

So simple, yet so effective

Ottavia M. Epifania

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## An example: The SNARC effect

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Small numbers: Perceived on the left

Large numbers: Perceived on the right

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## How do we investigate such an effect?

Small numbers:

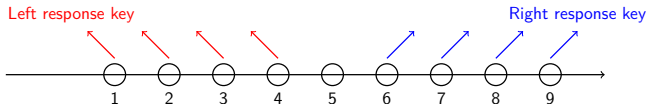
1, 2, 3, 4

Large numbers:

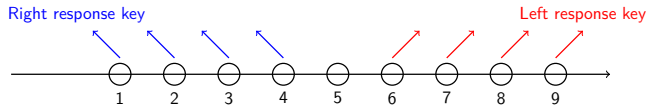
6, 7, 8, 9

Two conditions:

The “natural” one



The “innatural” one

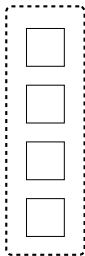


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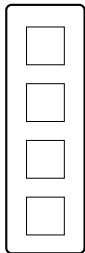
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$p_1$



$p_2$



$p_3$

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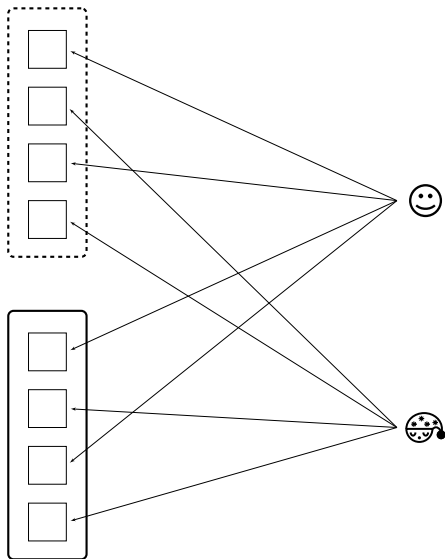
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$p_1$

$p_2$

$p_3$

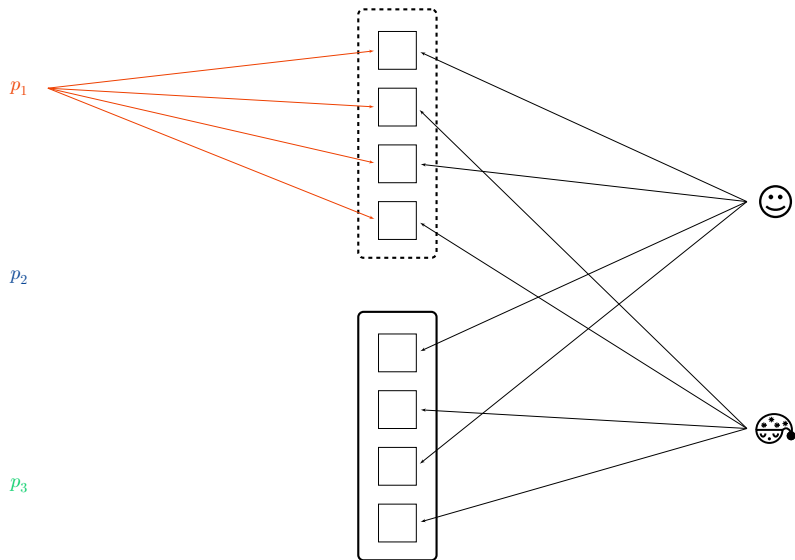




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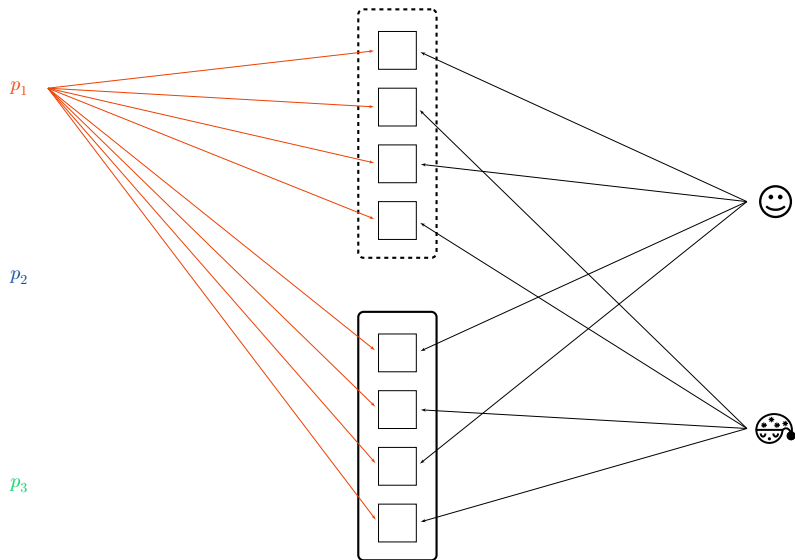
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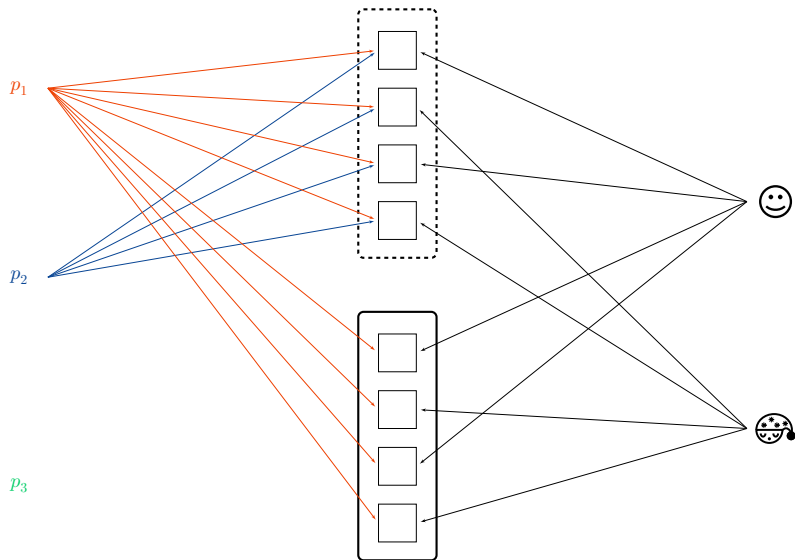
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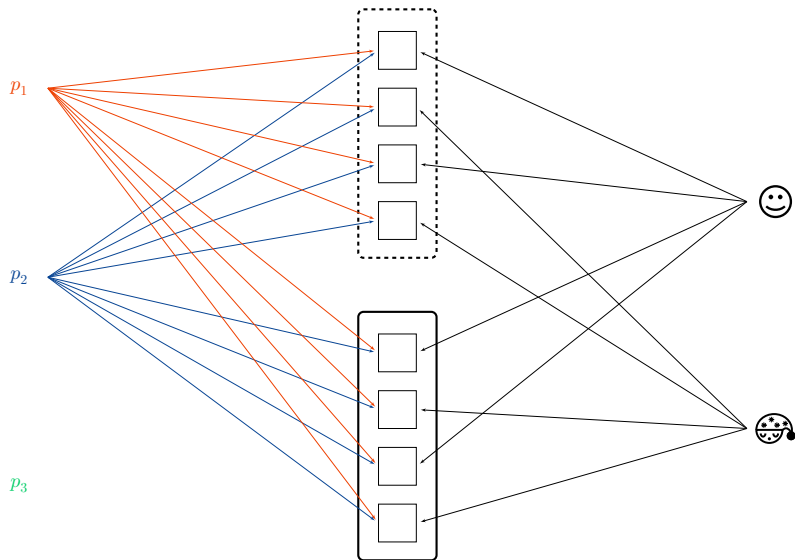
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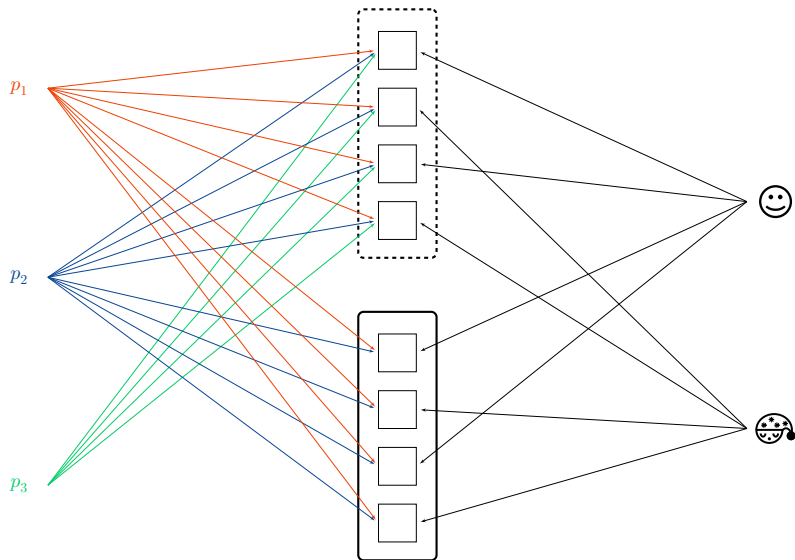
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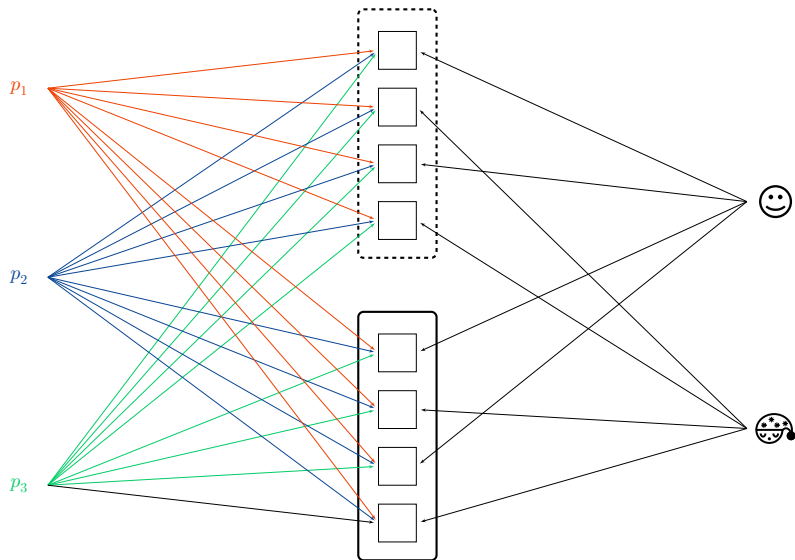
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Forse qui metterei Jane e John Does

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Every experiment where the same set of stimuli is administered multiple times within and between associative conditions within and between respondents

Sample-level differences

Individual differences



## Typical Scoring methods

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Inventa qualcosa di carino per rappresentare le medione attraverso i trial

Mettere come key concept il fatto che i soggetti sono effetti random e gli stimoli sono effetti fissi, ma che in questo ambito non ha senso perché gli stimoli sono dei rappresentati eccetera, riprendi la presentazione di Berlino

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## Issues of Typical scoring methods

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Two main big enourmous terrible issues:

- ① Completely ignore all the sources of error variance
- ② Ignoring the stimuli variability implies ignoring the information at the stimulus level

Problem 1: Linear Mixed Effects Models

Problem 2: Rasch model

The best solution: Rasch-like parametrization estimated with Linear Mixed Effects Models

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# The Rasch Model

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# A GLM for dichotomous responses

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# The log-normal model

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# A linear model

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# When psychometrics meets statistics

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La tabellina delle similarità

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Model matrix e cose varie con tanto di esempio con il gamma

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# I BLUP e le conditional modes

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# The maximal model

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Too complex

The models that are useful for one's aim

Given the structure of the experiments:

Common goal: Investigate the changes in the performance of the respondents between the associative conditions

Less common: Investigate the changes in the functioning of the stimuli between the associative conditions

# Preliminaries

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Index	Meaning	Variable
$p = 1, \dots, P$	Respondent	respondents
$s = 1, \dots, S$	Stimulus	stimuli
$c \in \{0, 1\}$	Associative condition	condition
$i$	Trial	

Accuracy:

GLMM

$$y \in [0, 1]$$

Log-time response

LMM

$$y \in [0, +\infty] \text{ (log-transformed)}$$
$$\varepsilon \sim \mathcal{N}(0, \sigma^2)$$

# Model 1

## Mathematical Notation

$$y = \beta_c X_c + \alpha_p[i] + \alpha_s[i]$$

## lme4 notation

```
y ~ 0 + condition + (1|stimuli) + (1|respondents)
```

## Rasch-like parametrization

	GLMM	LMM
respondents	$\theta_p$	$\tau_p$
stimuli	$b_s$	$\delta_s$

## Model 2

### Mathematical Notation

$$y = \beta_c X_c + \alpha_p[i] + \beta_s[i]c_i$$

### lme4 notation

```
y ~ 0 + condition + (0+condition|stimuli) + (1|respondents)
```

### Rasch-like parametrization

	GLMM	LMM
respondents	$\theta_p$	$\tau_p$
stimuli	$b_{sc}$	$\delta_{sc}$

## Model 3

### Mathematical Notation

$$y = \beta_c X_c + \beta_p[i]c_i + \alpha_s[i]$$

### lme4 notation

```
y ~ 0 + condition + (1|stimuli) + (0+condition|respondents)
```

### Rasch-like parametrization

	GLMM	LMM
respondents	$\theta_{pc}$	$\tau_{pc}$
stimuli	$b_s$	$\delta_s$



## All models are wrong...

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Find the useful model via model comparison: AIC and BIC

The lower the value, the better the model

! AIC, BIC, and model complexity:

Total number of parameters:  $\beta$  and  $\Gamma$

*NOT* the levels in  $d$

Model 2 and Model 3: Same complexity, different focus

The chosen model is the least wrong model *given the models considered*:

Relativity applies everywhere

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# Get set

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```
library(lme4) # Fitting LMMs  
library(ggplot2) # Plots
```

# The Implicit Association Test

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Individual Differences!

copia e incolla direttamente la slide del predoc!!

```
[1] "C:/Users/Ottavia/Documents/GitHub/beyond-summer-school/a
```