
Algorithm 1 Synthesize a DSPG from a non-DSPG

Require: Directed acyclic graph $G = (V, E)$

Ensure: DSPG-compliant graph $G' \subset G$

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1:  $pathsToProcess \leftarrow \text{GetAllPaths}(G)$ 
2: Sort  $pathsToProcess$  by uncertainty or by length
3:  $G' \leftarrow pathsToProcess.pop()$   $\triangleright$  pick the first and remove from the list
4:  $nodesToPNPS \leftarrow \{\}$   $\triangleright$  Maps node to highest-nested PNPS it is part of
5: while  $pathsToProcess \neq \emptyset$  do
6:    $currentPath \leftarrow pathsToProcess.pop()$ 
7:    $branch \leftarrow \emptyset$ 
8:    $endAddingPath \leftarrow false$ 
9:   while not  $endAddingPath$  do  $\triangleright$  Looking for the branch to try too add
10:     $edge \leftarrow currentPath.next()$ 
11:    if  $currentPath$  is empty then
12:       $endAddingPath \leftarrow true$ 
13:    end if
14:    if  $edge.sink$  is not in  $G'$  then
15:       $branch.add(edge)$ 
16:    end if
17:    if  $branch$  is not empty or  $edge$  is not in  $G'$  then
18:       $branch.add(edge)$ 
19:       $nodeSrc \leftarrow branch.source$ 
20:       $nodeTarget \leftarrow branch.target$ 
21:       $check \leftarrow dspgChecker(G', nodeSrc, nodeTarget)$ 
22:      if  $check.bool = True$  then
23:         $G'.addEdges(branch)$ 
24:        for  $node$  in  $check.intermediateNodes$  do
25:           $nodesToPNPS[node] \leftarrow smallerPNPS((nodeSource, nodeTarget), nodesToPNPS[node])$ 
26:        end for
27:        for  $node$  in  $branch.intermediateNodes$  do
28:           $nodesToPNPS[node] \leftarrow moreNestedPNPS((nodeSource, nodeTarget), nodesToPNPS[node])$ 
29:        end for
30:      end if
31:    else if then
32:       $endAddingPath \leftarrow True$ 
33:       $branch \leftarrow [nodeSource, nodeTarget]$ 
34:    end if
35:  end while
36: end while
```
