#### 01-PRactice

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- 2 Compute sum scores
- 3 Graphics
- 4 Esport graphs
- 5 R for statistical computing
- 6 Classical hypothesis testing in R
- 7 Generalized Linear Models (GLMs)

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### Import csv

6 1370.0146

954.3540

5

6

m

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- Sum across columns → sum scores of the respondents rowSums() (rowMean() for computing the mean)
- Sum across rows (righe) → sum scores of the items colSums() (colMean() for computing the mean)

## **Well-being**

```
library(readxl)
benessere = read xlsx("data/datiBenessere.xlsx")
head(benessere,2)
# A tibble: 2 \times 19
           età genere frat item1 item2 item3 item4 item5 au1
  <dbl> <dbl
            16
                                                       3
                                                                     5
                                                                     5
            21
  i 6 more variables: au5 <dbl>, au6 <dbl>, au7 <dbl>, au8 <dbl>, a
    au10 <dbl>
```

rowSums(benessere)

rowSums():

```
[1]
     65
              88
                 74
                       75
                            83
                                78
                                     79
                                         85
                                              87
                                                       88
                                                           83
                                                                     92 1
         79
                                                   80
                                                                84
             112 105
                       98
                            86
                                94
                                     94 120 108
                                                   98 100 107 111
```

"au7"

They must present a regular expression (common root):

colnames (benessere)

```
[1] "ID" "età" "genere" "frat" "item1" "item2"
"item3" "item4"
[9] "item5" "au1" "au2" "au3" "au4" "au5" "au6"
```

[17] "au8" "au9" "au10"

Columns with item  $\rightarrow$  well-being items

Columns with au  $\rightarrow$  self-esteem items

grep()e grep1(): functions for filtering data according to a regular expression (regex)

```
grep("regex", vector)
```

```
Same functioning, different results
(my vector = colnames(benessere))
```

```
[1] "TD"
               "età"
                         "genere" "frat"
                                             "item1"
                                                       "item2"
                                                                 "item3"
                                                                           "item4
 [9] "item5"
                                             "au4"
                                                                           "au7"
               "au1"
                         "au2"
                                   "au3"
                                                       "au5"
                                                                 "au6"
[17] "au8"
                         "au10"
               "au9"
grep()
grep("au", my_vector)
```

[1] 10 11 12 13 14 15 16 17 18 19

```
grepl("au", my_vector)
```

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grepl()

[1] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE TRUE TRUE. TRUE TRUE TRUE TRUE TRUE

## Compute sum scores

```
rowSums() conditioned on specific columns:
cat(rowSums(benessere[, grep("item", colnames(benessere))])[1:15],
```

```
14 14 13 13 17 10 16 16 9 13 14 16 17 12 9 ...
```

Assign to a new column (new variable)

```
benessere$score_ben = rowSums(benessere[, grep("item", colnames(benessere))
```

### summary()

```
babies <- read.table("data/babies.tab")
summary(babies$peso)</pre>
```

```
Min. 1st Qu. Median Mean 3rd Qu. Max. 5.411 7.809 9.429 9.970 11.268 17.343
```

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#### data set

#### summary(babies)

id

Length:10	Length:10	Min. : 5.411	Min.
Class :character	Class :character	1st Qu.: 7.809	1st Q
Mode :character	Mode :character	Median : 9.429	Media
		Mean : 9.970	Mean
		3rd Qu.:11.268	3rd Q
		Max. :17.343	Max.

genere

peso

### table()

table(babies\$genere)

f m

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genere

```
benessere = read.csv("data/benessere.csv", header = T)
# creo una nuova variabile dicotomica per descrivere
# il livello di benessere
benessere new benessere = with (benessere,
                                ifelse(benessere > mean(benessere),
                                       "alto".
                                       "basso"))
with(benessere, table(new_benessere, genere))
```

new benessere alto 22 18 basso 32 28

# table() and percentages

#### Single variable

```
(table(babies$genere)/nrow(babies))*100
```

coRso

```
f m 60 40
```

#### Multiple variables

```
my_perc = with(benessere, table(new_benessere, genere))
(my_perc = cbind(my_perc, rowSums(my_perc)))
```

```
f m
alto 22 18 40
basso 32 28 60
```

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```
# ta-dan!
my_perc/my_perc[,3]
```

f m
alto 0.5500000 0.4500000 1
basso 0.5333333 0.4666667 1

Aggregate a response variable according to grouping variable(s) (e.g., averaging per experimental conditions):

```
# one depenent variable (y) and single grouping variable
aggregate(y ~ x, data = data, FUN, ...)
```

```
# Multiple response variables, multiple grouping variables
aggregate(cbind(y1, y2) ~ x1 + x2, data = data, FUN, ...)
```

## **Aggregating: Examples**

benessere = read.csv("data/benessereScores.csv", header = T,
head(benessere)

```
età genere frat item1 item2 item3 item4 item5 au1 au2 au
       16
                                           4
                                                   3
                                                               5
                                                          3
                                                               5
      21
                                           3
                                                   4
   3
       28
                                           5
                                                               4
       15
                                                                   5
                                                               4
                                    5
                                                   5
                                                               3
   5
      23
   6
       31
                                    3
                                                   1
                                                               5
  au8 au9 au10 score ben score au
         2
    4
                          14
                                    33
    5
                          14
                                    40
3
    4
                          13
                                    38
```

```
aggregate(score_au ~ genere, data = benessere, mean)
```

```
genere score au
```

1 33.08750 2 32.62857

Compute the mean according of self esteem and well being according to gender

```
aggregate(cbind(score_ben, score_au) ~ genere, data = benesse
```

```
genere score_ben score_au
```

- 1 14.46250 33.08750 1
- 2 14.41429 32.62857



- Recode frat and assign it to a new var into the data frame (siblings: > 0 siblings  $\to$  no >> 1+ sibilings  $\to$  yes
- Compute the mean of score\_ben according to siblings
- Compute the mean of score\_ben and score\_au according to sibilingsand gender (assign it to the object mean\_dep)
- Compute the standard deviation of score\_ben and score\_au according to sibilingsand gender (assign it to the object sd\_dep)
- merge mean\_dep and sd\_dep and assign the resulting object to descr

#### **WARNING!**

When using merge the column names must be different

OME, UniPD (Lezioni UniCatt)

### Result

#### descr

	siblings	genere	${\tt mean\_score\_ben}$	mean_score_au	sd_score_ben	sd_score_au
1	no	1	13.90909	33.27273	3.250042	4.452734
2	no	2	14.51852	32.11111	3.309315	3.004270
3	yes	1	14.67241	33.01724	3.347625	3.743961
4	ves	2	14.34884	32.95349	3.228472	4.396717

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```
benessere$siblings = ifelse(benessere$frat == 0, "no", "yes")
mean_dep = aggregate(cbind(score_ben, score_au) ~ siblings + genere,
                     data = benessere.
                     mean)
colnames(mean_dep)[3:4] = paste("mean",
                                colnames (mean_dep) [3:4],
                                 sep = " ")
sd_dep = aggregate(cbind(score_ben, score_au) ~ siblings + genere,
                     data = benessere.
                   sd)
colnames(sd_dep)[3:4] = paste("sd", colnames(sd_dep)[3:4],
                              sep = "_")
descr = merge(mean_dep, sd_dep)
```

coRso

### tidyverse()

```
install.packages("tidyverse")
library(tidyverse)
```

### tidyverse()

```
install.packages("tidyverse")
library(tidyverse)
\begin{center}
\text{texttt}{%>%} (Pipe)
\end{center}
Use the combo shift + ctrl + M
Logic:
object %>%
  grouping %>%
  function
```

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```
benessere %>% # object
  group_by(siblings, genere) %>% # groupings
  summarise(m_benessere = mean(score_ben), # functions
            sd benessere = sd(score ben),
            m au = mean(score au),
            sd au = sd(score au))
# A tibble: 4 x 6
```

```
# Groups: siblings [2]
  siblings genere m_benessere sd_benessere m_au sd_au
  <chr>
           <int>
                       <dbl>
                                     <dbl> <dbl> <dbl>
1 no
                         13.9
                                     3.25 33.3 4.45
                         14.5
                                     3.31 32.1 3.00
2 no
                         14.7
                                     3.35 33.0 3.74
3 yes
                         14.3
                                     3.23 33.0 4.40
4 yes
```



- Compute minimum, maximum, median of score\_au and score\_ben with tidyverse
- Import the babies datas set and compute the descriptive stats of weight and height withtidyverse

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- Traditional graphics
- Grid graphics & ggplot2

#### For both:

- ullet High level functions o actually produce the plot
- Low level functions  $\rightarrow$  make it looks better =)

## Traditional graphics I

#### High level functions

```
plot()
           # scatter plot, specialized plot methods
boxplot()
hist()
           # histogram
qqnorm()
           # quantile-quantile plot
barplot()
pie()
          # pie chart
pairs()
           # scatter plot matrix
persp()
         # 3d plot
contour() # contour plot
coplot() # conditional plot
interaction.plot()
```

demo(graphics) for a guided tour of base graphics!

## Traditional graphics II

#### Low level functions

```
points()
                # add points
lines()
                # add lines
rect()
polygon()
abline()
                # add line with intercept a, slope b
arrows()
text()
                # add text in plotting region
mtext()
                # add text in margins region
axis()
                # customize axes
box()
                # box around plot
legend()
```

coRso

## **Plot layout**

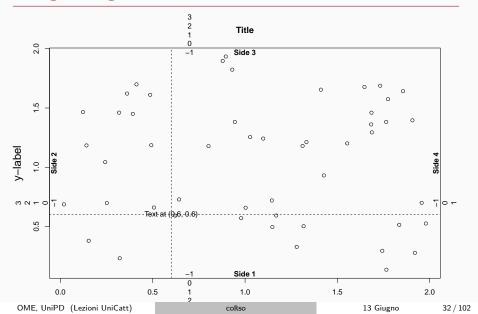
Each plot is composed of two regions:

- The plotting regions (contains the actual plot)
- The margins region (contain axes and labels)

#### Now add some text:

```
text(0.6, 0.6, "Text at (0.6, 0.6)")
abline(h=.6, v=.6, lty=2) # horizont. and vertic.
# lines
```

# Margins region



### Rome wasn't built in a day and neither your graph

Display the interaction between the two factors of a two-factorial experiment:

```
dat <- read.table(header=TRUE, text="
A B rt
a1 b1 825
a1 b2 792
a1 b3 840
a2 b1 997
a2 b2 902
a2 b3 786
")</pre>
```

Force A and B to be factor:

```
dat[,1:2] = lapply(dat[,1:2], as.factor)
```

## Modificare il layout dei plot

#### Vanno creati dei pannelli

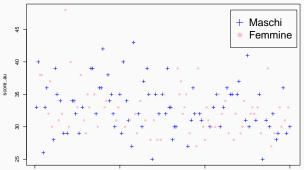
```
par(mfrow=c(nrighe, ncolonne)) # pannelli vengono riempiti per riga
par(mfcol=c(nrighe, ncolonne)) # pannelli vengono riempiti per colo
```

# plot()

```
plot(x) # solo una variabile
plot(x, y) # due variabile (scatter plot)
plot(y ~ x) # due variabile, y in funzione di x
```

# Esempi: plot(x)

```
with(benessere,
     plot(score_au,
          col = ifelse(genere == 1, "blue", "pink"),
          pch = ifelse(genere == 1, 3, 16)))
legend(x = 115, y = 48,
       c("Maschi", "Femmine"), pch = c(3, 16),
       col =c("blue", "pink"), cex = 2)
```

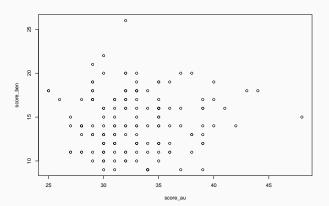


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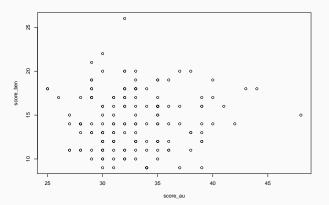
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## Esempi: plot(x, y)

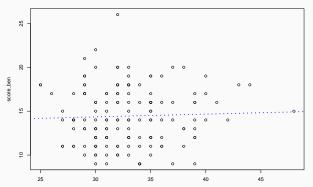
```
with(benessere,
    plot(score_au, score_ben))
```



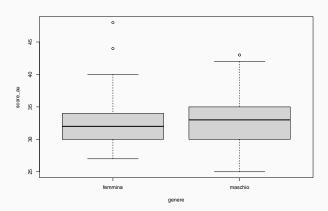
```
with(benessere,
    plot(score_ben ~ score_au))
```



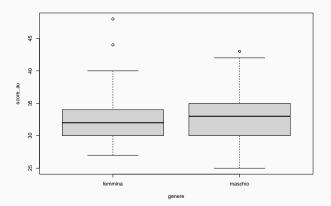
# Esempi: plot(y ~ x) con retta di regressione



## Esempi: plot(y ~ x) con x categoriale

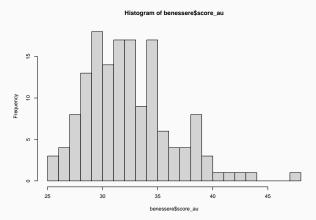


boxplot(score\_au ~ genere, data = benessere)



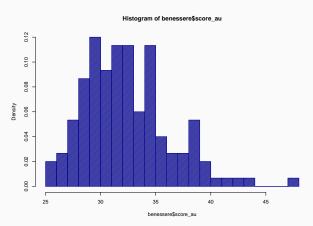
## hist(): Frequenze

hist(benessere\$score\_au, breaks = 20)



## hist(): Densità

#### Densità

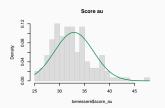


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# Multi plot (in riga)

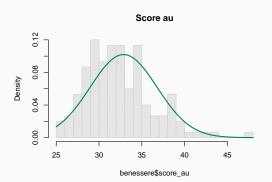
```
par(mfrow=c(1, 2))
hist(benessere\$score_au,density=\frac{50}{0}, breaks=\frac{20}{0}, prob=\frac{TRUE}{0},
     main = "Score au")
curve(dnorm(x, mean=mean(benessere$score_au),
              sd=sd(benessere$score_au)),
       col="springgreen4", lwd=2, add=TRUE, yaxt="n")
```

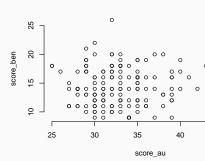
[...]



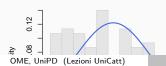


# Multiplot (in colonna)





#### Score benessere





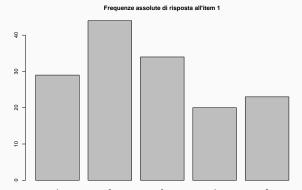


# Multiplot (in colonna), codice

```
par(mfcol = c(2,2))
hist(benessere\$score_au,density=\footnote{50}, breaks=\footnote{20}, prob=\footnote{TRUE},
     main = "Score au")
curve(dnorm(x, mean=mean(benessere$score_au),
             sd=sd(benessere$score au)),
      col="springgreen4", lwd=2, add=TRUE, yaxt="n")
hist(benessere$score ben,density=50, breaks=20, prob=TRUE,
     main = "Score benessere")
curve(dnorm(x, mean=mean(benessere$score ben),
             sd=sd(benessere$score ben)),
      col="royalblue", lwd=2, add=TRUE, yaxt="n")
with (benessere,
     plot(score_au, score_ben, frame = FALSE))
```

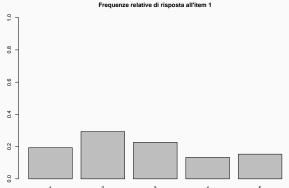
## barplot(): Frequenze assolute

Per creare i grafici a barre quando si hanno variabili discrete o categoriali

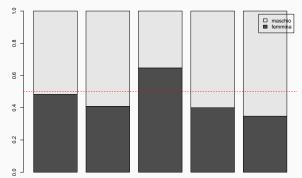


## barplot(): Frequenze relative

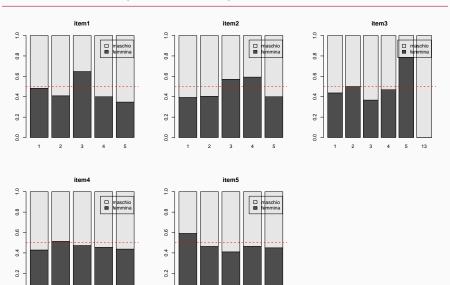
Richiede uno step in più ightarrow la creazione della tabella delle frequenze



# barplot() con più variabili



# Un altro esempio di multiplot



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```
item_ben = benessere[, grep("item", colnames(benessere))]
par(mfrow = c(2, round(ncol(item_ben)/2 + 0.2)))
temp = NULL
for (i in 1:ncol(item_ben)) {
 temp = table(benessere$genere, item_ben[,i])
 for (j in 1:nrow(temp)) {
    temp[j,] = temp[j,]/table(item_ben[,i])
barplot(temp, ylim=c(0,1), legend = rownames(temp),
        main = colnames(item_ben)[i])
abline(h = .5, ltv = 2, col = "red")
```

### interaction.plot()

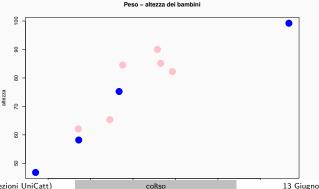
Permette di vedere l'interazione tra due variabili a seconda di una terza variabile:

interaction.plot(x, v. categoriale, y)

Permette di vedere l'interazione tra due variabili a seconda di una terza variabile:

interaction.plot(x, v. categoriale, y)

La relazione tra peso e altezza cambia a seconda del genere?

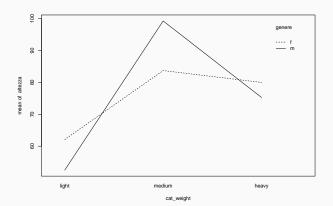


```
babies$cat weight = with(babies,
                          ifelse(
                            peso <= quantile(babies$peso)[2],</pre>
                            "light",
                            ifelse(peso > quantile(babies$peso)[2] &
                                      peso > quantile(babies$peso)[4],
       "medium".
       "heavy")))
babies$cat_weight = factor(babies$cat_weight,
                            levels = c("light",
                                        "medium",
                                        "heavy"))
```

#### babies

```
id genere
                              altezza cat weight
                        peso
                   7.424646 62.07722
    baby1
                                             light
1
2
                   7.442727 58.18877
    baby2
                                             light
                m
3
    baby3
                f
                   9.512598 84.52737
                                            heavy
4
    baby4
                f 11.306349 85.13573
                                           medium
5
    baby5
                   9.345165 75.23783
                                            heavy
    hahy6
                   5.411290 46.80163
                                             light
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                                     coRso
```

interaction.plot(cat\_weight, genere, altezza))



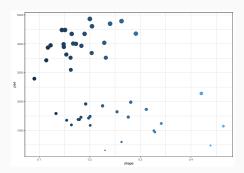
## ggplot2

ggplot2 (Grammar of Graphics plot, Wickman, 2016) is one of the best packages for plotting raw data and results:

```
install.packages("ggplot2"); library(ggplot2)

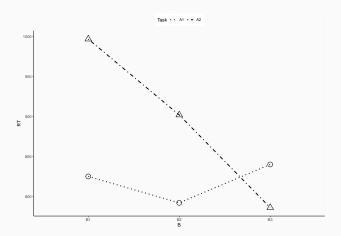
ggplot(data,
    ars(x = var.x,
        y = var.y,
        col = var.color, # factor or character
    fill = var.filling, # factor or character
    shape = var.shape, # actor or character
    size = var.size, # numeric
    ...)) + geom_graph.type() + ...
```

## Raw data

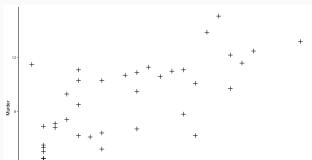


```
ggplot(dat, aes(x = B, y = rt, group = A)) +
  geom point(pch=dat$A, size = 5) +
  geom line(aes(linetype=A), size=1) + theme classic() +
  vlab("RT") + scale linetype manual("Task", values = c(3,4),
                                labels = c("A1", "A2")) +
  scale_x_discrete(labels = c("B1", "B2", "B3")) +
  theme(legend.position="top",
        panel.background = element rect(fill = "#FAFAFA",
                                         colour = "#FAFAFA"),
        plot.background = element_rect(fill = "#FAFAFA"),
        legend.key = element_rect(fill = "#FAFAFA"))
```

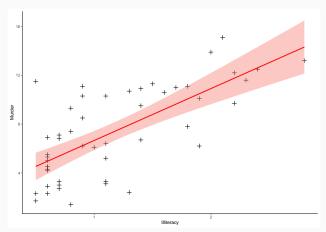
## The result



## **Scatter plot**



### Linear model



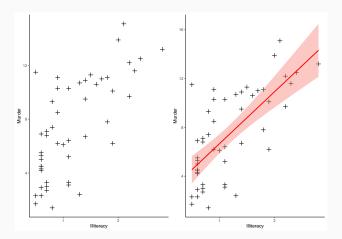
# Different plots in the same panel

```
use grid.arrange() function from the gridExtra package:
```

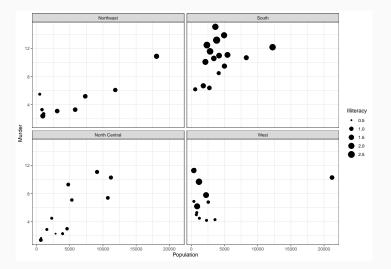
```
install.packages("gridExtra"); library(gridExtra)
murder_raw = ggplot(states, # raw data
               aes(x = Illiteracy, y = Murder)) +
murder_lm = ggplot(states, # lm
               aes(x = Illiteracy, y = Murder)) +
```

#### Combine the plots together:

```
grid.arrange(murder_raw, murder_lm,
             nrow=1) # plots forced to be the same row
```



## Multi Panel



```
states = data.frame(state.x77, state.name = state.name,
                    state.region = state.region)
ggplot(states,
       aes(x = Population, y = Murder,
           size = Illiteracy)) + geom point() +
  facet_wrap(~state.region) + theme_bw()
```

## boxplot() e violinplot()

#### Data need to be in long format:

id condition mean time

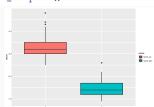
	Iu	Condition	mean_time
1	sbj1	Α	3.477760
2	sbj1	В	1.748681
3	sbj2	Α	2.405326
4	sbj2	В	2.915242
5	sbj3	Α	3.294477
6	sbi3	В	2.763332

```
small = benessere[, c("ID", "score_au", "score_ben")]
score_long = reshape(small,
    idvar = "ID",
    times =names(small)[-1],
    timevar = "score", v.names = "value",
    varying = list(names(small)[-1]),
    direction = "long")
head(score long)
```

```
ID score value
1.score_au 1 score_au 33
2.score_au 2 score_au 40
3.score_au 3 score_au 38
4.score_au 4 score_au 38
5.score_au 5 score_au 26
6.score_au 6 score_au 33
```

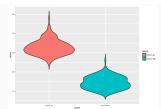
#### **Boxplot**

```
ggplot(score_long,
       aes(x = score, y = value,
           fill = score)) +
  geom_boxplot()
```

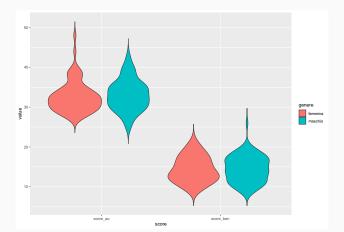


#### Violinplot

```
ggplot(score_long,
       aes(x = score, y = value,
           fill = score)) +
  geom_violin(trim = FALSE)
```



```
ggplot(score_long,
       aes(x = score, y = value,
           fill = genere)) + geom_violin(trim = FALSE)
```



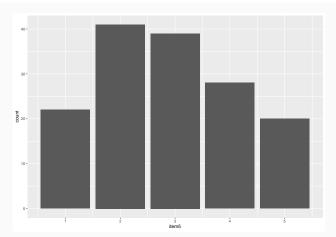
## barplot and histogram

```
geom_hist(): histogram (continuous variables)
geom_bar(): bar plot
```

#### Arguments:

- geom\_bar(stat = "count"): automatically counts the frequencies for each category, does not need a y variable
- geom\_bar(stat = "identity"): plots a value associated to each category does need a y variable

## geom\_bar(stat = "count"):



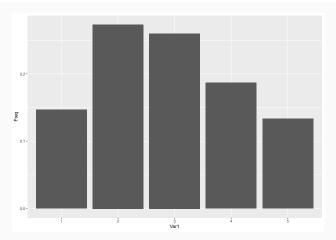
```
item_5 = data.frame(table(benessere$item5)/nrow(benessere))
item 5
```

```
1 0.1466667
     2 0.2733333
3
     3 0.2600000
     4 0.1866667
5
     5 0.1333333
```

Freq

Var1

```
ggplot(item_5,
       aes(x = Var1, y = Freq)) + geom_bar(stat = "identity")
```



# All together

#### Long format

```
new_item = benessere[, c(grep("ID", colnames(benessere)),
                        grep("item", colnames(benessere)))]
new_item = reshape(new_item,
        idvar = "ID".
        times =names(new_item)[-1],
        timevar = "item", v.names = "value",
        varying = list(names(new_item)[-1]),
        direction = "long")
new item
```

```
TD item value
2.item1
        2 item1
3.item1
       3 item1
4.item1
                3
       4 item1
5.item1 5 item1
```

. . . .

# Calcolo le proporzioni

Di ogni opzione di risposta value per ogni item item

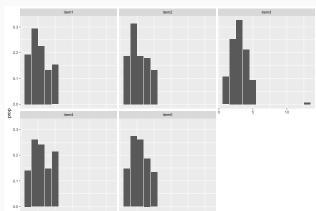
```
proporzione = new_item %>%
  group_by(item, value) %>%
  summarise(prop = n()/nrow(benessere))
```

proporzione

```
# A tibble: 26 \times 3
# Groups: item [5]
  item value prop
  <chr> <int> <dbl>
 1 item1 1 0.193
2 item1 2 0.293
```

```
The plot (finally)
```

```
ggplot(proporzione,
       aes(x = value, y = prop)) +
  geom_bar(stat = "identity") +
  facet_wrap(~item)
```



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#### In automnatico

```
pdf("nome_grafico.pdf")
png("nome_grafico.png")
tiff("nome grafico.tiff")
jpeg("nome_grafico.jpeg")
bmp("nome grafico.bmp")
```

#### Rember to turn off the graphical device

```
dev.off()
```

# Example

# **Manually**

knitr::include\_graphics("data/esporta.png")

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The stats package (built-in package in  ${\tt R}$ ) contains function for statistical calculations and random number generator

see library(help=stats)

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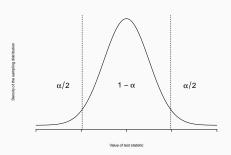
- chisq.test(): contingency table  $\chi^2$  tests
- cor.test(): association between paired samples
- t.test(): one- and two-sample t tests (also for paired data)
- lm(y ~ x1 + x2 + x3 ...): fit a linear model
- glm(y ~ x1 + x2 + x3 ...): fit a generalize linear model

# What is the *p*-value?

#### *p*-value:

conditional probability of obtaining a test stastic that is at least as extreme as the one observed, given that the null hyphothesis is true

If  $p < \alpha$  (i.e., the probability of rejecting the null hypothesis when it is true)  $\to$  the null hypothesis is rejected



#### Independence of observations

#### Hypothesis:

- $H_0$ :  $P(X_{ij} = k) = p_k$  for all i = 1, ..., r and j = 1, ..., c
- $H_0$ :  $P(X_{ij} = k) \neq P(X_{i'j} = k)$  for at least one  $i \in \{1, ..., r\}$  and  $j \in \{1, ..., c\}$

Test statistic:

$$\chi^2 = \sum_{i=1}^n \frac{(x_{ij} - \hat{x}_{ij})^2}{\hat{x}_{ij}}, \ \chi^2 \sim \chi^2(r-1)(c-1)$$

In R:

#### Correlation test

#### Hypothesis:

- $H_0$ :  $\rho_{XY} = 0$ ,  $H_1$ :  $\rho_{xy} \neq 0$
- $H_0$ :  $\rho_{XY} = 0$ ,  $H_1$ :  $\rho_{xy} < 0$
- $H_0$ :  $\rho_{XY} = 0$ ,  $H_1$ :  $\rho_{XY} > 0$

#### Test statistic:

$$T = \frac{r_{xy}}{\sqrt{1 - r_{xy}^2}} \sqrt{n - 2}, \ T \sim t(n - 2)$$

In R:

### Correlation matrix

```
cor(benessere[, grep("item", colnames(benessere))])
```

```
item1
                         item2
                                    item3
                                                 item4
                                                              it
item1
       1.00000000
                   0.07820461 0.11579134 -0.05894317 -0.18117
       0.07820461
                    1.00000000 0.24890831
                                            0.21963611 -0.07757
item2
item3
       0.11579134
                   0.24890831 1.00000000
                                            0.04977145
                                                        0.03830
item4 - 0.05894317
                   0.21963611 0.04977145
                                            1.00000000
                                                        0.05751
item5 -0.18117877 -0.07757221 0.03830005
                                            0.05751880
                                                         1.00000
```

coRso

# Two (indepdent) sample t test

Independent samples from normally distributions where  $\sigma^2$  are unknown but homogeneous

- $H_0$ :  $\mu_{x_1-x_2}=0$ ,  $H_1$ :  $\mu_{x_1-x_2}\neq 0$
- $H_0$ :  $\mu_{x_1-x_2}=0$ ,  $H_1$ :  $\mu_{x_1-x_2}<0$
- $H_0$ :  $\mu_{x_1-x_2}=0$ ,  $H_1$ :  $\mu_{x_1-x_2}>0$

Test statistic:

$$T = rac{ar{x_1} - ar{x_2}}{\sigma_{ar{x_1} - ar{y_2}}}, \ T \sim t(n_1 + n_2 - 2)$$

#### R function:

### Observations on the same sample

#### Hypothesis:

- $H_0$ :  $\mu_D = 0$ ,  $H_1$ :  $\mu_D \neq 0$
- $H_0$ :  $\mu_D = 0$ ,  $H_1$ :  $\mu_D < 0$
- $H_0$ :  $\mu_D = 0$ ,  $H_1$ :  $\mu_D > 0$

#### Test statistic:

$$T = rac{d}{\sigma_d}, \ T \sim t(m-1)$$

#### R function:

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#### **Formulae**

Statistical models are represented by formulae which are extremely close to the actual statistical notation:

in R	Model
y ~ x y ~ 0 + x	$y_i = \beta_0 + \beta_1 x_i + \varepsilon_i$ (same but short) $y_i = \beta_1 x_i + \varepsilon_i$ $y_i = \beta_0 + \beta_1 x_i + \beta_2 x_j + (\beta_1 \beta_2) x_{ij} + \varepsilon_{ij}$

#### **Linear models**

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \ldots + \beta_k x_k + \varepsilon$$

In R:

$$lm(y \sim x1 + x2 + ... + xk, data)$$

### **Extractor functions I**

## **Extractor functions II**

```
vcov()
          # Return the variance-covariance matrix of the
          # main parameters of a fitted model object
predict() # A new data frame must be supplied having the
          # same variables specified with the same labels
          # as the original. The value is a vector or
            matrix of predicted values corresponding to
          # the determining variable values in data frame
step()
          # Select a suitable model by adding or dropping
          # terms and preserving hierarchies. The model
          # with the smallest value of AIC (Akaike's
          # Information Criterion) discovered in the
          # stepwise search is returned
```

coRso

### **Generalized linear models**

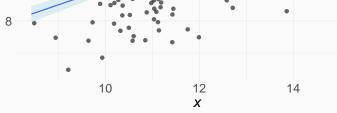
$$g(\mu) = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \ldots + \beta_k x_k + \varepsilon$$

g() is the link functions that connects the mean to the linear combination of predictors.

A GLM is composed of three elements: The response distribution, the link function, and the linear combination of predictors

In R:

$$glm(y \sim x1 + x2 + ... + xk, family(link), data)$$



#### LM: Model

```
model = lm(y ~ x, data = data)
summary(model)
```

```
Call:
```

```
lm(formula = y ~ x, data = data)
```

#### Residuals:

```
Min 1Q Median 3Q Max
-5.2559 -1.1314 0.0162 1.1889 4.4123
```

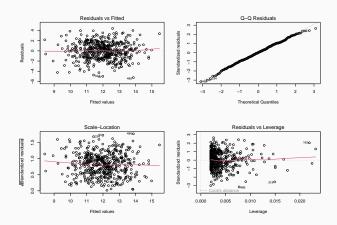
#### Coefficients:

```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

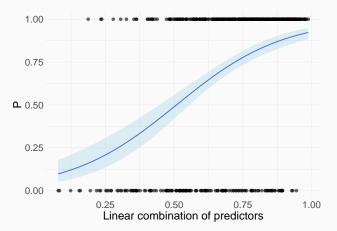
Residual standard error: 1.672 on 498 degrees of freedom Multiple R-squared: 0.3025, Adjusted R-squared: 0.3011 F-statistic: 216 on 1 and 498 DF, p-value: < 2.2e-16

# **Diagnostic**

```
par(mfrow = c(2,2))
plot(model)
```



#### **GLM:** Data



## **GLM:** Model

```
model bin <- glm(z ~x, data = data, family = "binomial")
summary(model bin)
Call:
glm(formula = z ~ x, family = "binomial", data = data)
Coefficients:
          Estimate Std. Error z value Pr(>|z|)
0.53713 0.06486 8.281 <2e-16 ***
x
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
   Null deviance: 612.55 on 499 degrees of freedom
Residual deviance: 521.91 on 498 degrees of freedom
ATC: 525.91
Number of Fisher Scoring iterations: 4
```

# Interpreting the parameters

#### **Families**

A special link function to each response variable. In R some different link functions are available by default:

## Family name	Link functions
Binomial	logit, probit, log, cloglog
gaussian	identity, log, inverse
Gamma	identity, inverse, log
inverse.gaussian	<pre>1/mu^2, identity, inverse, log</pre>
poisson	log, identity, sqrt
quasi	logit, probit, cloglog, identity, inverse,
	log, 1/mu^2, sqrt