CUT IT SHORT: A NEW ITEM RESPONSE THEORY-BASED APPROACH FOR SHORTENING TESTS

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- Introduction
- 2 Item Response Theory and information functions
- 3 IRT procedures for shortening tests
 - Benchmark procedure
 - ullet Procedures based on heta targets
- **4** Practical Implications
- **5** Some final remarks

Many items/questions in a questionnaire

Good

High assessment precision

High information/reliability

But

Respondent's fatigue

Response quality might be compromised

A viable solution

A short test form (STF) with few items but high reliability

European Social Surveys

Cross-national survey carried on every two years since 2001

Assessment of attitudes, beliefs, and behavior patterns of diverse populations in different countries. Main focus \rightarrow change/stability of:

- Living conditions
- Social structure
- Public opinion

Round 10:

Socio-demographic information



Well being, social exclusion, human values



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Focus on the item

The information at the item level is crucial \rightarrow Each item taps on a specific location of the latent trait

Item Response Theory

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Item Response Theory 2-PL Model

$$P(x_{pj} = 1 | \theta_p, b_j, a_j) = \frac{exp[a_j(\theta_p - b_j)]}{1 + exp[a_j(\theta_p - b_j)]}$$

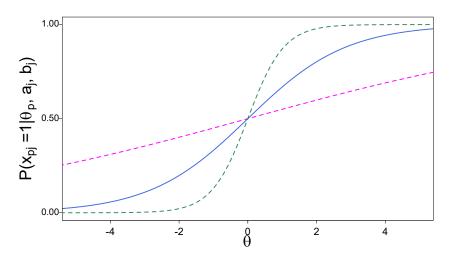
where:

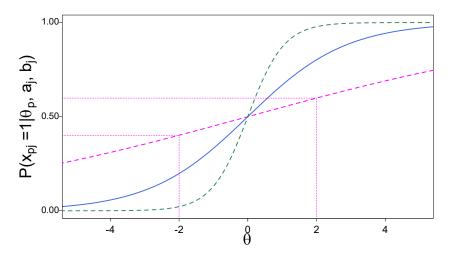
 $P(x_{pj} = 1)$: Probability of endorsing item j by respondent p

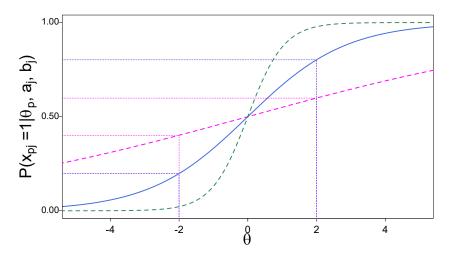
 θ_p : Ability of respondent p

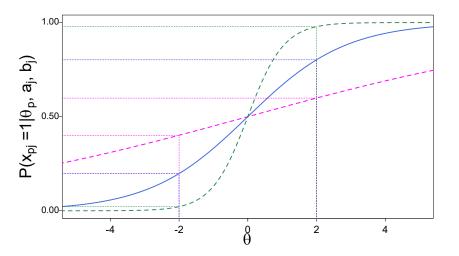
 b_i : Difficulty (location on the latent trait) of item j

 a_i : Discrimination of item j









Item Information Function

$$IIF_j = a_j^2 [P(\theta)(1 - P(\theta))]$$

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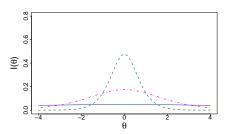


Figure 1:
$$a = 0.20$$
, $a = 0.70$, $a = 1.90$, $b = 0$

Item Information Function

$$IIF_j = a_j^2 [P(\theta)(1 - P(\theta))]$$

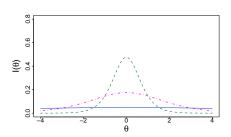


Figure 1: a = 0.20, a = 0.70, a = 1.90, b = 0

Test Information Function

$$TIF = \sum_{j=1}^{J} IIF_j$$

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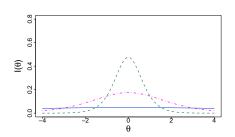


Figure 1: a = 0.20, a = 0.70, a = 1.90, b = 0

Test Information Function

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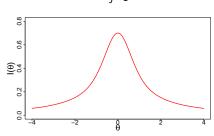


Figure 2: $TIF = IIF_1 + IIF_2 + IIF_3$

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Benchmark procedure

Selected items \rightarrow items with the highest *IIF*s

e.g.: 3-item short form from 10-item full-length test

item	b	а	IIF
1	-0.67	0.71	0.08
2	0.50	1.19	0.15
3	-2.43	0.25	0.01
4	2.12	1.98	0.24
5	1.72	0.39	0.03
6	-2.28	1.62	0.19
7	0.64	0.50	0.05
8	-2.51	1.68	0.19
9	-0.66	0.44	0.04
10	0.72	0.33	0.02

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).24
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Selected items \rightarrow items with highest *IIF*s in respect to θ targets (θ') e.g.: 3-item short form from 10-item full-length test

			an reng
	$ heta_{1}^{\prime}$	$ heta_2'$	θ_3'
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4			
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9			
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1	0.04	0.12	0.08
2	0.09	0.33	0.03
3	0.01	0.01	0.02
4	0.73	0.06	0.01
5	0.04	0.03	0.02
6	0.01	0.06	0.59
7	0.05	0.06	0.03
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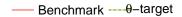
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An overall look



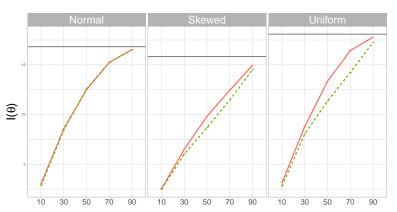


Figure 3: Overall Information of the short test forms

A closer look

— Benchmark ···θ-target

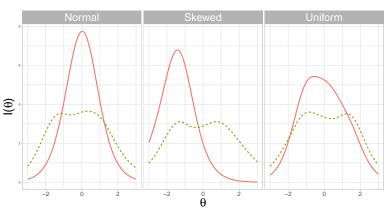


Figure 4: TIF of the 10-item short test form

An even closer look

— Benchmark —θ-target

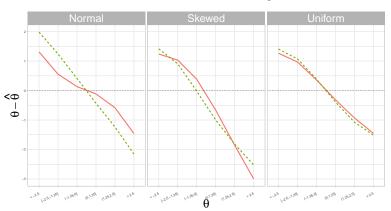


Figure 5: $bias = \theta - \hat{\theta}$ of the 10-item short test form

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- Item response theory provides a valid framework fro shorteing tests without losing information and reliability
- Targeting vs. ordering: There is no "one-fits-all" solution
- In the future → Which is the ideal number of item?

Thank you!

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