

# BACHELOR FINAL THESIS



UNIVERSITAT POLITÈCNICA DE CATALUNYA  
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## Real-Time Optimal Trajectory Generation for Fixed-Wing UAVs in Firefighting Missions via Numerical Integration and Constrained Optimization

**Document:**

Report

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**Degree:**

Bachelor in Aerospace Technology Engineering

**Examination session:**

Autumn 2025

# **Abstract**

# Acknowledgments

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# Preface

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## **Scope and Objectives**

## **Motivation and Justification**

## **Methodological Approach**

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# Acronyms

**NLP** Non-linear Programming.

**OCP** Optimal Control Problem.

**OCT** Optimal Control Theory.

# **1 | Fundamentals of Optimal Control and its Implementation**

## **1.1 Introduction to Optimal Control Theory**

The Optimal Control Theory (OCT) is a control field related branch where an objective function has to be optimised -most of the times, it has to be minimised- in order to find the control trajectory for a determined dynamical system. This theory is historically related with calculus of variations, where optimal points -either maxima or minima- are found using little variations in functions or functionals (CITA). This field of study, proposed by Isaac Newton, was developed as a solving approach for the brachistochrone problem, posed by Bernoulli in 1696. The brachistochrone curve is defined as the fastest descent path -most optimal path for minimising time- between two points A and B under a uniform gravitational field. Counterintuitively, it was found that the most optimal path was not but the cycloidal ramp, as can be seen on the image below, where ball has to roll under gravity only at the different paths, and the same grade shaded figures correspond to same time-instants.

In essence, the OCT responds the need to solve continuous time optimisation problems, as the once presented. Thus, the Optimal Control Problem (OCP) can be understood as a n-dimensional extension of the Non-linear Programming (NLP) problem. The NLP problem can be defined as the minimisation of a given function subject to a different set of equations or inequations, called constraints.