development

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liquid

Mahyar Naderi<sup>1</sup>, Guozhu Liang<sup>2a</sup> and Hasan Karimi<sup>3</sup>

propellant rocket engines based on MATLAB Simulink

simulation software

Abstract. Focusing on Liquid Propellant Rocket Engine (LPRE) major components, a steady state modular simulation software has been established in MATLAB Simulink. For integrated system analysis, a new algorithm dependant on engine inlet mass flow rate and pressure is considered. Using the suggested algorithm, it is possible to evaluate engine component operation, similar to the known initial parameters during hot fire test of the engine on stand. As a case study, the reusable Space Shuttle Main Engine (SSME) has been selected and the simulation has been performed to predict engine's throttled operation at 109 percent of the nominal thrust value. For this purpose the engine actual flow diagram has been converted to 34 numerical modules and the engine has been modelled by solving a total of 101 steady state mathematic equations. The mean error of the simulation results is found to be less than 5% compared with the published SSME data. Using the presented idea and developed modules, it is possible to build up the numerical model and simulate other LPREs.

# 1 Introduction

Modular

In order to reduce the costs during design and enhancement phases, using software capable of precise modeling and simulating is favorable. For this purpose in this research a simulation tool is developed for steady state analysis of a RLPRE which can be further extended for simulating other types of LPREs.

In development of simulation software for LPRE analysis, many contributions have been done for example in 1995, C. Goertz suggested a modular method for static performance analysis of different LPRE cycles using Fortran (as it appears). [1]. In 2000, K. Liu, Y. Zhang developed a methodology for modularization modeling and transient simulation of LPREs and created an object oriented program using Microsoft Visual C++ 6.0 [2]. In 2009, C. R. Koppel et al.; used EcosimPro tool kit along with ESPSS libraries to implement and validate satellite propulsion systems modellings [3]. In 2011, F. D. Matteo and M. D. Rosa developed steady state library for ESPSS software for static simulation of liquid propellant engines [4]. In 2012, Y. Zheng et al. used the AMEsim software to simulate the dynamic behavior of unified spacecraft propulsion system [5]. In 2013, M. Naderi, A.R.Jalali et al. developed a GUI software for dynamic simulation of open cycle LPRE using FORTRAN 90 [6]. In 2015, L. Wei et al. used Modelica to establish component model libraries for LPRE [7]. As it is visible, by the evolution of computers, the researchers are tending towards

<sup>&</sup>lt;sup>1</sup>Ph.d Candidate, School of Aeronautics and Astronautics, 100191 Beihang University, China

<sup>&</sup>lt;sup>2</sup>Professor, School of Aeronautics and Astronautics, 100191 Beihang University, China <sup>3</sup>Associate Professor, Faculty of Aerospace Engineering, K.T. University of Technology, Iran

<sup>&</sup>lt;sup>a</sup> Guozhu Liang : lgz@buaa.edu.cn

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developing more general softwares similar to toolkits. In the current research in order to analyze different types of LPRE cycle performance, a modular simulation software has been developed for steady state analysis, using MATLAB Simulink. Here MATLAB is chosen due to its high accessibility, applicability, simple programming language, convinient usage, rich library and toolboxes for different mathematical solution methods and finally ease of operation for future researchers to enhance the current software. Despite some of the previous literatures, the presented algorithm uses engine inlet mass flowrate and pressure as the system input, similar to the known initial conditions during hot fire test. For case study, SSME, as one of the most complicated, successful and comprehensive LPRE built up to now, is simulated and the results are compared with published data.

# 2 Realization approach for modular simulation of LPRE

The process of modular simulation is classified into five major steps: 1) Developing modular models for LPRE main components (here in MATLAB Simulink); 2) Validating the modules; 3) Establishing the desired LPRE numerical flow model from the actual flow diagram; 4) Developing an algorithm for determining the sequential solution order and method, based on module's input/output data; 5) Establishing the integrated model.

Reviewing the major elements for different types LPRE cycles, it is found that LPREs are generally constructed of seven major modules. These include connecting pipes, combustion chamber, nozzle, pre-burner (gas generator), pumps, turbines and controling valves. In this paper the cooling jacket is also considered as a module therefor a total of eight madules have been considered (Table 1). Some of these modules can also be connected to form a subsystem such as turbo-pump assembly or thrust chamber. With modular form of simulation, it possible to use the same modules for other LPREs containing similar componenets. Here the modules are constructed of linear/nonlinear lamped parameter steady state equations. Despite frequently used algorithms for steady state analysis [8-10], the chamber or pre-burner pressure is not known, but itself is a parameter required to be simulated. For this pupose an algorithm is developed which is based on the known parameters at main feed line enterance (i.e. oxidizer and fuel mass flow and pressure at engine inlet), similar to the case of testing the engine on test stand. The solution method is based on Newton Raphson iterative loops. For interpolating between the required inputs, the shape-preserving piecewise cubic interpolation method was used as Matlab function and showed good accuracy.

Table 1. Main modules in LPRE flow diagram

Mode			THREE	<			1	()	<b>∑</b> □		<u>\</u>
Subsystem	(		C	No	P	P	Pu	Tu	V	T	T
·	C	J	J	zzle	ipe	В	mp	rbine	alve	C	P

# 3 Case study

In this paper, SSME is selected as a case study. This engine is not only a SCCLPRE but also a RLPRE and is among one the most successful LPREs ever built. Furthermore, due to its special design, it has most of the complexities that all other engines might have, namely: using cryogenic propellant, separate turbo-pump assemblies on each propellant line, low and high pressure turbo-pumps, hydraulic turbine and etc. A detail description of SSME can be found in [11]. In order to model the engine, with regard to its actual flow diagram, a numerical model using the eight modules already discussed is prepared (Figure 1). The model is constructed of 34 modules as described in Table 1. Each module is based on steady state linear/nonlinear lumped parameter model mathematical equation.

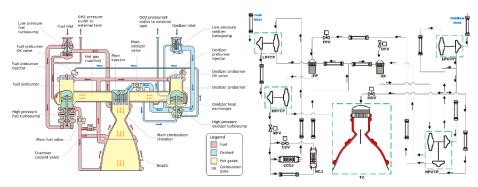


Figure 1. Comparison between SSME actual (left-[12]) and current simulated model flow diagram

The required input and produced output data for modules is described in Table 2 to Table 5 but due to page number limitations, only the modules on fuel line are mentioned.

The input variables are devided into three main catagories: Type "a" parameters: constant input values (e.g. LPFTP disk diameter) and in Figure 2 are depicted by pink color; Type "b" parameters: curves and graphs from which the desired value should be interpolated (e.g. combustion product gas temperature which is plotted versus propellant mixture ratio), depicted by orange color in Figure 2; Type "c" parameters: estimated in other blocks and will later be given to the current block as input (e.g. LPFTP pump outlet pressure is an input for HPFTP pump) depicted by cyan color in Figure 2.

LPTFP Turbine Parameter	T ype	at.	LPFTP Pump Parameter	T ype	at.
LPFTP Shaft Rotational Speed	In put	С	LPFTP Shaft Rotational Speed	In put	с
CC Main Fuel Injector Pressure	In put	c	CC Main Fuel Injector Pressure	In put	c
CC Cooling Passage Pressure	In put	c	Fuel Density	In put	a
Fuel Vapor Gas Constant	In put	a	LPFTP Characteristic Map	In put	b
CC Cooling Passage heat ratio	In put	c	LPFTP Pump Shaft Torque	O utput	-
LPFTP Turbine Polytropic Efficiency	In put	a	LPFTP Pump Input mass flow rate	O utput	-
CC Cooling Passage Temperature	In put	a			
LPFTP Characteristic Map	In put	b			
LPFTP Turbine Shaft Torque	O utput	-			
LPFTP Turbine mass flow rate	utput	-			

Table 2. LPFTP turbo-pump input/output data

Table 3. MFV and CCV input/output data

MFV Parameter	T		CCV Parameter	T	C
	ype	at.	CCV Parameter	ype	at.
HPFTP Pump Discharge	In		MFV Discharge Pressure	In	c
Pressure	put	C	WIF V Discharge Fressure	put	C
HPFTP Pump Discharge mass	In		Pre-Burners Main Fuel Supply	In	
flow	put	c	Line	put	С
MFV Nominal Area Ratio	In	l.	CCV Nominal Area Ratio	In	ь.
Graph	put	b	Graph	put	b
MFV Throttle Situation	In		CCV Throttle Situation	In	
WIF V Throttle Situation	put	a	CCV Throttle Situation	put	a
MEV Dischange Brossyre	0		CCV Dischause mass fllow note	О	
MFV Discharge Pressure	utput	-	CCV Discharge mass fllow rate	utput	-

Table 4. Fuel pre-burner and combustion chamber input/output data

Fuel Pre-Burner Parameter	T		(	Combustion Chamber	T	
	ype	at.		Parameter	ype	at.
Fuel Pre-Burner Fuel mass flow rate	In put		c	MOV mass flow rate	In put	с
Fuel Pre-Burner Oxid mass flow rate	In put		c	CC Fuel Injector mass flow rate	In put	c
Nozzle Cooling Passage Temperature inlet	In put		c	<b>HPOTP Boost Pump mass flow</b>	In put	c
Nozzle Cooling Passage mass flow	In put		c	HPFTP Pump mass flow	In put	c
Nozzle Cooling Passage Temperature	In put		a	CC Temperature-Mixture Ratio Graph	In put	b
CCV mass flow rate	In put		c	Product gama-Mixture Ratio Graph	In put	b
Fuel Pre-Burner Throat Diameter	In put		a	Gas Constant-Mixture Ratio Graph	In put	b
Pre-Burner Temperature-Mixure Ratio	In put		b	Combustion Chamber Throat Area	In put	a
Fuel Pre-Burner Pressure	O utput		-	<b>Combustion Chamber Pressure</b>	O utput	-
Fuel Pre-Burner Temperature	O utput		-	Combustion Chamber Temperature	O utput	-

Table 5. Nozzle cooling jacket and FP fuel line Inlet input/output data

Nozzle Cooling Jacket Parameter	T ype at.		ED E1 !	T	С
_			FP Fuel line parameter	ype	at.
MFV Discharge Pressure	In put	c	Fuel Pre-Burner Pressure	In put	с
Nozzle Cooling Passage Pressure	In put	c	Pre-Burners Main Fuel Supply Line	In put	c
Nozzle Cooling Passage Friction Graph	In put	b	Nozzle Cooling mass flow	In put	c
Nozzle Cooling Passage Discharge mass flow	Output	-	CCV mass flow	In put	c
			Fuel Pre-Burner Fuel mass flow	O utput	-
			Fuel Density Feeding the Pre- Burners	Output	-

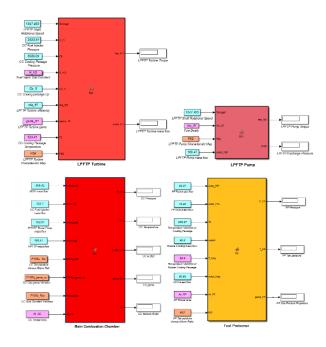


Figure 2. LPFTP turbine, pump, fuel pre-burner and combustion chamber Simulink module

After each module is verified, in order to form the integrated system model, the modules should be linked together with a correct logic according to the desired engine flow diagram (Figure 3).

Using given input data and nine initial guesses, the equations are solved by Newton Raphson iteration method. By correct connection of modules, an integrated model based on desired flow diagram can be formed. Considering SSME as our case study, the outer layer of the integrated Simulink model is shown in Figure 4.

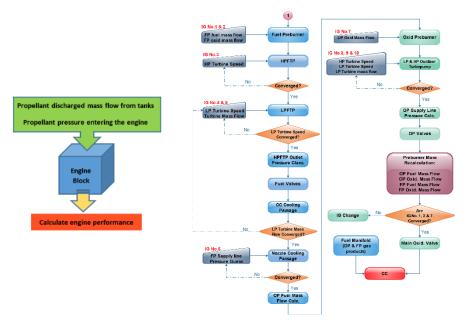


Figure 3. System simulation block diagram (left); SSME simulation algorithm (right)

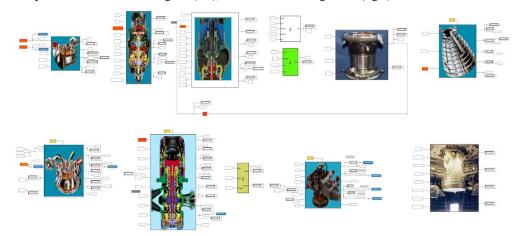


Figure 4. SSME integrated Simulink system simulation

### 4 Results

For validating the suggested algorithm and simulation software, SSME RLPRE data throttled at 109 percent of nominal operation condition is used from Rocketdyne report [13]. For this purpose using the suggested algorithm in Figure 3, the integrated model of the engine (containing 34 modules) is formed in MATLAB Simulink. The total system of equations consisting of 101 linear/nonlinear equations are solved with Newton Raphson method. The required system level input values can be found in Table 6.

Input Parameter	Value
Fuel tank discharge mass flow	72.79 kg/s
Oxidizer tank discharge mass flow	436.72 kg/s
Absolute pressure at the end of the fuel tank	2.04 atm
Absolute pressure at the end of the	68 atm

Table 6. SSME System input parameters at 109% thrust level

The simulation results can be found at Table 7. As it can be seen from the results, the governing equations used for turbo-pump system has leaded to fairly good accuracy except for the LPFTP wahich was in lack of initial data. The outlet pressure which is of course quiet dependable on the pump performance has been affected by the torque and speed, and the results seem to be following the expected trend. The turbine mass flow rate analysis shows great convergence and the results are satisfactory. The pre-burner pressure are precise which confirm the usage of the introduced equation sets for this element. For the combustion chamber, using CEA software for computing the gas product thermodynamic properties, the results do not show good precision but using the suggested equation for computing the gas properties from [13], the simulation results for this element are far better.

Shaft	HPFTP 36954.02		3/354.67	-1.07/
rotational	HPOTP	31497.53	31133.36	1.17
speed, Ω	LPFTP 15235.47		15806.83	-3.61
(rpm)	LPOTP	5505.54	5447.11	1.07
	HPFTP	14389.05	14594.05	-1.40
Torque T	HPOTP	6489.89	6350.64	2.19
Torque, $\tau$	HPOBTP	449.72	438.58	2.54
(N.m)	LPFTP	1238.39	1327.43	-6.71
	LPOTP	2305.37	2271.32	1.50
	HPFTP	463.92	476.61	-2.66
Pump outlet	HPOTP	361.1	350.62	2.99
pressure	HPOBTP	590.79	573.95	2.93
(atm)	LPFTP	16.05	17.63	-8.96
	LPOTP	30.82	30.10	2.39
Turbine	HPFTP	72.79	73.32	-0.72
mass flow	HPOTP	30.01	28.61	4.89
rate, $\dot{m}_t$	LPFTP	15.1	15.73	-4.01
(kg/s)	LPOTP	79.35	78.73	0.79
PB pressure	FP	404.02	401.30	0.68
(atm)	OP	401.96	399.30	0.67

Table 7. Comparing simulation results Simulation

Rocketdyne [13]

227.00

227.00

-0.27

23.77

Parameter

CC pressure

(atm)

Exp. Gas prop.

CEA

226.39

280.96

## 5 Conclusion

A modular simulation software for steady state simulation of RLPRE was developed based on MATLAB Simulink. Eight general simulation modules for simulating engine main components was established. In the current simulation, despite commonly used algorithms, the simulation is not dependant on engine down stream parameters. As a case study, SSME as the most successful RLPRE ever built, was selected and the engine flow diagram was simplified and modularized to 34 component modules. A total of 101 linear/nonlinear equations were solved using Newton-Raphson iteration method. Comparing with the actual results for the engine's throttled operation at 109 percent of the nominal thrust value, it is concieved that the simulation has an acceptable average precision of more than 95 percent. As future work, the current precision can be enhanced by introducing more detailed initial data especially for the LPFTP assembley and the software can be further verified with other engine cycles.

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### **Abbreviation**

CC	Combustion Chamber	LPRE	Liquid Propellant Rocket Engine
CCV	Cooling Control Valve	MFV	Main Fuel Valve
CJ	Cooling Jacket	MOV	Main Oxidizer Valve
FP	Fuel Pre-Burner	OP	Oxidizer Pre-Burner
FPV	Fuel Pre-Burner Valve	OPV	Oxidizer Pre-Burner Valve
HPFTP	High Pressure Fuel Turbo-pump	PB	Pre-Burner
НРОТР	High Pressure Oxidizer Turbo- Pump	RLPRE	Reusable Liquid Propellant Rocket Engine
IG	Initial Guess	SCCLPRE	Stage Combustion Cycle LPRE
LPFTP	Low Pressure Fuel Turbo-pump	TC	Thrust Chamber
LPOTP	Low Pressure Oxidizer Turbo- Pump		