Questionnaires and beyond: The Rasch model

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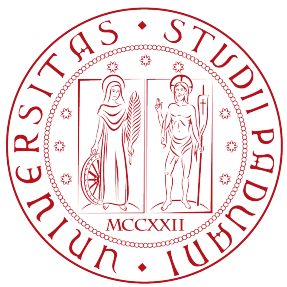
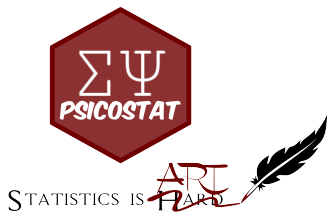




A_{Bart}

A_{Lisa}

Q1

$4 + 5 = ?$

d_{q1}

Q2

$\frac{3}{2}x^2 + \frac{5}{4}x = ?$

d_{q2}

A_{Bart}

A_{Lisa}

Q1

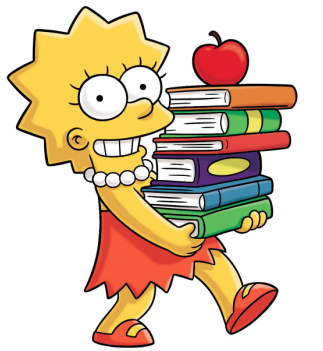
$4 + 5 = ?$

d_{q1}

Q2

$\frac{3}{2}x^2 + \frac{5}{4}x = ?$

d_{q2}



A_{Bart}

A_{Lisa}

$$\frac{A_p}{d_i} \qquad (1)$$

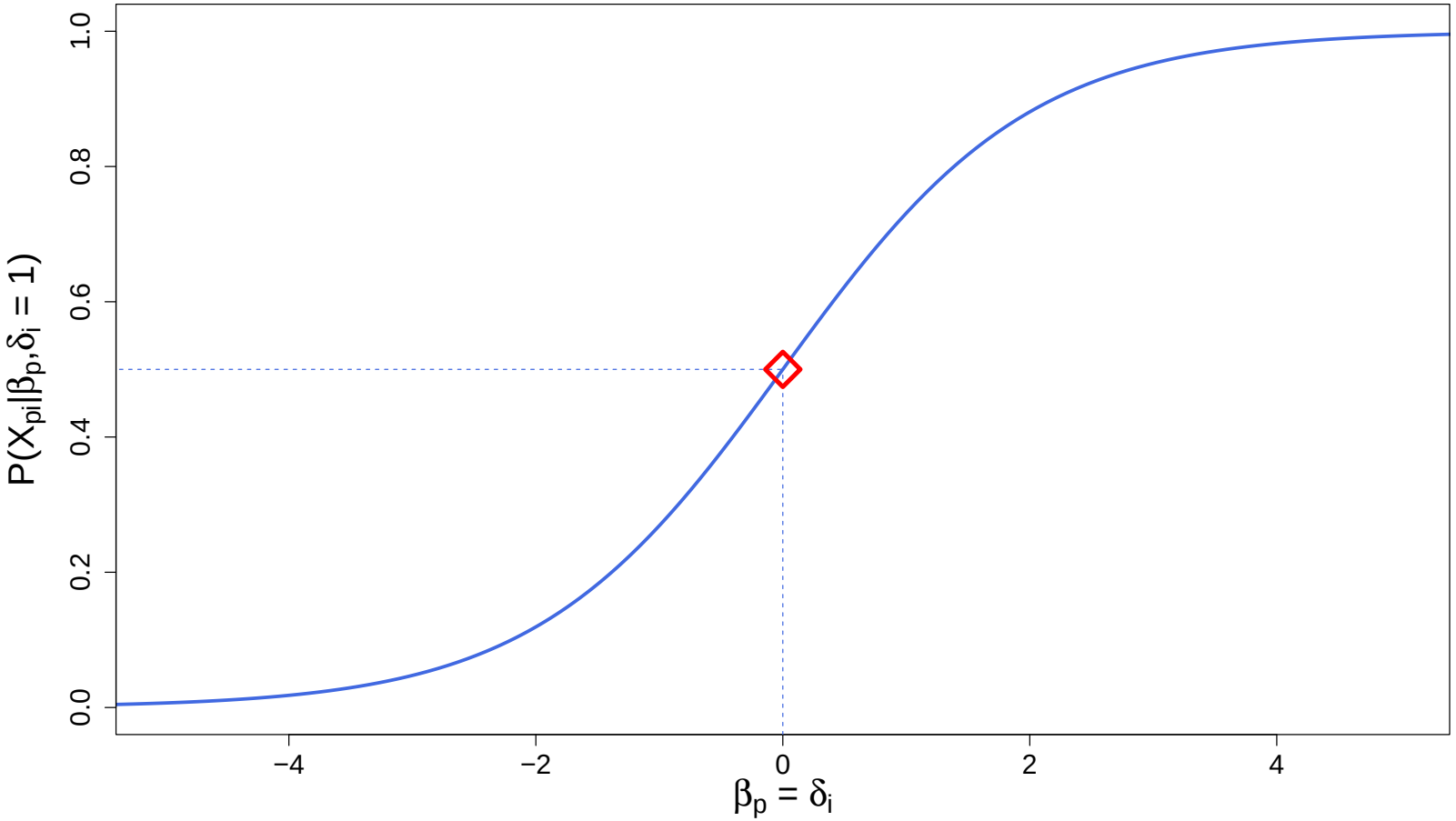
> 1 if $A_p > d_i$

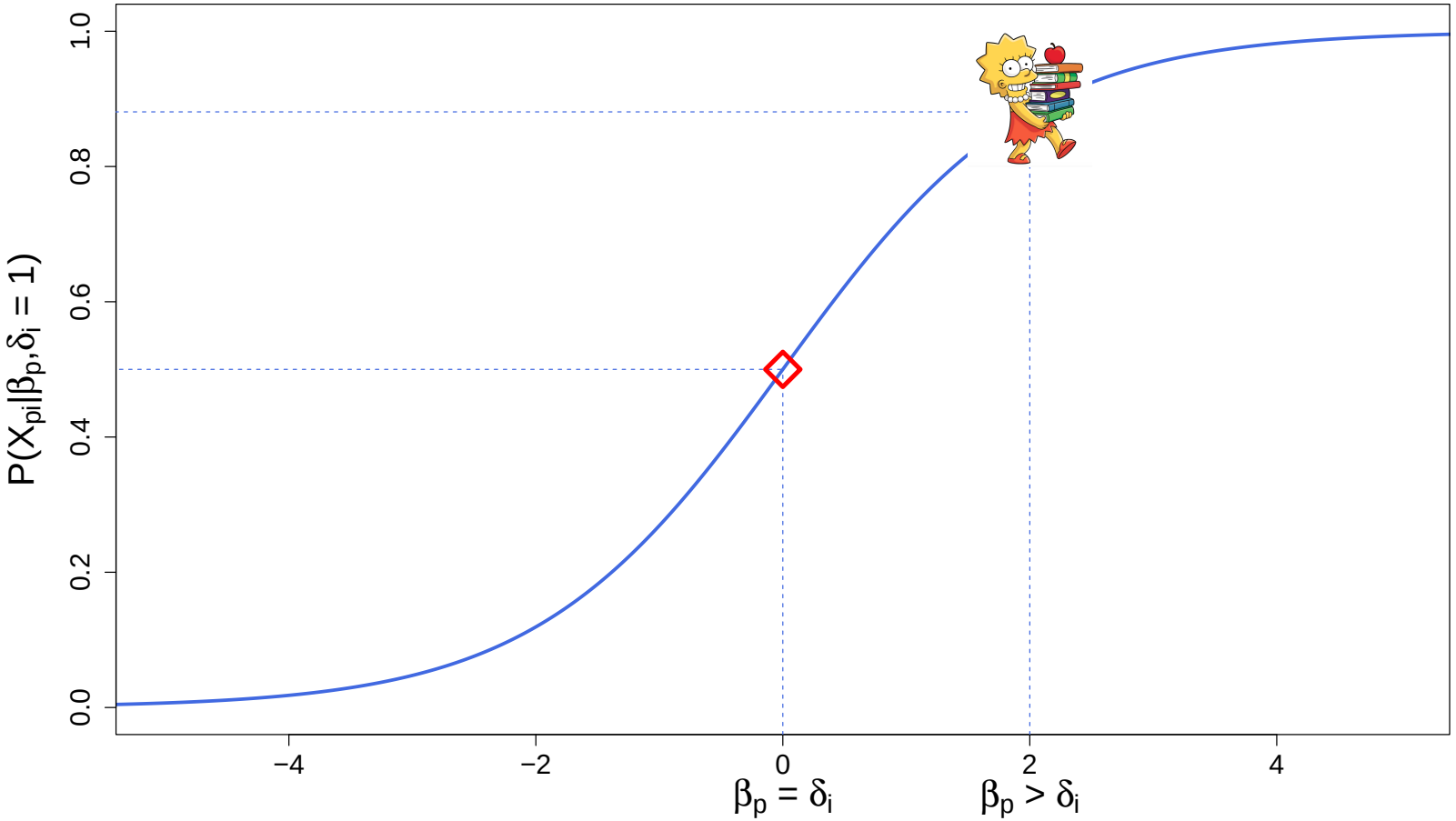
< 1 if $A_p < d_i$

$$P(X_{pi} = 1) = \frac{\frac{A_p}{d_i}}{1 + \frac{A_p}{d_i}} \qquad (2)$$

$$ln(A_p) = \beta_p \qquad ln(d_i) = \delta_i$$

$$P(X_{pi} = 1|\beta_p, \delta_i) = \frac{exp(\beta_p - \delta_i)}{1 + exp(\beta_p - \delta_i)} \tag{3}$$


1.0
0.8
0.6
0.4
0.2
0.0
P(X_pi|β_p,δ_i = 1)
−4
−2
0
2
4
β_p = δ_i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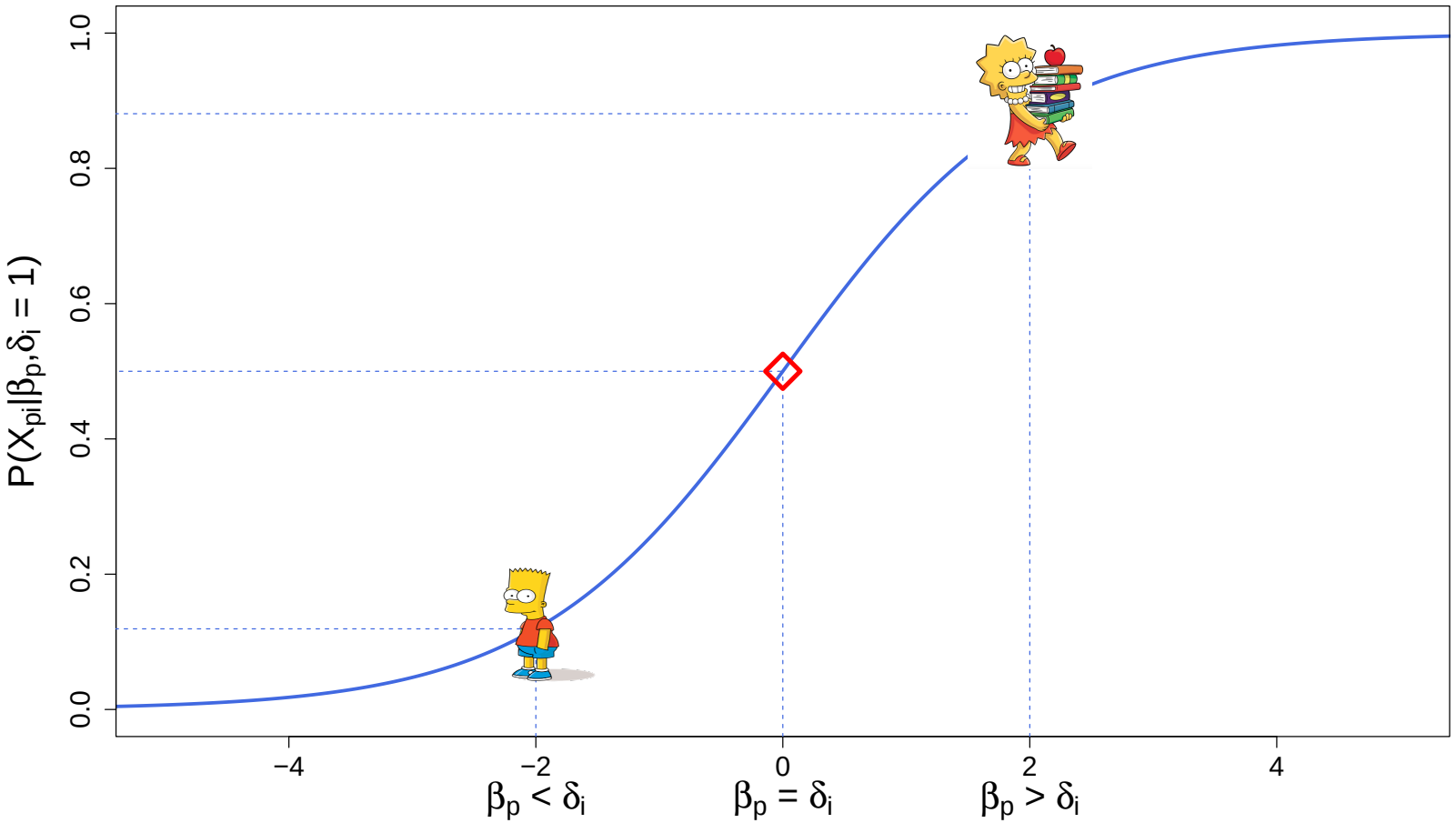
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β_p < δ_i
β_p = δ_i
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* Eureka moment *

Generalized Linear Model (GLM)
binomially distributed responses

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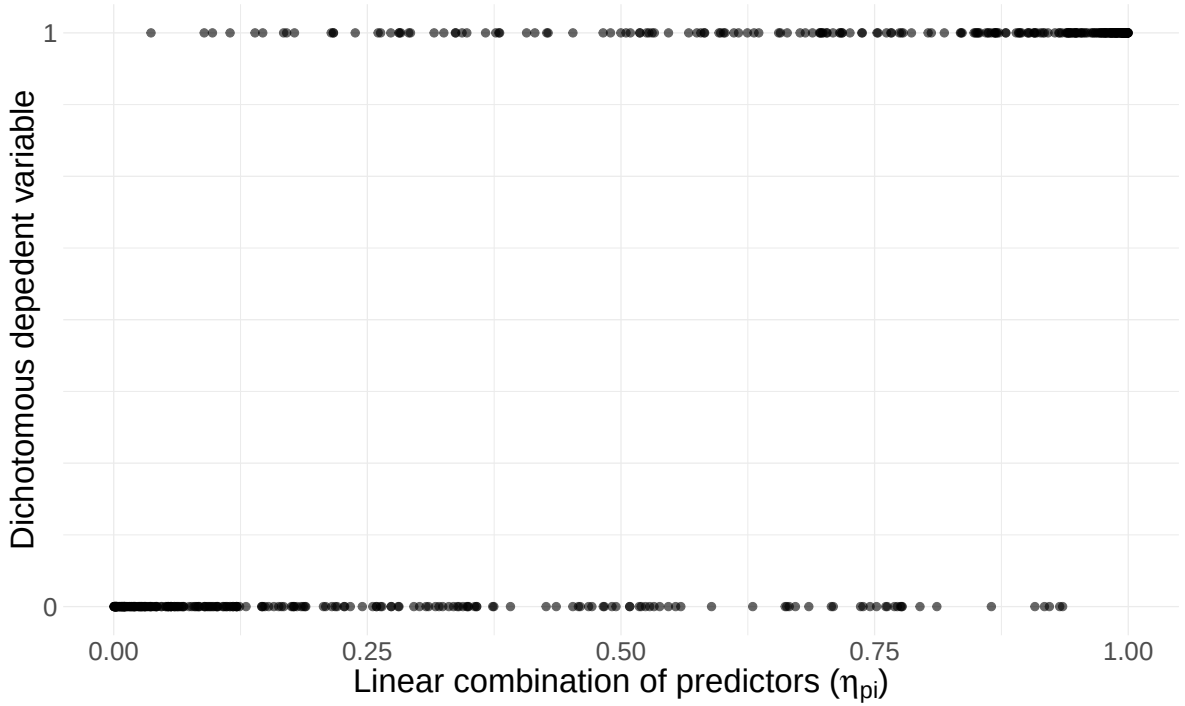
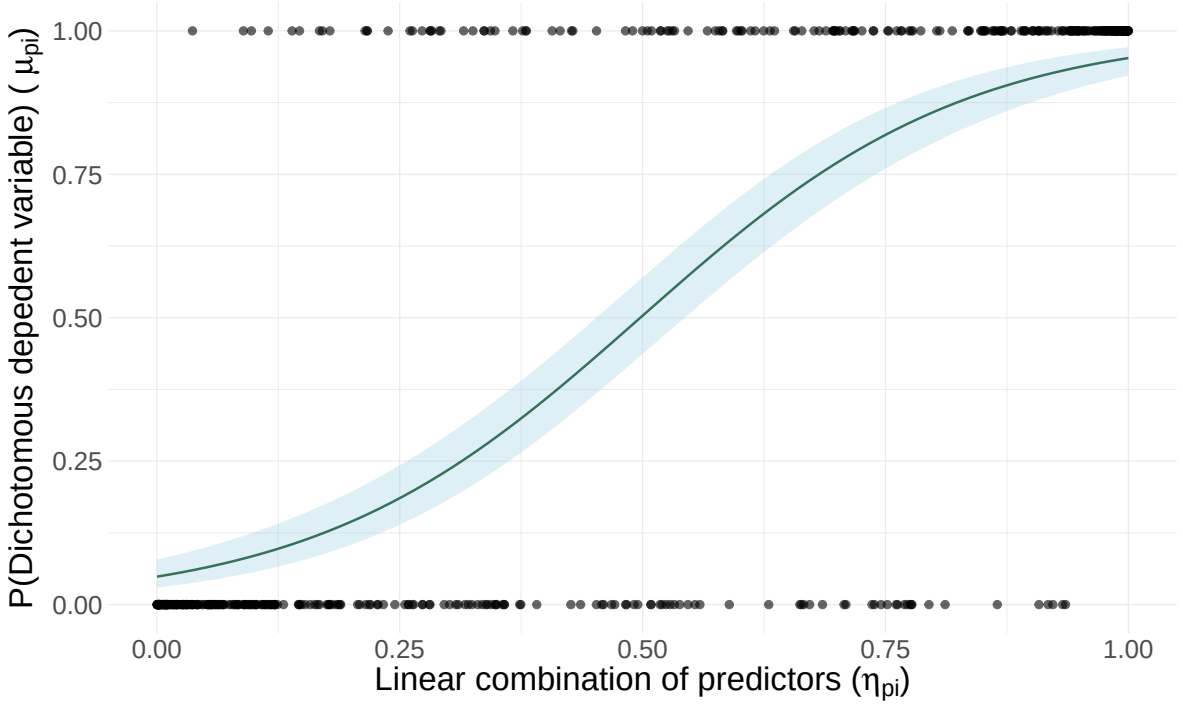
binomially distributed responses



$$\mu_{pi} = g(\eta_{pi}) = log\left(\frac{\mu_{pi}}{1-\mu_{pi}}\right)$$

Generalized Linear Model (GLM)
binomially distributed responses



$$\mu_{pi} = g(\eta_{pi}) = log\left(\frac{\mu_{pi}}{1-\mu_{pi}}\right)$$

$$g^{-1} = \frac{exp(\eta_{pi})}{1+exp(\eta_{pi})}$$

Rasch model: Dichotomous responses

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Issue

Quite limiting in Psychological Research

Rasch model: Dichotomous responses

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(Generalized) Linear Model: "Any" kind of response

Rasch model: Dichotomous responses

Issue

Quite limiting in Psychological Research

(Generalized) Linear Model: "Any" kind of response

e.g.: Response times

log-transformation and log-normal model parametrization

- **Linearity of the scores**
  Logarithm transformation → Respondents and items on the same latent trait
- **Comparison invariance**
  Respondents can be compared between each other without considering the items....and vice versa!
- **Local independence**
  Given the person → The responses to the items are independent

Unidimensionality

- **Linearity of the scores**

  Logarithm transformation → Respondents and items on the same latent trait

- **Comparison invariance**

  Respondents can be compared between each other without considering the items....and vice versa!

- **Local independence**

  Given the person → The responses to the items are independent

	Condition A	Condition B
Giorgio		
Giulia		
Jessica		

	Condition A	Condition B
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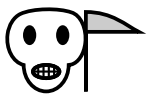

Local independence

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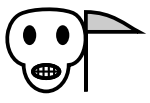
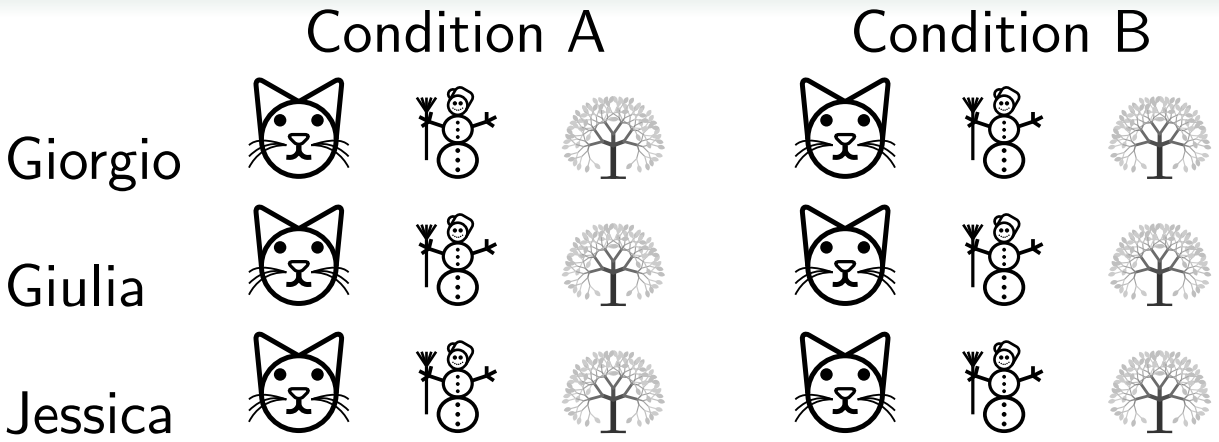
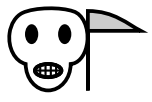


Local independence

Rasch model

Generalized Linear Model





Local independence

Rasch model

- Can't be applied
- The estimates would make no sense

Generalized Linear Model

- Add the random part (Go Mixed)
- Obtain a Rasch-like parametrization of the data

Think outside of the box!

Yes

But

Think outside of the box!

Yes

Rasch estimates

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Rasch-like parametrization

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Rasch estimates

The sky is the limit

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Rasch-like parametrization

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Thank you

Questions!