Test length doesn't matter, it's how you use the items that counts: An intelligent procedure for item selection in Item Response Theory

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Social Sciences







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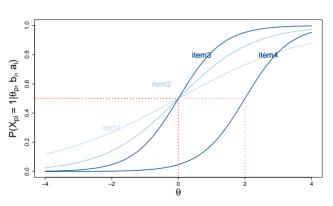
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### AIM

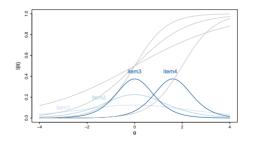
New automated procedure for item selection in IRT that only requires the definition of the desired characteristics of a test

$$P(x_{pi} = 1 | \theta_p, b_i, a_i) = \frac{\exp[a_i(\theta_p - b_i)]}{1 + \exp[a_i(\theta_p - b_i)]}$$

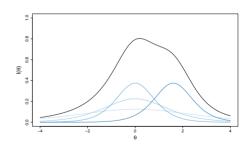


 $\theta_p$ : Latent trait level of person p  $b_i$ : Location of item i on  $\theta$   $a_i$ : Discrimination ability of item i

# Item Information Function (IIF): $I_i(\theta) = a_i^2 P_i(\theta, b_i, a_i) [1 - P_i(\theta, b_i, a_i)]$



# Test Information Function (TIF): $I(\theta) = \sum_{i=1}^{N} I_i(\theta)$



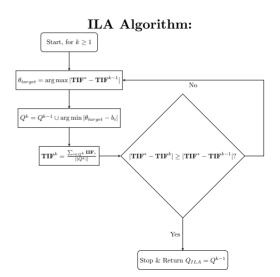
# Set up:

N: number of items included in the item bank

 $Q^k$ : Set of item indexes selected for inclusion in the STF up to iteration  $k \ (Q^0 = \emptyset)$ 

**TIF**\*: TIF target

$$\mathbf{TIF}^0 = (0, 0, \dots, 0)$$



For each  $Q_m \subset Q$  with  $Q_m \neq \emptyset$ , calculate:

$$\mathbf{1} \mathbf{TIF}^{Q_m} = \frac{\sum_{i \in Q_m} IIF_i}{||Q_m||}$$

$$Q_{BFP} = \arg\min_{\emptyset \neq Q_m \subset Q} \overline{\Delta}_{\mathbf{TIF}^{Q_m}}$$

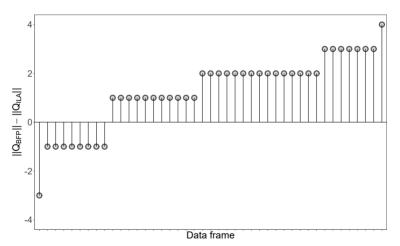
## 100 data frames:

- ① Generate an item bank B of N=6 items:
  - Difficulty parameters:  $\mathcal{U}(-3,3)$
  - Discrimination parameters:  $\mathcal{U}(.90, 2.0)$
- 2 Random item selections of lengths l from B ( $M_l = 3.34 \pm 1.13$ ) + modification parameters  $\mathcal{U}(-0.20, 0.20) \to \mathbf{TIF}^*$
- 3 Considering **TIF**\* at Step 2 and item parameters at Step 1:
  - ILA  $\rightarrow$  Forwardly searches
  - $\bullet$  BFP  $\rightarrow$  Systematically tests

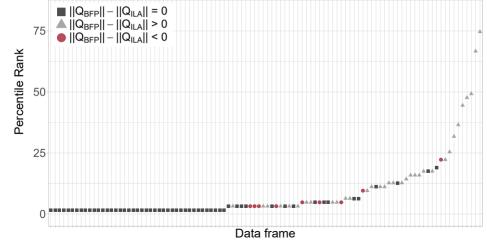
# Comparison:

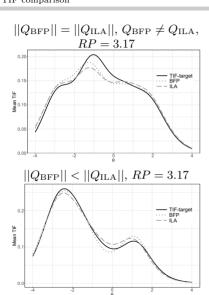
- $\qquad \qquad ||Q_{\mathrm{BFP}}|| ||Q_{\mathrm{ILA}}||$
- ullet Percentile rank of the distance  $\mathbf{TIF}_{\mathrm{BFP}} \mathbf{TIF}_{\mathrm{ILA}}$

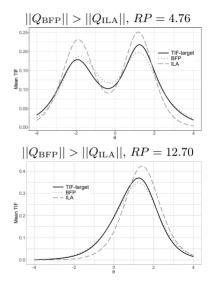
$$||Q_{\text{BFP}}|| - ||Q_{\text{ILA}}|| = 0 \text{ in } 57\% \text{ of cases}$$



ILA  $\sqsubseteq_{\mathrm{Simulation\ Study}}$  $\sqcup_{\text{Distance}}$ 100 







# Pros of ILA

- It selects items that are able to recreate the desired characteristics of a test (usually)
- It is computationally "Light"

# Cons of ILA

- It grounds its selection on a single  $\theta_{target}$  at a time  $\rightarrow$  it might select items minimizing the distance on that target but that are not very useful for the test
- It only forwardly searches an item  $\rightarrow$  once it is in, it can't get out
- It does not account for the discrimination parameters of the items