

CUT IT SHORT: A NEW ITEM RESPONSE THEORY-BASED APPROACH FOR SHORTENING TESTS

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NUOVA DATA, BOLOGNA

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1 Introduction

2 Item Response Theory and information functions

3 IRT procedures for shortening tests

Benchmark procedure

Procedures based on θ targets

4 Practical Implications

5 Some final remarks

The struggle

Rule of thumb → more questions more reliability

Drawback → too many questions, too many questionnaire → assessment precision might be compromised by the length of the assessment

Esempio che mi manda Andrea per l'indagine dei giovani, tantissimi questionari, indagine lunghissima

The Ideal Solution

A short test form (STF) as informative as the full-length test

Focus on the item

The information at the item level is crucial → each item taps on a specific location of the latent trait

Item Response Theory

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Item Response Theory

2-PL Model

$$P(x_{pj} = 1 | \theta_p, b_j, a_j) = \frac{\exp[a_j(\theta_p - b_j)]}{1 + \exp[a_j(\theta_p - b_j)]}$$

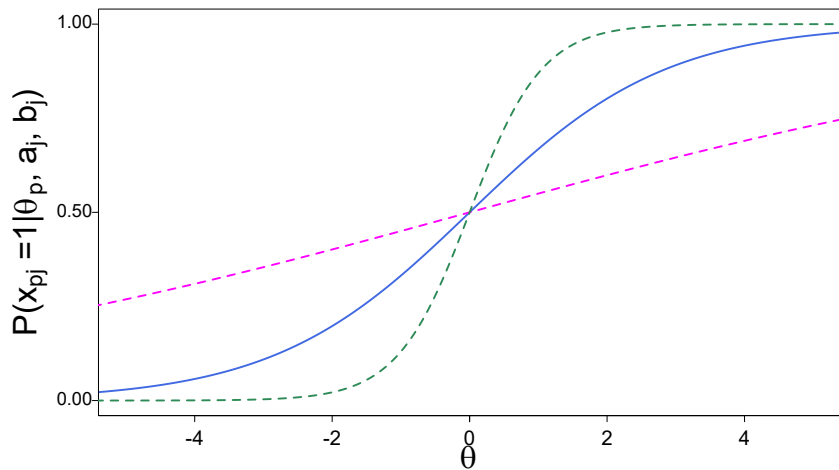
where:

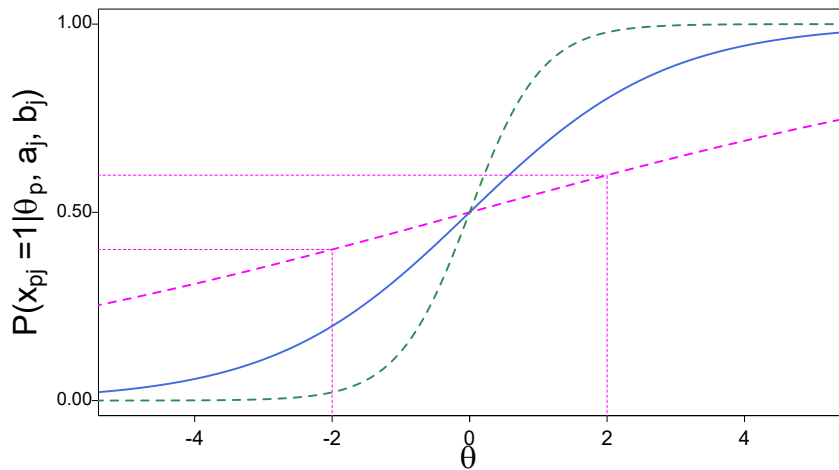
$P(x_{pj} = 1)$: Probability of a correct response to item j by respondent p

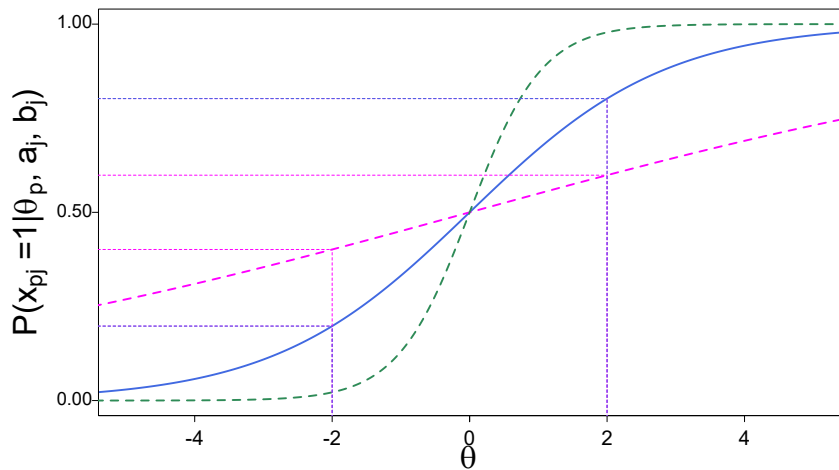
θ_p : Ability of respondent p

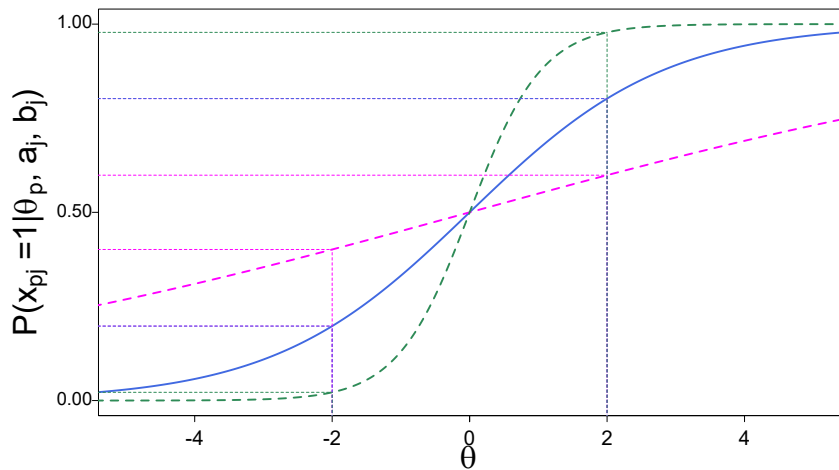
b_j : Difficulty of item j

a_j : Discrimination of item j









Information functions

Item Information Function

$$IIF_j = a_j^2 [P(\theta)(1 - P(\theta))]$$

Information functions

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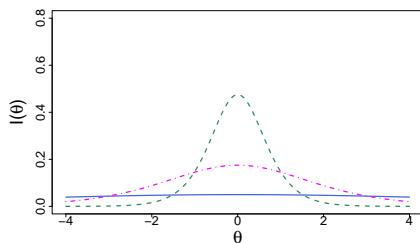


Figure 1: $a = 0.20$, $a = 0.70$, $a = 1.90$,
 $b = 0$

Information functions

Item Information Function

$$IIF_j = a_j^2 [P(\theta)(1 - P(\theta))]$$

Test Information Function

$$TIF = \sum_{j=1}^J IIF_j$$

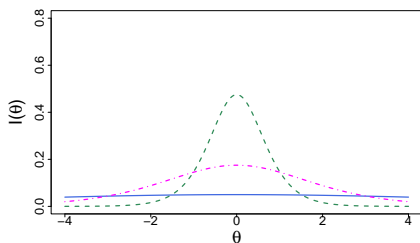


Figure 1: $a = 0.20$, $a = 0.70$, $a = 1.90$,
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Information functions

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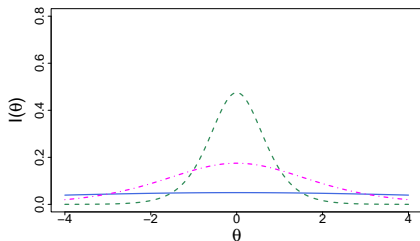


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Test Information Function

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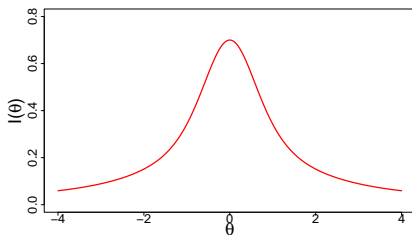


Figure 2: $TIF = IIF_1 + IIF_2 + IIF_3$

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Benchmark procedure

Selected items → items with the highest *IIFs*

e.g.: 3-item short form from 10-item full-length test

item	<i>b</i>	<i>a</i>	<i>IIF</i>
1	−0.67	0.71	0.08
2	0.50	1.19	0.15
3	−2.43	0.25	0.01
4	2.12	1.98	0.24
5	1.72	0.39	0.03
6	−2.28	1.62	0.19
7	0.64	0.50	0.05
8	−2.51	1.68	0.19
9	−0.66	0.44	0.04
10	0.72	0.33	0.02

Benchmark procedure

Selected items → items with the highest *IIFs*

e.g.: 3-item short form from 10-item full-length test

item	<i>b</i>	<i>a</i>	<i>IIF</i>
4	2.12	1.98	0.24
8	−2.51	1.68	0.19
6	−2.28	1.62	0.19
2	0.50	1.19	0.15
1	−0.67	0.71	0.08
7	0.64	0.50	0.05
9	−0.66	0.44	0.04
5	1.72	0.39	0.03
10	0.72	0.33	0.02
3	−2.43	0.25	0.01

- └ Short form procedures
- └ Procedures based on θ targets

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θ -target procedures

Selected items \rightarrow items with highest $IIFs$ in respect to θ targets (θ')

e.g.: 3-item short form from 10-item full-length test

	θ'_1	θ'_2	θ'_3
item	−2.67	0.01	2.67
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item	-2.67	0.01	2.67
1	0.04	0.12	0.08
2	0.09	0.33	0.03
3	0.01	0.01	0.02
4	0.73	0.06	0.01
5	0.04	0.03	0.02
6	0.01	0.06	0.59
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An overall look

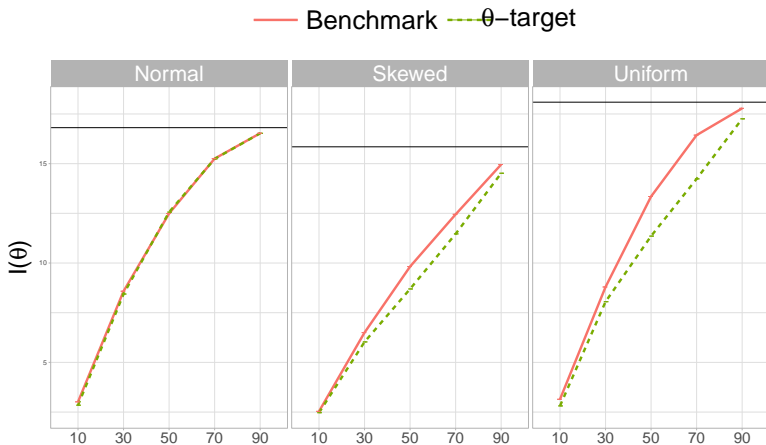


Figure 3: Overall Information of the short test forms

A closer look

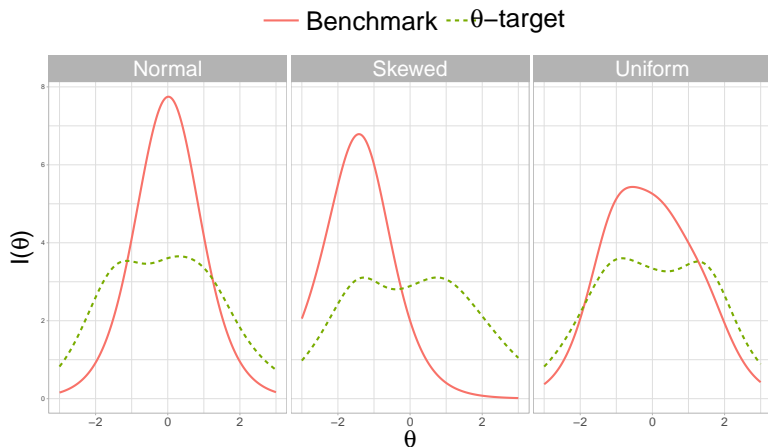


Figure 4: TIF of the 10-item short test form

An even closer look

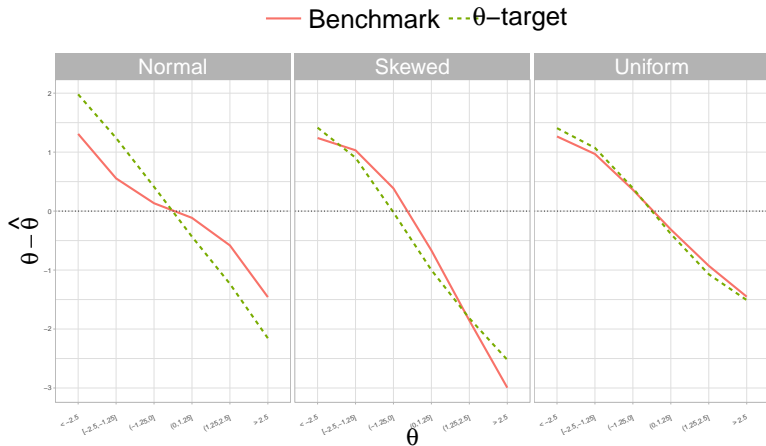


Figure 5: $\text{bias} = \theta - \hat{\theta}$ of the 10-item short test form

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Good!

There's no “one-fits-all” solution

The θ distribution is a key element

Good!

There's no “one-fits-all” solution

The θ distribution is a key element

..but work is still needed

Real life applications are missing

The CAT is missing

Thank you!

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