

# Constraint Programming

**1 year ago**

**determine the available**

**determine the available**

*arrival times*

**determine the available**

*arrival times*

days

# determine the available

*arrival times*

days

tables

**satisfying**

**satisfying**

available tables



**satisfying**

*existing reservations*

*available tables*

**satisfying**

*existing reservations*

*available tables*

*opening times*

tests

**satisfying**

*existing reservations*

*available tables*

*the size of the group*

*opening times*

tests

*business rule #1*

**satisfying**

*existing reservations*

*available tables*

*the size of the group*

*opening times*

tests

business rule #2

*business rule #1*

**satisfying**

*existing reservations*

*available tables*

*the size of the group*

release dates

opening times

tests

business rule #2

business rule #3

business rule #1

**satisfying**

existing reservations

available tables

the size of the group

release dates

opening times

tests  
which ones?

business rule #2

business rule #3

business rule #1

**satisfying**

existing reservations

available tables

the size of the group

release dates

opening times

tests  
which ones?

business rule #2

business rule #3

business rule #1

**satisfying**


existing reservations

available tables

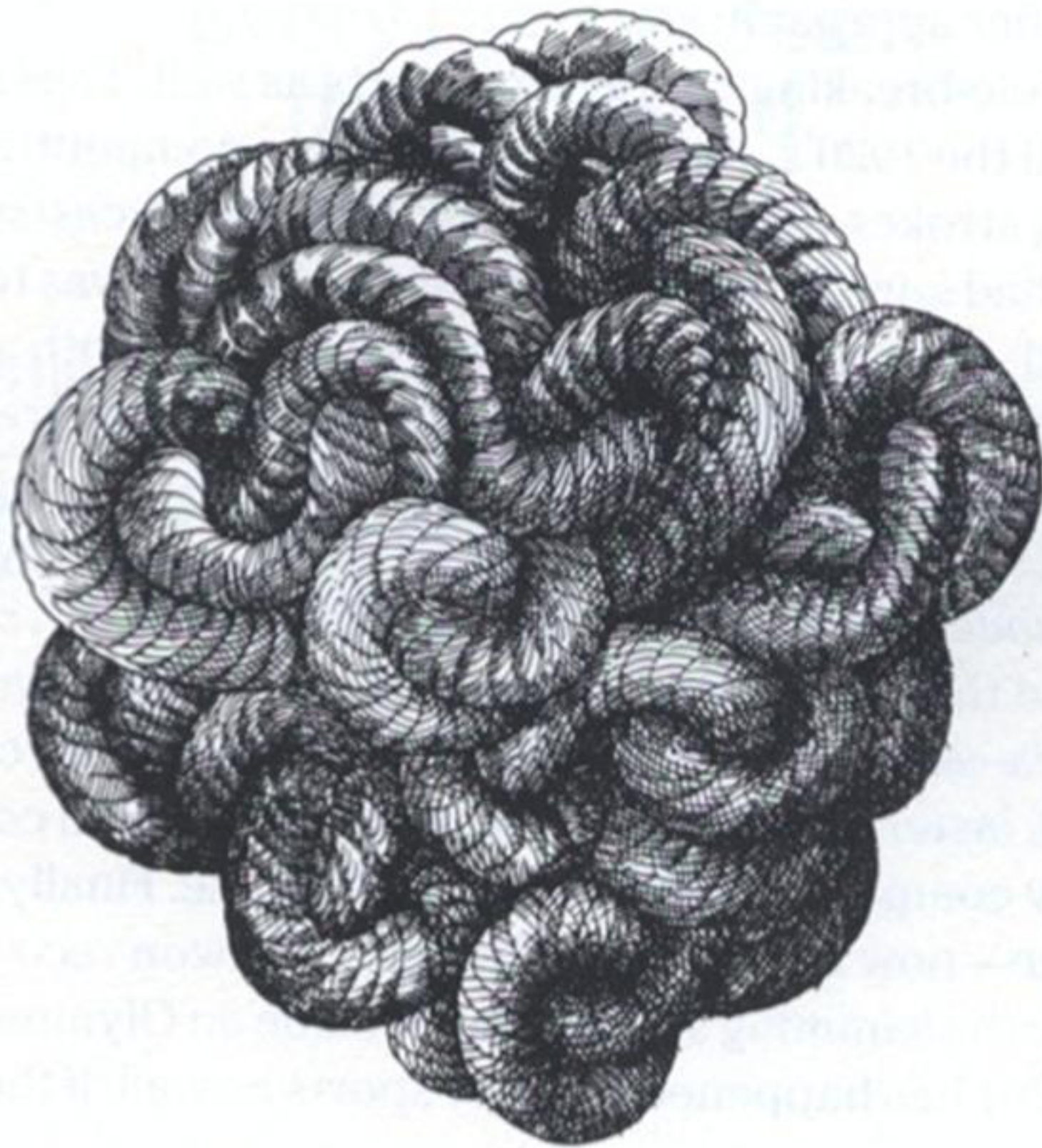
the size of the group

release dates

opening times

business rule #137812 





# Google

Google Search

I'm Really Desperate 😞

# Late night problem googling



Google Search

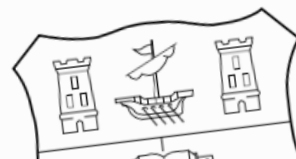
I'm Really Desperate 😞

# **'Managing Restaurant Tables Using Constraint Programming'**

# 'Managing Restaurant Tables Using Constraint Programming'

Managing Restaurant Tables  
Using  
Constraint Programming

ALFIO VIDOTTO



**Thank you, Alfio Vidotto**

Thank you,  Alfio Vidotto

**Lets define by example**



MY HOBBY:  
EMBEDDING NP-COMPLETE PROBLEMS IN RESTAURANT ORDERS

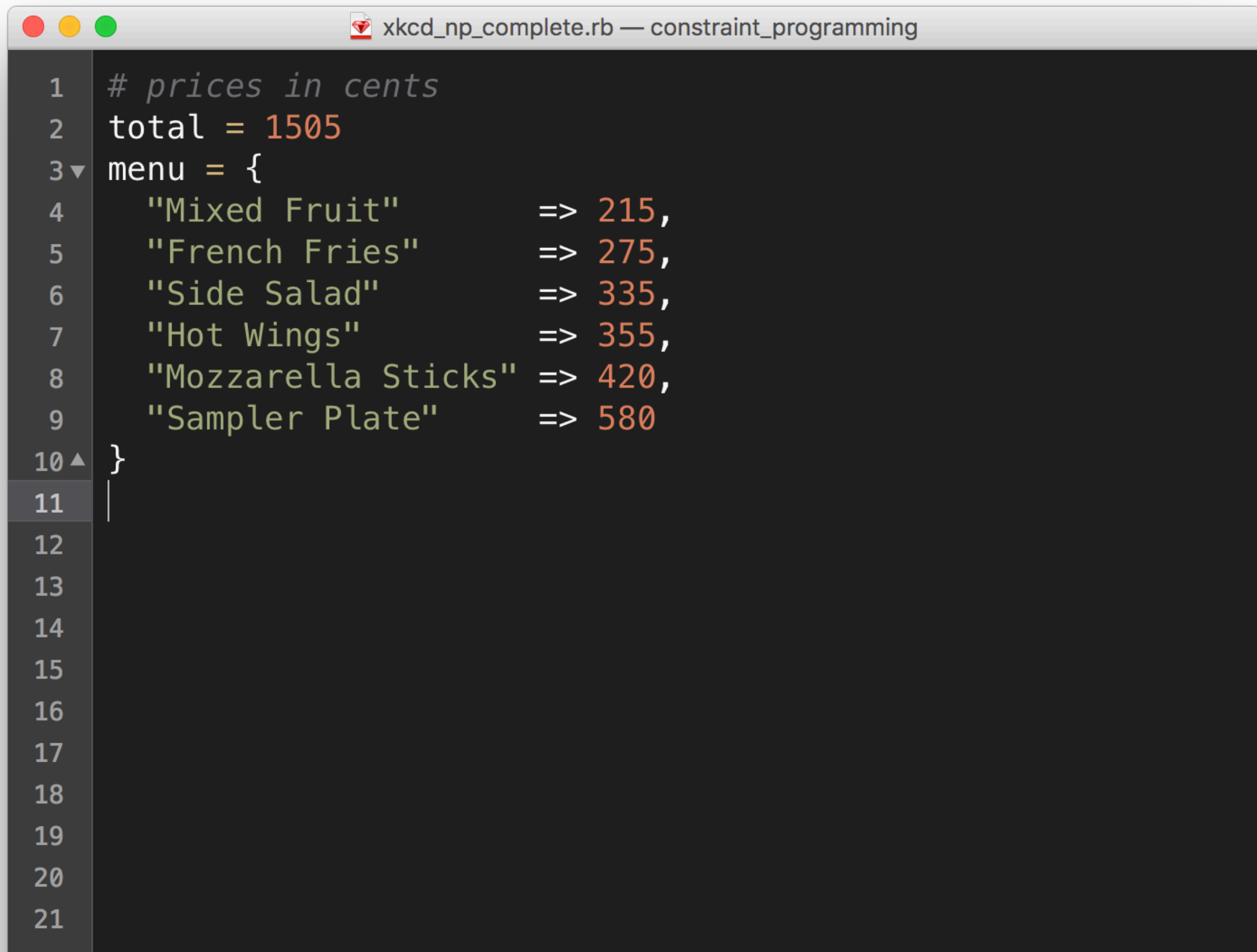
CHOTCHKIES RESTAURANT	
~ APPETIZERS ~	
MIXED FRUIT	2.15
FRENCH FRIES	2.75
SIDE SALAD	3.35
HOT WINGS	3.55
MOZZARELLA STICKS	4.20
SAMPLER PLATE	5.80
~ SANDWICHES ~	
BARBECUE	6.55



**/kən'streɪnt/**

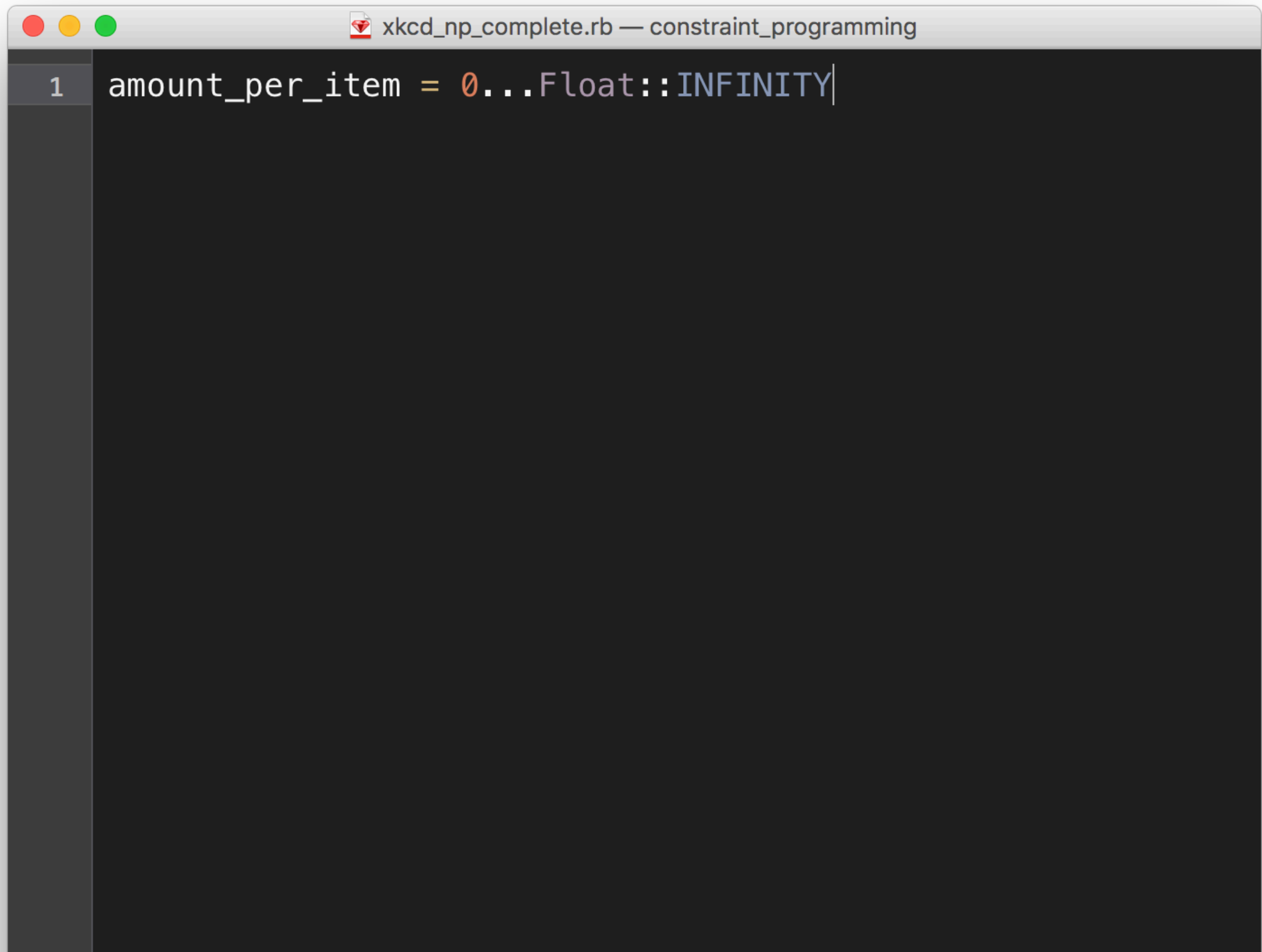
A constraint is a logical relation  
among several variables,  
each taking a value in a given domain.

# several variables



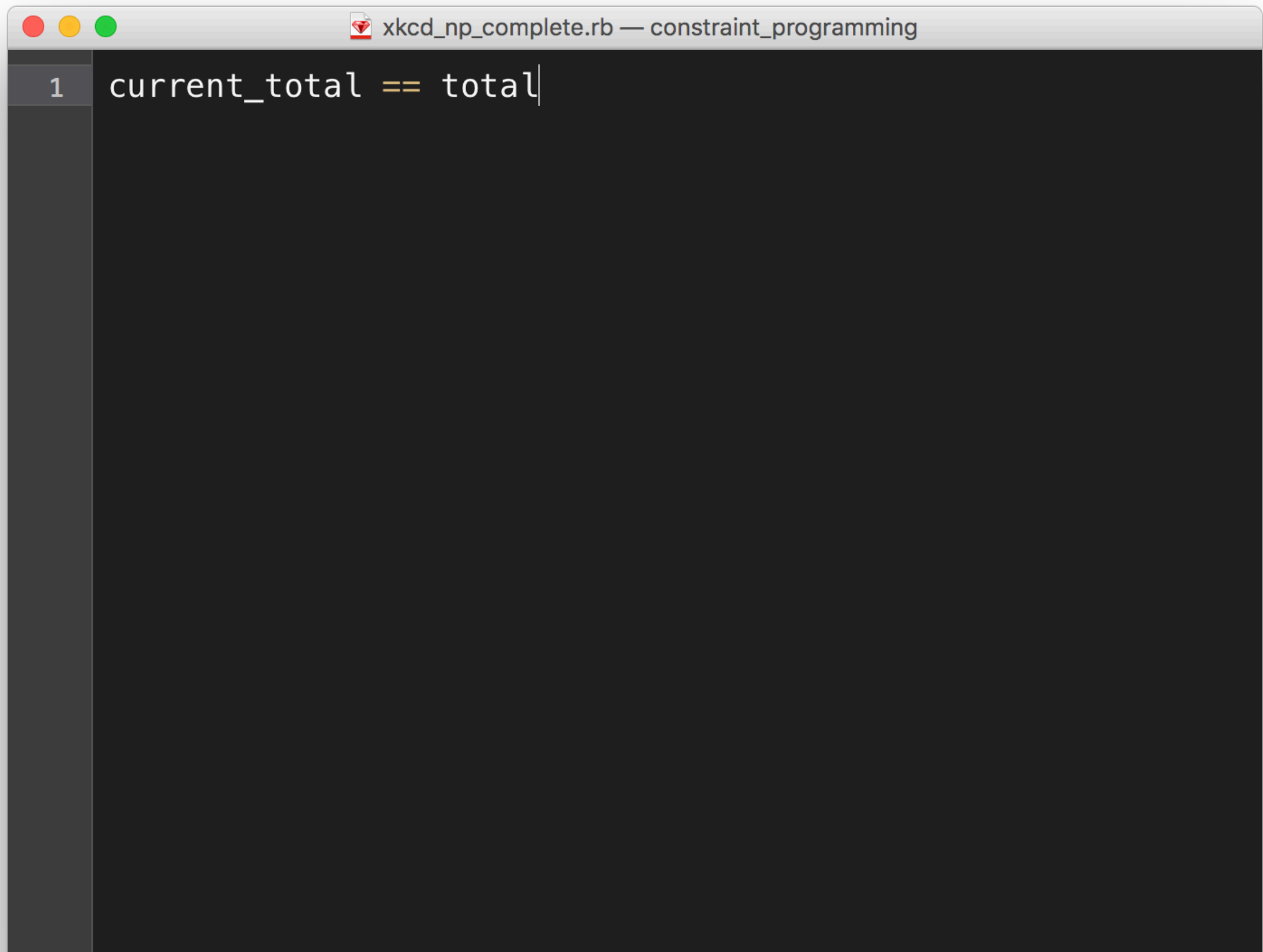
```
1  # prices in cents
2  total = 1505
3  menu = {
4    "Mixed Fruit"      => 215,
5    "French Fries"     => 275,
6    "Side Salad"       => 335,
7    "Hot Wings"        => 355,
8    "Mozzarella Sticks" => 420,
9    "Sampler Plate"    => 580
10 }
11
12
13
14
15
16
17
18
19
20
21
```

# domain

A screenshot of a code editor window. The title bar at the top shows three colored window control buttons (red, yellow, green) on the left, followed by a file icon and the text "xkcd\_np\_complete.rb — constraint\_programming". The editor area has a dark background. On the left side of the editor, there is a vertical line of numbers, with "1" highlighted in a light gray box. The code on line 1 is "amount\_per\_item = 0...Float::INFINITY|", where "0" is orange, "..." is light blue, "Float::" is light blue, and "INFINITY" is light blue. A white cursor is positioned at the end of the line.

```
1 amount_per_item = 0...Float::INFINITY|
```

# logical relation



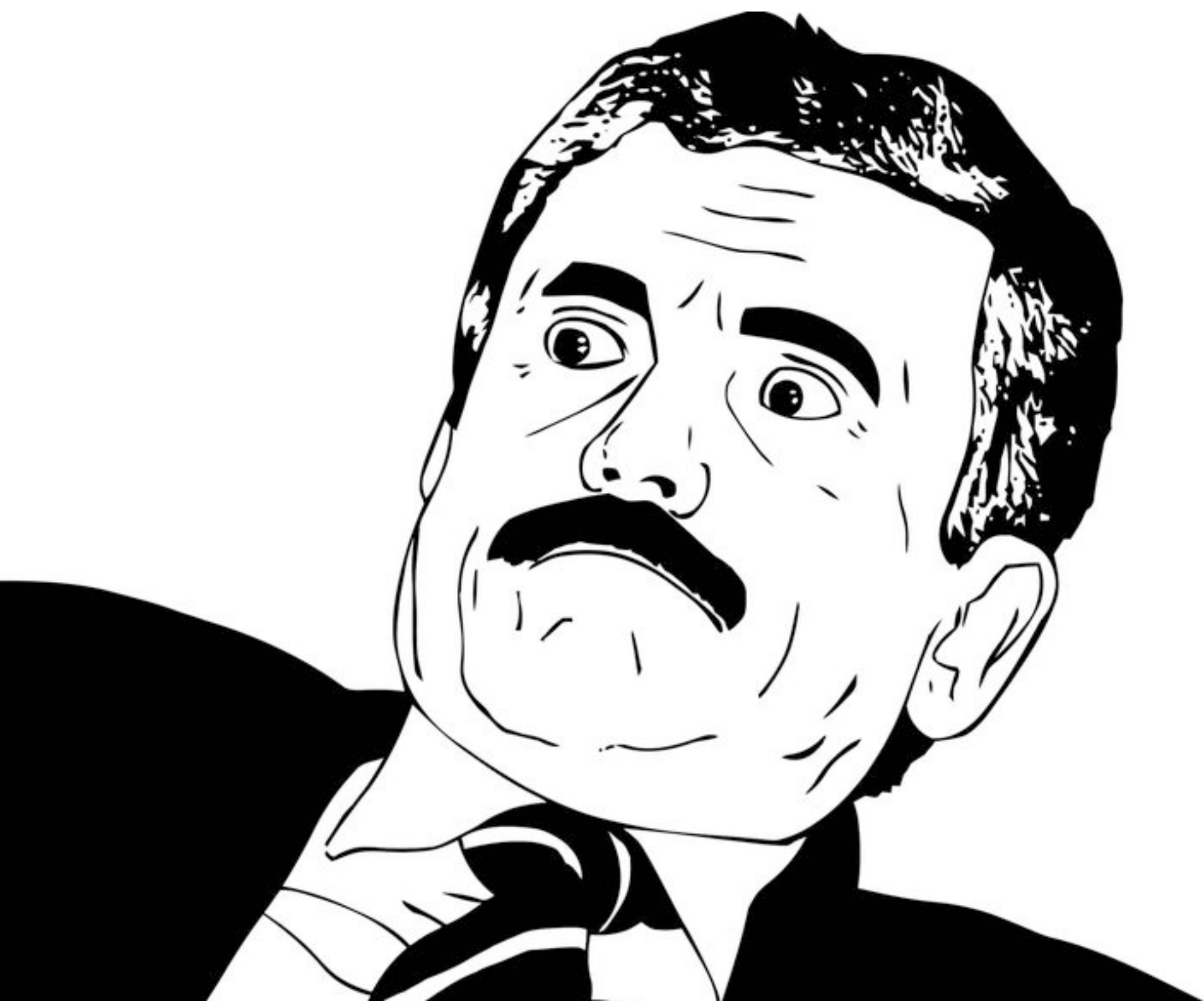
A screenshot of a code editor window. The title bar at the top shows three colored window control buttons (red, yellow, green) on the left, followed by a file icon and the text "xkcd\_np\_complete.rb — constraint\_programming". The editor area has a dark background. On the left side of the editor, there is a vertical line of numbers, with "1" highlighted in a light gray box. The code "current\_total == total|" is written in a light gray font on the first line, with the cursor at the end of the line.

```
1 current_total == total|
```

# Easier done than said.

```
xkcd_np_complete.rb — constraint_programming

1  require_relative 'lib/amb.rb'; include Amb
2
3  total = 1505
4  menu = {
5    "Mixed Fruit" => 215, "French Fries" => 275,
6    "Side Salad" => 335, "Hot Wings" => 355,
7    "Mozzarella Sticks" => 420, "Sampler Plate" => 580
8  }
9
10 order = {}
11 menu.each do |_, price|
12   amount_per_item = choose(0..10)
13   order[price] = amount_per_item
14 end
15
16 current_total = order.inject(0) do |sum, (price, amount)|
17   sum += price * amount
18 end
19 failure unless current_total == total
20
21 p Hash[menu.map { |label, price| [label, order[price]] }]
```



# Simple Backtracking in Ruby



**meet call/cc**



# Simple Backtracking in Ruby

```
np_complete_without_require.rb — constraint_programming

1  require "continuation"
2
3  def failure
4    @backtrack.pop.call
5  end
6
7  def choose(enum)
8    @backtrack ||= [-> {raise "exhausted"}]
9    enum.each do |choice|
10     callcc do |cb|
11       @backtrack << cb
12       return choice
13     end
14   end
15   failure
16 end
17
18 total = 1505
19 menu = {
20   "Mixed Fruit" => 215, "French Fries" => 275,
21   "Side Salad" => 335, "Hot Wings" => 355,
```

**Thank you, Jim Weirich**

Thank you, Jim Weirich



**First research on constraint  
satisfaction problems  
dates back to the 70s**

**Montanary 1974**  
**Waltz 1975**

**Systematic use of constraints  
described in**

**'Constraint logic programming'  
Jaffar, Lassez 1987\***



**30 years**

# constraint satisfaction landscape

areas of research			
search	generate and test		
	back tracking	back jumping	back marking
consistency	node consistency	arc consistency	path consistency
constraint propagation	forward checking	look ahead	
reducing search			
constraint optimisation			

**use constraint programming**

**use constraint programming**

use constraint programming  
for scheduling, planning

**use constraint programming**

**use constraint programming**

use constraint programming  
**for resource allocation\***



use constraint programming

**Main advantages**

**Model programs  
closely to their real world  
entities.**

**Vast open research  
in optimising  
difficult problem areas.**

**Clever modelling can get  
you around NP-hard  
problems.**

**\*satisfaction not guaranteed**

**Interested in more?**

# Upcoming events

- ACP Summer Schools  
<http://www.a4cp.org/events/summer-schools>
- CP Conference Series  
<http://www.a4cp.org/events/cp-conference-series>

August 28th to September 1st 2017, Melbourne, Australia

**Thank you, beloved audience**



A background pattern of small red hearts scattered across the white page.

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# References

- <http://tidel.mie.utoronto.ca/pubs/Theses/vidotto.phd.pdf>
- <http://rubyquiz.com/quiz70.html>
- <http://www.math.unipd.it/~frossi/cp-school/CPschool05notes.pdf>
- <http://kti.mff.cuni.cz/~bartak/constraints/index.html>
- [http://www.hakank.org/constraint\\_programming\\_blog/](http://www.hakank.org/constraint_programming_blog/)
- <http://www.a4cp.org>