# matRiks: An R package for the automatic generation of rule-based matrices

by Quietest Quokka and Bounciest Bilby

#### 1 Introduction

cattell1963 defined fluid intelligence (*g*) as the ability of solving novel reasoning problems that has little to do with concepts learned in schools or through acculturational processes. The adjective "fluid" explicitly refers to its ability to "flow" into a variety of tasks and cognitive activities (Horn, 1972). Given this definition of fluid intelligence, it appears natural that the instruments used for its evaluation tap on the respondent's ability to solve abstract problems that involve acculturation as little as possible, such as figural analogies, figure classifications, matrices, and number and letter series (Horn, 1968).

The Raven's progressive matrices (RPM, raven1938) are among the most famous tools for the assessment of g. The RPM consists in a series of non-verbal multiple-choice stimuli where respondents are required to complete a series of drawings composed of different figures by identifying the relevant features that rule the relationships between the figures. These drawings are often referred to as matrices. To pursue this aim, the respondents must choose the figure that complete the drawing among a list of other figures, the so-called distractors. This task should measure the ability of the respondents to identify and take into account the features (also called "rules") that govern the relationship between the figures to compose the drawing. Different versions of the RPM exist, according to the target population (i.e., children with less then 12 years of age or adults) to which they are administered. The Colored Progressive Matrices (CPM, cit) are composed of sets of  $2 \times 2$ matrices (i.e., 4-cell matrices), some of which (CONTROLLARE) includes colored figures. The advanced progressive matrices (ADM, cit) are composed of sets of  $3 \times 3$  matrices meant for assessment in gifted population (DIRE MEGLIO). Finally, the RPM are meant for the assessment among the general population and are composed of both  $2 \times 2$  and  $3 \times 3$  matrices. The colored figures are presnt only in the CPM.

The RPM and similar tasks (here denoted as Raven-like matrices or Raven-like tasks) are employed in different fields, from clinical evaluation of intelligence to the selection processes in organizational psychology (citation needed). Since Raven's and Raven-like tasks involve the ability to solve new abstract problems, the stimuli composing these tasks should not be spread among the general population to preserve the novelty of the tasks. The rules that govern the relastionhsip between the figures of a matrix can also be used to generate new stimuli, and different resources have been developed throuought the years with this specific aim, such as Sandia (cit), Corvus (cit), and the R package Imak (cit).

The stimuli generated with Sandia have been analysed in an Item Response Theory framework to validate them as a test for measuring fluid intelligence. The stimuli are available upon request to the authors, however no new stimuli can be generated because the code on which Sandia is based is no longer maintained. Corvus represents another possible resource for generating Raven-like tasks. Corvus is written in Javascript but the Author provided a nice and easy-to-use graphical interface where the user can specify the figures and the rule(s) for the generation of the matrices. However, Corvus provides few degrees of freedom in terms of both the figures and the number of rules that can be manipulated through the graphical interface. Any customization from the user, like adding other figures, modifying existing ones, or implementing new rules, require to modify the JavaScript code, which might be quite demanding for people with little to null experience in JavaScript coding. Finally, the ImaK package is an R package that allows for generating visual analogies. The code for generating such stimuli (along with their response options) is quite straightforward and easy to use. However, the stimuli that can be generated with the ImaK package are mostly based on the rotation of the same figure to which some objects can be added or removed. As such, the only rule that is manipulated is the spatial rotation of

the figures.

Given the limitations of the existing resources for generating Raven-like tasks, there is the need of an open-source, easy-to-use, and constantly maintained resource for generating such stimuli through the systematic manipulation of rules applied to different figures. The matRiks package (matRiks) has been developed to pursue these aims. The package enables the generation of matrices by manipulating one or multiple rules on one or multiple figures. Additionally, it automatically generates the response list associated with the matrix. Beyond the default settings, the matRiks package allows for the generation of new figures and customization of matrices and response lists. The systematic manipulation of both the rules and the figures for the matrix generation should grant the possibility of grading the granularity of the complexity of the matrices by varying one element at the time. In a similar vein, the package should allow for generating matrices that can be considered equivalent in terms of rules employed for their generation but that differ in terms of figures composing the drawing. In what follows, the term stimulus is used to identify the matrix with its associated response list.

The manuscript is organized as follows. The next section presents the rules that are usually employed in the RPM along with the specific types of error responses (i.e., distractors) that compose the response list associated with a matrix. A complete example of the generation of a stimulus (i.e., the matrix and the associated response list) and some final remarks on the potential applications of this package conclude the presentation.

# 2 Background

#### Rule based matrices

Literature highlights a plethora of rules that can be manipulated for the generation of the Raven-like tasks (cit cit cit). Beyond the fact that some of these rules have different names in different sources but refer to the same manipulation (e.g., the rule defined as "and problem" in Harris el a. 2020 is called "intersection" rule in Arendasy et al. 2005), they can be summarized into different macro-categories, namely visuospatial rules (i.e., the manipulation concerns the graphical and spatial features of the figures, Figure ??), and logical rules (i.e., the manipulation concerns the logical relationships between the figures composing the matrix, Figure ??). The rules can be used to manipulate to different figures to generate a matrix.

In Figure ??, the manipulation concerns a specif feature of the figure, that is its size, and it can be observed as the the figure decreases its size across the cells. The leftmost cell contains the figure with its original size, the middle cell contains a smaller figure, while the rightmost cells contains the smallest one. In Figure ??, the manipulation concerns the relationships between the objects composing the figures, which are combined together according to a logical rule based on the insiemistic intersection of the objects. Specifically, the figure in the rightmost cell results from the intersection between the figures in the leftmost cell and those in the middle cell.

Both visuospatial and logical rules can be manipulated according to directional logic. Specifically, the rules can be applied horizontally (i.e., the manipulation of the rule can be seen across columns but not across rows, H direction), vertically (i.e., the manipulation of the rule can be seen across rows but not across columns, V direction), or diagonally (i.e., the manipulation of the rule can be seen both across columns and across rows). Concerning the diagonal directional logic, it can follow either the main diagonal of the matrix (i.e., the manipulation of the rule can be seen from the top-left corner to the low-right corner, TL-LR direction) or the secondary diagonal of the matrix (i.e., the manipulation of the rule can be seen from the low-left corner to the top-right corner, LL-TR direction).

## The response options

A large corpus of literature has investigated the role of the distractors in the response processes involved when solving the Raven matrices, focusing on the specific error responses chosen by the respondent (fort, kunda, storme). The underlying logic is that the incorrect response is not chosen at random by the respondent, but it can be the result of an educated guess, or it can be chosen because the respondent is misled by a specific feature. In other words, the incorrect responses might reflect an incorrect solution strategy resulting in the choice of a specific type of distractor over another one [@kunda]. The distractors can be classified according to the incorrect response strategy they represent. @kunda present a list of criteria for the identification of the distractors in the SPM based on classification of the error types from the CPM and APM manuals [@raven2004]. The distractor that is chosen in place of the correct response option can be collected into four main four conceptual errors: (i) Repetition (R) errors occur when the chosen response option is a cell adjacent to the blank space, (ii) Difference (D) errors occur when the chosen response option is completely different from any entry of the matrix, (iii) Wrong Principle (WP) errors occur when the chosen response option follows rules other than the ones used in the matrix, and (iv) Incomplete Correlate (IC) errors occur when the chosen response option is in fact the correct response with a variation on a single feature.

All the macro categories of error types can be further sub categorized accoriding to the characteristics of the speicific erro response. For instance, the repertion category can be divided according to the position of the repeated cell with respect to the blank cell. As such, three error types of the repetition category can be identified, namely R-Left, R-Top, and R-Diagonal according to whether they represent the cell to the left, on topo, or in diagonal with repsect to the blank cell. Concerning the wrong principle macro category, some of the speicfic error types might refer to the reption of a cell not adjacent to the blank space (i.e., WP-Copy) ot to the combination of different elements of different cells, not according to the rule(s) used for creating the matrix. Some of the specific errors of the incomplete correlate macro category includes the cchange of the orientation of the coprrect response (i.e., IC-flip), the change in color of the correct response (i.e., IC-Neg), the change in the size of the correct response (IC-Size) or the lack of an element of the correct response (IC-Inc). Finally, concering the difference macro category, the specific error might be a cell completely white or black (D-Blank) or the merge of different cells of the matrix (D-Union).

NON RIESCO A COMMENTARE DIO PORCO Difference errors occur when the chosen response option is completely different from any entry of the matrix. Wrong principle errors occur when the chosen response option follows rules other than the ones used in the matrix. Incomplete Correlate errors occur when the chosen response option is in fact the correct response with a variation on a single feature. Each of the four main error types can be further described by their subcategories.

Table 1 summarizes the definitions of the error types.

The criteria for the classification of the error types were used for the formal definition and generation of the distractors implemented in the matRiks package. SIAMO SICURI CHE QUESTA ROBA VADA QUI? These criteria were included in the response options operator with the aim of providing the user with a response list composed of 11 elements (ten distractors and the correct response) among which they could choose the most appropriate ones. Specifically, the response options operator generates a response list composed of the correct response, three reptition distractors, one difference distractor, two wrong principle distractors, and four incomplete correlate distractors. Further details on the formal definition of each of the distractors and on their generation are given in the "Generation of the response list" Section.

## 3 The matRiks package

The matRiks package [@matRiks] can generate  $2 \times 2$  and  $3 \times 3$  Raven-like matrices with their corresponding set of responses (i.e., the correct response and all the distractors described in

**Table 1:** Taxonomy of error types

Distractors	Definition		
Repetition (R)	Entries of the matrix adjacent to the blank cell		
Difference (D)	Combination of all the entries of the matrix or the combination of some of their fea		
Wrong Principle (WP)	Copy or combination of the matrix entries according to another rule		
Incomplete Correlate (IC)	Correct response with a variation on only a single feature.		

the Generation of response list section). The Raven-like matrices are generated according to either visuospatial or logic rules, which can be concatenated with three different directional logic, namely vertically, horizontally, and diagonally. Finally, it is possible to print the generated matrices and set of distractors as either single images (i.e., each cell of the matrix and each distractor are printed separately) or as a complete figure with the set of single distractors.

#### Installation

The matRiks package is available on CRAN and can be installed as:

install.packages("matRiks")

The code vignette(package ="matRiks") allows for obtaining the list of all the vignettes included in the package, which illustrates the default figures included in the package and a basic example of its application. Each vignette can be accessed via vignette("vignette-name", package="matRiks"). For instance, the code vignette("generate\_matriks", package ="matRiks") opens the vignette that contains the instruction on how to generate an RMarkdown file where both the matrix and its associated response options are plotted together.

## **Definition of figures**

The matRiks package contains several default figures that can be used for the generation of the matrices and of new figures. All figures have class figure and they are defined as functions, such that the syntax figure\_name() must be used to draw them and visualize their structures. The arguments that can be modified inside the parentheses might vary from figure to figure, and they allow for changing different features. The default features of the figures are stored in a list of length 15, and they might vary from figure to figure although the length is unchanged. The features of the figures are defined inside of the list as follows:

- shape: character, the name of the figure
- size.x: numeric, the length of the semi-major axis of the ellipse within which the figure is inscribed (see the documentation of the **DescTools** for further details)
- size.y: numeric, the length of the semi-minor axis of the ellipse within which the figure is inscribed (see the documentation of the **DescTools** for further details)

- theta. 1: numeric, radiants of the rotation of the circle
- theta. 2: numeric, radiants of the rotation of the circle
- rotation: numeric, radiants of the rotation of the ellipse within which the figure is inscribed
- pos.x: numeric, the position on the x-axis
- pos.y: numeric, the position on the y-axis
- 1ty: integer, the line type of the margins of the figure
- 1wd: integer, the width of the margins of the figure
- num: numeric, it is equal to 1 if the figure is draw inscribed into an ellipse, and it equal to 2 if the figure is draw as a arc of a circle
- nv: integer, the number of vertices of the figures (might vary from 2 lines to 100 circle and ellipse –)
- shade: character, the filling of a figure (can also be NA –empty figure–)
- visible: integer, the visibility of the figure
- tag: character, properties of the figure used for the definition of the distractors

The draw function is designed to print all the figrues, as well as the matrices and the response list. To print a figure, the only argument neede inside of the draw function is the name of the figure. For instance, a simple square (Figure @ref{fig:square}) can be printed with the command line:

INTRODUZIONE DI TAG SENZA PARLARE D.INT E D.EXT

```
draw(square())
```

The figures in matRiks are summarized in different categories (e.g., closed figures, black figures, lines), for each of which a vignette lists all the figures. The following types of figure are available in the matRiks package:

NON RIESCO A COMMENTARE

## Concatenation of figures

Other then the pre-existing figures, the matRiks package allows for the generation of new figures by concatenating the existing ones. The cof() (Concatenation Of Figures) function is designed for this aim. The arguments of the cof() function are the names of the default figures presented in the previous section.

For instance, the figure in Figure ?? is obtained by concatenating a circle() and a dot().

eye <- cof(circle(), dot()) # create the new figure eye by concatenating the circle and the dot
draw(eye)</pre>

The resulting figure eye is a named list of lists of class figure. However, the two original figures are still available and can be considered as separate figures, and as such the object eye is considered a concatenation of two figures.

eye\$shape

```
#> [1] "circle" "dot"
```

Function cof() has also two optional arguments, namely single and name, which allow for the generation of new figures. If set to TRUE, the first argument forces the outcome of the concatenation to be considered as a new single figure, while the second argument defines a new name for such a figure. The following code recreated the figure in Figure ?? but it forces the new figure to be a single figure named "eye".

```
s_eye <- cof(circle(),dot(),single = TRUE, name = "eye")
s_eye$shape</pre>
```

Table 2: Four-cell matrix

Sq1	Sq3
Sq2	Sq4

Table 3: Nine-cell matrix

Sq1	Sq4	Sq7
Sq2	Sq5	Sq8
Sq3	Sq6	Sq9

Although this difference is trivial from a graphical standpoint (the single figure and the concatenation of two distinct figures appear exactly the same), it is relevant for the application of some of the rules that require a minimum number of figures for their application (e.g., inferential rules).

MI SONO FERMATA QUI CON LE MODIFICHE 24/10/2024

## Available rules and matrix generation

The function mat\_apply(Sq1, hrules="identity", vrules ="idenity", mat.type=9) is the main function for the generation of matrices based on rules. This function allows for the generation of matrices of different dimension, either 4-cell or 9-cell matrices. The dimension of the matrix can be specified with the argument mat.type, such that mat.type = 4 results in 4-cell matrices (Table 2)

and mat.type = 9 results in 9-cell matrices (default, Table 3).

The Sq1 argument defines the starting figure (i.e., the figure to be plotted in the first cell Sq1), which can also be a concatenation of figures. The arguments hrules and vrules allow for the definition of the directional logic with which the rule(s) is applied, such that the rules specified in hrules are manipulated horizontally and those specified in vrules are applied vertically.

The application of the mat\_apply() function results in a named list of class matriks that contains the characteristic of the matrix, such as the figures that are visible in each cell, the rule(s) applied horizontally and/or vertically and the type of matrix, either 4-cell or 9-cell. The following example is based on a 9-cell matrix where the identity rule was applied both horizontally and vertically:

In a matriks each cell of the matrix is an elements of the named list. Specifically, the elements which contains a cells are called Sq follows by the number of the cell. In the above example, nine elements (from Sq1 to Sq9) are listed corresponding to the nine cells as depicted in Table 3. In the case of a 4-cells matrix four elements will be present named from Sq1 to Sq4. In addition to the Sq elements, the class matriks contains hrule, vrule and mat.type. The first two are vectors containing the rule(s) applied horizontally and vertically, respectively. The last one is the dimension of the matrix.

The rules are methods that transform a feature of the figure to obtain a different figure or a figure with a modified feature. The matRiks package implements several rules, each of which may be classified differently. All the rules functions are characterized by three arguments, namely fig,n, and rules. The fig argument specifies the initial figure to which the rule is applied. Some rules, such as size, can be applied to any type of figure, while others have specific constraints; for example, the shape rule requires concatenation of three figures. Detailed definitions for each rule are provided in Table @ref{tab:rule-types},under the 'Definitions' column.

The n argument specifies either the elements of the permutation or the increment value, depending on whether the rule is permutational or incremental. In mat\_apply(), there is also a link between the cell number and the constant n, which ensures that the rule's directional logic is maintained.

Finally, a single function can apply different rules (see the 'function' column in Table XXX). The rules argument allows us to specify which specific rule to apply. For example, the margin function manipulates line attributes of figures, with options to adjust line width margin(..., rules = "lwd") or line type margin(..., rules = "lty"). Another use of the rules argument is to reverse the default direction of rule application. For instance, size(..., rules = "size") typically decreases in size from right to left (see Figure ??. By adding inv to the rules vector, the rule is applied in reverse order. Figure ?? shows the output of mat\_apply(square(size.x=10), hrules = "size.inv") applied to a sequence of squares.

The reverse application of the rules can be done with permutational rules as well. By starting with the same set of figures as the one used to generate Figure ??, the specification of the argument hrules = "shape.inv" would result in a reverse ordering of the figures across the cells (Figure ??).

Logical rules AND, OR and XOR are a special case rules that cannot be applied in reverse.

The rule classification, originally introduced in the literature as visuospatial and logical, has been modified in the **matRiks** package to focus on constructing matrices rather than solving them. Consequently, the rules are reclassified into incremental and permutational categories.

Figure ?? illustrates the application of the change in size rule on a square. the change in size rule is an incremental rule, in which the size of the square decreases of a fixed quantity in each subsequent object according to a directional logic. Incremental rules apply a fixed increase (or decrease) on each cell of the matrix to obtain the features of the figure in the following cell, starting from the first cell. The order in which the fixed increase (decrease) is applied depends on the directional logic used for the generation of the matrix.

This rule is incremental in the sense that the order of the squares in the cells is determined by the fixed variation in their size, from the larger to the smaller one. If the positions of the squares across the cells is changed, then the definition of the rule is no longer satisfied, unless the squares are ordered from the smaller to the larger. In this case, the rule is still incremental but with a reverse application.

The operation underlying the functioning of the permutational rules is the permutation of the figures (or of their features) across the cells according to a directional logic. For instance, consider a matrix where a set of three figures (hexagon(), pentagon(), square()) are manipulated according to the shape rule following an horizontal directional logic (Figure ??).

By default, the starting order of the figures is the order with which the figures are concatenated in the set defined by the user. When the user change the starting order, the rule will adapt consequentially.

It may appear trivial at this point that the transformation obtained from a rule becomes evident only in the comparison between figures. For instance, in Figure ??, the change in size is noticeable only when two cells are considered together. The figure in the first cell is smaller than the one in the second cell, that is smaller than the one in the third and so on. This straightforward concept underlies the creation of a matrix starting from a figure using mat\_apply().

The procedure underlying mat\_apply() consists of three serial steps. For the sake of simplicity, they will be illustrated for the 9-cell matrices only. The same reasoning applies to 4-cell matrices.

The first step is to generate a named list of all the cells from Sq1 to Sq9. Each cell contains the initial figure defined in Sq1, with no rules applied yet. For example, considering the concatenation of figures cof(square(), circle(), dot()), the resulting matrix will be displayed in Figure @ref{fig:examplestep1}.

The second step checks whether the arguments hrules or vrules contain a logical rule. If they do, an error occurs in the following cases: if the logical rule is combined with a visuospatial rule, if a logical rule is used to generate a 4-cell matrix, or if two different logical rules are concurrently applied to the same figures with differing directional logic. Since applying logical rules requires a well-defined relationship between the cells of the matrix, only one logical rule can be applied at a time. If there is a logical rule and none of these error conditions are met, the procedure will generate the entire matrix in a single step.

If there are no logical rules, the procedure enters the third step. The rules in hrules are applied following a horizontal directional logic, meaning they are iterated among the elements across columns. Subsequently, the rules specified in vrules are applied following a vertical directional logic, meaning they are iterated among the elements across rows.

Since the third and forth steps are made one after another using the same rule, for instance size, both with a horizontal a vertical logic, the two transformation on the cells ends up to cumulate. For instance, considering the code mat\_apply(square(),hrules="size", vrules="size"), at the end of the third step the figure in Sq5 will be half the size of Sq1. During the forth the size of Sq5 will be halve again resulting in a figure that is a quarter of the initial Sq1.

It is worth mentioning that the combination of the same rule horizontally and vertically ends up in the definition of a diagonal directional logic. In particular, if the same rule is applied in reverse in one direction and applied direct in the other, it will result in a TL-LR directional logic. On the other hand if the same rule is direct (or reverse) in both horizontal and vertical directional logic they will give rise to a LL-TR logic.

RIPRENDO DA QUI 24/10/2024

#### Concatenation of matrices

The com() (Concatenation Of Matrices) function allows for combining and layering different matrices together to generate a multi-layer matrix.

Figure ?? and Figure ?? depict a matrix created by manipulating the same set of rules. Specifically, two rules are manipulated horizontally (i.e., shade and shape) and one rule is manipulated vertically (i.e., 'rotate"). As such, the figures in the cells and the shading change across columns, while the rotation of the figures change across rows.

The matrix depicted in Figure ?? results from the manipulation of the set of rules to obtain a single-layer matrix, such that all rules are concurrently applied to the same set of figures (i.e., hexagon(), square(), pentagon()). The same set of rules is manipulated to obtain the matrix in Figure ??. However, the three rules are manipulated to obtain three different single-layer matrices, one for each rule (Figures ??, ??, and ??), which are then concatenated together. Each of these single-layer matrices can be considered as a layer of the multi-layer matrix. The layering of the matrices moves from the background (considered as external) to the foreground (considered as internal). Layers are counted inwards m = 1, ..., M (where M is the total number of matrices to concatenate), such that the background matrix is layer 1 and the foreground matrix is layer M. The matrix in Figure ??(fig:multi-layer) is composed of M = 3 layers: (1) background layer obtained with horizontal manipulation of the shape rule (Figure ??), (2) middle layer obtained with horizontal manipulation of the shade rule(Figure ??).

The com() function concatenates the single-layer matrices to obtain the multi-layer one:

```
com(multi_a, multi_b, multi_c)
```

The matrices have to be concatenated hierarchically from the background layer to the foreground layer The hierarchy between the layers is of the uttermost importance for definition of the distractors, specifically for the generation of the incomplete correlate ones. Generally, the manipulation of the correct response to obtain the incomplete correlate

\$3 \times 3\$ matrices Distractors R-Left SQ8 R-Top SO<sub>6</sub> SO<sub>5</sub> R-diag Wp-Copy SQ1 or SQ3 WP-Matrix SQ1 or SQ3 with the superimposition of another cell. Difference SQ1 or SQ3, SQ4, SQ7 with the superimposition of a figure which is not manipulated in the matrix IC-Inc It is the correct response with a missing element Single-Layer: Not possible Multi-layer: The most internal figure is removed from the correct response. Logic matrices: The element that is removed is randomly selected. IC-Neg Color inversion of the correct response (single-layer matrix) or of one of its figures (multi-layer matrix) Single-layer matrix: Color inversion of the figure in the correct response Multi-layer matrix: Color inversion of the most internal figure of the correct response IC-Flip Rotation or reflection of the correct response (single-layer matrix) or of one of its figures (multi-layer matrix) Single-layer matrix: Reflection/Rotation of the figure in the correct response Multi-layer matrix: Reflection/Rotation of the most internal figure of the correct response IC-Scale Resize of the correct response (single-layer matrix) or of one of its figures (multi-layer matrix) Single-layer: Resize of the figure in the correct response Multi-layer matrix: Only the most internal figure in the correct response is resized

**Table 4:** Definition of the distractors implemented in the **matRiks** package for  $3 \times 3$  and  $2 \times 2$  matrices

distractors is applied to the figures in the foreground layer *M*. Further details on the definition and on the generation of the incomplete correlate distractors of multi-layer matrices are given in section Response list.

## Generation of the response list

The generation of the distractors composing the response list is constrained to: (i) the type of matrix (i.e., single-layer matrix vs. multi-layer matrix), (ii) the rule(s) manipulated for the matrix generation, and (iii) the directional logic of the rule manipulation. To the best of our knowledge, there is not a formal definition of the specific features of each distractor and on their applicability given the above-mentioned constrained.

As such, the development of the response option operator required the formal definition of the distractors and of all the possible exceptions given the constraints imposed by the matrices generated via the matrix operator. The definitions of the distractors implemented in the  $\mathbf{matRiks}$  package is reported in Table 4.

The response option operator (implemented in the response\_list() function) runs through different steps. First, it checks for the number of rules and the directional logic with which that have been manipulated, as well as whether the matrix is a single matrix or a multi-layer matrix. This check is crucial for the generation of the incomplete correlate distractors, but not for the other tyoes of ditsractors (i.e., R, WP, and D) since they are generated by considering the figures in a cell as a single figure. Conversely, since the IC distractors are a moficiation of a single feature of the correct response, there is the need to determine whether they can be generated in the first place and, if so, on which element of the correct response the change should be applied.

In single-layer matrices, the IC-inc distractor cannot be generated given that it requires the removal of an element of the figure, while all other IC distractors can be generated, unless a figure with specific tags is employed. For instance, the s-shaped figures such as the miley() cannot change color, and, as such, the "shade" tag is not present in their tag list. When the response response option generator does not find the shade tag among the tags of miley() to generate the IC-neg distractor, it throws a warning and the IC-neg distractor is replaced by the correct response canceled out by a black thick cross.

In multi-layer matrices, the IC distractors are generated by modifying the figure in

the foreground matrix. Before applying the manipulation, the tags of the figure in the foreground matrix are checked to investigate whether all the IC distractors can be generated from that figure. If this tests false, then the response option generator moves towards the background of the multi-layer matrix, until it finds a figure whose tags satisfy the condition for creating all the IC distractors.

For the generation of WP and D distractors, the choice between using cell SQ1 or cell SQ3 stictly depends on the number of rules and on the directional logic with which they are manipulated. Specifically, cell SQ1 is selected when the matrix is generated via the manipulation of a single rule with V, H, or TL-LR directional logic. If the manipulation of the single rule follows a LL-TR directional logic or two rules are manipulated with all possible directional logic, the SQ3 cell is chosen. This is done to avoid that the WP-Copy distractors can be interpreted as IC distractors. In some instances, the R distractors in  $3 \times 3$  matrices cannot be generated because they are equal to the correct response. For instance, if a matrix is generated with the vertical manipulation of a single rule, the R-Left distractor (SQ8) is equal to the correct response. In such instances, the distractor that is equal to the correct response is generated by the response options operator but it is covered with a thick black cross.

A similar procedure is applied for choosing which cell to use between SQ3 and SQ2 or between SQ3 and SQ1 for the generation of WP-Matrix and Difference distractors in  $2 \times 2$  matrices. In both cases, the choice depends on whether at least one rule is applied both horizontally and vertically. If the same rule is applied both horizontally and vertically, then SQ3 is chosen, otherwise SQ2 and SQ1 are chosen.

The response options operator generates the response list (i.e., the correct response and all the distractor presented in the Table) through the response\_list() function, which results in a list of figures that correspond to each of the distractors. For instance, the distractors of the matrix in Figure ?? can be obtained with:

```
response_list(single_matrix)
```

The function response\_list() results in a named list of length 11 containing all the response options:

and it can be plotted as:

```
#> Warning in ic_inc.matriks(obj): IC-Inc cannot be obtained with a single figure
```

As it can be noted, a warning has appeared and it refers to the IC-Inc distractor. As per Table 4., the distractor IC-Inc is defined as the correct response with a missing element. However, having a single-layer matrix does not allow for the removal of any element, hence the warning "IC-Inc cannot be obtained with a single figure" is thrown and the IC-Inc distractor is replaced by the correct response over which a black thick cross is imposed.

Given that the matrix in Figure ?? is composed of three layers, it is possible to obtain also the IC-Inc distractor:

However, the difference distractor is not well defined. The user can change the random seed for the generation of this distractor with the argument seed(), such that another random figure is chosen among the available ones:

```
draw(response_list(multi_matrix, seed = 7),
    main = TRUE)
```

## A complete example

This section presents a complete example on how to generate a multi-layer  $3 \times 3$  matrix with logical rules and its related response options.

The first layer is generated by manipulating the AND logical rule according to an H directional logic on a square composed of 4 lines:

The second layer is generated by manipulating the OR logical rule according to a V directional logic on a flower composed of 4 petals:

The multi-layer matrix can be composed with the com() function by concatenating the two single-layer matrices:

The response options associated with the multi-layer matrix can be generated with the response\_list() function:

Since the filling color the miley cannot be changed, the IC-Neg distractor cannot be generated and the function throws a warning and the ic\_neg distractor is replaced by the correct response with the superimposition of a thick black cross. The difference distractor does not look good. The figure that is superimposed to the cell taken from the matrix can be changed by changing the seed in the response\_list() function:

Assuming that a response list of length 8 (the correct response along with seven distractors) is associated with the multi-layer matrix, a character vector with the labels of the chosen distractors can be specified directly in the draw function:

# 4 Summary

This article briefly illustrates the functioning of the **matRiks** package for the automatic generation of Raven-like stimuli. This package has been developed with the intention of providing the users with a flexible, open-source, and easy-to-use tool for generating Raven-like matrices according to different rules, encompassing both visuo-spatial and logical rules, along with their associated response list.

The rules for generating the matrices and for generating the distractors associated to each matrix that are implemented in the **matRiks** package derive from vast literature concerning Raven's matrices and the error patterns observed on the CPM and the APM. As such, this package potentially provide the possibility for generating stimuli that are equivalent in terms of rules and response options to the standard Raven's stimuli. This allows for a comparison between the responses observed with the standard stimuli and those generated with the package.

This package has been developed within a broader project founded by the Italian Ministry of University and Research, which is aimed at the development of an intelligent system for the adaptive assessment of executive functions and fluid intelligence among general and clinical populations. The test used for assessment of fluid intelligence (named MatriKS) was developed following the principles of Raven's Matrices. Specifically, the stimuli composing the test have been developed with the **matRiks** package (mdpi).

This package allows for high degrees of freedom in the generation of matrices with different difficulty. For instance, it allows for the generation of stimuli that combine multiple rules by exploiting the possibility of layering multiple matrices together. Moreover, the high degree of control provided to the users allow them to thoroughly manipulate the difficulty of the matrix, for instance by adding or removing objects and combining together different rules.

The package is regularly maintained and new functions will be available in the future. As such, the users should refer to the official documentation of the package that is constantly updated.

Although the functions implemented in **matRiks** are quite straightforward and easy to use, they need a basic knowledge of the R language. To overcome this issue and allow for a wider use of the package even among people that are not familiar with R, a web application

built with the **shiny** package (shiny) will be developed in the future.

Quietest Quokka University of Little Mates Department of Letter Q Somewhere, Australia

https://www.britannica.com/animal/quokka

ORCiD: 0000-1721-1511-1101

qquo@ulm.edu

bbil@ulm.edu

Bounciest Bilby
University of Little MatesUniversity of Aussie Animals
Department of Letter Q, Somewhere, Australia
Department of Marsupials, Somewhere, Australia
https://www.britannica.com/animal/bilby
ORCiD: 0000-0002-0912-0225