

# When randomness opens new possibilities: Acknowledging the stimulus sampling variability in Experimental Psychology

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# Introduction

Stimuli are fixed, respondents are random

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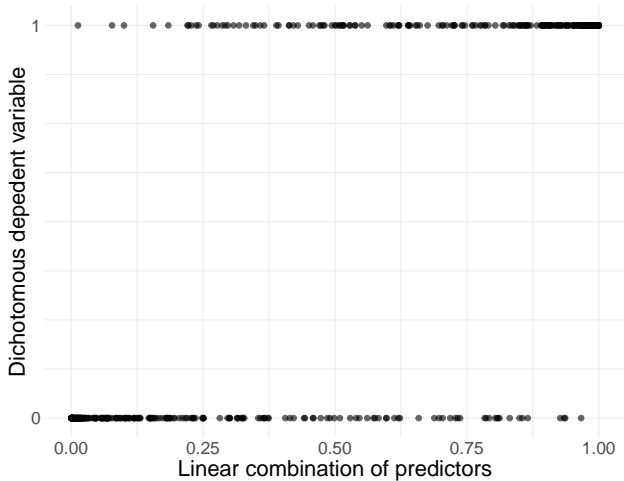
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What if

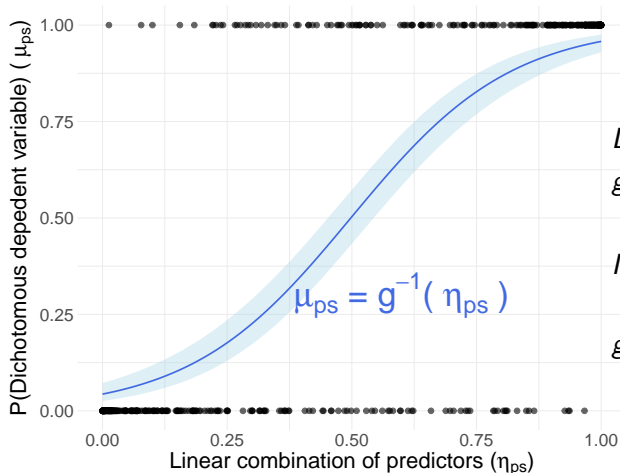
What if

# Generalized linear model for dichotomous responses



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Logit link function  $g$   

$$g(\eta_{ps}) = \log \left( \frac{\mu_{ps}}{1 - \mu_{ps}} \right)$$

Inverse  $g^{-1}$

$$g^{-1} = \frac{\exp(\eta_{ps})}{1 + \exp(\eta_{ps})}$$

## Random effects and random factors

Linear component in a (G)LM:

$$\eta = \beta X, \quad (1)$$

where  $\beta$  indicates the coefficients of the fixed intercept and slope(s), and  $X$  is the model-matrix.

Linear components in a (Generalized) Linear Mixed-Effects Model (GLMM):

$$\eta = \beta X Z d, \quad (2)$$

where  $Z$  is the matrix and  $d$  is the vector of the random effects (not parameters!)

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# The Rasch model

$$P(x_{ps} = 1 | \theta_p, b_s) = \frac{\exp(\theta_p - b_s)}{1 + \exp(\theta_p - b_s)}$$

where:

$\theta_p$ : ability of respondent  $p$  (i.e., latent trait level of respondent  $p$ )

$b_s$ : difficulty of stimulus  $s$  (i.e., "challenging" power of stimulus  $s$ )

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GLM

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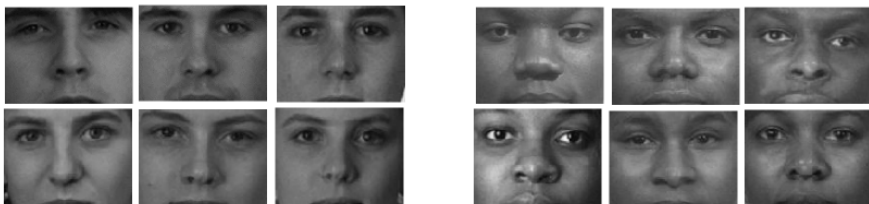
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GLM

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**Stimuli:**

## 12 Object stimuli



16 Attributes (Good, laughter, pleasure, glory, peace, happy, joy, love and  
and Evil, bad, horrible, terrible, nasty, pain, failure, hate)

Participants: 62 (F = 48.39%, Age =  $24.92 \pm 2.11$  years)

**Conditions:**

WGBB: White-Good/Black-Bad, 60 trials

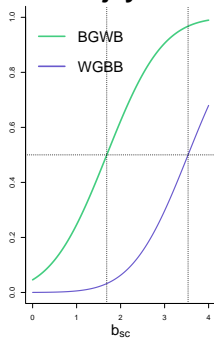
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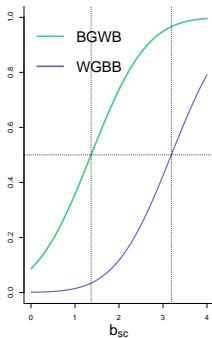
# Condition-specific easiness

## HIGH CONTRIBUTION STIMULI

**joy**



**evil**



## LOW CONTRIBUTION STIMULI

