QUESTIONNAIRES AND BEYOND: THE RASCH MODEL

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- The intuition
- The model
- Wait...
- Why is it useful?
- Closing time



0





 A_{Lisa}



Q1

$$4 + 5 = ?$$

 d_{q1}

 A_{Bart}

Q2

$$\frac{3}{2}x^2 + \frac{5}{4}x = 0$$

$$d_{q2}$$



 A_{Lisa}



Q1

$$4 + 5 = ?$$
 d_{q1}

 A_{Bart}

$$rac{A_p}{d_i}$$
 (1)
 $> 1 ext{ if } A_p > d_i$
 $< 1 ext{ if } A_p < d_i$

Q2

$$\frac{3}{2}x^2 + \frac{5}{4}x = ?$$

$$d_{q2}$$



 A_{Lisa}

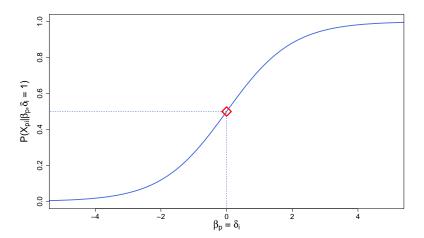
$$P(X_{pi} = 1) = \frac{\frac{A_p}{d_i}}{1 + \frac{A_p}{d_i}}$$
 (2)

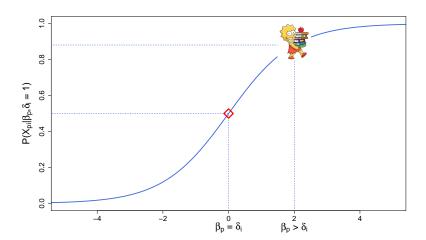
- The intuition
- 2 The model
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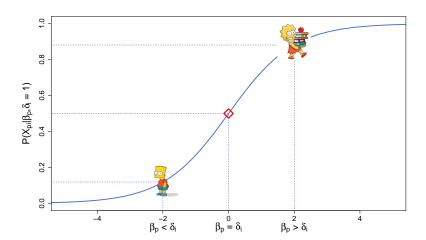


$$ln(A_p) = \beta_p$$
 $ln(d_i) = \delta_i$

$$P(X_{pi} = 1 | \beta_p, \delta_i) = \frac{\exp(\beta_p - \delta_i)}{1 + \exp(\beta_p - \delta_i)}$$
(3)







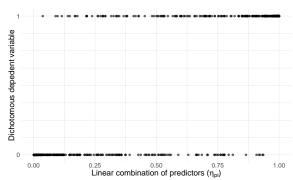
- Wait...

* Eureka moment *

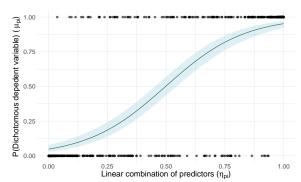


$$P(X_{pi} = 1 | \beta_p, \delta_i) = \frac{exp(\beta_p - \delta_i)}{1 + exp(\beta_p - \delta_i)}$$

Generalized Linear Model (GLM) binomially distributed responses

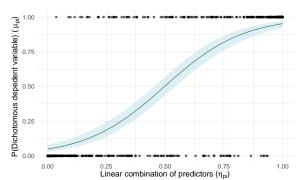


Generalized Linear Model (GLM) binomially distributed responses



$$\mu_{pi} = g(\eta_{pi}) = log\left(\frac{\mu_{pi}}{1 - \mu_{pi}}\right)$$

Generalized Linear Model (GLM) binomially distributed responses



$$\mu_{pi} = g(\eta_{pi}) = log\left(\frac{\mu_{pi}}{1 - \mu_{pi}}\right)$$

$$g^{-1} = \frac{exp(\eta_{pi})}{1 + exp(\eta_{pi})}$$



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Rasch model: Dichotomous responses

Issue

Quite limiting in Psychological Research

(Generalized) Linear Model: "Any" kind of response

e.g.: Response times

log-transformation and log-normal model parametrization

Linearity of the scores

Logarithm transformation \rightarrow Respondents and items on the same latent trait

- Comparison invariance
 - Respondents can be compared between each other without considering the items....and vice versa!
- Local independence

Given the person \rightarrow The responses to the items are independent

Unidimensionality

Linearity of the scores

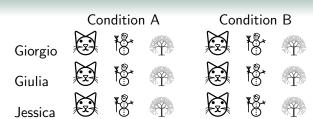
Logarithm transformation \rightarrow Respondents and items on the same latent trait

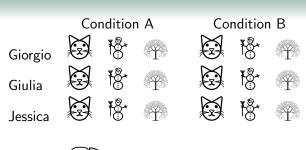
Comparison invariance

Respondents can be compared between each other without considering the items....and vice versa!

Local independence

Given the person \rightarrow The responses to the items are independent





Local independence

Rasch model

- Can't be applied
- The estimates would make no sense

Generalized Linear Model

- Add the random part (Go Mixed)
- Obtain a Rasch-like parametrization of the data



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- **5** Closing time

Think outside of the box!

Yes

Rasch estimates
The sky is the limit
Keep it maximal

But

Rasch-like parametrization

Don't over complicate things

Keep it minimal

Think outside of the box!

Yes

Rasch estimates
The sky is the limit
Keep it maximal

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Rasch-like parametrization

Don't over complicate things

Keep it minimal





Thank you



Questions!



https://ottaviae.github.io/AIP2022/Rasch/epifaniaRasch.pdf