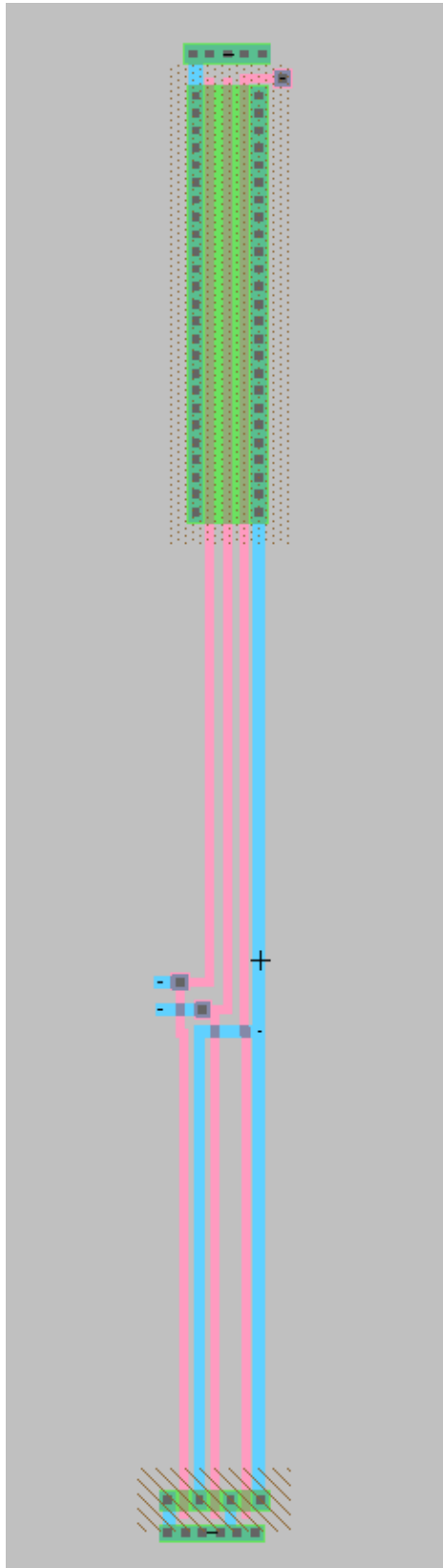


Figure 14

## Propagation Delays

$T_{pdf}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	8.02686e-010	9.83728e-010	1.32986e-009	2.08501e-009
100 ps	3.41543e-010	5.45943e-010	9.57151e-010	1.76099e-009
400 ps	3.94494e-010	5.91036e-010	9.94362e-010	1.79426e-009
800 ps	4.88405e-010	6.74705e-010	1.05999e-009	1.85214e-009

$T_{pdr}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	1.43853e-010	3.298e-011	1.41144e-010	4.23943e-010
100 ps	8.42204e-011	1.4274e-010	2.62941e-010	4.96743e-010
400 ps	7.05747e-011	1.33614e-010	2.48029e-010	4.84508e-010
800 ps	2.95349e-011	1.07891e-010	2.36477e-010	4.65934e-010

## Linear Delay Model

### Using Tpdf

$$3.41543e-010 = (K1 * 130e-15) + (K2 * 100e-12) + K3$$

$$1.32986e-009 = (K1 * 520e-15) + (K2 * 0e-12) + k3$$

$$6.74705e-010 = (K1 * 260e-15) + (K2 * 800e-12) + K3$$

$$K1 = 2535.3$$

$$K2 = 5.1e-3$$

$$K3 = 1.144e-11$$

$$T_{pdf} = 2535.3 \times \text{cload} + 5.1e-3 \times \text{transition time} + 1.144e-11$$

### Using Tpdr

$$7.05747e-011 = (K1 * 130e-15) + (K2 * 400e-12) + K3$$

$$1.41144e-010 = (K1 * 520e-15) + (K2 * 0e-12) + k3$$

$$4.96743e-010 = (K1 * 1040e-15) + (K2 * 100e-12) + K3$$

$$K1 = 604.43$$

$$K2 = 0.41299$$

$$K3 = -1.73164e-10$$

$$T_{pdr} = 604.43 \times \text{cload} + 0.41299 \times \text{transition time} - 1.73164e-10$$



**Size 4:**  
**Layout**

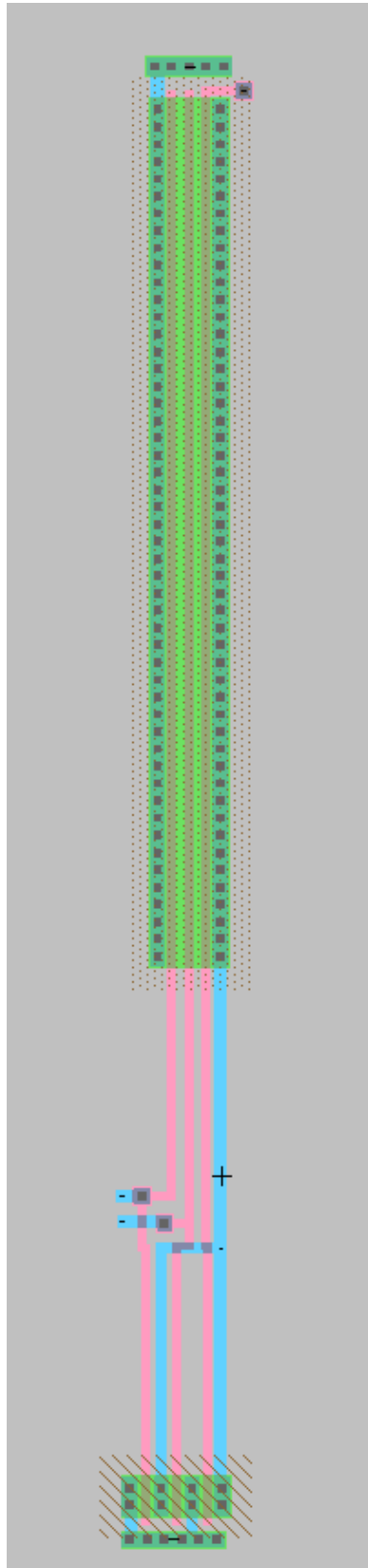


Figure 15

## Propagation Delays

$T_{pdf}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	7.02417e-010	7.96499e-010	9.77584e-010	1.32885e-009
100 ps	2.35193e-010	3.36829e-010	5.39488e-010	9.45689e-010
400 ps	2.96108e-010	3.90524e-010	5.84973e-010	9.81251e-010
800 ps	4.00421e-010	4.87898e-010	6.67044e-010	1.05058e-009

$T_{pdr}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	2.12099e-010	1.41945e-010	3.18707e-011	1.43226e-010
100 ps	5.53591e-011	8.49669e-011	1.43694e-010	2.61303e-010
400 ps	3.33368e-011	7.06056e-011	1.32919e-010	2.48245e-010
800 ps	1.81337e-011	2.958e-011	1.08157e-010	2.35829e-010

## Linear Delay Model

### Using Tpdf

$$2.35193e-010 = (K1 * 130e-15) + (K2 * 100e-12) + K3$$

$$1.32885e-009 = (K1 * 1040e-15) + (K2 * 0e-12) + k3$$

$$6.67044e-010 = (K1 * 520e-15) + (K2 * 800e-12) + K3$$

$$K1 = 1196.37$$

$$K2 = -0.0496$$

$$K3 = 8.462e-11$$

$$T_{pdf} = 1196.37 \times \text{cload} - 0.0496 \times \text{transition time} + 8.462e-11$$

### Using Tpdr

$$1.05e-10 = 130e-15 k1 + 0 + k3$$

$$5.56e-11 = 130e-15 k1 + 100e-12 k2 + k3$$

$$9.02e-11 = 260e-15 k1 + 400e-12 k2 + k3$$

$$K1 = 1406.15$$

$$K2 = -0.494$$

$$K3 = -7.78e-11$$

$$T_{pdr} = 1406.15 \times \text{cload} - 0.494 \times \text{transition time} - 7.78e-11$$

#### 4- The function $f(x, y, z, w) = \overline{xy} + wz$

Stick Diagram

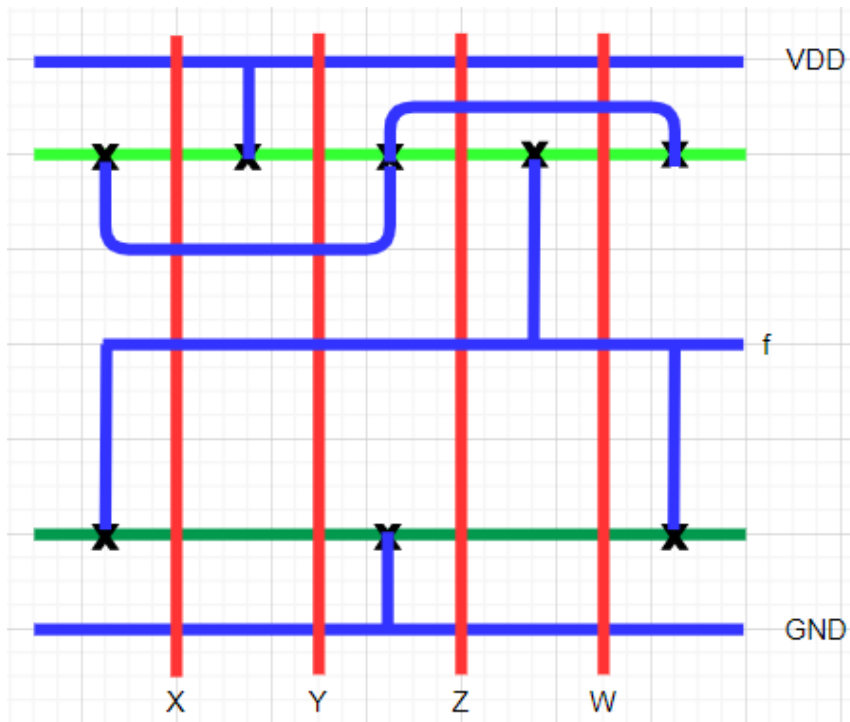


Figure 16

$height = 48\lambda$

#### Schematic

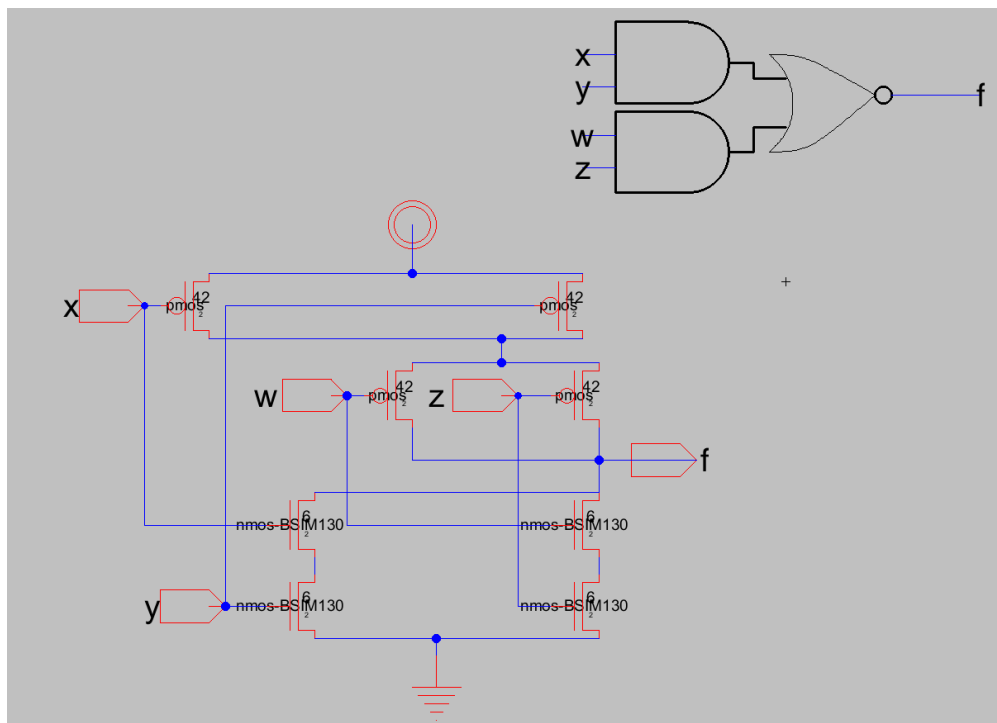


Figure 17

**Size 1:**

**Layout**

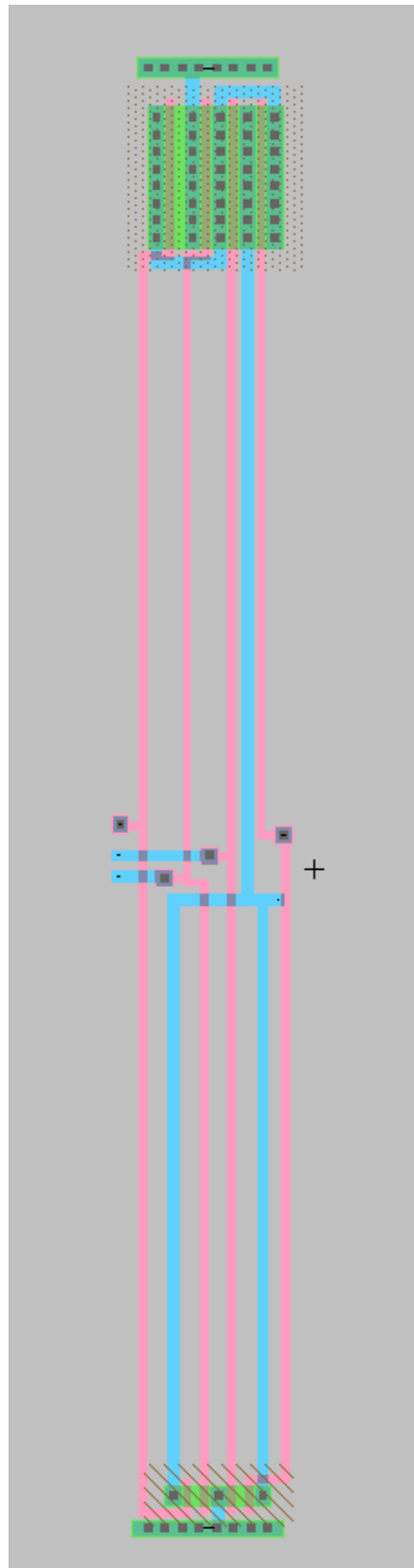


Figure 18

## Propagation Delays

$T_{pdf}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	7.7993e-010	1.04467e-009	1.61458e-009	2.78472e-009
100 ps	4.03291e-010	7.16808e-010	1.33595e-009	2.54249e-009
400 ps	4.4658e-010	7.49322e-010	1.3632e-009	2.57081e-009
800 ps	5.22926e-010	8.19162e-010	1.41624e-009	2.61198e-009

$T_{pdr}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	8.57293e-011	2.72756e-010	5.62745e-010	1.05083e-009
100 ps	1.49387e-010	2.7536e-010	5.26061e-010	1.01262e-009
400 ps	1.56695e-010	2.75856e-010	5.23412e-010	1.01095e-009
800 ps	1.55713e-010	2.91029e-010	5.29459e-010	1.02787e-009

## Linear Delay Model

### Using Tpdf

$$7.799\text{e-}10 = 130\text{e-}15 k_1 + 0 + k_3$$

$$4.03\text{e-}10 = 130\text{e-}15 k_1 + 100\text{e-}12 k_2 + k_3$$

$$1.36\text{e-}9 = 520\text{e-}15 + 400\text{e-}12 k_2 + k_3$$

$$K_1 = 5353.07$$

$$k_2 = -3.769$$

$$K_3 = 8.4 \text{ e-}11$$

$$T_{pdf} = 5353.07 \times \text{cload} - 3.769 \times \text{transition time} + 8.4 \text{ e-}11$$

### Using Tpdr

$$8.57\text{e-}11 = 130 \text{ e-}15 k_1 + 0 + k_3$$

$$5.26\text{e-}10 = 520\text{e-}15 k_1 + 100\text{e-}12 + k_3$$

$$1.56\text{e-}10 = 130\text{e-}15 k_1 + 400\text{e-}12 k_2 + k_3$$

$$K_1 = 1083.91$$

$$K_2 = 0.17575$$

$$K_3 = -5.52\text{e-}11$$

$$T_{pdr} = 1083.91 \times \text{cload} + 0.17575 \times \text{transition time} - 5.52\text{e-}11$$

**Size 2:**  
**Layout**

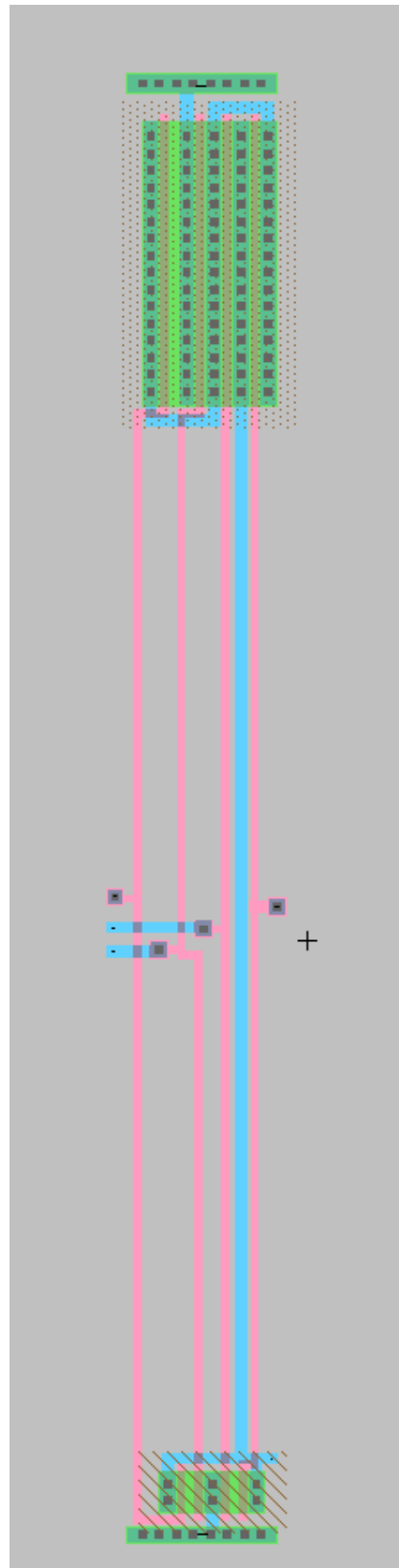


Figure 19



## Propagation Delays

$T_{pdf}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	6.28306e-010	7.83317e-010	1.0507e-009	1.60331e-009
100 ps	2.43963e-010	3.97512e-010	7.15835e-010	1.32275e-009
400 ps	2.93852e-010	4.40244e-010	7.50177e-010	1.34947e-009
800 ps	3.78422e-010	5.16643e-010	7.99635e-010	1.40225e-009

$T_{pdr}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	3.33506e-011	8.69611e-011	2.72328e-010	5.6115e-010
100 ps	8.56002e-011	1.48168e-010	2.72846e-010	5.24541e-010
400 ps	9.02878e-011	1.55428e-010	2.73644e-010	5.20531e-010
800 ps	7.34747e-011	1.55666e-010	2.88397e-010	5.27924e-010

## Linear Delay Model

### Using Tpdf

$$5.47e-10 = 130e-15 k_1 + 0 + k_3$$

$$2.42e-10 = 260e-15 k_1 + 100e-12 + k_3$$

$$7.98e-10 = 1040e-15 k_1 + 800e-12 + k_3$$

$$K_1 = 1307.101$$

$$K_2 = -1.173$$

$$k_3 = 3.77e-10$$

$$T_{pdf} = 1307.101 \times \text{cload} - 1.173 \times \text{transition time} + 3.77e-10$$

### Using Tpdr

$$1.05e-10 = 130e-15 k_1 + 0 + k_3$$

$$5.56e-11 = 130e-15 k_1 + 100e-12 k_2 + k_3$$

$$9.02e-11 = 260e-15 k_1 + 400e-12 k_2 + k_3$$

$$K_1 = 1406.15$$

$$K_2 = -0.494$$

$$K_3 = -7.78e-11$$

$$T_{pdr} = 1406.15 \times \text{cload} - 0.494 \times \text{transition time} - 7.78e-11$$

**Size 4:**  
**Layout**

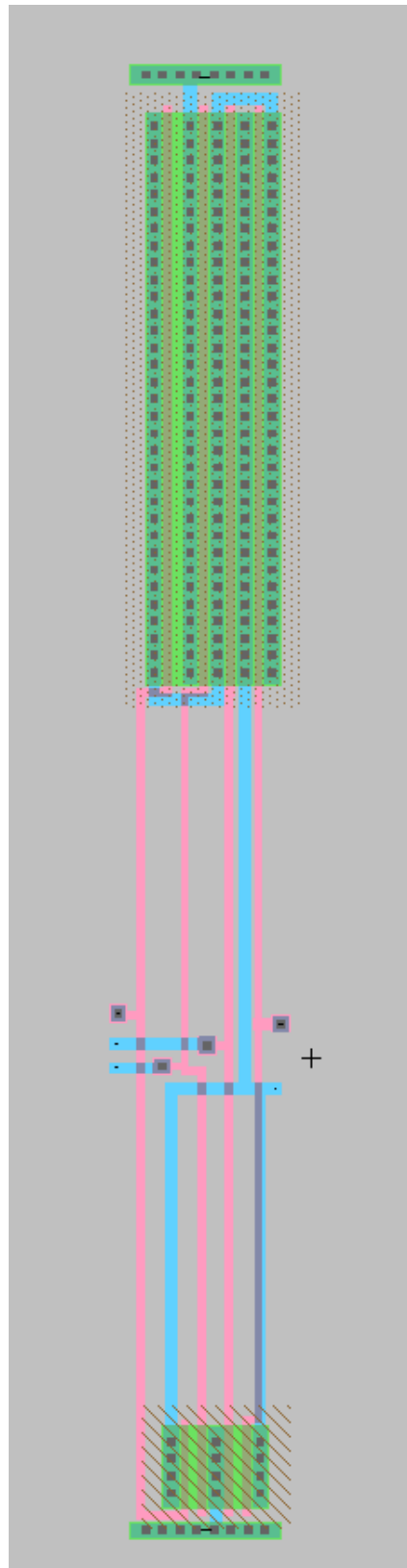


Figure 20

## Propagation Delays

$T_{pdf}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	5.47285e-010	6.30326e-010	7.79139e-010	1.04957e-009
100 ps	1.65828e-010	2.42059e-010	3.96217e-010	6.98302e-010
400 ps	2.23003e-010	2.92129e-010	4.35127e-010	7.35261e-010
800 ps	3.09629e-010	3.79907e-010	5.15467e-010	7.98991e-010

$T_{pdr}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	1.05787e-010	3.17408e-011	8.77894e-011	2.7221e-010
100 ps	5.56799e-011	8.59193e-011	1.47289e-010	2.6797e-010
400 ps	5.05174e-011	9.02109e-011	1.56887e-010	2.7419e-010
800 ps	2.06591e-011	7.2543e-011	1.55723e-010	2.8991e-010

## Linear Delay Model

### Using Tpdf

$$1.79038e-010 = (K1 * 130e-15) + (K2 * 100e-12) + K3$$

$$5.56749e-010 = (K1 * 620e-15) + (K2 * 0e-12) + k3$$

$$7.67043e-010 = (K1 * 1040e-15) + (K2 * 800e-12) + K3$$

$$K1 = 744.6963$$

$$K2 = -0.1280$$

$$K3 = 9.503728e-11$$

$$T_{pdf} = 744.6963 \times \text{cload} - 0.1280 \times \text{transition time} + 9.503728e-11$$

### Using Tpdr

$$1.31135e-010 = (K1 * 130e-15) + (K2 * 100e-12) + K3$$

$$5.08172e-010 = (K1 * 260e-15) + (K2 * 0e-12) + k3$$

$$7.25733e-010 = (K1 * 520e-15) + (K2 * 800e-12) + K3$$

$$K1 = 2487.55$$

$$K2 = -0.53654$$

$$K3 = 1.385928e-10$$

$$T_{pdr} = 2487.55 \times \text{cload} - 0.53654 \times \text{transition time} + 1.385928e-10$$

## 5- The function $g(x, y, z) = \overline{xy + xz + yz}$ Stick Diagram

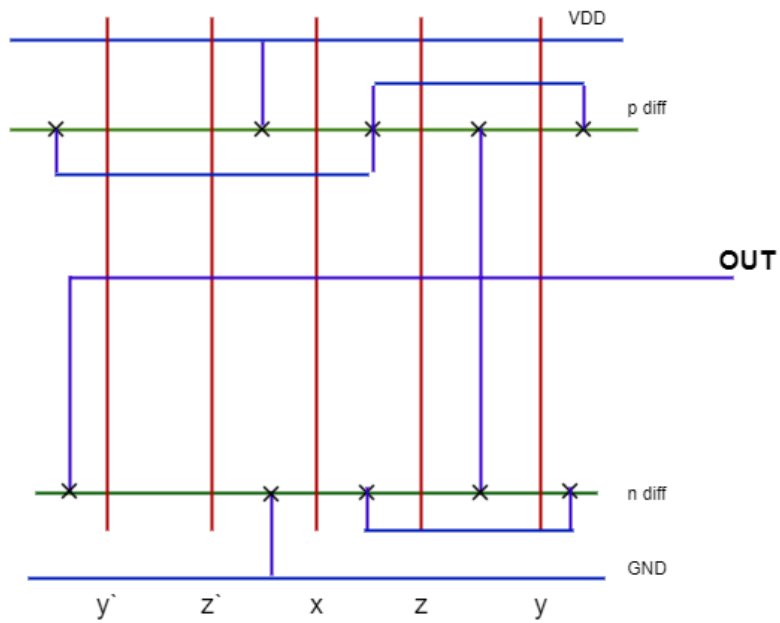


Figure 21

$$height = 56\lambda$$

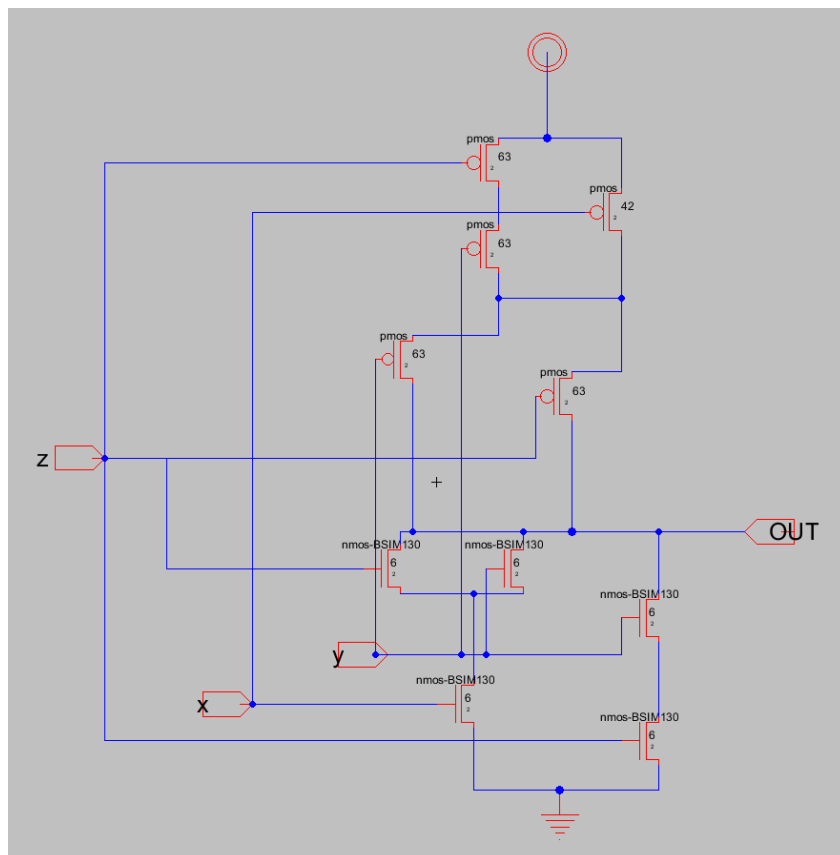


Figure 21

**Size 1:**  
**Layout**

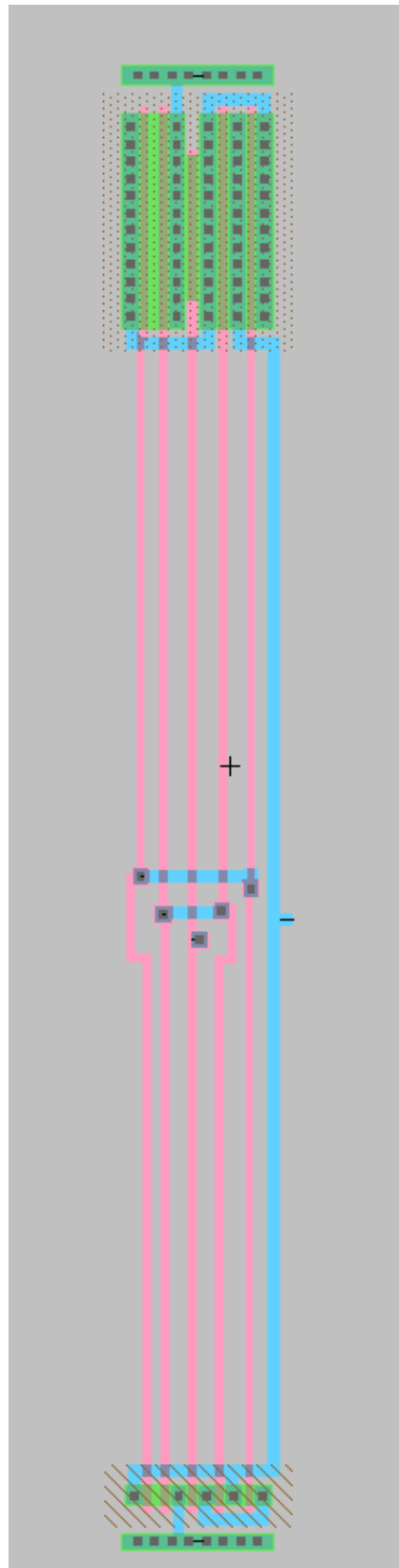


Figure 22

## Propagation Delays

**T<sub>pdf</sub>**

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	6.96894e-010	9.53528e-010	1.51668e-009	2.68267e-009
100 ps	4.22112e-010	7.34425e-010	1.34565e-009	2.561e-009
400 ps	4.39067e-010	7.44635e-010	1.35873e-009	2.5675e-009
800 ps	4.92484e-010	7.85939e-010	1.38653e-009	2.5878e-009

**T<sub>pdr</sub>**

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	6.52635e-010	9.22698e-010	1.47636e-009	2.64939e-009
100 ps	3.70615e-010	6.79984e-010	1.30028e-009	2.51616e-009
400 ps	3.91647e-010	6.92703e-010	1.30498e-009	2.52213e-009
800 ps	4.47489e-010	7.37409e-010	1.33483e-009	2.5409e-009



## Linear Delay Model

### Using Tpdf

$$4.22112e-010 = (K1 * 130e-15) + (K2 * 100e-12) + K3$$

$$1.51668e-009 = (K1 * 520e-15) + (K2 * 0e-12) + k3$$

$$2.5878e-009 = (K1 * 1040e-15) + (K2 * 800e-12) + K3$$

$$K1 = 2699.9076$$

$$K2 = -0.41604$$

$$K3 = 1.12728e-10$$

$$T_{pdf} = 2699.9076 \times \text{cload} - 0.41604 \times \text{transition time} + 1.12728e-10$$

### Using Tpdr

$$3.70615e-010 = (K1 * 130e-15) + (K2 * 100e-12) + K3$$

$$1.47636e-009 = (K1 * 520e-15) + (K2 * 0e-12) + k3$$

$$7.37409e-010 = (K1 * 260e-15) + (K2 * 800e-12) + K3$$

$$K1 = 2690.42$$

$$K2 = -0.0492$$

$$K3 = 7.72794e-11$$

$$T_{pdr} = 2690.42 \times \text{cload} - 0.0492 \times \text{transition time} + 7.72794e-11$$

**Size 2:  
Layout**

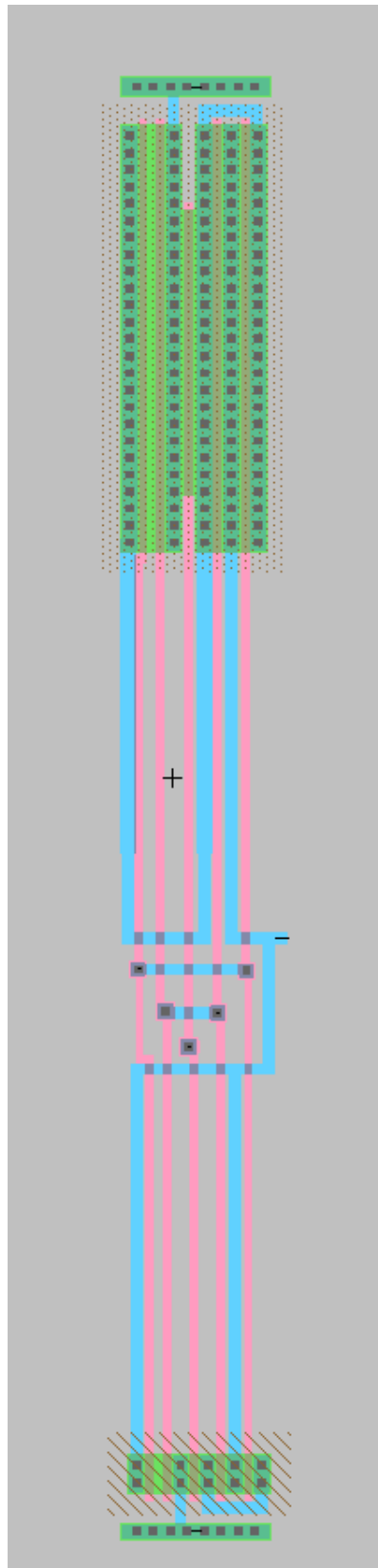


Figure 23

## Propagation Delays

$T_{pdf}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	5.56696e-010	6.87823e-010	9.49712e-010	1.50267e-009
100 ps	2.58636e-010	4.13089e-010	7.20544e-010	1.33706e-009
400 ps	2.88122e-010	4.34556e-010	7.35064e-010	1.34735e-009
800 ps	3.54498e-010	4.83445e-010	7.70966e-010	1.3692e-009

$T_{pdr}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	5.05691e-010	6.48891e-010	9.16454e-010	1.4723e-009
100 ps	2.09841e-010	3.63682e-010	6.71145e-010	1.28297e-009
400 ps	2.42086e-010	3.86394e-010	6.8561e-010	1.29318e-009
800 ps	3.1223e-010	4.43407e-010	7.27228e-010	1.32609e-009

## Linear Delay Model

### Using Tpdf

$$2.58636e-010 = (K1 * 130e-15) + (K2 * 100e-12) + K3$$

$$1.50267e-009 = (K1 * 1040e-15) + (K2 * 0e-12) + k3$$

$$7.70966e-010 = (K1 * 520e-15) + (K2 * 800e-12) + K3$$

$$K1 = 1363.91$$

$$K2 = -0.0279$$

$$K3 = 8.41264e-11$$

$$T_{pdf} = 1363.91 \times \text{cload} - 0.0279 \times \text{transition time} + 8.41264e-11$$

### Using Tpdr

$$2.09841e-010 = (K1 * 130e-15) + (K2 * 100e-12) + K3$$

$$1.4723e-009 = (K1 * 1040e-15) + (K2 * 0e-12) + k3$$

$$7.27228e-010 = (K1 * 520e-15) + (K2 * 800e-12) + K3$$

$$K1 = 1383.82$$

$$K2 = -0.03178$$

$$K3 = 3.312276e-11$$

$$T_{pdr} = 1383.821 \times \text{cload} - 0.03178 \times \text{transition time} + 3.312276e-11$$

**Size 4:**

## Layout

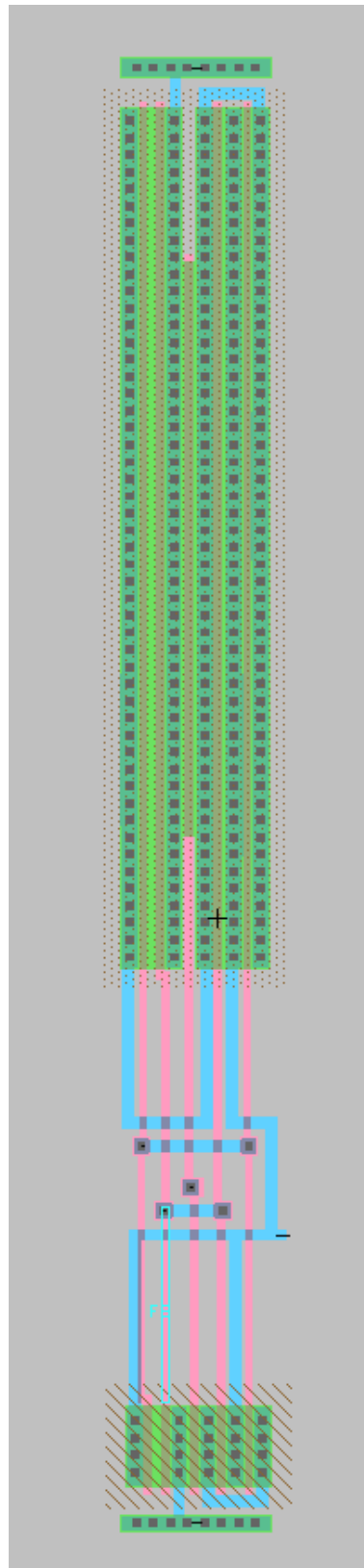


Figure 24

## Propagation Delays

**T<sub>pdr</sub>**

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	4.83209e-010	5.56749e-010	6.91667e-010	9.53362e-010
100 ps	1.79038e-010	2.55775e-010	4.09018e-010	7.14334e-010
400 ps	2.16786e-010	2.8582e-010	4.29921e-010	7.27116e-010
800 ps	2.84614e-010	3.50855e-010	4.85088e-010	7.67043e-010

**T<sub>pdr</sub>**

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	4.24459e-010	5.08172e-010	6.5128e-010	9.18806e-010
100 ps	1.31135e-010	2.08094e-010	3.61279e-010	6.66689e-010
400 ps	1.73123e-010	2.4213e-010	3.85985e-010	6.80629e-010
800 ps	2.40103e-010	3.08917e-010	4.4536e-010	7.25733e-010

## Linear Delay Model

### Using Tpdf

$$1.79038e-010 = (K1 * 130e-15) + (K2 * 100e-12) + K3$$

$$5.56749e-010 = (K1 * 620e-15) + (K2 * 0e-12) + k3$$

$$7.67043e-010 = (K1 * 1040e-15) + (K2 * 800e-12) + K3$$

$$K1 = 744.6963$$

$$K2 = -0.1280$$

$$K3 = 9.503728e-11$$

$$T_{pdf} = 744.6963 \times \text{cload} - 0.1280 \times \text{transition time} + 9.503728e-11$$

### Using Tpdr

$$1.31135e-010 = (K1 * 130e-15) + (K2 * 100e-12) + K3$$

$$5.08172e-010 = (K1 * 260e-15) + (K2 * 0e-12) + k3$$

$$7.25733e-010 = (K1 * 520e-15) + (K2 * 800e-12) + K3$$

$$K1 = 2487.55$$

$$K2 = -0.53654$$

$$K3 = 1.385928e-10$$

$$T_{pdr} = 2487.55 \times \text{cload} - 0.53654 \times \text{transition time} + 1.385928e-10$$

## 6- The function $h(w, x, y, z) = \overline{xyz + (x + y + z)w}$ Stick Diagram

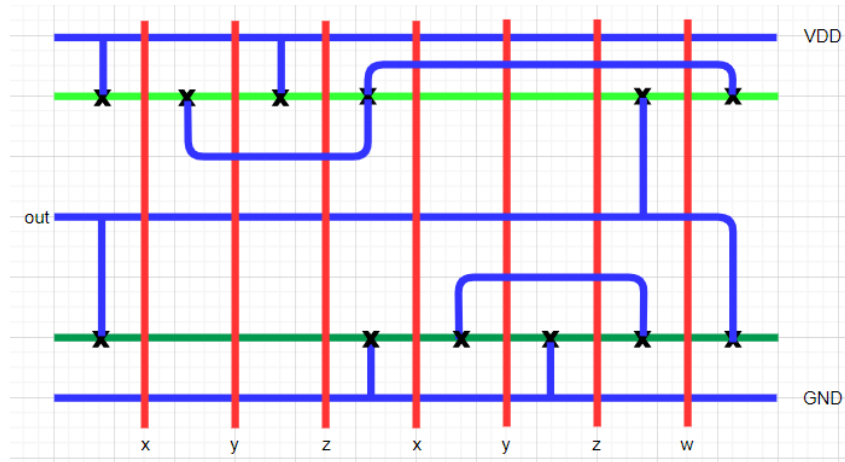


Figure 25

$$height = 72\lambda$$

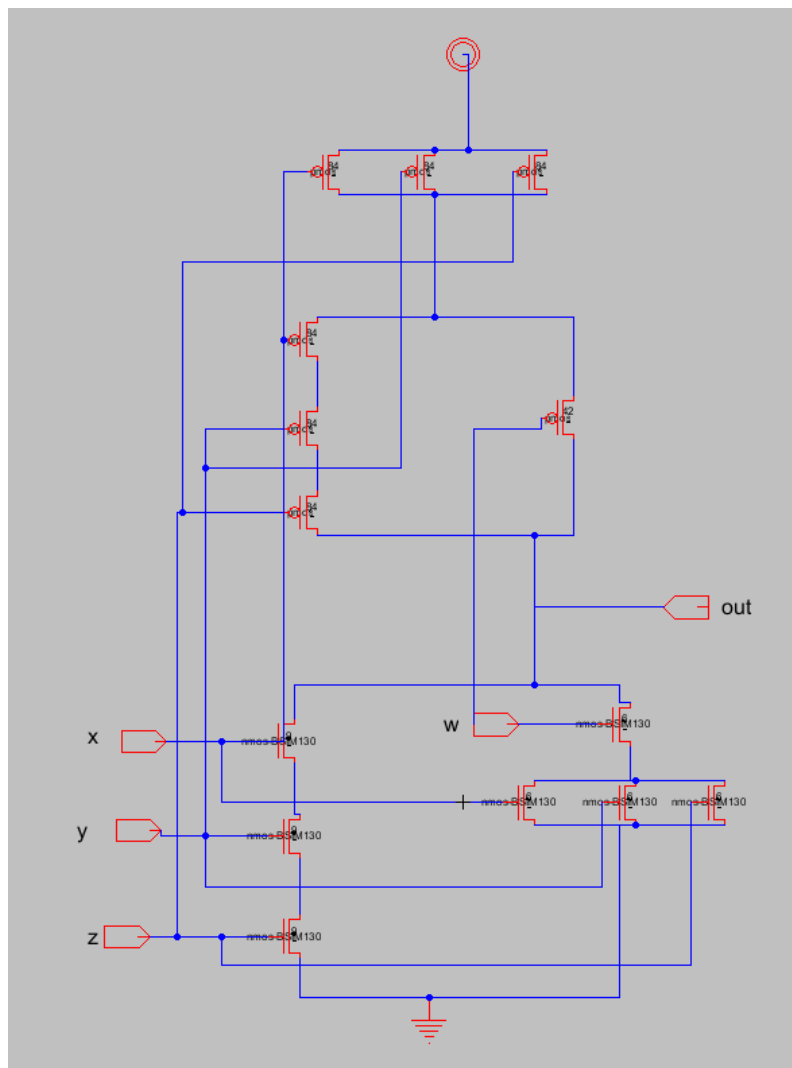


Figure 26



**Size 1:**  
**Layout**

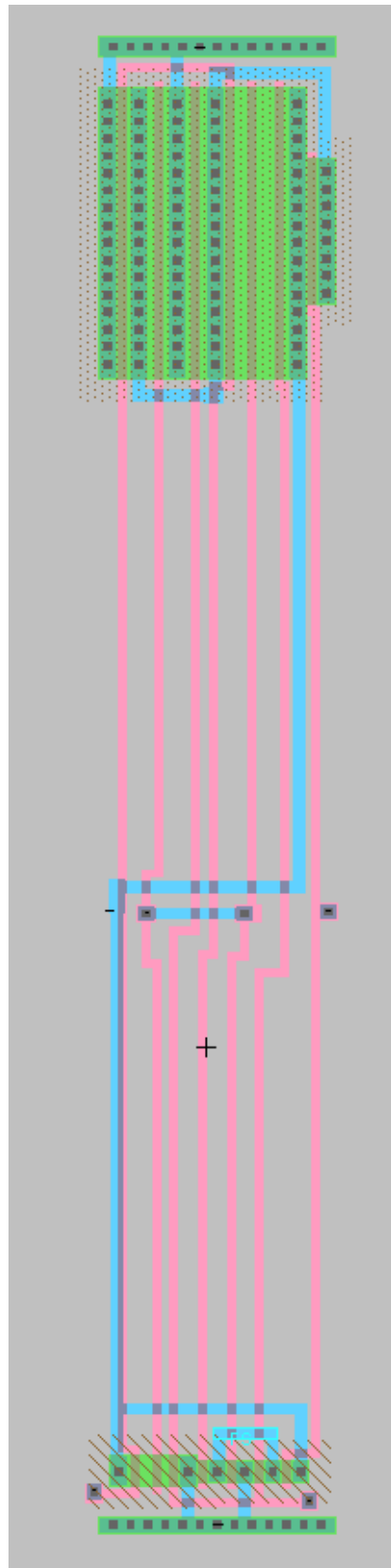


Figure 27

## Propagation Delays

$T_{pdf}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	8.23758e-010	1.05296e-009	1.54763e-009	2.56104e-009
100 ps	4.09499e-010	6.88334e-010	1.24288e-009	2.3053e-009
400 ps	4.49268e-010	7.1962e-010	1.26536e-009	2.32584e-009
800 ps	5.30066e-010	7.8373e-010	1.31883e-009	2.37263e-009

$T_{pdr}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	7.96914e-010	1.0476e-009	1.58164e-009	2.74629e-009
100 ps	4.64221e-010	7.76108e-010	1.39188e-009	2.6032e-009
400 ps	4.84167e-010	7.88169e-010	1.39924e-009	2.61026e-009
800 ps	5.46521e-010	8.32074e-010	1.43521e-009	2.63234e-009

## Linear Delay Model

### Using Tpdf

$$8.23e-10 = 130e-15 k_1 + 0 + k_3$$

$$4.094 e10 = 130e-15 k_1 + 100e-12 k_2 + k_3$$

$$1.265e-9 = 520e-15 k_1 + 400e-12 k_2 + k_3$$

$$K_1 = 5375.384$$

$$K_2 = -4.136$$

$$K_3 = 1.242 e-10$$

$$T_{pdf} = 5375.384 \times \text{cload} - 4.136 \times \text{transition time} + 1.242 e-10$$

### Using Tpdr

$$7.96e-10 = 130e-15 k_1 + 100 e-12 k_2 + k_3$$

$$4.6422e-10 = 130e-15 k_1 + 100e-12 k_2 + k_3$$

$$1.399e-9 = 520e-15 + 400 e-12 k_2 + k_3$$

$$K_1 = 4949.03$$

$$K_2 = -3.3178$$

$$k_3 = 1.5262e-10$$

$$T_{pdr} = 4949.03 \times \text{cload} - 3.3178 \times \text{transition time} + 1.5262e-10$$

**Size 2:**  
**Layout**

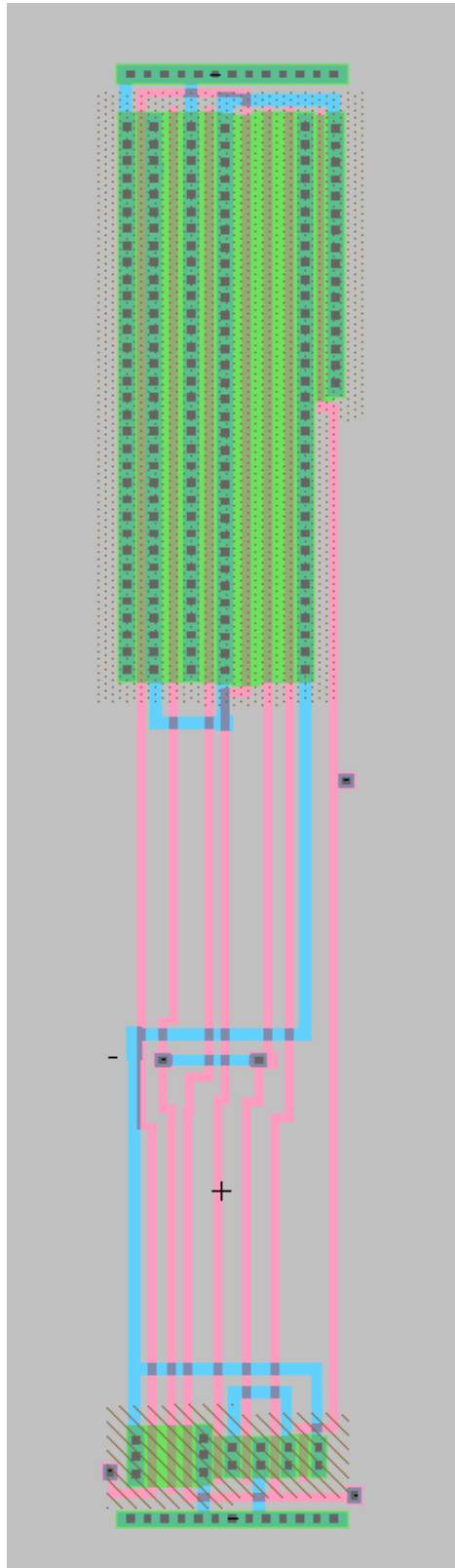


Figure 28

## Propagation Delays

$T_{pdf}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	6.91235e-010	8.16775e-010	1.05038e-009	1.53881e-009
100 ps	2.64358e-010	4.02451e-010	6.76022e-010	1.23006e-009
400 ps	3.11657e-010	4.45533e-010	7.06194e-010	1.25504e-009
800 ps	4.03887e-010	5.25701e-010	7.79443e-010	1.30769e-009

$T_{pdr}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	6.61459e-010	7.84813e-010	1.03669e-009	1.58795e-009
100 ps	2.97159e-010	4.50903e-010	7.59026e-010	1.37028e-009
400 ps	3.27228e-010	4.75243e-010	7.78841e-010	1.38773e-009
800 ps	4.05676e-010	5.42132e-010	8.18619e-010	1.41484e-009

## Linear Delay Model

### Using Tpdf

$$6.912e-10 = 130e-15 k_1 + 0 + k_3$$

$$4.02e-10 = 260e-15 k_1 + 100e-12 k_2 + k_3$$

$$1.255e-10 = 1040 e-15 k_1 + 400e-12 k_2 + k_3$$

$$K_1 = 4.412$$

$$K_2 = -8.623$$

$$K_3 = 1.176 e-10$$

$$T_{pdf} = 4.412 \times \text{cload} - 8.623 \times \text{transition time} + 1.176 e-10$$

### Using Tpdr

$$6.52e-10 = 130e-15 k_1 + 0 + k_3$$

$$3.706e-10 = 130e-15 k_1 + 100e-12 k_2 + k_3$$

$$1.30e-9 = 520 e-15 k_1 + 400e-12 k_2 + k_3$$

$$K_1 = 4547$$

$$K_2 = -2.814$$

$$K_3 = 6.08e-11$$

$$T_{pdr} = 4547 \times \text{cload} - 2.814 \times \text{transition time} + 6.08e-11$$

**Size 4:**  
**Layout**

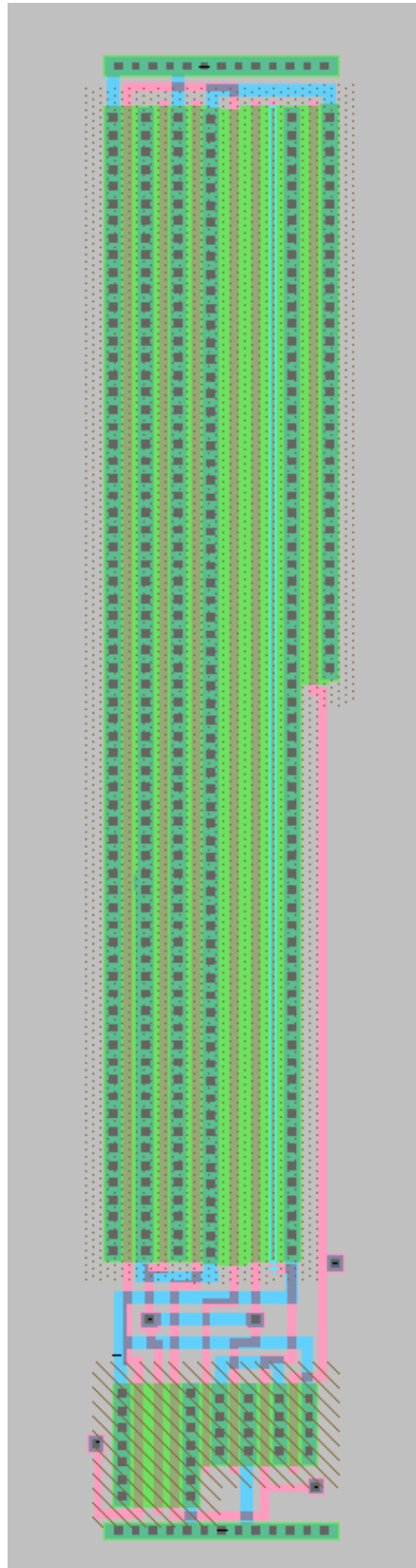


Figure 29

## Propagation Delays

$T_{pdf}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	6.23976e-010	6.91979e-010	8.15826e-010	1.04903e-009
100 ps	1.92941e-010	2.63131e-010	4.02232e-010	6.71701e-010
400 ps	2.47861e-010	3.1157e-010	4.40401e-010	7.04835e-010
800 ps	3.44529e-010	4.05096e-010	5.25548e-010	7.73373e-010

$T_{pdr}$

	Cinv	2Cinv	4Cinv	8Cinv
0 ps	5.92793e-010	6.60356e-010	7.87321e-010	1.03882e-009
100 ps	2.17746e-010	2.9541e-010	4.48863e-010	7.5383e-010
400 ps	2.59274e-010	3.29519e-010	4.73972e-010	7.71332e-010
800 ps	3.40315e-010	4.05881e-010	5.39018e-010	8.20457e-010



## Linear Delay Model

### Using Tpdf

$$6.23e-10 = 130e-15 k_1 + 0 + k_3$$

$$4.02e-10 = 520e-15 + 100e-12 k_2 + k_3$$

$$1.92e-10 = 130e-15 + 100e-12 k_2 + k_3$$

$$K_1 = 538.46$$

$$K_2 = -4.31$$

$$K_3 = 5.53e-10$$

$$T_{pdf} = 538.46 \times \text{cload} - 4.31 \times \text{transition time} + 5.53e-10$$

### Using Tpdr

$$5.927e-10 = 130e-15 k_1 + 0 + k_3$$

$$2.177e-10 = 130e-15 k_1 + 100e-12 + k_3$$

$$1.038e-9 = 1040e-15 + 0 + k_3$$

$$K_1 = -6.51 e22$$

$$K_2 = -5.927e20$$

$$K_3 = 6.77e10$$

$$T_{pdr} = -6.51 e22 \times \text{cload} - 5.927e20 \times \text{transition time} + 6.77e10$$

**Contribution work:**

Every member took two functions and was responsible for creating its stick diagram, schematic, layout, simulations and its calculations.

Marwan	Function 3,4
Mohammed	Function 1,6
Donia	Function 2,5