## Questionnaires and beyond: The Rasch model

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Antani convegno AIP







The intuition

The model

Wait...

Q1

$$4 + 5 = ?$$

Q2

$$\frac{3}{2} + \frac{5}{4} = ?$$

Q1

$$4 + 5 = ?$$

 $I_{q1}$ 

Q2

$$\frac{3}{2} + \frac{5}{4} = ?$$



Q1

 $d_{q1}$ 

 $A_{\mathsf{Bart}}$ 

$$rac{A_p}{d_i}$$
 (1)
 $> 1 ext{ if } A_p > d_i$ 
 $< 1 ext{ if } A_p < d_i$ 

Q2

$$\frac{3}{2} + \frac{5}{4} = ?$$
 $d_{q2}$ 



 $A_{\mathsf{Lisa}}$ 

$$P(X_{pi} = 1) = \frac{\frac{A_p}{d_i}}{1 + \frac{A_p}{d_i}}$$
 (2)

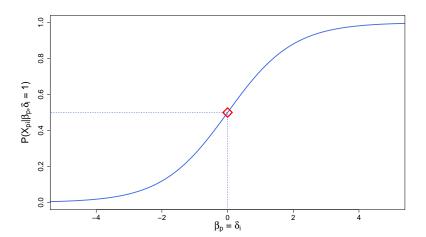
- The intuition
- 2 The model

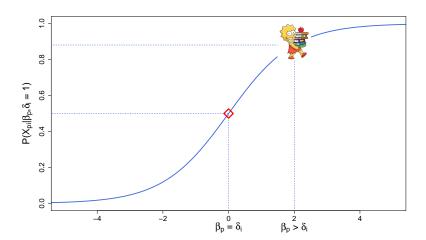
Wait...

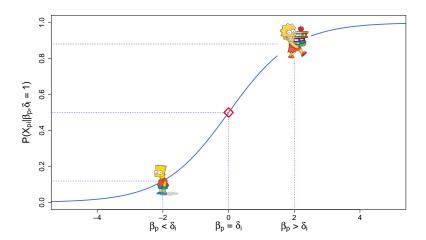


$$ln(A_p) = \beta_p$$
  $ln(d_i) = \delta_i$ 

$$P(X_{vi}|\beta_p, \delta_i) = \frac{\exp(\beta_p - \delta_i)}{1 + \exp(\beta_p - \delta_i)}$$
(3)







The intuition

The mode

Wait...

The intuition

The mode

Wait...



Sono illustrati solo alcuni dei possibili k campioni

Popolazion

 $M_3$ 

 $M_4$ 

 $M_1$ 

 $M_2$ 

 $M_5$ 

Statistica

 $\mu_{\bar{X}} = \mu$ 

## N.B.:

Sono illustrati solo alcuni dei possibili k campioni

Distribuzione

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